

High Dynamic Range Imaging

Introduction to Computational Photography:

EECS 395/495

Northwestern University

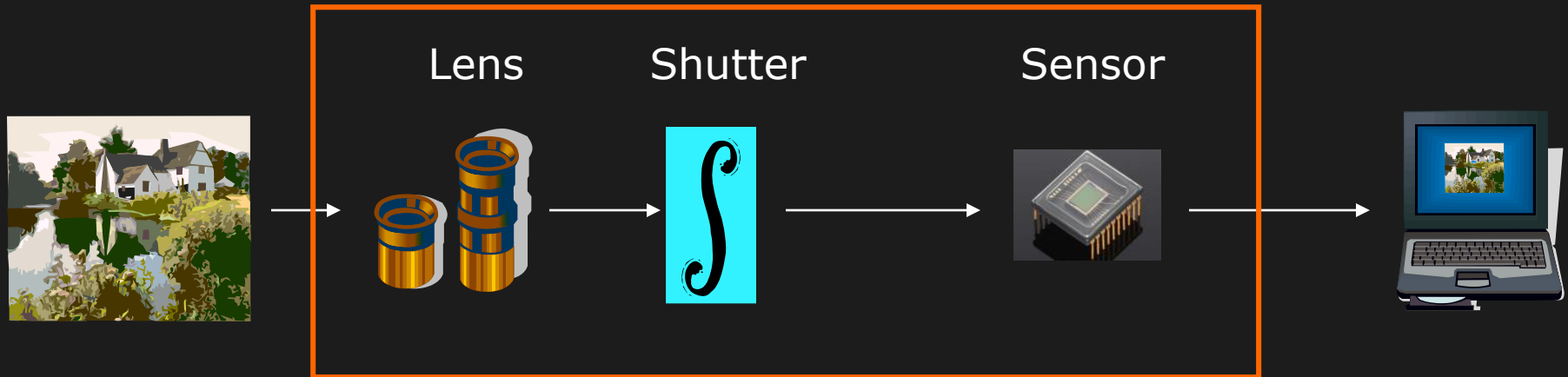
High Dynamic Range Imaging

How to extend the range of brightness values that can be represented by your digital camera

Topics:

- (1) Camera Response Function
- (2) Recovering High Dynamic Range Images
- (3) Tone-Mapping
- (4) Assorted Pixel Camera

From Radiance to Intensity

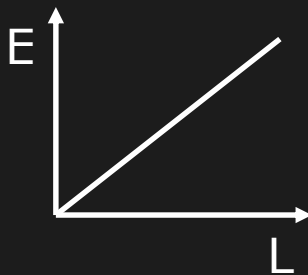


L: Scene
Radiance
watts/sr/m²

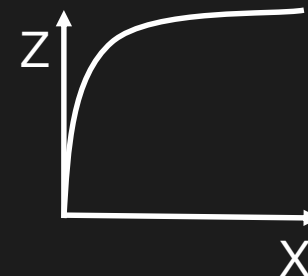
E: Image
Irradiance
watts/m²

X: Exposure
Value (EV)
J/m²

Z: Final
Digital Image
8bit Intensity



$$X = E \cdot \Delta t$$

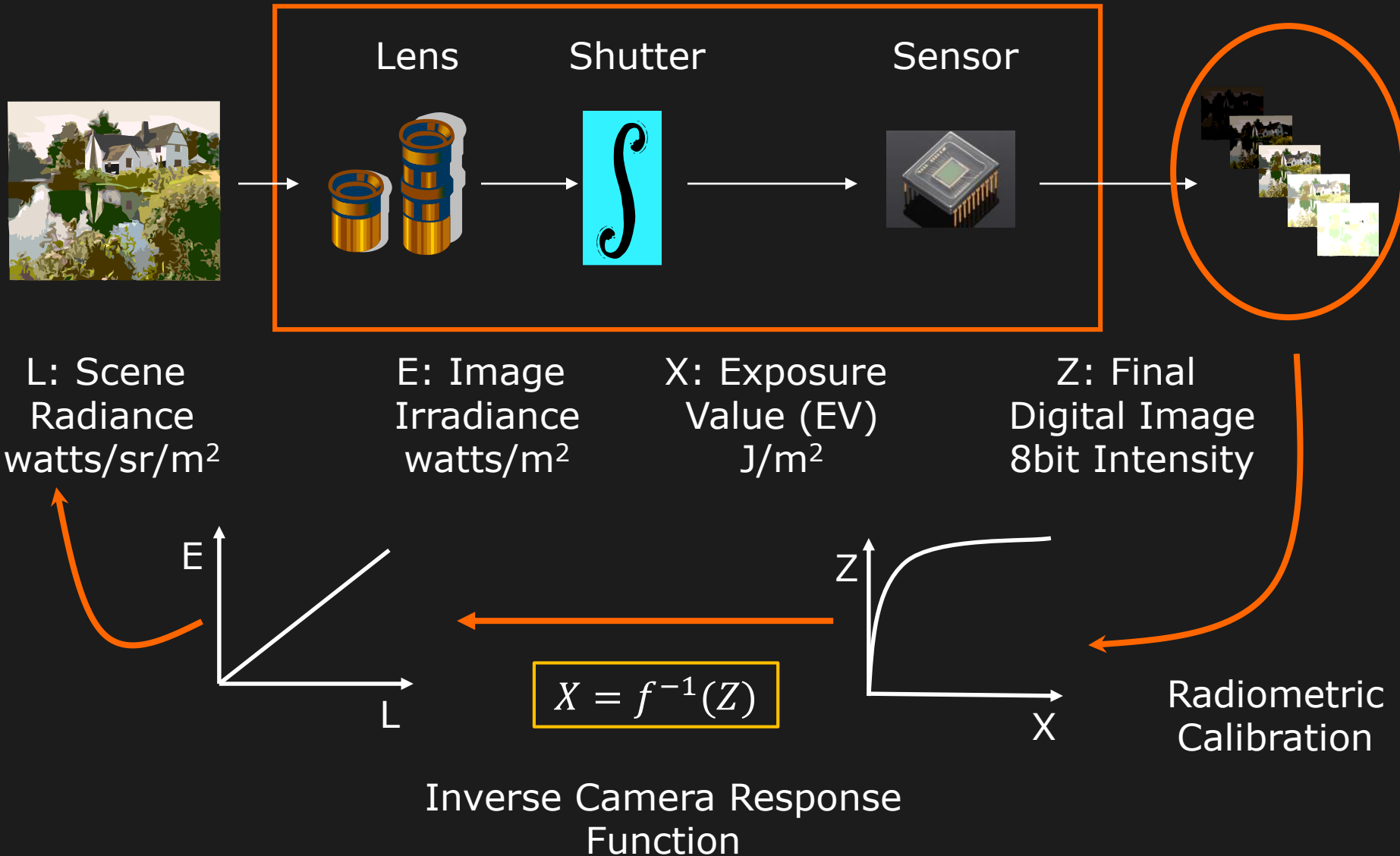


Camera
Response
Function

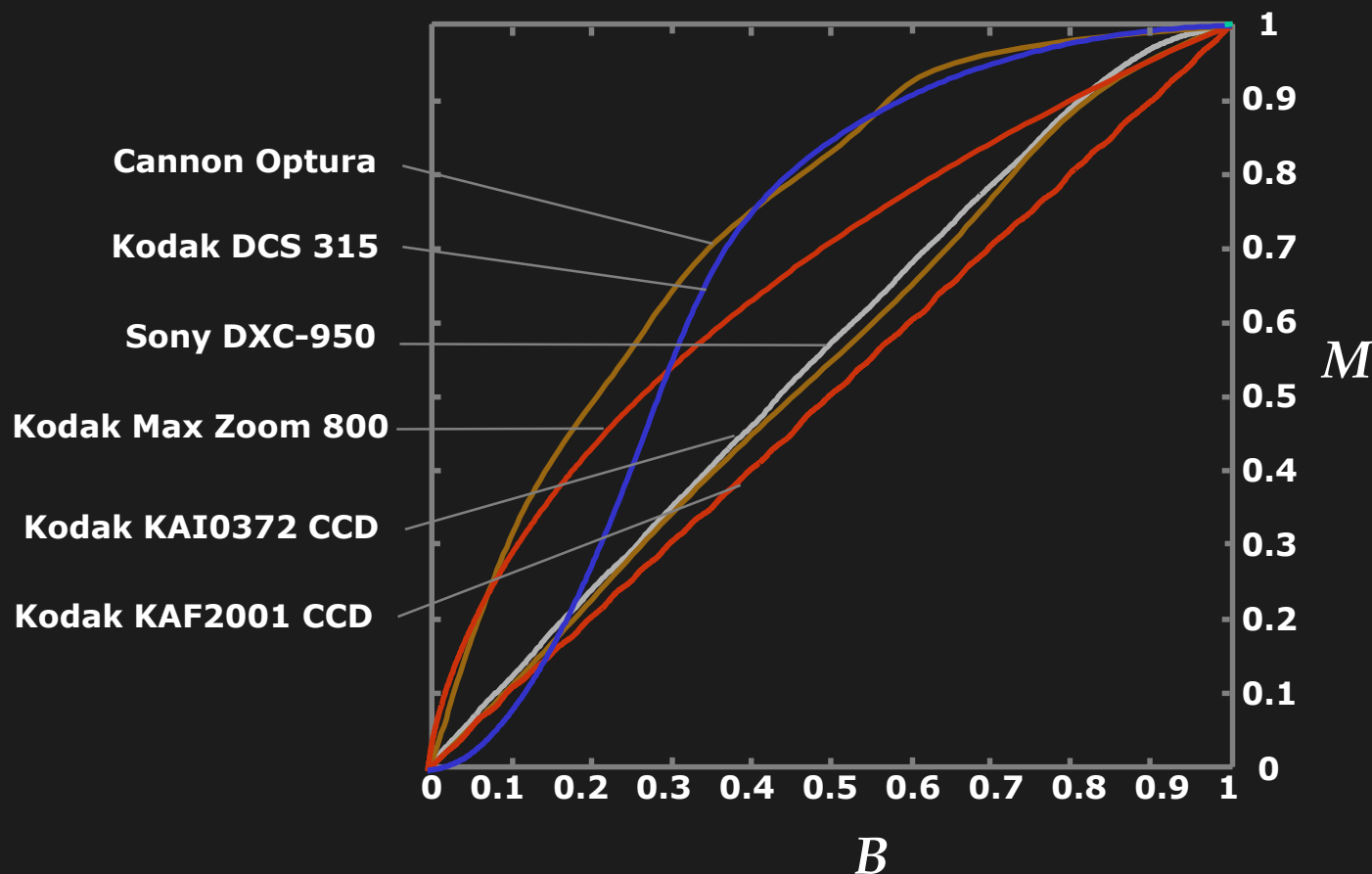
$$E = L \cdot \frac{\pi}{4} \left(\frac{d}{f} \right)^2 \cos^4 \alpha$$

$$Z = f(X)$$

From Intensity to Radiance



Camera Response Function $f(\cdot)$



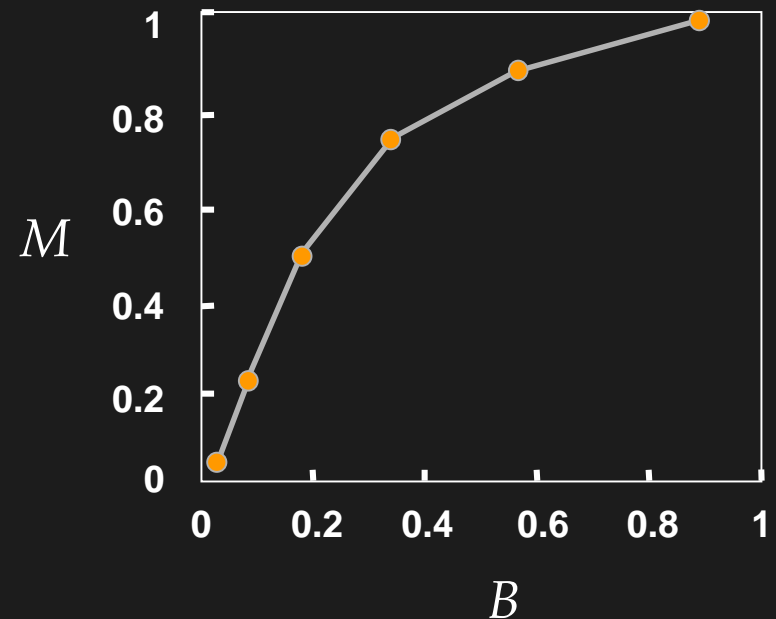
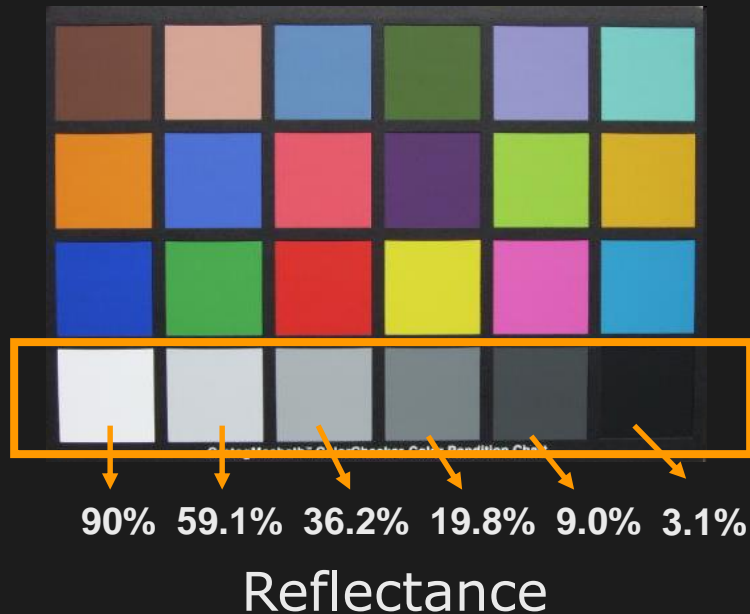
"Gamma Curves"

Radiometric Calibration: Finding $f(\cdot)$

Calibration using a chart:

1. Patches with known reflectance (when uniformly lit)
2. Fit linear segments or curve

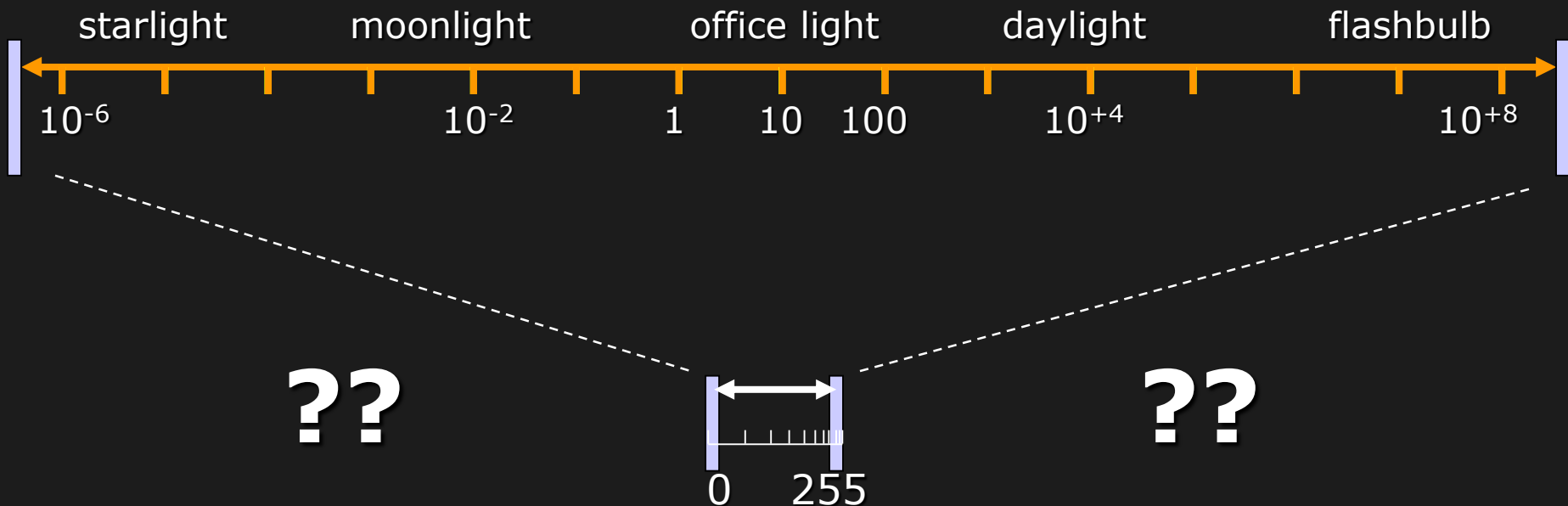
Macbeth Chart



Dynamic Range of Imaging

Domain of Human Vision:

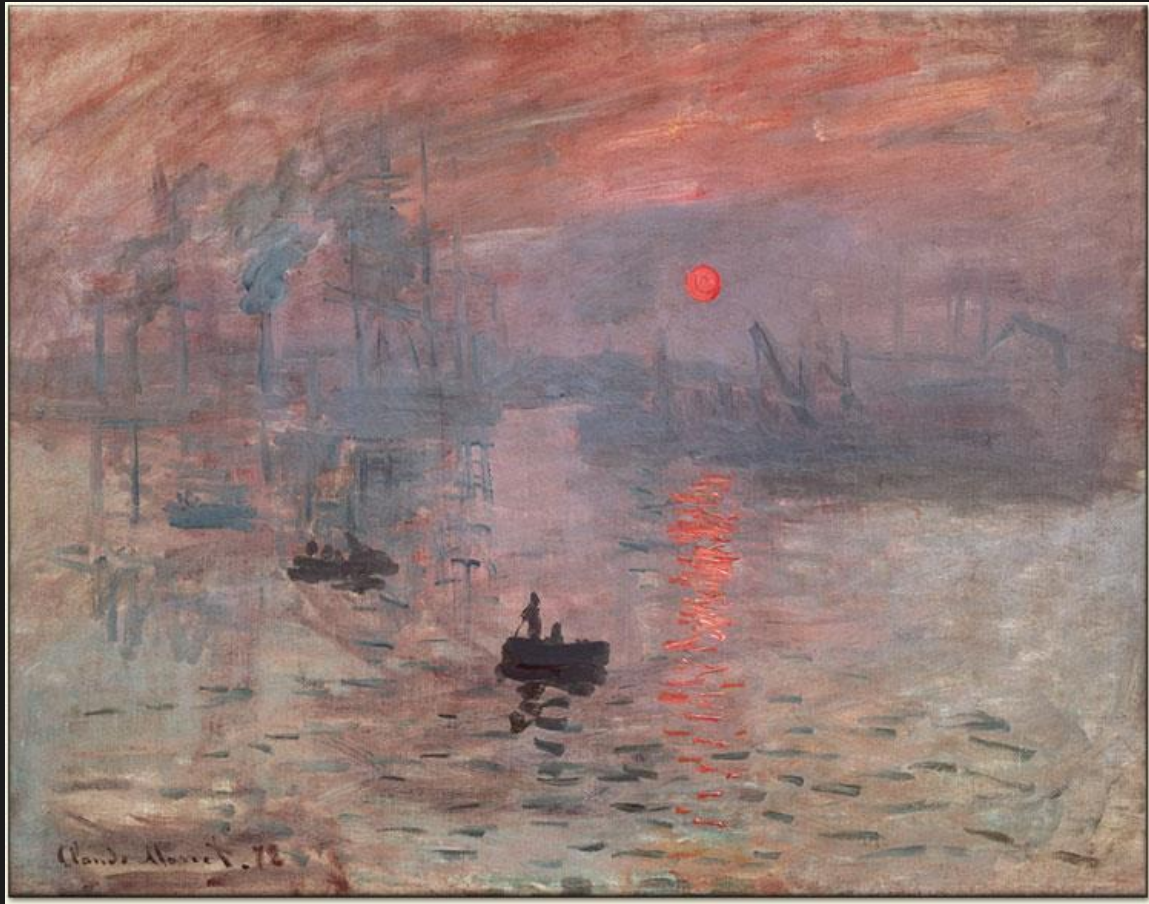
from $\sim 10^{-6}$ to $\sim 10^{+8}$ cd/m²



Range of Typical Displays:

from ~ 1 to ~ 100 cd/m²

Local Contrast and Perceived Higher Dynamic Range



Impression Sunrise, Claude Monet, 1873
<http://webexhibits.org/colorart/monet.html>

High Dynamic Range: Multiple Exposures

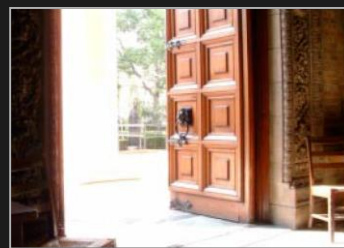
Assume Camera Response $f(\cdot)$ is Linear



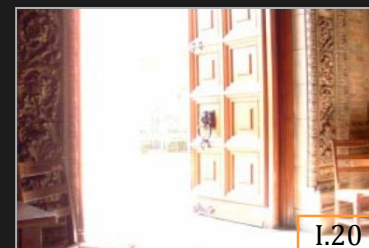
with t_0



t_1



t_2



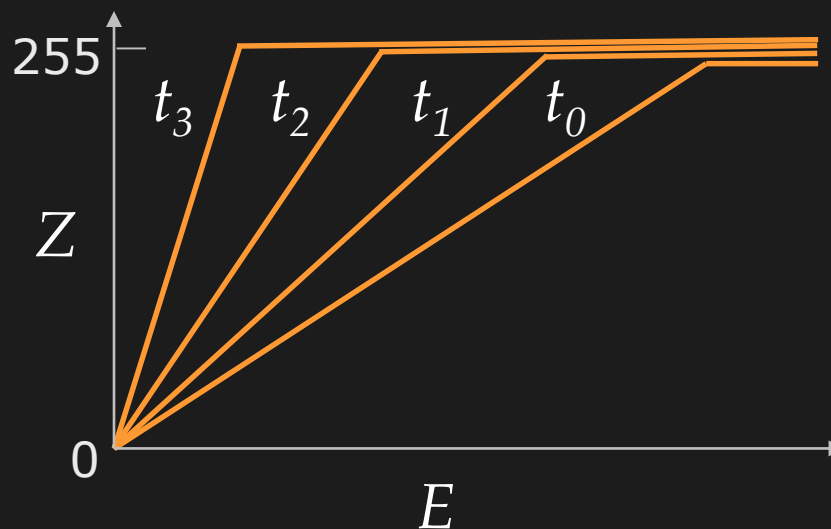
t_3

$$Z_0 = \min(t_0 \cdot E, 255)$$

$$Z_1 = \min(t_1 \cdot E, 255)$$

$$Z_2 = \min(t_2 \cdot E, 255)$$

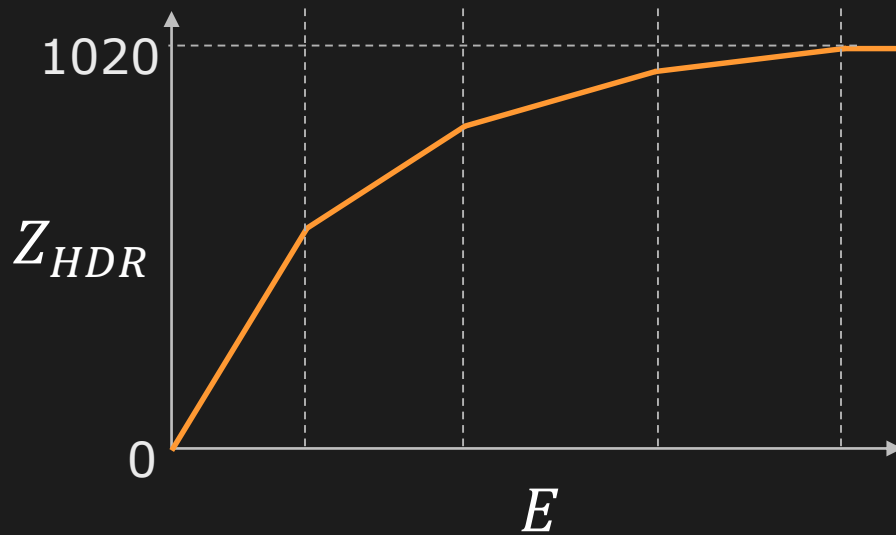
$$Z_3 = \min(t_3 \cdot E, 255)$$



High Dynamic Range: Multiple Exposures

$$\text{Aggregate Image: } Z_{HDR} = Z_0 + Z_1 + Z_2 + Z_3$$

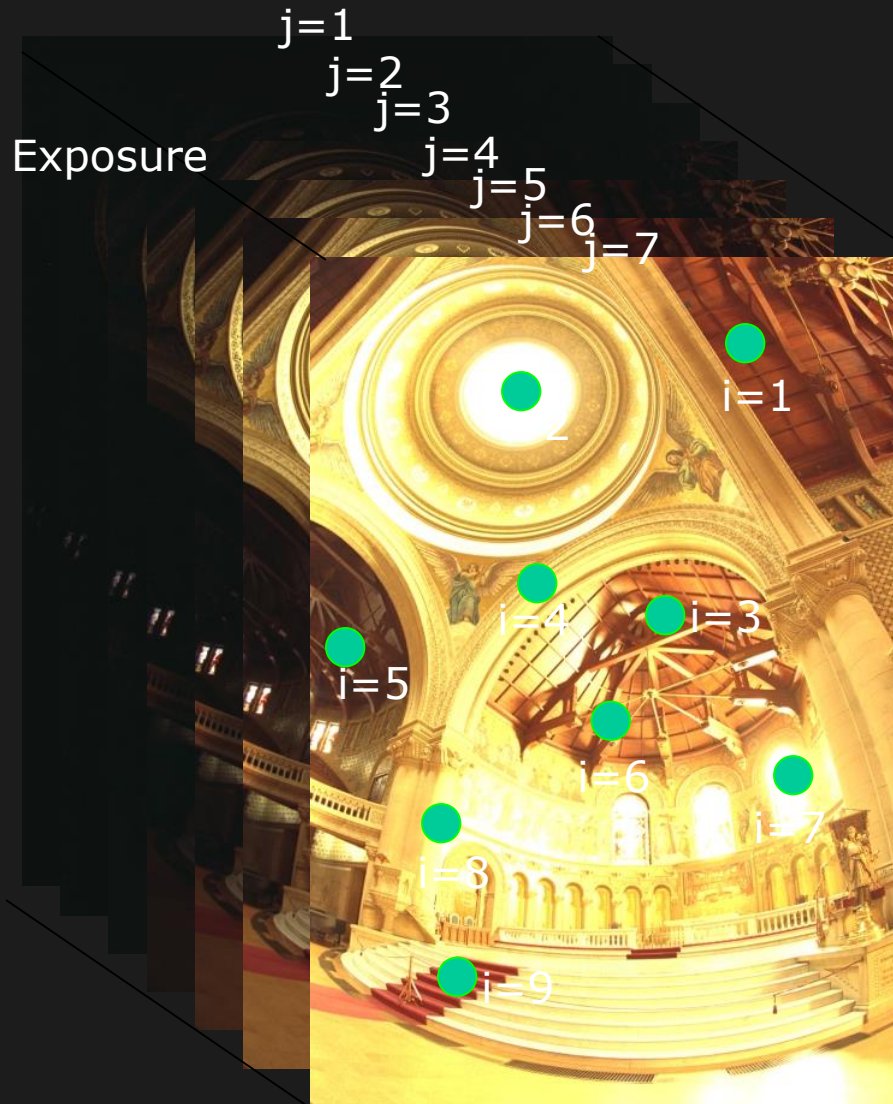
Camera Response $f(\cdot)$ for Aggregate Image:



HDR Imaging without a ColorChecker

- Input: multiple images of the same scene with different exposures
- Assumptions:
 - Lighting changes can be ignored.
 - Images should be registered well.
 - Camera response is the same for all pixels.
 - Working in the middle range of the response curve, where *reciprocity* will not fail.
 - Smooth, monotonic camera response curve

Proposed Algorithm

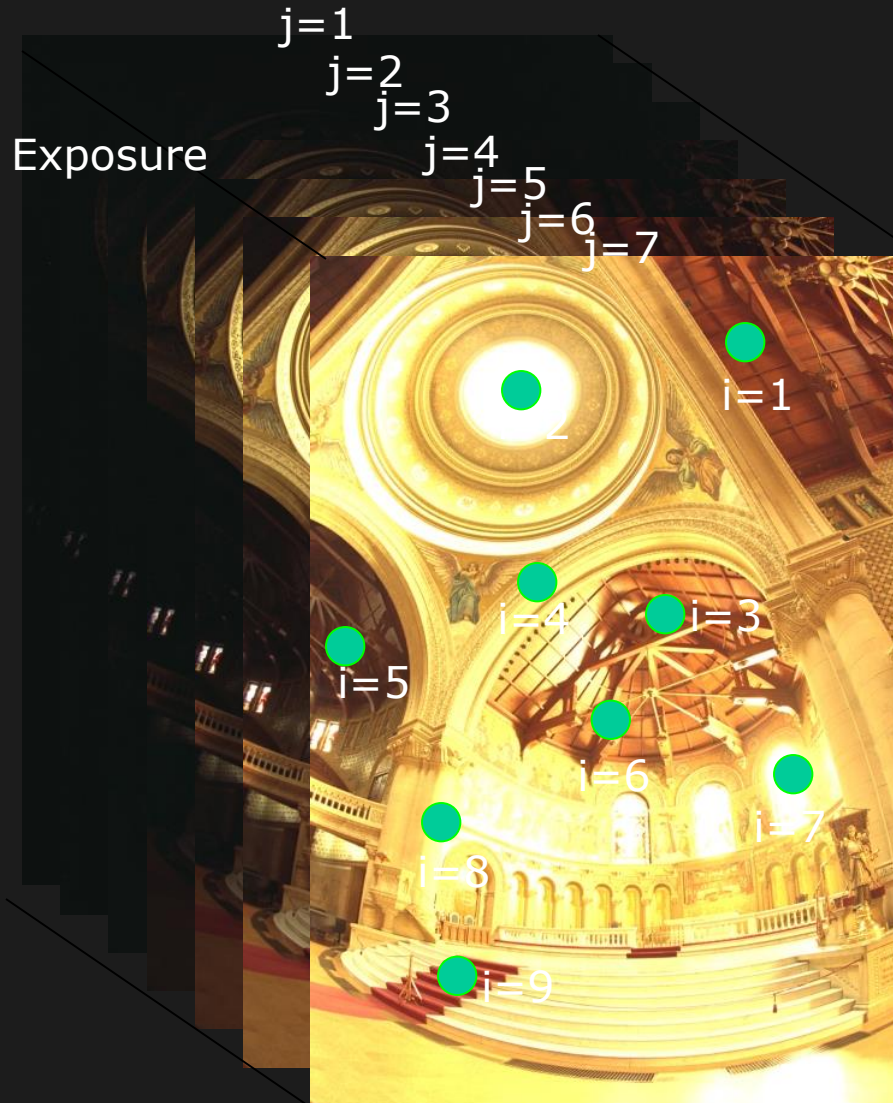


- Z_{ij} : image intensity of the i -th point in the j -th image.
- E_i : irradiance of the i -th point
- Δt_j : exposure time of the j -th image

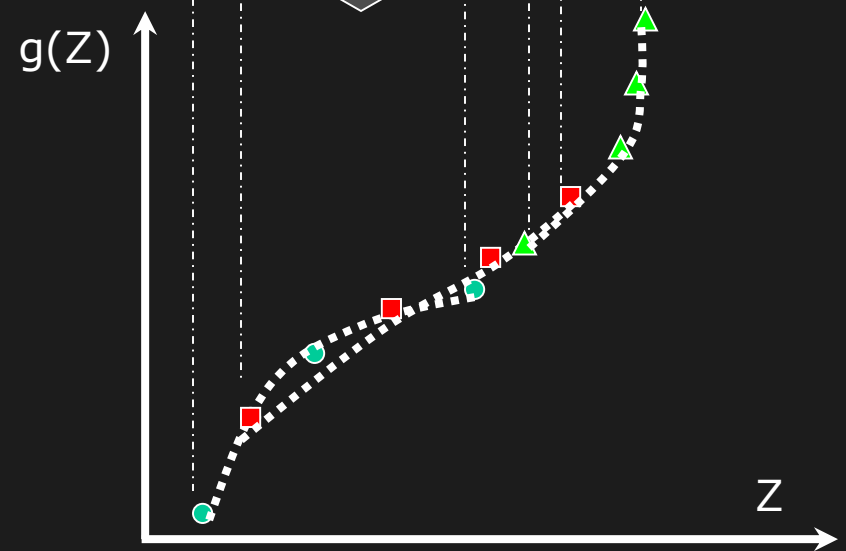
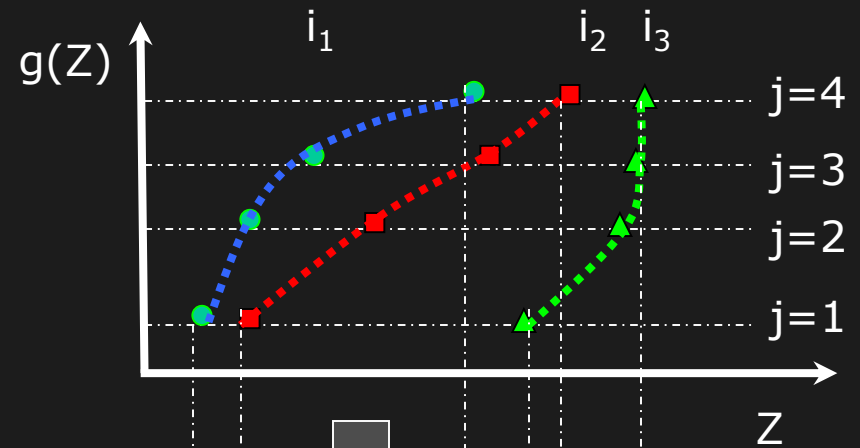
$$Z_{ij} = f(X) = f(E_i \Delta t_j)$$

$$g(Z_{ij}) = \ln f^{-1}(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

Proposed Algorithm



$$g(Z_{ij}) = \ln E_i + \ln \Delta t_j$$



Proposed Algorithm

$$g(Z_{ij}) = \ln E_i + \ln \Delta t_j$$

- $g(Z)$ is unknown, but only discrete values are enough under smooth assumption.
- $N \times P$ equations, $N + Z_{\max} - Z_{\min} + 1$ variables
- Thus, $g(Z)$ and $\ln E$ can be solved by minimizing:

$$\sum_{i=1}^N \sum_{j=1}^P \left[g(Z_{ij}) - \ln E_i - \ln \Delta t_j \right]^2 + \lambda \sum_{z=Z_{\min}+1}^{Z_{\max}-1} \left[g(z-1) - 2g(z) + g(z+1) \right]^2$$

Least Square Error Smoothness of $g(Z)$

Linear Least Square Problem
which can be robustly solved by SVD

Proposed Algorithm

- $g(Z)$ and E are solved up to a scale, but relative E are good enough for many applications.
- Weighting function is used to emphasize the central working range.



Optimization: Linear Least Square

$$\mathcal{O} = \sum_{i=1}^N \sum_{j=1}^P \{w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]\}^2 +$$

$$\lambda \sum_{z=Z_{min}+1}^{Z_{max}-1} [w(z)g''(z)]^2$$

1. Set partial derivatives zero
- 2.

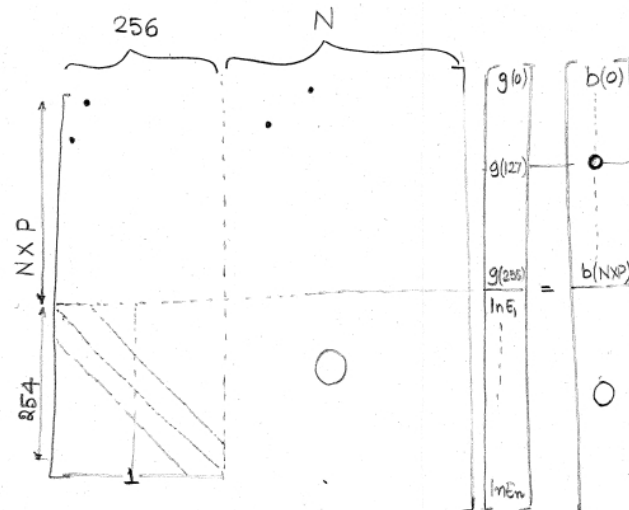
$$\min \sum_{i=1}^M (\mathbf{a}_i \mathbf{x} - \mathbf{b}_i)^2 \rightarrow \text{least - square solution of } \begin{bmatrix} \mathbf{a}_1 \\ \mathbf{a}_2 \\ \vdots \\ \mathbf{a}_N \end{bmatrix} \mathbf{x} = \begin{bmatrix} \mathbf{b}_1 \\ \mathbf{b}_2 \\ \vdots \\ \mathbf{b}_N \end{bmatrix}$$

Optimization: Linear Least Square

$$\sum_{i=1}^N \sum_{j=1}^P \left\{ w(z_{ij}) [g(z_{ij}) - \ln E_i - \ln \Delta t_j] \right\}^2 + \lambda \sum_{z=z_{min}+1}^{z=z_{max}-1} [w(z) g''(z)]^2 = 0$$

Least square Solver

$$[A]_{N \times P+256, 256+N} \{x\}_{256+N, 1} = \{b\}_{N \times P}$$



$$A_{ij} = W(z_{ij}) g(z_{ij}) - W(z_{ij}) \ln E_i \quad i \leq N \times P$$

$$= + \lambda W(z_{i-1}) - 2W(z_i) \lambda + \lambda W(z_{i+1}) \quad i > N \times P$$

$$b_{ij} = W(z_{ij}) \ln \Delta t_j$$

Proposed Algorithm

- Merging to HDR is straightforward once we know $g(Z)$:

$$\ln E_i = \frac{\sum_{j=1}^P w(Z_{ij}) (g(Z_{ij}) - \ln \Delta t_j)}{\sum_{j=1}^P w(Z_{ij})}$$

- For color images, do it for R, G, B channels separately, and scale them by the color balance of the radiance map, either achromatic or proportional to color of the light sources.

Matlab Code

Matlab code

```
%  
% gsolve.m - Solve for imaging system response function  
%  
% Given a set of pixel values observed for several pixels in several  
% images with different exposure times, this function returns the  
% imaging system's response function g as well as the log film irradiance  
% values for the observed pixels.  
%  
% Assumes:  
%  
%   Zmin = 0  
%   Zmax = 255  
%  
% Arguments:  
%  
%   Z(i,j) is the pixel values of pixel location number i in image j  
%   B(j)   is the log delta t, or log shutter speed, for image j  
%   l      is lamdba, the constant that determines the amount of smoothness  
%   w(z)   is the weighting function value for pixel value z  
%  
% Returns:  
%  
%   g(z)    is the log exposure corresponding to pixel value z  
%   lE(i)   is the log film irradiance at pixel location i  
%
```

Matlab Code

```
function [g,lE]=gsolve(Z,B,l,w)

n = 256;
A = zeros(size(Z,1)*size(Z,2)+n+1,n+size(Z,1));
b = zeros(size(A,1),1);

k = 1;                %% Include the data-fitting equations
for i=1:size(Z,1)
    for j=1:size(Z,2)
        wij = w(Z(i,j)+1);
        A(k,Z(i,j)+1) = wij; A(k,n+i) = -wij; b(k,1) = wij * B(i,j);
        k=k+1;
    end
end

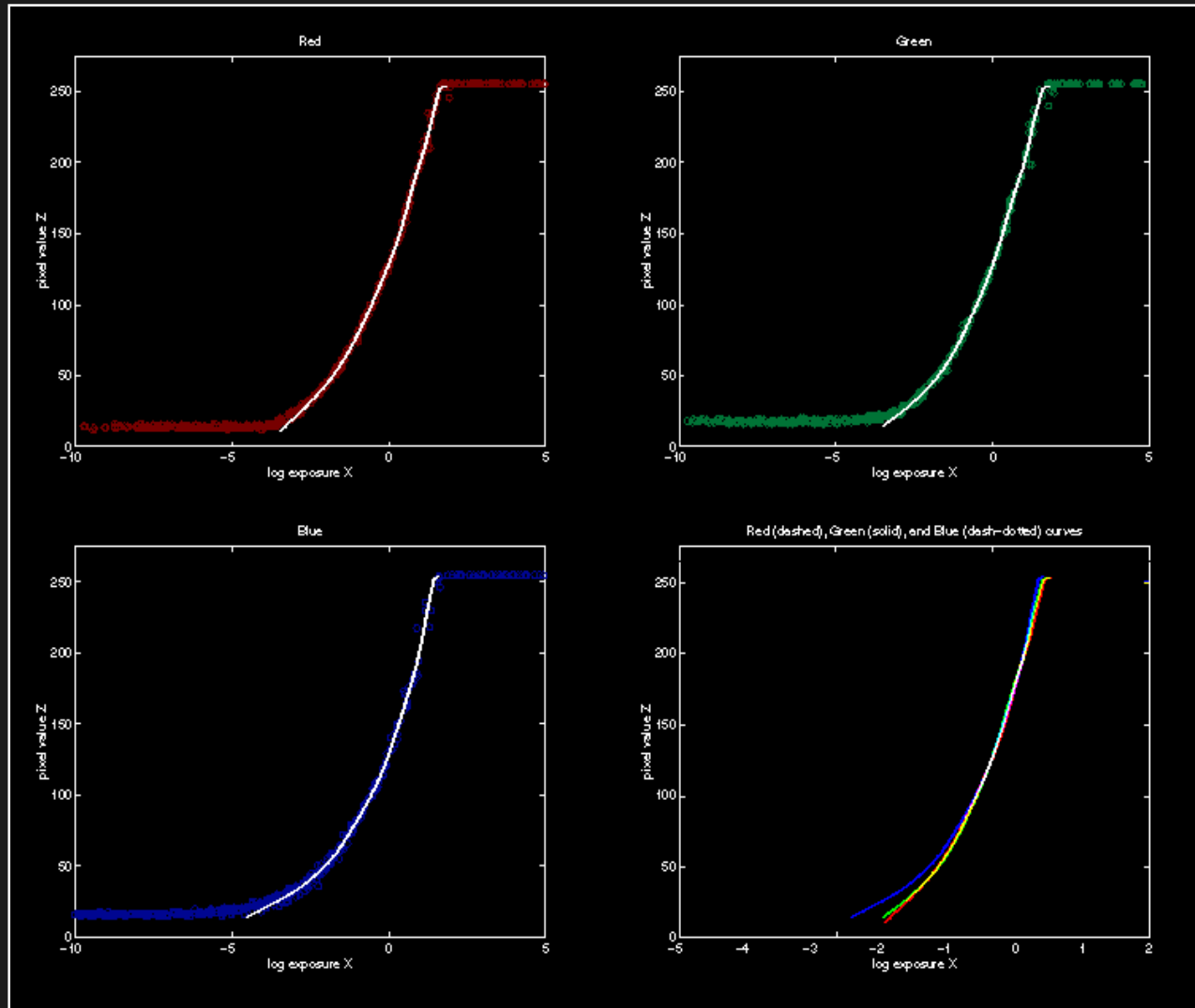
A(k,129) = 1;         %% Fix the curve by setting its middle value to 0
k=k+1;

for i=1:n-2           %% Include the smoothness equations
    A(k,i)=l*w(i+1); A(k,i+1)=-2*l*w(i+1); A(k,i+2)=l*w(i+1);
    k=k+1;
end

x = A\b;              %% Solve the system using SVD

g = x(1:n);
lE = x(n+1:size(x,1));
```

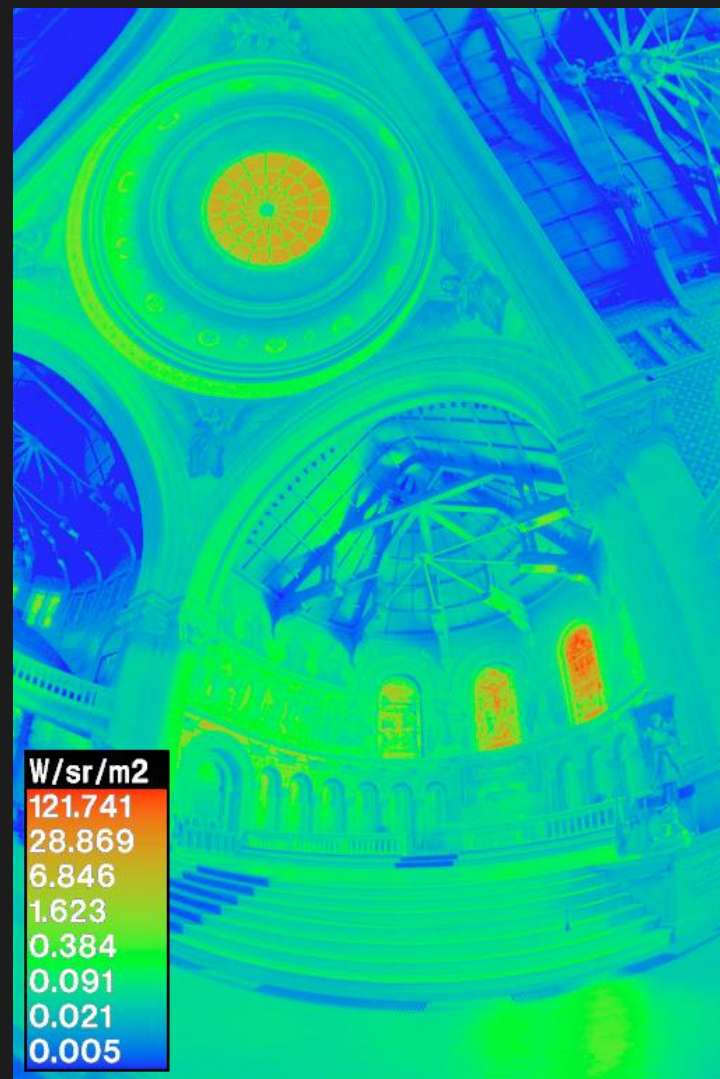
Recovered Response Function



Results



Original Photograph



Radiance Map

Radiance format (.pic, .hdr, .rad)

32 bits/pixel



$$\begin{aligned} (145, 215, 87, 149) &= \\ (145, 215, 87) * 2^{(149-128)} &= \\ (1190000, 1760000, 713000) \end{aligned}$$

$$\begin{aligned} (145, 215, 87, 103) &= \\ (145, 215, 87) * 2^{(103-128)} &= \\ (0.00000432, 0.00000641, & \\ 0.00000259) \end{aligned}$$

Ward, Greg. "Real Pixels," in Graphics Gems IV, edited by James Arvo, Academic Press, 1994

Rendering HDR Images: Tone Mapping

- Due to the limitation of current LDR 8-bit displays
- The goal is to compress the dynamic range of the input image and reproduce a realistic rendering based on human perception



Photograph



HDR



Photograph



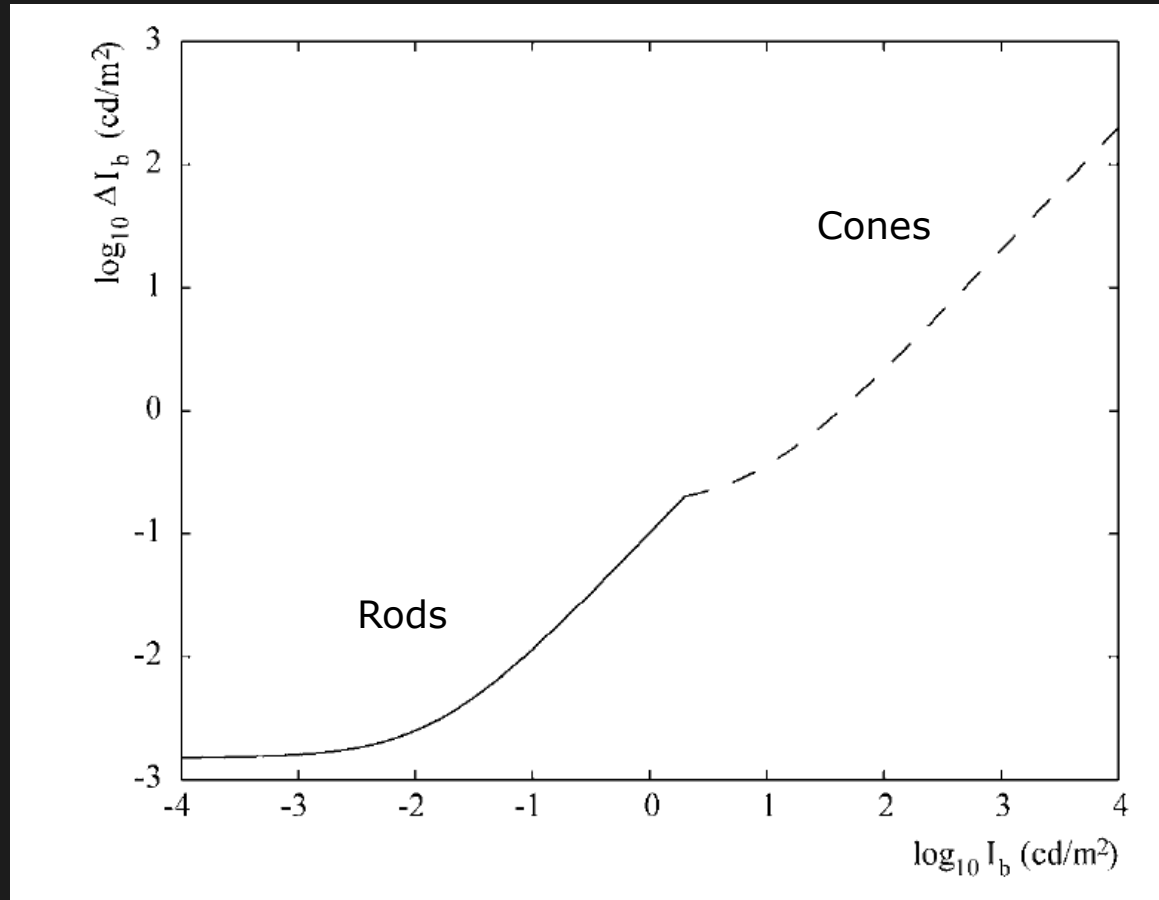
HDR

Human Visual Adaptation



FIGURE 6.4 Although the headlights are on in both images, during daylight our eyes are less sensitive to car headlights than at night.

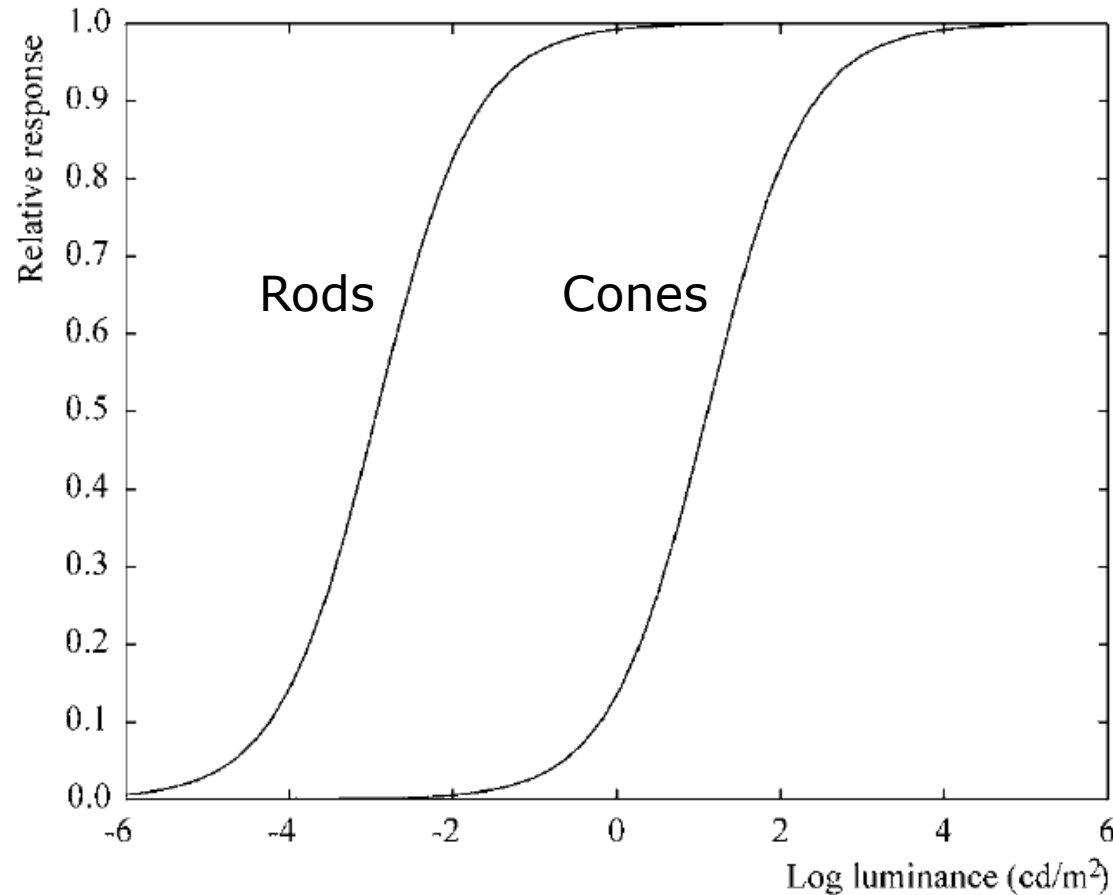
JND of Human Visual System



Weber's Law

$$\Delta I_b / I_b = \text{const}$$

Response Curves of Rods and Cones

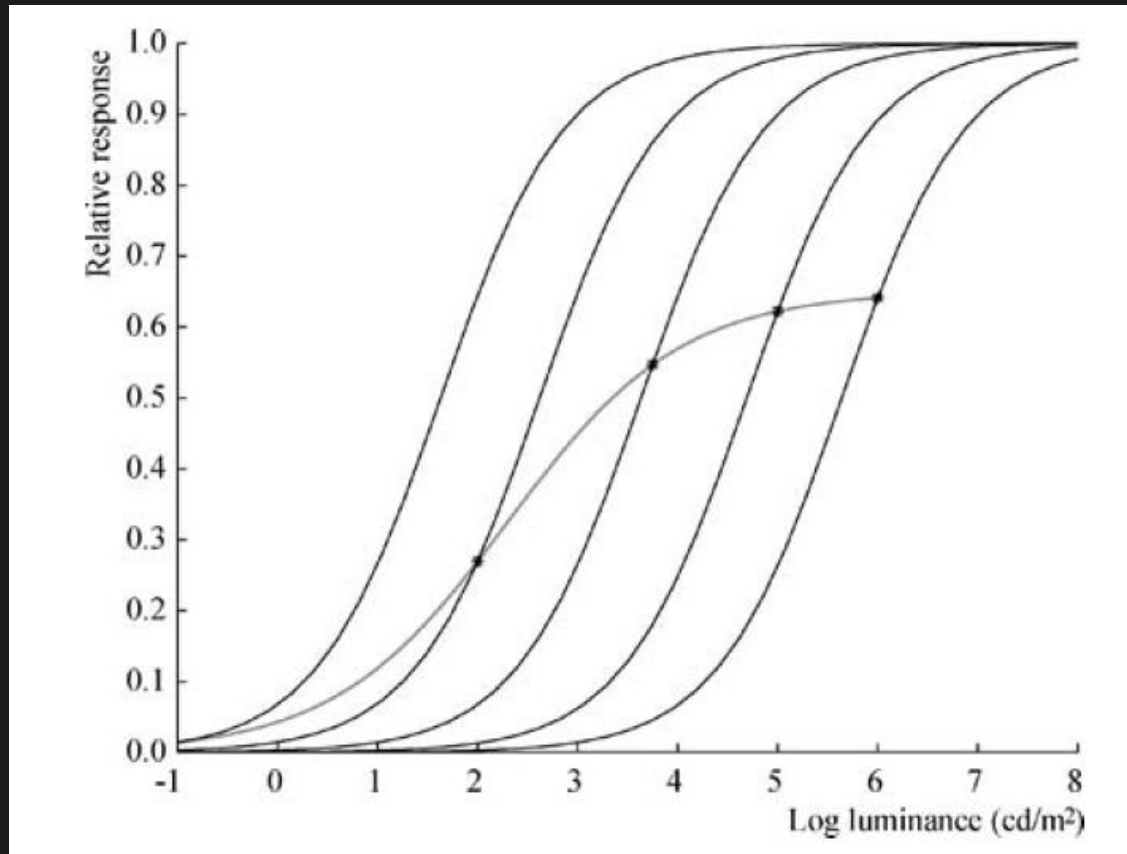


Michaelis-Menten Equation
(or, Naka-Rushton Equation)

$$\frac{R}{R_{\max}} = \frac{I^n}{I^n + \sigma^n}$$

n is between 0.7 and 1.

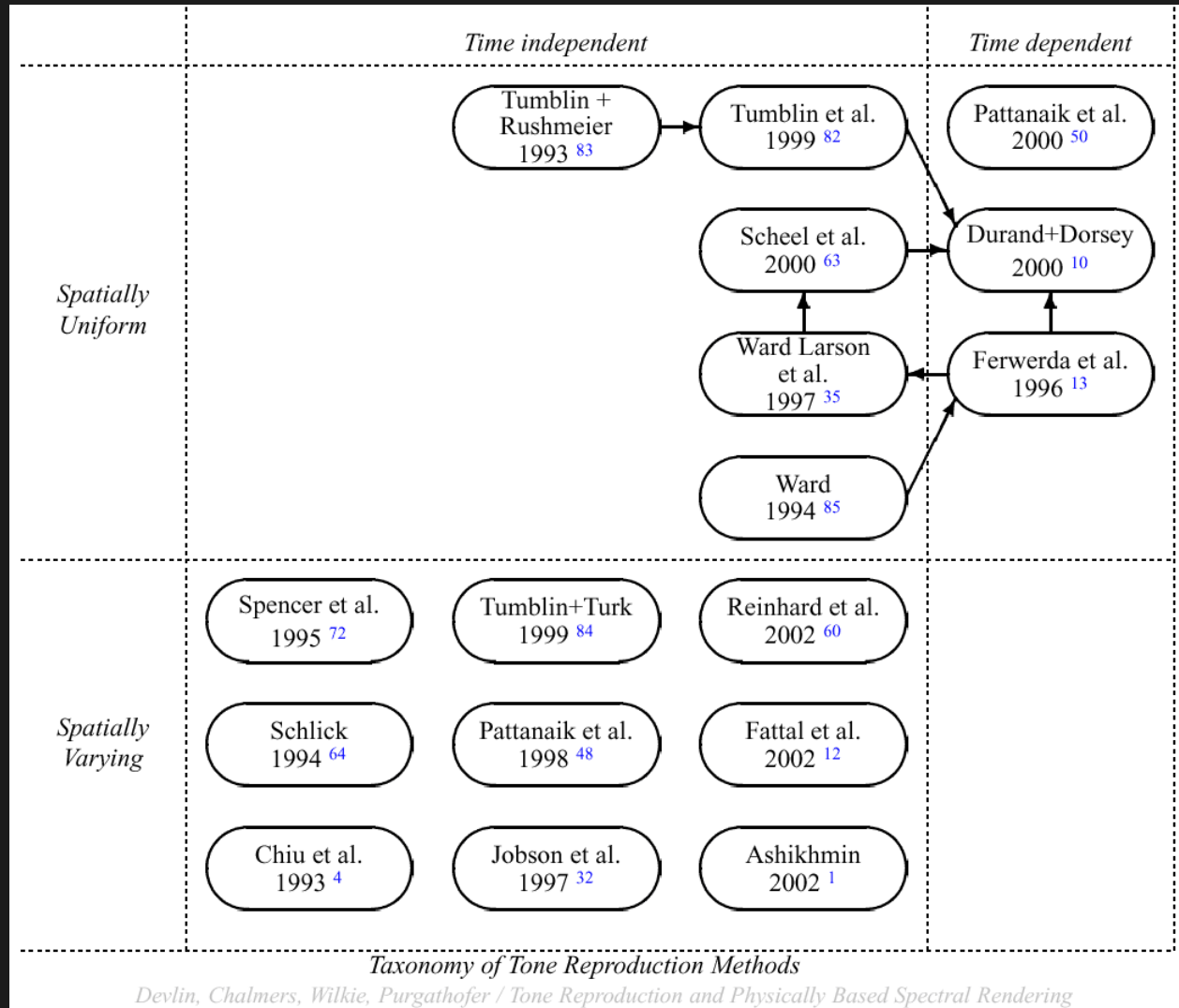
Photoreceptor Adaption



$$\frac{R}{R_{\max}} = \frac{I^n}{I^n + \sigma_b^n}$$

σ_b varies with background light intensity.

Tone Mapping: Many Operators



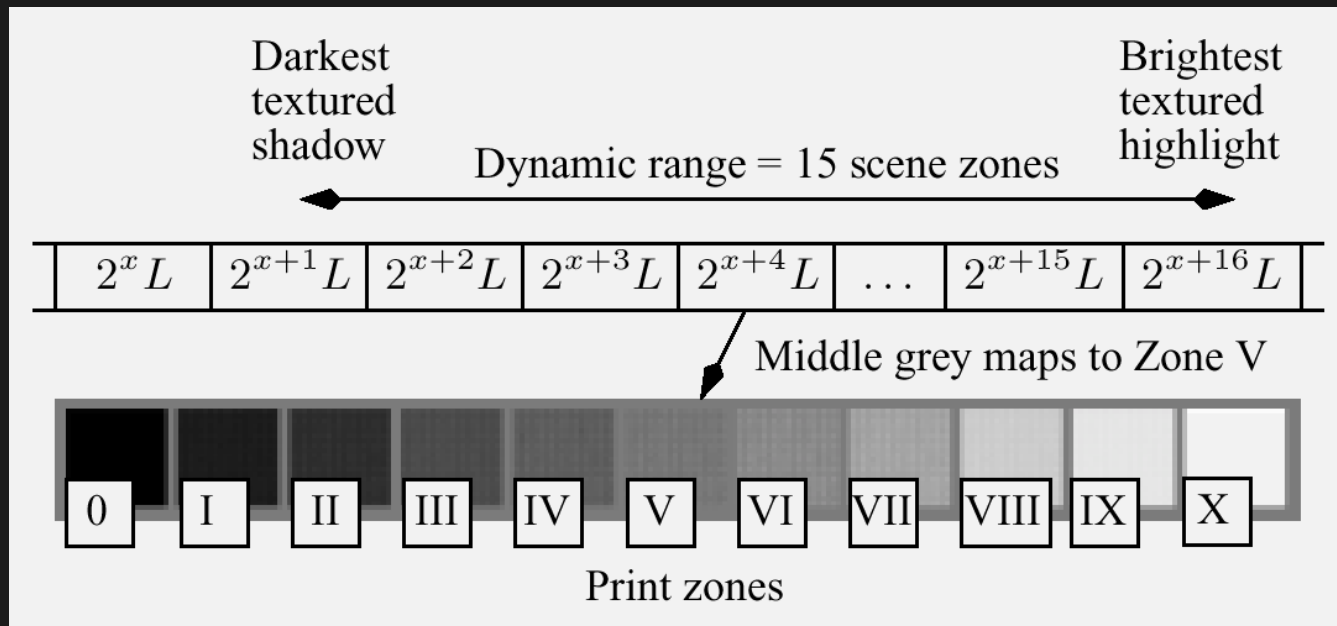
Spatially Uniform Operators

- “Gamma Curve” operator
- Focused on preserving overall brightness
- Subjective brightness, B
- k = constant
- L_0 = minimum luminance visible
- α = [.333, 0.49]
- Not valid for complex scenes; chosen for computational simplicity

$$B = k(L - L_0)^\alpha$$

Spatially Varying Operators

- Reinhard et al. 2002 "Photographic Tone Reproduction for Digital Images"
- Technique is based on famous photographer Ansel Adams studies on tone reproduction using the Zone System (his invention); still widely used and practical



Spatially Varying Operators

Algorithm:

- Use the log-average luminance to find the "key" of a scene
- Automatic "dodging" or "burning" (as in photography): all portions of the print receive difference exposure time.

Spatially Varying Operators

- Step 1. Log Average:

$$\bar{L}_w = \exp \left(\frac{1}{N} \sum_{x,y} \log (\delta + L_w(x, y)) \right)$$

- Step 2. Scale Luminance to a key:

$$L(x, y) = \frac{a}{\bar{L}_w} L_w(x, y)$$

a is called the “key value”

Spatially Varying Operators

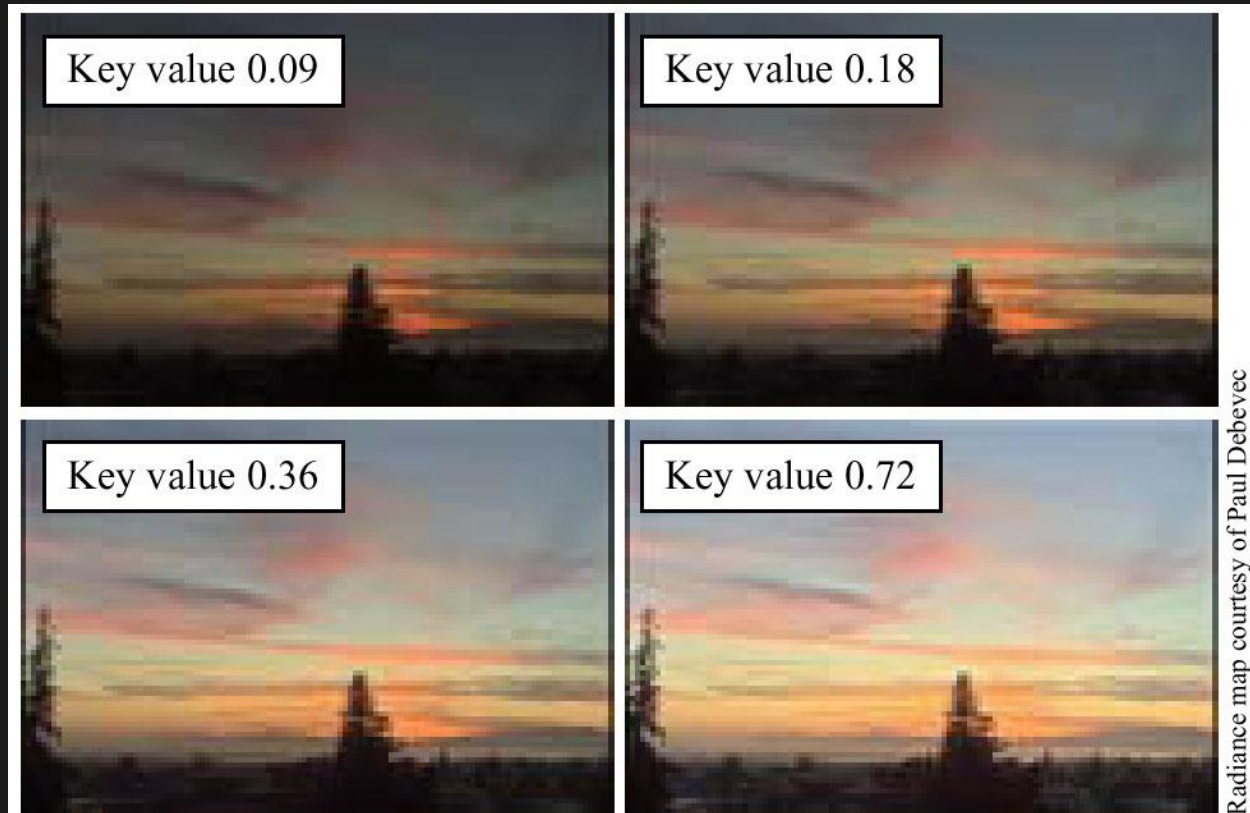


Figure 5: *The linear scaling applied to the input luminance allows the user to steer the final appearance of the tone-mapped image. The dynamic range of the image is 7 zones.*

Spatially Varying Operators

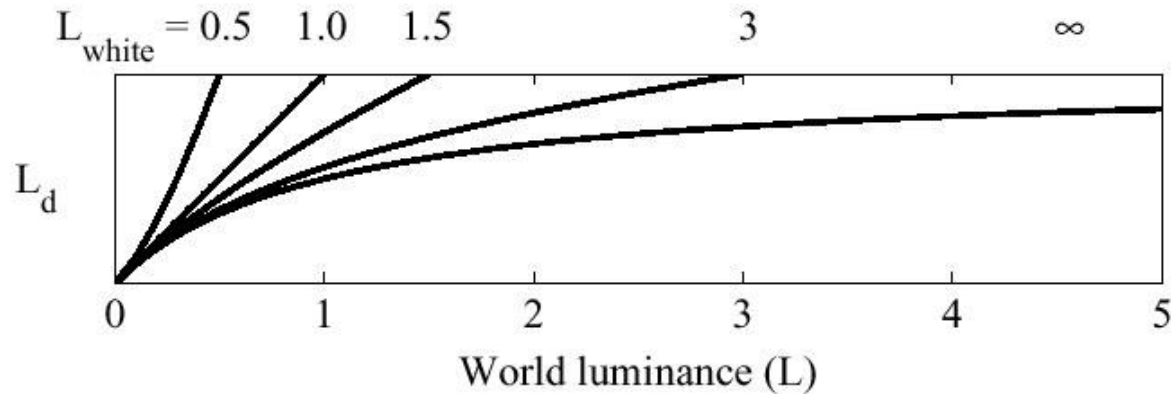
- Step 3. Compress the high luminance:

$$L_d(x, y) = \frac{L(x, y)}{1 + L(x, y)}$$

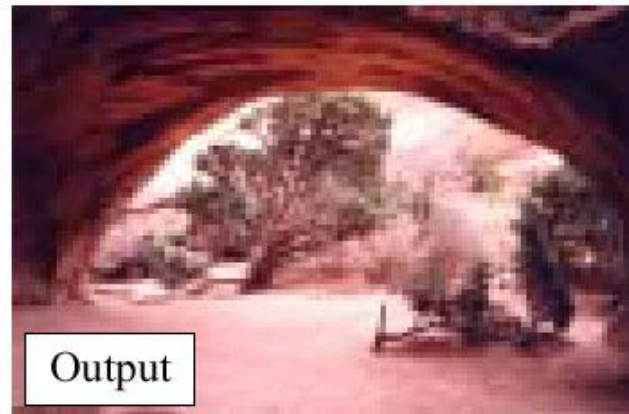
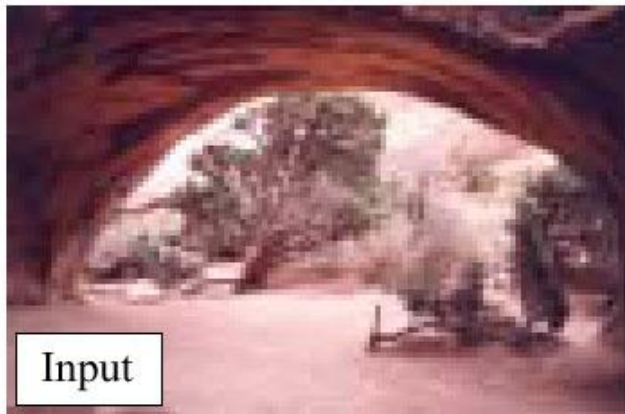
- Or, Step 3. Burning high luminance in a controlled fashion:

$$L_d(x, y) = \frac{L(x, y) \left(1 + \frac{L(x, y)}{L_{\text{white}}^2} \right)}{1 + L(x, y)}$$

Spatially Varying Operators



Display luminance as function of world luminance for a family of values for L_{white} .



Spatially Varying Operators

$L_w=0.15$



$L_w=0.25$



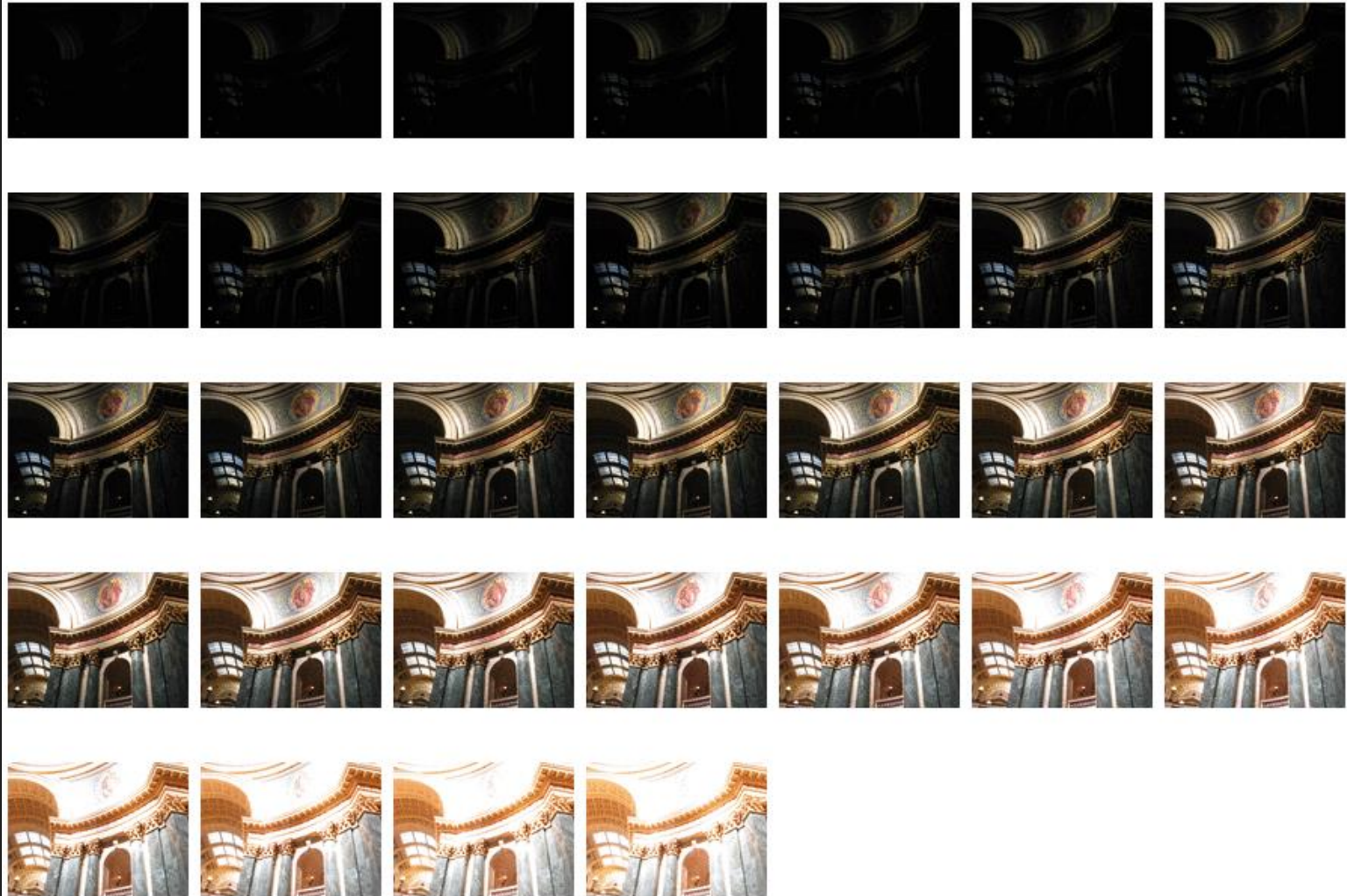
$L_w=0.35$



$L_w=0.45$



Spatially Varying Operators



Spatially Varying Operators

Reinhard '02 Tone Mapping

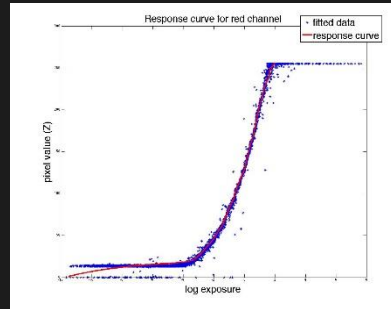


http://pages.cs.wisc.edu/~csverma/CS766_09/HDRI/hdr.html

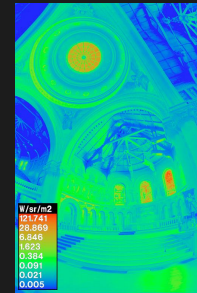
Homework 3: HDR Imaging



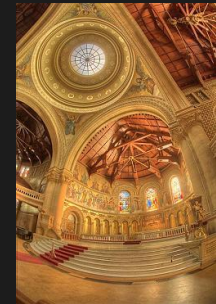
Exposure
Sequence



Camera
Response



Radiance
Map



Tone-mapped
Image

Fcam Programming

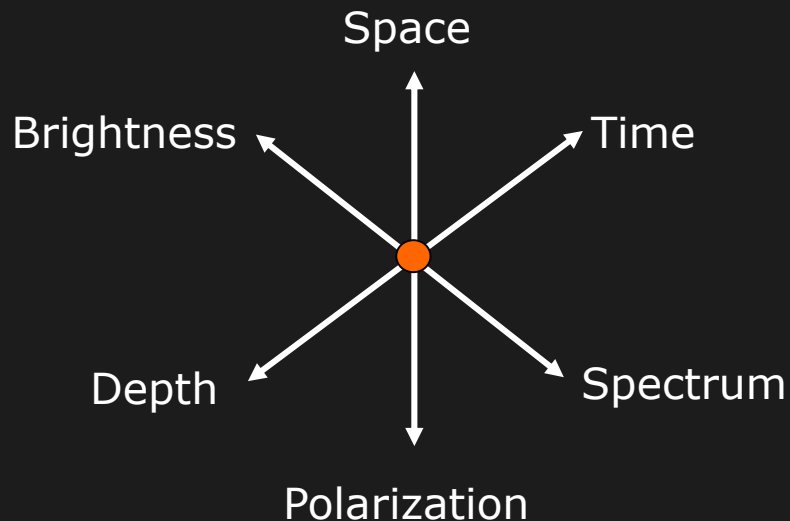
1. Write an exposure bracketing routine for your N900 phone

MATLAB Programming

1. Estimate the camera response curve and the radiance map of the scene
2. Apply a tone mapping operator to radiance map

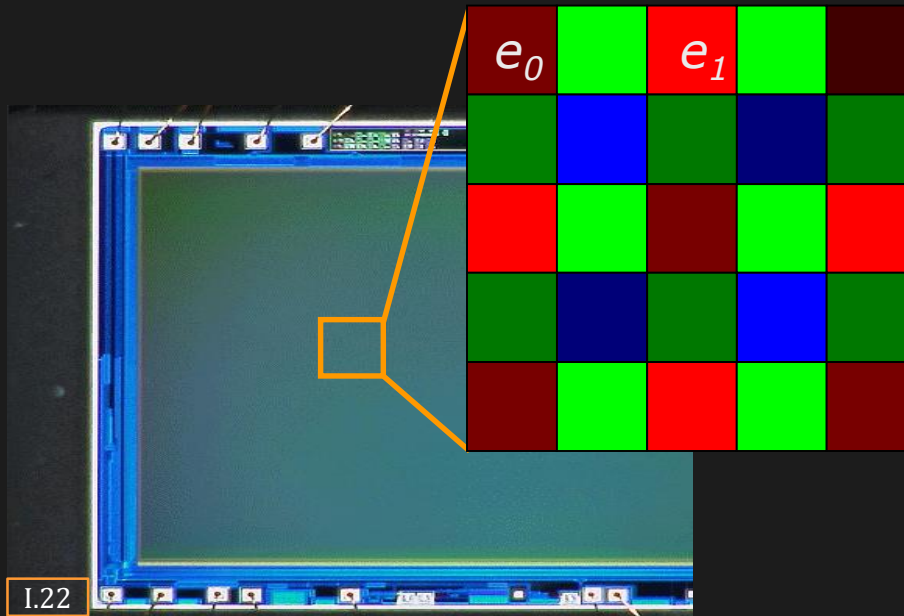
Due before class on Thursday 2/7

Dimensions of Imaging

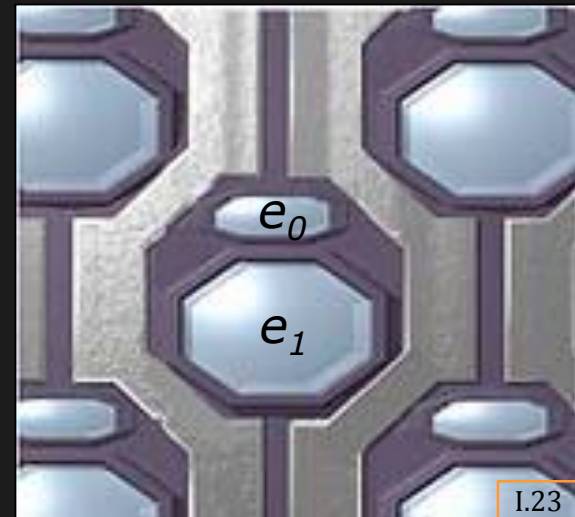


How can we capture information in multiple dimensions using only a two-dimensional array of pixels ?

High Dynamic Range: Single Shot

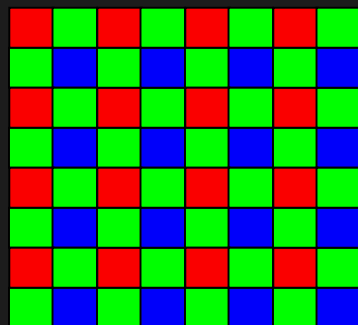


Assorted Pixels:
Spatially Varying Color & Exposure



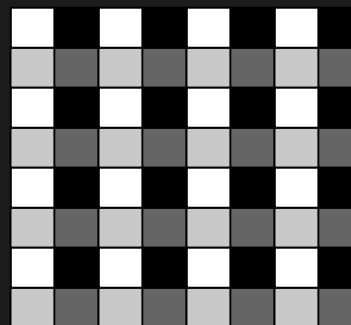
SuperCCD SR, FujiFilm:
Pixels with Subpixels

Assorted Pixels: Multi-Sampled Images



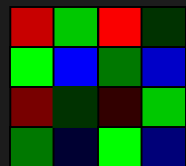
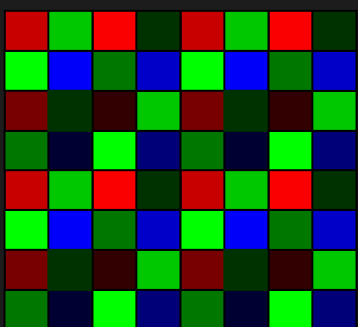
Base Pattern

SVC : Spatially Varying Color
(Bayer Pattern)



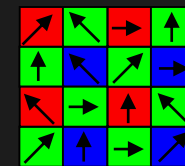
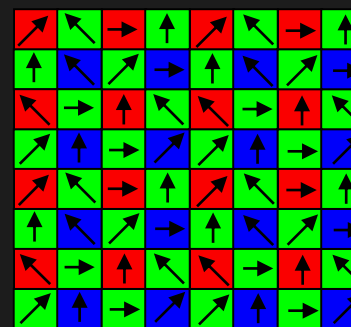
Base Pattern

SVE : Spatially Varying Exposure
(Nayar et al., 00)



Base Pattern

SVEC : Spatially Varying Color
and Exposure

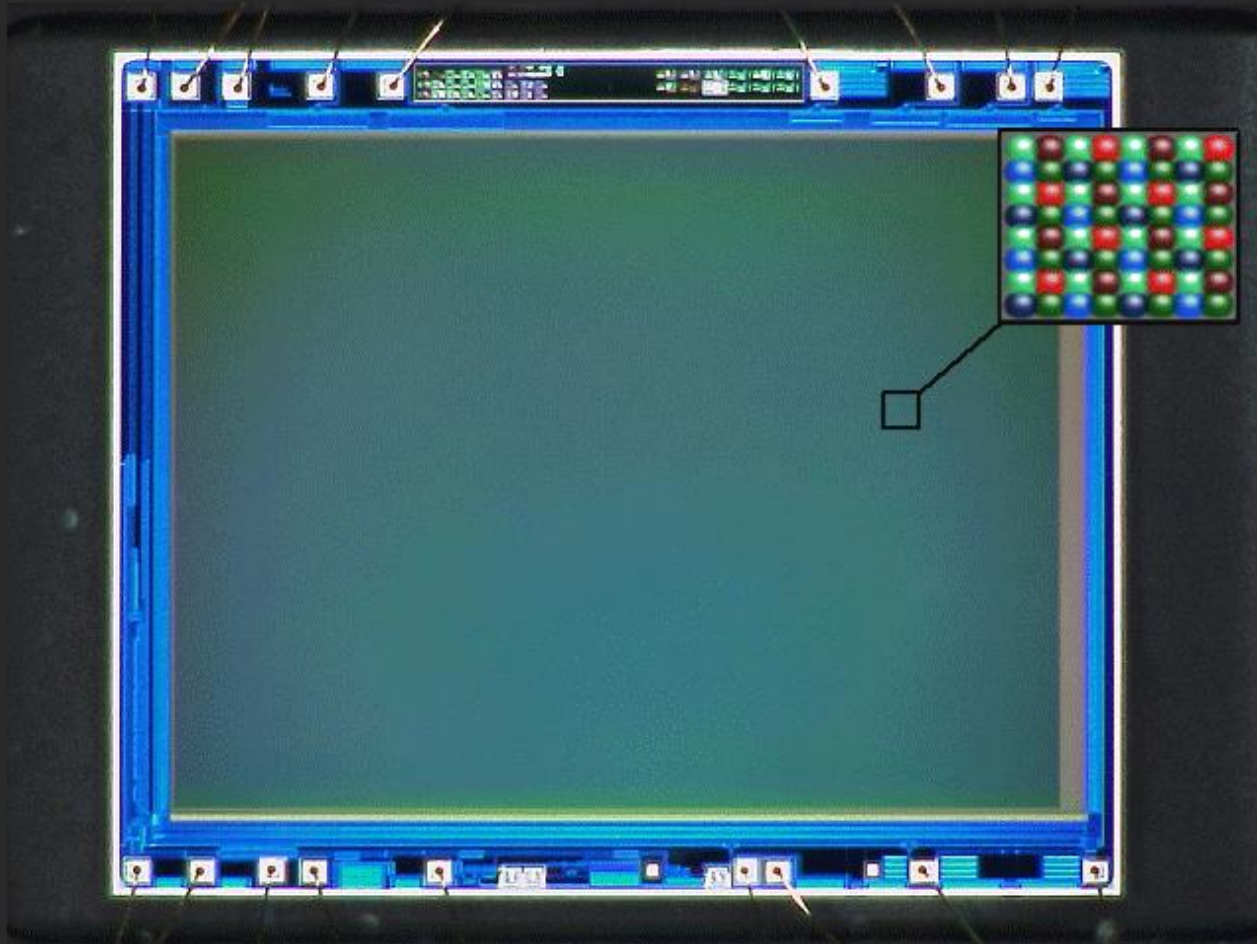


Base Pattern

SVCP : Spatially Varying Color
and Polarization

Simultaneous Sampling along Multiple Dimensions₄₅

Assorted Pixel Sensor



Assorted Pixel Camera: HDR Example

Normal Camera



Assorted Pixel Camera



References: Papers

[Grossberg 2003] M. D. Grossberg and S. K. Nayar. "What is the Space of Camera Response Function?". *CVPR*, 2003.

[Mitsunaga 1999] T. Mitsunaga and S. K. Nayar. "Radiometric Self Calibration". *CVPR*, 1999.

[Nakamura 2006] J. Nakamura. *Image Sensors and Signal Processing for Digital Still Cameras*. CRC Press, 2006.

[Nayar 2000] S. K. Nayar and T. Mitsunaga. "High Dynamic Range Imaging: Spatially Varying Pixel Exposures". *CVPR*, 2000.

[Nayar 2002] S. K. Nayar and S. G. Narasimhan. "Assorted Pixels: Multi-Sampled Imaging with Structured Models". *ECCV*, 2002.

Image Credits

- I.20 S. K. Nayar and T. Mitsunaga. "High Dynamic Range Imaging: Spatially Varying Pixel Exposures". CVPR, 2000
- I.21 S. K. Nayar and T. Mitsunaga. "High Dynamic Range Imaging: Spatially Varying Pixel Exposures". CVPR, 2000.
- I.22 <http://www.dpreview.com/news/0301/03012202fujisuperccdsr.asp>
- I.23 <http://www.dpreview.com/news/0301/03012202fujisuperccdsr.asp>