

Equitable Equations: *Uniform random variables*

Problem 1

Suppose the random variable X has a uniform distribution on the interval $[-1, 7]$.

- (a) Compute $P(X > 0)$.

$$P(X > 0) = \frac{2}{8}$$

- (b) Compute $P(X < 0)$.

$$P(X < 0) = \frac{7}{8} \text{ or } 1 - \frac{2}{8}$$

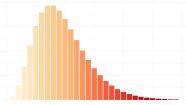
- (c) Briefly explain why $P(X = 0)$ is zero.

The numbers are continuous random variables so the chance of $X=0$ is infinitesimal

- (d) Compute $P(X < 2 \text{ or } X \geq 4)$.

$$P(X < 2) + P(X \geq 4)$$

$$\frac{3}{8} + \frac{3}{8} = \frac{6}{8}$$

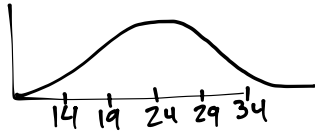


Equitable Equations: *Calculating with the normal distribution*

Problem 1

Suppose X has a normal distribution with mean μ 24 and standard deviation σ 5.

- (a) Sketch the distribution. Label at least 5 points on the x -axis.

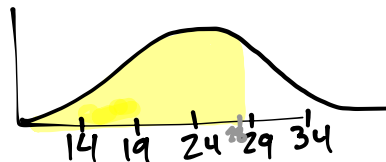


- (b) Fill in the blank: $P(\underline{19} < X < \underline{29}) = 68\%$. Use the empirical rule.
 $\mu - \sigma$ $\mu + \sigma$

- (c) Fill in the blank: $P(\underline{14} < X < \underline{34}) = 95\%$. Use the empirical rule.
 $\mu - 2\sigma$ $\mu + 2\sigma$

- (d) Fill in the blank: $P(\underline{9} < X < \underline{39}) = 99.7\%$. Use the empirical rule.
 $\mu - 3\sigma$ $\mu + 3\sigma$

- (e) Sketch $P(X \leq 28)$.



- (f) Compute $P(X \leq 28)$. Include both *R* code and a numerical answer.

$$\text{pnorm}(28, 24, 5) = 0.788 = 78.8\%$$

- (g) Compute $P(X > 26)$. Include both *R* code and a numerical answer.

$$1 - \text{pnorm}(26, 24, 5) = 0.345 = 34.5\%$$

- (h) Compute $P(26 \leq X \leq 28)$. Include both *R* code and a numerical answer.

$$\text{pnorm}(28, 24, 5) - \text{pnorm}(26, 24, 5) = 0.133 = 13.3\%$$