**KABARAK** 



## **UNIVERSITY**

#### **UNIVERSITY EXAMINATIONS**

#### SECOND SEMESTER, 2016/2017 ACADEMIC YEAR

## EXAMINATION FOR THE BACHELOR OF SCIENCE IN COMPUTER SCIENCE

UNIT CODE: MATH 121

UNIT NAME: INTEGRAL CALCULUS II

STREAM: Y1S2

EXAMINATION SESSION: APRIL TIME: 2.00-4.00PM YEAR: 13/04/2017

#### **INSTRUCTIONS**

- (i) Answer ONE and any other TWO questions
- (ii) Do not write on the question paper
- (iii) Show your working clearly

#### **QUESTION ONE (30MKS)**

a)(i)A curve passes through the point (4,-2) and its gradient function is  $2x^2 + 7$ . Find its equation (2Mks)

(ii)Evaluate 
$$\int_{0}^{2} \frac{2x}{x^2 - 5} dx$$
 (3Mks)

b) i) Evaluate using partial fractions 
$$\int \frac{-2x+4}{(x^2+1)(x-1)^2} dx$$
 (5mks)

ii) Find the length of the arc of the semicubical parabola  $y^2 = x^3$  between the points (1,1) and (4,8).

c) i) Use integration by parts to evaluate 
$$\int e^{2x} \sin x \, dx$$
 (4mks)

ii)Evaluate 
$$\int_{0}^{\frac{\pi}{6}} \tan 2x \, dx \tag{3Mks}$$

d) (i) Evaluate 
$$\int 2^{\sin x} \cos x \, dx \, dx$$
 (2Mks)

e) (i)Evaluate the improper integral 
$$\int_{0}^{9} \frac{1}{\sqrt[3]{x-1}} dx$$
 (4Mks)

ii) Find the area enclosed by the curve  $y = x^2 - 4$  and the x-axis (4mks)

## **QUESTION TWO (20MARKS)**

a)i)Evaluate 
$$\int_{0}^{1} \tan^{-1} x \, dx$$
 (3Mks)

ii) Evaluate the definite integral 
$$\int_{1}^{5} \frac{x}{\sqrt{2x-1}} dx$$
 (4Mks)

b) The region enclosed by the curves y = x and  $y = x^2$  is rotated about the x-axis . Find the volume of the resulting solid. (4Mks)

c) Evaluate using Partial fractions 
$$\int \frac{2}{x^2 - 1} dx$$
 (4Mks)

d) Evaluate the following improper integrals.

i) 
$$\int_{0}^{1} \frac{1}{\sqrt{1-x^2}} dx$$
 (3mks)

$$ii) \int_{1}^{\infty} \frac{1}{1+x^2} dx$$
 (2mks)

#### **QUESTION THREE (20MARKS)**

a) Find the following integrals by substitution method

$$i) \qquad \int \frac{x^3}{2x^4 + 1} \ dx \tag{3mks}$$

ii)Find 
$$\int_{\frac{\sqrt{2}}{2}}^{\frac{\sqrt{3}}{2}} \frac{1}{\sqrt{1-x^2}} dx$$
 (3mks)

b) Find the value  $\int_{0}^{1} \frac{dx}{1+x^2}$  taking 5 sub-intervals by trapezoidal rule correct to five decimal

places. Compare it with the exact value (5mks).

c) Evaluate 
$$\int \frac{x^2}{\sqrt{9-x^2}} dx$$
 (6Mks)

c) Prove the reduction formula  $\int \sin^n x \, dx = -\frac{1}{n} \cos x \sin^{n-1} x + \frac{n-1}{n} \int \sin^{n-2} x \, dx$  where  $n \ge 2$ 

#### **QUESTION FOUR(20MARKS)**

a)Derive a reduction formula 
$$I_m = \int \cos^m x \, dx$$
 and use it to solve  $I_7$  (7mks)

b) Show that 
$$\int \frac{1}{a^2 + u^2} du = \frac{1}{a} \tan^{-1} \frac{u}{a} + c$$
 (5Mks)

b) Evaluate 
$$\int \frac{1}{10+x^2} dx$$
 (4mks)

c) Find the area of the surface obtained by revolving about x- axis of the curve  $y = \sqrt{x}$  from x=0 to x=2. (4Mks)

## **QUESTION FIVE (20MARKS)**

a)Estimate the area under the curve  $y = \frac{1}{x}$  between x=1 and x=2 using n=10 by

- i. Trapezoidal rule
- ii. Simpson's rule (7Mks)
- b) Use partial fractions to evaluate  $\int \frac{x^2 + 2x 1}{2x^3 + 3x^2 2x} dx$  (5Mks)
- c) Find the volume of solid generated by revolving about x-axis of the graph  $y = x^2 + 1$  from x=-1 to x=1 (4mks)
- d) Find the area enclosed by the curve  $y = x^3 4x$  and the x -axis from x=-2 to x=2 (4mks)



## KABARAK

## UNIVERSITY

# UNIVERSITY EXAMINATIONS MAIN CAMPUS

## FIRST SEMESTER, 2017/2018 ACADEMIC YEAR

EXAMINATION FOR THE DEGREE OF BACHELOR OF COMPUTER SCIENCE, BACHELOR OF EDUCATION SCIENCE, BACHELOR OF EDUCATION ARTS, BACHELOR OF SCIENCE IN ECON/MATH AND BACHELOR OF SCIENCE IN ECON/STAT

MATH 121: INTEGRAL CALCUS II

STREAM: Y2S1 &Y1S2 DATE: 7/12/2017

EXAMINATION SESSION: DECEMBER TIME: 2.00-4.00 PM

#### **INSTRUCTION TO CANDITATES:**

- 1. Answer **QUESTION ONE** and **TWO** other questions
- 2. Do not write on the question paper
- 3. Show all your working and be neat

## **QUESTION ONE (30 MARKS)**

- a) A company determines that its marginal revenue, in dollars, is expressed by the equation  $R'(x) = -0.03x^2 + 500x 12000$  where x is the number of units sold. They also know that if they have no sales they still must pay operating costs of \$23000. Find their revenue equation. (3mks)
- b) What is the area under the curve  $y(\theta) = 3\sin\theta$  between  $0 = \theta$  and  $\frac{\pi}{4}$ ? (2marks)
- c) Suppose  $v = t^2 + 1$  t 25 and s(1) = 4. Find s(t) (3 marks)
- d) Use integration by parts to evaluate  $\int x^2 e^x dx$  (3marks)
- e) prove that  $\int \tan x dx = In |\sec x| + c$  (3marks)
- f) Evaluate  $\int_{0}^{1} x(x^2+1)^3 dx$  (4marks)
- g) Integrate the following using substitution techniques

i) 
$$\int \frac{dx}{2+2x^2}$$
 (3marks)

$$ii) \qquad \int \frac{10x+3}{x^2+16} dx \tag{4marks}$$

h) Determine the area of the region bounded by  $x=-y^2+10$  and  $x=(y-2)^2$  (5marks)

## **QUESTION TWO (20 MARKS)**

a) Given the following information determine the function f(x).

$$f''(x)15\sqrt{x} + 5x^3 + 6$$
,  $f(1) = \frac{5}{4}$ ,  $f(4) = 404$  (6marks)

- b) Sketch the graphs  $y = 2x^2 + 10$  and y = 4x + 16 on the same set of axes. Find the area of the region bounded by these two graphs (8marks)
- c) Evaluate  $\int (3t+5)\cos(\frac{t}{4})dt$  (6marks)

## **QUESTION THREE (20 MARKS)**

a) Integrate 
$$\int x^3 \sqrt{4 - x^2} dx$$
 (5marks)

b) Integrate 
$$\int x^2 \sin x dx$$
 (5marks)

c) Use partial fraction to evaluate the indefinite integral  $\int \frac{x^4 - 5x^3 + 6x^2 - 18}{x^3 - 3x^2} dx$  (10marks)

## **QUESTION FOUR (20 MARKS)**

a) Derive a reduction formula for any positive integer n and a, that

$$I_n = \int x^n e^{ax} dx = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx$$
 (7marks)

And hence apply the formula to find constants in the following integral

$$\int x^4 e^{3x} dx = (a_0 x^4 + a_1 x^3 + a_2 x^2 + a_3 x + a_4) e^{3x} + c$$
 (5 marks)

b) Evaluate the following by partial fraction

$$\int \frac{x^2 + 4}{3x^3 + 4x^2 - 4x} dx$$
 (8marks)

## **QUESTION FIVE (20 MARKS)**

a) Evaluate the following integral

$$\int x\sqrt{x+1}dx$$

- (i) Using integration by part (5marks)
- (ii) Using a standard calculus substitution (5 marks)
- b) Evaluate  $\int w^2 \sin(10w) dx$  (7marks)
- c) Evaluate  $\int \cos(15x)\cos(4x)dx$  (3marks)



#### UNIVERSITY EXAMINATIONS

## THIRD SEMESTER, 2016/2017 ACADEMIC YEAR

# EXAMINATION FOR THE DEGREE OF BACHELOR OF SCIENCE IN COMPUTER <u>SCIENCE</u>

## **MATH 121: INTEGRAL CALCULUS II**

STREAM: Y1S2 TIME: 2.00-4.00PM

EXAMINATION SESSION: AUGUST YEAR: 27/7/2017

## **INSTRUCTIONS**

- (i) Answer Question ONE and any other TWO
- (ii) Do not write on the question paper
- (iii) Show your working clearly

#### **QUESTION ONE (30MKS)**

a)(i)A curve passes through the point (4,-2) and its gradient function is  $5x^2 + 7$ . Find its equation (2Mks)

(ii)Evaluate 
$$\int_{0}^{2} \frac{2x}{x^2 - 5} dx$$
 (3Mks)

b) i) Evaluate using partial fractions 
$$\int \frac{x^2 + 4x + 1}{(x - 1)(x + 1)(x + 3)} dx$$
 (5mks)

ii) Find the length of the arc of the semicubical parabola  $y^2 = x^3$  between the points (1,1) and (4,8).

(4mks)

c) i) Use integration by parts to evaluate 
$$\int e^{2x} \sin x \, dx$$
 (4mks)

$$ii) \int x^3 \ln x \, dx \tag{3Mks}$$

d) (i) Evaluate 
$$\int 2^{\sin x} \cos x \, dx \, dx$$
 (2Mks)

e) (i)Evaluate the integral 
$$\int \sin^2 x \, dx$$
 (4Mks)

ii) Find the area enclosed by the parabola  $y = 2 - x^2$  and the line y = -x. (4mks)

## **QUESTION TWO (20MARKS)**

a)i)Evaluate 
$$\int \sin^{-1} x \ dx$$
 (3Mks)

ii) Evaluate the definite integral 
$$\int_{1}^{5} \frac{x}{\sqrt{2x-1}} dx$$
 (4Mks)

b) The region enclosed by the curves y = x and  $y = x^2$  is rotated about the x-axis . Find the volume of the resulting solid. (4Mks)

c) Evaluate using Partial fractions 
$$\int \frac{2}{x^2 - 1} dx$$
 (4Mks)

d) Evaluate the following improper integrals.

i) 
$$\int_{0}^{1} \frac{1}{\sqrt{1-x^2}} dx$$
 (3mks)

$$ii) \int_{1}^{\infty} \frac{1}{1+x^2} dx$$
 (2mks)

## **QUESTION THREE (20MARKS)**

a) Find the following integrals by substitution method

$$i) \qquad \int \frac{x^3}{2x^4 + 1} \ dx \tag{3mks}$$

ii)Find 
$$\int_{\frac{\sqrt{2}}{2}}^{\frac{\sqrt{3}}{2}} \frac{1}{\sqrt{1-x^2}} dx$$
 (3mks)

b) Find the value  $\int_{0}^{1} \frac{dx}{1+x^2}$  taking 5 sub-intervals by trapezoidal rule correct to five decimal

places. Compare it with the exact value (5mks).

c) Evaluate 
$$\int \frac{x^2}{\sqrt{9-x^2}} dx$$
 (6Mks)

c) Obtain a formula that expresses the integral  $\int \cos^n x \, dx$  in terms of an integral of a lower

power of 
$$\cos x$$
 (4Mks)

#### **QUESTION FOUR(20MARKS)**

a)Derive a reduction formula 
$$I_m = \int \cos^m x \, dx$$
 and use it to solve  $I_7$  (7mks)

b) Show that 
$$\int \frac{1}{a^2 + u^2} du = \frac{1}{a} \tan^{-1} \frac{u}{a} + c$$
 (5Mks)

b) Evaluate 
$$\int \frac{1}{10+x^2} dx$$
 (4mks)

c) Find the area of the surface obtained by revolving about x- axis of the curve  $y = \sqrt{x}$  from x=0 to x=2. (4Mks)

## **QUESTION FIVE (20MARKS)**

a)Calculate the value of  $\int_{0}^{1} \frac{x}{1+x} dx$  using n=6 by:

i. Trapezoidal rule

b) Evaluate 
$$\int \frac{1}{x(\ln x)^3} dx$$
 (5Mks)

c) Find the volume of solid generated by revolving about x-axis of the graph  $y = x^2 + 1$  from

$$x=-1 \text{ to } x=1$$
 (4mks)

d)Evaluate 
$$\int_{-1}^{1} 3x^2 \sqrt{x^3 + 1} \ dx \tag{4mks}$$