The Concurrent Missile VDM++ Model

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1 The World Class

```
World() \triangle
              env := new \ Environment ("scenario.txt");
              env.addSensor(FighterAircraft'sensor0);
              env.addSensor(FighterAircraft'sensor1);
              env.addSensor(FighterAircraft'sensor2);
              env.addSensor(FighterAircraft'sensor3);
              FighterAircraft'controller0.addDispenser(FighterAircraft'dispenser0);
              FighterAircraft'controller0.addDispenser(FighterAircraft'dispenser1);
              FighterAircraft'controller0.addDispenser(FighterAircraft'dispenser2);
              FighterAircraft'controller0.addDispenser(FighterAircraft'dispenser3);
              FighterAircraft'detector.addController(FighterAircraft'controller0);
              FighterAircraft'controller1.addDispenser(FighterAircraft'dispenser4);
              FighterAircraft'controller1.addDispenser(FighterAircraft'dispenser5);
              FighterAircraft'controller1.addDispenser(FighterAircraft'dispenser6);
              FighterAircraft'controller1.addDispenser(FighterAircraft'dispenser7);
              FighterAircraft'detector.addController(FighterAircraft'controller1);
              FighterAircraft'controller2.addDispenser(FighterAircraft'dispenser8);
              FighterAircraft'controller2.addDispenser(FighterAircraft'dispenser9);
              FighterAircraft'controller2.addDispenser(FighterAircraft'dispenser10);
              FighterAircraft'controller2.addDispenser(FighterAircraft'dispenser11);
              FighterAircraft'detector.addController(FighterAircraft'controller2);
start
(FighterAircraft'detector)
          );
public
       Run: () \xrightarrow{o} ()
       Run() \triangleq
start
(env);
              env.isFinished();
              FighterAircraft'detector.isFinished();
              env.showResult()
{\it end}\ World
     Test Suite:
                     vdm.tc
     Class:
                     World
```

 $World: () \stackrel{o}{\rightarrow} World$

Name	#Calls	Coverage
World'Run	1	$\sqrt{}$
World'World	1	$\sqrt{}$
Total Coverage		100%

2 The FighterAircraft Class

```
class FighterAircraft
instance variables
       public static detector : MissileDetector := new MissileDetector ();
       public static sensor0: Sensor := new Sensor (detector, 0);
       public static sensor1: Sensor := new Sensor (detector, 90);
       public static sensor2 : Sensor := new Sensor (detector, 180);
       public static sensor3: Sensor := new Sensor (detector, 270);
       public static controller 0 : Flare Controller := new Flare Controller (0);
       public static controller1: FlareController: = new FlareController(120);
       public static controller 2 : Flare Controller := new Flare Controller (240);
       public static dispenser0: FlareDispenser:= new FlareDispenser(0);
       public static dispenser1: FlareDispenser:= new FlareDispenser (30);
       public static dispenser2: FlareDispenser: = new FlareDispenser(60);
       public static dispenser3: FlareDispenser:= new FlareDispenser (90);
       public static dispenser4 : FlareDispenser := new FlareDispenser (0);
       public static dispenser5: FlareDispenser:= new FlareDispenser(30);
       public static dispenser6: FlareDispenser:= new FlareDispenser (60);
       public static dispenser7: FlareDispenser:= new FlareDispenser(90);
       public static dispenser8 : FlareDispenser := new FlareDispenser (0);
       public static dispenser9: FlareDispenser:= new FlareDispenser(30);
       public static dispenser 10: Flare Dispenser := new Flare Dispenser (60);
       public static dispenser11: FlareDispenser:= new FlareDispenser(90);
```

end FighterAircraft

3 The Environment Class

```
io:IO:=new\ IO\ ();
          inlines: inline^*:=[];
          busy: \mathbb{B}:=\mathsf{true};
          outlines : outline^* := [];
         ranges : \mathbb{N} \xrightarrow{m} (Angle \times Angle) := \{ \mapsto \};
         sensors : \mathbb{N} \xrightarrow{m} Sensor := \{ \mapsto \};
         inv dom ranges = dom sensors
          evid : [EventId] := nil;
operations
public
         Environment: \mathsf{char}^* \stackrel{o}{\to} Environment
         Environment (fname) \triangle
            def mk-(-,input) = io.freadval[inline^*](fname) in
            inlines := input;
public
          addSensor : Sensor \xrightarrow{o} ()
          addSensor(psens) \triangleq
                 dcl\ id: \mathbb{N} := card\ dom\ ranges + 1;
                  atomic ( ranges := ranges \bowtie \{id \mapsto psens.getAperature()\};
                       sensors := sensors \bowtie \{id \mapsto psens\}
            );
private
          createSignal: () \xrightarrow{o} [EventId]
          createSignal() \triangleq
                 if len inlines > 0
                  then (
                             dcl\ curtime : \mathbb{N} := World `timerRef. GetTime" (),
                                  done: \mathbb{B}:=\mathsf{false};
                             while \neg done
                             do def mk-(eventid, pmt, pa, pt) = hd inlines in
                                 if pt < curtime
                                 then ( for all id \in \text{dom } ranges
```

```
do def mk- (papplhs, pappsize) = ranges(id)
in
                                                if canObserve(pa, papplhs, pappsize)
                                                then sensors (id) .trip(eventid, pmt, pa);
                                             inlines := tl \ inlines;
                                             done := len inlines = 0;
                                             {\tt return}\ event id
                                            done := true;
                                 else (
                                            return nil
                             busy := false;
                             return nil
            );
public
          handleEvent: EventId \times FlareType \times Angle \times \mathbb{N} \times \mathbb{N} \stackrel{o}{\rightarrow} ()
          handleEvent (evid, pfltp, angle, pt1, pt2) \triangleq
                  outlines := outlines \cap [mk-(evid, pfltp, angle, pt1, pt2)]
            );
public
         showResult: () \xrightarrow{o} ()
         showResult() \triangle
            def - = io.writeval[outline^*](outlines) in
            skip;
public
         isFinished: () \stackrel{o}{\rightarrow} ()
          isFinished() \triangle
            skip;
         ResponseStarted: () \stackrel{o}{\rightarrow} ()
          ResponseStarted() \triangleq
             evid := nil
sync
         mutex(handleEvent);
         per isFinished \Rightarrow \neg busy;
         per ResponseStarted \Rightarrow evid \in \{out.\#1 \mid out \in elems \ outlines\}
thread
         while true
```

Name	#Calls	Coverage
Total Coverage		1%

4 The Global Class

```
class GLOBAL
values
public
        SENSOR-APERATURE = 90;
public
        FLARE-APERATURE = 120;
public
        DISPENSER-APERATURE = 30
types
        public MissileType = MissileA | MissileB | MissileC | None;
        public FlareType = FlareOneA | FlareTwoA | DoNothingA |
                            FLAREONEB | FLARETWOB | DONOTHINGB |
                            FLAREONEC | FLARETWOC | DONOTHINGC;
        public Angle = \mathbb{N}
        inv num \triangleq num < 360;
        \mathsf{public}\ \mathit{EventId} = \mathbb{N}
operations
public
        canObserve: Angle \times Angle \times Angle \stackrel{o}{\rightarrow} \mathbb{B}
        canObserve\ (pangle, pleft, psize) \triangleq
          def pright = (pleft + psize) \mod 360 in
          if pright < pleft
          then return (pangle < pright \lor pangle \ge pleft)
          else return (pangle \ge pleft \land pangle < pright);
```

```
\begin{array}{c} \textit{public} \\ \textit{getAperature}: () \overset{o}{\rightarrow} \textit{Angle} \times \textit{Angle} \\ \textit{getAperature} () \overset{\triangle}{\subseteq} \\ \text{is subclass responsibility} \\ \text{end } \textit{GLOBAL} \\ \textbf{Test Suite}: \quad \text{vdm.tc} \\ \textbf{Class}: \qquad \text{GLOBAL} \end{array}
```

Name	#Calls	Coverage
GLOBAL'canObserve	77	$\sqrt{}$
GLOBAL'getAperature	0	0%
Total Coverage		96%

5 Sensor Class

```
class Sensor is subclass of GLOBAL
instance variables
        private detector : MissileDetector;
        private aperature : Angle;
operations
public
        Sensor: Missile Detector \times Angle \xrightarrow{o} Sensor
        Sensor(pmd, psa) \triangleq
               detector := pmd;
               aperature := psa
          );
public
        getAperature: () \xrightarrow{o} GLOBAL'Angle \times GLOBAL'Angle
        getAperature() \triangleq
          return mk- (aperature, SENSOR-APERATURE);
public
        trip : EventId \times MissileType \times Angle \xrightarrow{o} ()
        trip(evid, pmt, pa) \triangleq detector.
          addThreat(evid, pmt, pa, World'timerRef.GetTime())
        pre canObserve (pa, aperature, SENSOR-APERATURE)
\mathsf{end}\ Sensor
     Test Suite:
                       vdm.tc
     Class:
                       Sensor
```

Name	#Calls	Coverage
Sensor'trip	7	61%
Sensor'Sensor	4	
Sensor'getAperature	4	$\sqrt{}$
Total Coverage		77%

6 Missile Detector Class

```
class MissileDetector is subclass of GLOBAL
instance variables
          ranges : \mathbb{N} \xrightarrow{m} (Angle \times Angle) := \{ \mapsto \};
          controllers: \mathbb{N} \xrightarrow{m} FlareController:= \{ \mapsto \};
          inv dom ranges = dom \ controllers
          threats: (EventId \times MissileType \times Angle \times \mathbb{N})^* := [];
          busy : \mathbb{B} := false;
operations
public
           addController: FlareController \stackrel{o}{\rightarrow} ()
           addController(pctrl) \triangleq
                   dcl\ nid: \mathbb{N}:= card\ dom\ ranges+1;
                   atomic ( ranges := ranges \bowtie \{ nid \mapsto pctrl.getAperature () \};
                         controllers := controllers \boxminus \{nid \mapsto pctrl\}
                   );
start
(pctrl)
             );
public
           addThreat: EventId \times MissileType \times Angle \times \mathbb{N} \stackrel{o}{\rightarrow} ()
           addThreat(evid, pmt, pa, pt) \triangleq
                   threats := threats \cap [mk-(evid, pmt, pa, pt)];
                   busy := true
             );
private
          getThreat: () \xrightarrow{o} EventId \times MissileType \times Angle \times \mathbb{N}
          qetThreat() \triangle
                   dcl\ res: EventId \times MissileType \times Angle \times \mathbb{N} := hd\ threats;
```

```
threats := tl \ threats;
                return res
           );
public
        isFinished: () \stackrel{o}{\rightarrow} ()
         isFinished() \triangleq
           for all id \in \text{dom } controllers
                             (id ) .isFinished()
           do controllers
sync
         mutex(addThreat, getThreat);
        per qetThreat \Rightarrow len threats > 0;
        per isFinished \Rightarrow \neg busy
thread
        while true
                def mk-(evid, pmt, pa, pt) = getThreat() in
        do (
                 for all id \in \text{dom } ranges
                 do def mk-(papplhs, pappsize) = ranges(id) in
                    if canObserve(pa, papplhs, pappsize)
                    then controllers
                                          (id) . addThreat(evid, pmt, pa, pt);
                 busy := len \ threats > 0
{\tt end}\ {\it Missile Detector}
     Test Suite:
                        vdm.tc
     Class:
                        MissileDetector
```

Name	#Calls	Coverage
MissileDetector'addThreat	7	√
MissileDetector'getThreat	7	$\sqrt{}$
MissileDetector'isFinished	1	$\sqrt{}$
MissileDetector'addController	3	$\sqrt{}$
Total Coverage		100%

7 Flare Controller Class

```
class FlareController is subclass of GLOBAL instance variables  \begin{array}{c} \text{private } aperature: Angle; \\ ranges: \mathbb{N} \xrightarrow{m} (Angle \times Angle) := \{ \mapsto \}; \\ dispensers: \mathbb{N} \xrightarrow{m} FlareDispenser: = \{ \mapsto \}; \end{array}
```

```
inv dom ranges = dom dispensers
         threats: (EventId \times Missile Type \times Angle \times \mathbb{N})^* := [];
          busy : \mathbb{B} := \mathsf{false};
operations
public
          FlareController: Angle \xrightarrow{o} FlareController
          FlareController(papp) \triangleq
             aperature := papp;
public
          addDispenser : FlareDispenser \xrightarrow{o} ()
          addDispenser(pfldisp) \triangleq
            let angle = aperature + pfldisp.GetAngle () in
                 dcl\ id: \mathbb{N} := card\ dom\ ranges + 1;
                  atomic ( ranges := ranges \bowtie \{id \mapsto \mathsf{mk-}(angle, DISPENSER-APERATURE)\};
                       dispensers := dispensers \boxminus \{id \mapsto pfldisp\}
                  );
start
(pfldisp)
            );
public
         getAperature: () \xrightarrow{o} GLOBAL'Angle \times GLOBAL'Angle
         getAperature() \triangleq
            return mk-(aperature, FLARE-APERATURE);
public
          addThreat: EventId \times MissileType \times Angle \times \mathbb{N} \stackrel{o}{\rightarrow} ()
          addThreat(evid, pmt, pa, pt) \triangleq
                  threats := threats \cap [mk-(evid, pmt, pa, pt)];
                  busy := true
            );
private
         qetThreat: () \xrightarrow{o} EventId \times MissileType \times Angle \times \mathbb{N}
         getThreat() \triangleq
                 dcl\ res: EventId \times MissileType \times Angle \times \mathbb{N} := hd\ threats;
                  threats := tl \ threats;
                  return res
            );
public
```

```
isFinished: () \stackrel{o}{\rightarrow} ()
          isFinished() \triangleq
             for all id \in \text{dom } dispensers
             do dispensers
                                   (id) .isFinished()
sync
          mutex(addThreat, getThreat);
          per getThreat \Rightarrow len threats > 0;
          per isFinished \Rightarrow \neg busy
thread
               for all id \in \text{dom } dispensers
               do
start
(dispensers
                    (id);
               while true
                        \mathsf{def}\ \mathsf{mk-}\left(\mathit{evid},\mathit{pmt},\mathit{pa},\mathit{pt}\right) = \mathit{getThreat}\left(\right)\ \mathsf{in}
               do (
                         for all id \in \text{dom } ranges
                         do def mk-(papplhs, pappsize) = ranges(id) in
                            if canObserve(pa, papplhs, pappsize)
                            then dispensers
                                                    (id) .addThreat(evid, pmt, pt);
                         busy := len \ threats > 0
                   )
{\tt end} \ \mathit{FlareController}
      Test Suite:
                            vdm.tc
                            FlareController
      Class:
```

Name	#Calls	Coverage
FlareController'addThreat	7	$\sqrt{}$
FlareController'getThreat	7	$\sqrt{}$
FlareController'isFinished	3	
FlareController'addDispenser	12	$\sqrt{}$
FlareController'getAperature	3	$\sqrt{}$
FlareController 'FlareController	3	
Total Coverage		100%

8 Flare Dispenser Class

class ${\it FlareDispenser}$ is subclass of ${\it GLOBAL}$ values

```
responseDB: MissileType \xrightarrow{m} Plan = \{MissileA \mapsto [mk-(FlareOneA, 900), \}
                                                         mk-(FLARETWOA, 500),
                                                         mk-(DoNothingA, 100),
                                                         mk-(FLAREONEA, 500)],
                                                        MISSILEB \mapsto [mk-(FLARETWOB, 500),
                                                         mk-(FLARETWOB, 700)],
                                                         MISSILEC \mapsto [mk-(FLAREONEC, 400),
                                                         mk-(DoNothingC, 100),
                                                         mk-(FLARETWOC, 400),
                                                         mk-(FLAREONEC, 500)];
         missilePriority: MissileType \xrightarrow{m} \mathbb{N} = \{ \text{None} \mapsto 0, \}
                                                        MISSILEA \mapsto 1,
                                                        MISSILEB \mapsto 2,
                                                        MISSILEC \mapsto 3
types
         public Plan = PlanStep^*;
         public PlanStep = FlareType \times \mathbb{N}
instance variables
         public curplan : Plan := [];
         curprio: \mathbb{N}:=0;
         busy : \mathbb{B} := \mathsf{false};
         angle : \mathbb{N};
         eventid : [EventId];
operations
public
         FlareDispenser : \mathbb{N} \xrightarrow{o} FlareDispenser
         FlareDispenser(ang) \triangleq
                 angle := ang
            );
public
         GetAngle: () \stackrel{o}{\rightarrow} \mathbb{N}
         GetAngle() \triangle
            return angle;
public
         addThreat: EventId \times MissileType \times \mathbb{N} \stackrel{o}{\rightarrow} ()
         addThreat(evid, pmt, ptime) \triangleq
            if missilePriority(pmt) > curprio
            then (
                      dcl\ newplan : Plan := [],
                           newtime : \mathbb{N} := ptime;
```

```
for mk- (fltp, fltime) in responseDB (pmt)
                              newplan := newplan \curvearrowright [mk-(fltp, newtime)];
                              newtime := newtime + fltime
                         );
                      def mk-(fltp, fltime) = hd newplan in
                      releaseFlare(evid, fltp, fltime, World'timerRef.GetTime());
                      curplan := tl \ newplan;
                      eventid := evid;
                      curprio := missilePriority(pmt);
                      busy := true
                );
private
        evalQueue: () \xrightarrow{o} ()
         evalQueue() \triangle
               if len curplan > 0
                then (
                          dcl\ curtime : \mathbb{N} := World `timerRef.GetTime" (),
                              done : \mathbb{B} := false;
                          while \neg done
                                  dcl\ first: PlanStep := hd\ curplan,
                          do (
                                       next: Plan := tl \ curplan;
                                   let mk-(fltp, fltime) = first in
                                       if fltime \leq curtime
                                                 releaseFlare(eventid, fltp, fltime, curtime);
                                                  curplan := next;
                                                  if len next = 0
                                                  then (
                                                            curprio := 0;
                                                            done := true;
                                                            busy := false
                                       else done := true
                     )
           );
private
        releaseFlare: EventId \times FlareType \times \mathbb{N} \times \mathbb{N} \stackrel{o}{\rightarrow} ()
        releaseFlare\ (evid, pfltp, pt1, pt2) \triangleq World'env.
           handleEvent(evid, pfltp, angle, pt1, pt2);
public
```

```
isFinished: () \stackrel{o}{\rightarrow} ()
         isFinished() \triangleq
            skip
sync
         mutex(addThreat, evalQueue);
         per isFinished \Rightarrow \neg busy
thread
         while true
                  World `timerRef. \textit{WaitRelative}(\textit{TimeStamp}` stepLength) ;
         do (
                  evalQueue()
\verb|end|| Flare Dispenser|
      Test Suite:
                          vdm.tc
      Class:
                          FlareDispenser
```

Name	#Calls	Coverage
FlareDispenser'GetAngle	12	$\sqrt{}$
FlareDispenser'addThreat	7	
FlareDispenser'evalQueue	4753	
FlareDispenser'isFinished	12	$\sqrt{}$
FlareDispenser'releaseFlare	21	$\sqrt{}$
FlareDispenser 'FlareDispenser	12	
Total Coverage		100%

9 The WaitNotify Class

```
class WaitNotify instance variables waitset: \mathbb{N}\text{-set}:= \{\}; operations \mathsf{public} Wait: () \xrightarrow{o} () \\ Wait: () \xrightarrow{\triangle} \\ ( \quad AddToWaitSet(\mathsf{threadid}) \ ; \\ \quad Awake() \\ ); \mathsf{public}
```

```
Notify : () \stackrel{o}{\rightarrow} ()
           Notify\left(\right)\triangleq
              let p \in waitset in
              waitset := waitset \setminus \{p\};
public
           NotifyThread: \mathbb{N} \stackrel{o}{\rightarrow} ()
           NotifyThread(tId) \triangleq
              waitset := waitset \setminus \{tId\};
public
           NotifyAll: () \xrightarrow{o} ()
           NotifyAll() \triangleq
              waitset := \{\};
private
           AddToWaitSet: \mathbb{N} \stackrel{o}{\rightarrow} ()
           AddToWaitSet(n) \triangleq
              waitset := waitset \cup \{n\};
private
           Awake:()\stackrel{o}{\rightarrow}()
           Awake() \triangleq
              skip
sync
           per Awake \Rightarrow threadid \notin waitset;
           mutex(AddToWaitSet)
end WaitNotify
      Test Suite:
                              vdm.tc
      Class:
                              WaitNotify
```

Name	#Calls	Coverage
WaitNotify'Wait	4776	$\sqrt{}$
WaitNotify'Awake	4754	
WaitNotify'Notify	0	0%
WaitNotify'NotifyAll	0	0%
WaitNotify'AddToWaitSet	4776	
WaitNotify'NotifyThread	4650	
Total Coverage		60%

10 TimeStamp Class

class TimeStamp is subclass of WaitNotify

```
values
public
          stepLength : \mathbb{N} = 10
instance variables
          currentTime : \mathbb{N} := 0;
          wakeUpMap : \mathbb{N} \xrightarrow{m} \mathbb{N} := \{ \mapsto \};
operations
public
          WaitRelative : \mathbb{N} \stackrel{o}{\rightarrow} ()
          WaitRelative(val) \triangleq
                  AddToWakeUpMap(threadid, currentTime + val);
                   WaitNotify' Wait()
             );
public
          WaitAbsolute : \mathbb{N} \stackrel{o}{\rightarrow} ()
          WaitAbsolute(val) \triangleq
                  AddToWakeUpMap(threadid, val);
                   WaitNotify' Wait()
             );
          AddToWakeUpMap: \mathbb{N} \times \mathbb{N} \stackrel{o}{\rightarrow} ()
          AddToWakeUpMap(tId, val) \triangleq
             wakeUpMap := wakeUpMap \dagger \{tId \mapsto val\};
public
          NotifyThread: \mathbb{N} \stackrel{o}{\rightarrow} ()
          NotifyThread(tId) \triangleq
                  WaitNotify`NotifyThread(tId)
             );
public
          Notify: () \stackrel{o}{\rightarrow} ()
          Notify() \triangleq
             let tId \in \text{dom } wakeUpMap \text{ in }
             NotifyThread(tId);
public
          NotifyAll: () \xrightarrow{o} ()
          NotifyAll() \triangleq
                  wakeUpMap := \{ \mapsto \};
                   WaitNotify'NotifyAll()
             );
```

```
public
         NotifyAndIncTime: () \stackrel{o}{\rightarrow} ()
         NotifyAndIncTime() \triangleq
                 currentTime := currentTime + stepLength;
                 for all t \in \text{dom} (wakeUpMap \rhd \{currentTime\})
                 do NotifyThread(t)
public
         GetTime: () \stackrel{o}{\rightarrow} \mathbb{N}
         GetTime() \triangle
            {\tt return}\ current Time
sync
         mutex(AddToWakeUpMap, Notify, NotifyThread, NotifyAll)
\quad \text{end} \ \textit{TimeStamp}
     Test Suite:
                          vdm.tc
     Class:
                          TimeStamp
```

Name	#Calls	Coverage
TimeStamp'Notify	0	0%
TimeStamp'GetTime	1134	
TimeStamp'NotifyAll	0	0%
TimeStamp'NotifyThread	4650	\checkmark
TimeStamp'WaitAbsolute	0	0%
TimeStamp'WaitRelative	4777	$\sqrt{}$
TimeStamp'AddToWakeUpMap	4776	
TimeStamp'NotifyAndIncTime	200	
Total Coverage		73%

11 Standard IO Class

```
class IO types  \text{public } filedirective = \text{START} \mid \text{APPEND}  functions  \text{public} \\ writeval[@p]: @p \rightarrow \mathbb{B} \\ writeval(val) \triangleq \\ \text{is not yet specified;}  public
```

```
fwriteval[@p] : char^+ \times @p \times filedirective \rightarrow \mathbb{B}
             fwriteval (filename, val, fdir) \triangleq
                 is not yet specified;
public
             freadval[@p] : char^+ \to \mathbb{B} \times [@p]
              freadval(f) \triangleq
                  is not yet specified
               post let mk- (b, t) = RESULT in
                      \neg b \Rightarrow t = \text{nil}
operations
public
               echo: \mathsf{char}^* \overset{o}{\to} \mathbb{B}
               echo(text) \triangleq
                  fecho("", text, nil );
public
               fecho: \mathsf{char}^* \times \mathsf{char}^* \times [filedirective] \stackrel{o}{\to} \mathbb{B}
               fecho (filename, text, fdir) \triangleq
                   is not yet specified
                 pre \ \mathit{filename} = \verb""" \ \Leftrightarrow \ \mathit{fdir} = \verb"nil" \ ; 
public
               \mathit{ferror}:()\overset{o}{\to}\mathsf{char}^*
               ferror() \triangleq
                   is not yet specified
     \mathsf{end}\ IO
```