## 1. 3.2d p.187

 $M_1$  recognizes  $B = \{w \# w \mid w \in \{0,1\}^*\}$  so the input, 10#11, should be rejected:

q <sub>1</sub> 10#11	q7x0#x1
xq₃0#11	xq <sub>1</sub> 0#x1
x0q <sub>3</sub> #11	xxq <sub>2</sub> #x1
x0#q <sub>5</sub> 11	xx#q <sub>4</sub> x1
x0q <sub>6</sub> #x1	xx#xq <sub>4</sub> 1
xq <sub>7</sub> 0#x1	xx#x1q <sub>reject</sub>

## 2. 3.2e p.187

 $M_1$  recognizes  $B = \{w \# w \mid w \in \{0,1\}^*\}$  so the input, 10#10, should be accepted:

q <sub>1</sub> 10#10	xq <sub>1</sub> 0#x0	xxq <sub>1</sub> #xx
xq₃0#10	xxq <sub>2</sub> #x0	xx#q <sub>8</sub> xx
x0q₃#10	xx#q <sub>4</sub> x0	xx#xq <sub>8</sub> x
x0#q <sub>5</sub> 10	xx#xq40	xx#xxq <sub>8</sub>
x0q <sub>6</sub> #x0	xx#q <sub>6</sub> xx	xx#xxq <sub>accept</sub>
xq70#x0	xxq <sub>6</sub> #xx	
q7x0#x0	xq <sub>7</sub> x#xx	

## 4.

$$\delta(q_0, \#) = (q_1, \#, R)$$

$$\delta(q_1, 0) = (q_1, 0, R)$$

$$\delta(q_1, b) = (q_1, b, R)$$

$$\delta(q_1, \#) = (q_2, \#, R)$$

$$\delta(q_2, b) = (q_3, \#, L)$$

$$\delta(q_3, \#) = (q_4, \#, L)$$

$$\delta(q_4, b) = (q_5, b, R)$$

$$\delta(q_4, b) = (q_6, 0, R)$$

$$\delta(q_4, 0) = (q_6, 0, R)$$

$$\delta(q_6, *) = (q_7, 0, L)$$

$$\delta(q_7, 0) = (q_4, 0, L)$$

$$\delta(q_7, b) = (q_4, b, L)$$

$$\delta(q_4, \#) = (q_8, \#, R)$$

$$\delta(q_8, *) = (q_{accept}, b, L)$$

## 5. 3.5d p.188

No, by definition a Turing machine has  $q_{accept}$  and  $q_{reject}$  where  $q_{accept} \neq q_{reject}$ . Additionally, the TM must have an initial state or the machine would immediately halt upon execution. Therefore, a TM requires a minimum of three states.

<sup>\* =</sup> wildcard and therefore can be any symbol of  $\Gamma = \{0, b, \#\}$ .