

Language Syntax

Webpage

We first have the syntax of the body of the webpage <body>...</body>,

```
bodyexp: anyHtmlCode <{exp}> anyHtmlCode)*
```

Expressions

General expressions:

```
exp: e, e', e'', ... ::=  
    let <identifier> = e in e'  
  | fun <identifier> -> e  
  | fixfun <identifier> <identifier> -> e  
  | e e'  
  | if e then e' else e''  
  | e;e'  
  | <identifier>  
  | <aexp>  
  | <bexp>  
  | <sexp>  
  | <texp>  
  | <uexp>  
  | <html>  
  | (e)  
  | begin e end
```

Arithmetic expressions:

```
aexp:  
    <exp> + <exp>  
  | <exp> - <exp>  
  | <exp> * <exp>  
  | <exp> / <exp>  
  | <exp> ^ <exp>  
  | <int literal>
```

Boolean expressions:

```
bexp:  
    <exp> < <exp>  
  | <exp> > <exp>  
  | <exp> <= <exp>  
  | <exp> >= <exp>  
  | <exp> = <exp>  
  | <exp> <> <exp>  
  | <exp> && <exp>  
  | <exp> || <exp>  
  | not <exp>  
  | <boolean literal>
```

String expressions:

```
sexp: <exp> ++ <exp> | <fstring literal>
```

Tuple expressions:

```
texp: fst <exp> | snd <exp> | <exp>, <exp>
```

Unit expression:

`uexp: ()`

HTML:

`html: <[anyHtmlCode]>`

For now, only couples are allowed, and (x_1, x_2, x_3, x_4) is parsed as $(x_1, (x_2, (x_3, x_4)))$.

Identifiers (variable and function names)

`(_|[a-z])(_|'||[0-9]||[a-z]||[A-Z])*`

Examples:

- variable
- my_function
- _MyFunction
- myVariable

But not:

- MyFunction
- 01var

Literals

Integers

For readability for the programmer, we allow underscores in numbers.

`[0-9](([0-9]|_)*)`

Examples:

- 123
- 100_000
- 1_2_____3_____

Strings

Strings are delimited by quotes: "...".

Format strings

Format strings are delimited by: `f"..."`. A formatter can be inserted in a format string with `%{value}`

Booleans

`true, false`

Type system

Types

`<tlit> : int | bool | string | unit | html`

$\alpha, \beta, \dots ::= \alpha \rightarrow \beta \mid \alpha \times \beta$

Typing rules

$$\frac{\Gamma \vdash e : \alpha \quad \Gamma, x : \alpha \vdash e' : \beta}{\Gamma \vdash \text{let } x = e \text{ in } e' : \beta} \quad
 \frac{\Gamma, x : \alpha \vdash e : \beta}{\Gamma \vdash \text{fun } x \rightarrow e : \alpha \rightarrow \beta} \quad
 \frac{\Gamma, f : \alpha \rightarrow \beta, x : \alpha \vdash e : \beta}{\Gamma \vdash \text{fixfun } f \ x \rightarrow e : \alpha \rightarrow \beta}$$

$$\frac{\Gamma \vdash e : \alpha \rightarrow \beta \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e \ e' : \beta} \quad
 \frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e' : \alpha \quad \Gamma \vdash e'' : \alpha}{\Gamma \vdash \text{if } e \text{ then } e' \text{ else } e'' : \alpha} \quad
 \frac{\Gamma \vdash e : \text{unit} \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e; e' : \alpha}$$

$$\begin{array}{c}
\otimes: +, -, *, /, \text{or} \wedge \frac{\Gamma \vdash e : \text{int} \quad \Gamma \vdash e' : \text{int}}{\Gamma \vdash e \otimes e' : \text{int}} \quad \otimes: >, <, \geq, \leq, = \text{ or } \Leftrightarrow \frac{\Gamma \vdash e : \alpha \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e \otimes e' : \text{bool}} \\
\otimes: \& \& \text{ or } || \frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e' : \text{bool}}{\Gamma \vdash e \otimes e' : \text{bool}} \quad \frac{\Gamma \vdash e : \text{bool}}{\Gamma \vdash \text{not } e : \text{bool}} \quad \frac{\Gamma(x) = \alpha}{\Gamma \vdash x : \alpha} \\
\hline
\frac{\Gamma \vdash b : \text{bool} \quad \Gamma \vdash n : \text{int} \quad \Gamma \vdash \langle \text{f} \rangle \text{string literal} : \text{string} \quad \Gamma \vdash \langle \text{html code} \rangle : \text{html}}{\Gamma \vdash \langle \text{html code} \rangle : \text{html}} \\
\frac{\Gamma \vdash e : \alpha \quad \Gamma \vdash e' : \beta \quad \Gamma \vdash e : \alpha \times \beta \quad \Gamma \vdash e : \alpha \times \beta}{\Gamma \vdash (e, e') : \alpha \times \beta} \quad \frac{\Gamma \vdash \text{fst } e : \alpha}{\Gamma \vdash \text{fst } e : \alpha} \quad \frac{\Gamma \vdash \text{snd } e : \beta}{\Gamma \vdash \text{snd } e : \beta} \quad \frac{}{\Gamma \vdash () : \text{unit}}
\end{array}$$

Program semantics

Values

values: $v, v', \dots ::= \langle E, \text{function} \rangle \mid n \mid \text{true} \mid \text{false} \mid \langle \text{string literal} \rangle \mid (v, v')$

function: $\text{fun } x \rightarrow e \mid \text{fixfun } f \rightarrow e$

Evaluation rules

We implement a big-step call-by-value semantics.

$$\begin{array}{c}
\frac{}{\vdash n \Downarrow n} \quad \frac{}{\vdash \text{true} \Downarrow \text{true}} \quad \frac{}{\vdash \text{false} \Downarrow \text{false}} \quad \frac{}{\vdash \langle \text{string} \rangle \Downarrow \langle \text{string} \rangle} \\
\frac{}{\vdash \text{fun } x \rightarrow e \Downarrow \langle E, \text{fixfun } f \rightarrow e \rangle} \quad \frac{}{\vdash \text{fixfun } f \rightarrow e \Downarrow \langle E, \text{fun } x \rightarrow e \rangle} \\
\frac{\vdash e \Downarrow v \quad \vdash e' \Downarrow v'}{\vdash (e, e') \Downarrow (v, v')} \quad \frac{\vdash e \Downarrow n \quad \vdash e' \Downarrow m}{\vdash e \otimes e' \Downarrow n \otimes m} \quad \frac{\vdash e \Downarrow n}{\vdash \text{not } e \Downarrow \neg n} \quad \frac{\vdash e \Downarrow b \quad \vdash e' \Downarrow b'}{\vdash e \otimes e' \Downarrow b \otimes b'} \\
\frac{\vdash e \Downarrow b}{\vdash \text{not } e \Downarrow \neg b} \quad \frac{\vdash e \Downarrow s \quad \vdash e' \Downarrow s'}{\vdash e \neq e' \Downarrow s \neq s'} \\
\frac{\vdash e \Downarrow \langle E', \text{fun } x \rightarrow e_f \rangle \quad \vdash e' \Downarrow v \quad E', x \mapsto v \vdash e_f \Downarrow v'}{\vdash e \ e' \Downarrow v'} \quad \frac{\vdash e' \Downarrow v' \quad E, x \mapsto v' \vdash e' \Downarrow v'}{\vdash \text{let } x = e \text{ in } e' \Downarrow v} \\
\frac{\vdash e \Downarrow \langle E', \text{fixfun } f \rightarrow e_f \rangle \quad \vdash e' \Downarrow v \quad E, f \mapsto \text{fixfun } f \rightarrow e_f, x \mapsto v \vdash e_f \Downarrow v'}{\vdash e \ e' \Downarrow v'} \\
\frac{\vdash e \Downarrow v \quad \vdash e' \Downarrow v'}{\vdash e; e' \Downarrow v'} \quad \frac{\vdash e \Downarrow \text{true} \quad \vdash e' \Downarrow v'}{\vdash \text{if } e \text{ then } e' \text{ else } e'' \Downarrow v'} \quad \frac{\vdash e \Downarrow \text{false} \quad \vdash e'' \Downarrow v''}{\vdash \text{if } e \text{ then } e' \text{ else } e'' \Downarrow v''} \\
\frac{\vdash e \Downarrow (v, v')}{\vdash \text{fst } e \Downarrow v} \quad \frac{\vdash e \Downarrow (v, v')}{\vdash \text{snd } e \Downarrow v'} \quad E(x) = v \frac{\vdash e \Downarrow x}{\vdash e \Downarrow v}
\end{array}$$

TODO

- Don't lex ml located in html comment
- Add syntactic sugar for multiple variables functions.
- Add t-uples
- Add pattern-matching
- Add superglobal variables (e.g. given in argument of the interpreter in a yaml format)
- Add user-defined global variables

- Add user-defined types
- Once it's done, implement basic types such as list directly within the language.
- Maybe revisit sequence's semantics. We may want <{"<tag>"; "hey</tag>"}> to produce the html code <[tag](#)>hey</[tag](#)> .
- Allow type annotations from the user
- Allow importing other ml files (as modules ?)
- Keep line number information on parsed term for better typing error messages (?)