

Language Syntax

Webpage

We first have the syntax of the body of the webpage `<body>...</body>`,

`bodyexp: anyHtmlCode> (<{exp}> anyHtmlCode)*`

Expressions

General expressions:

```
exp: e, e', e'', ... ::=
    let <id> = e in e'
    | fun <id> -> e
    | fixfun <id> <id> -> e
    | e e'
    | if e then e' else e''
    | e;e'
    | <id>
    | <aexp> | <bexp> | <sexp>
    | <texp>
    | <uexp>
    | <html> | <dbexp>
    | (e)
    | begin e end
```

Arithmetic expressions:

```
aexp:
    <exp> + <exp>
    | <exp> - <exp>
    | <exp> * <exp>
    | <exp> / <exp>
    | <exp> ^ <exp>
    | <int literal>
```

Boolean expressions:

```
bexp:
    <exp> < <exp>
    | <exp> > <exp>
    | <exp> <= <exp>
    | <exp> >= <exp>
    | <exp> = <exp>
    | <exp> <> <exp>
    | <exp> && <exp>
    | <exp> || <exp>
    | not <exp>
    | <boolean literal>
```

String expressions:

```
sexp: <exp> ++ <exp> | <fstring literal>
```

Tuple expressions:

```
texp: fst <exp> | snd <exp> | <exp>, <exp>
```

Unit expression:

```
uexp: ()
```

TODO

HTML:

```
html: <[ anyHtmlCode ]>
```

Database expression:

```
dbexp: sqlite_opendb | sqlite_closedb | sqlite_exec
```

For the time being, only couples are allowed, and `(x1, x2, x3, x4)` is parsed as `(x1, (x2, (x3, x4)))`.

Identifiers (variable and function names)

```
(_[a-z])(_|'|[0-9]|[a-z]|[A-Z])*
```

Examples:

- variable
- my_function_n_362
- _MyFunction
- myVariable067

But not:

- MyFunction
- 01var

Literals

Integers

For better readability for the programmer, we allow underscores in numbers.

```
[0-9]([0-9]|_)*
```

Examples:

- 123
- 100_000
- 1_2_____3_____

Strings

Strings are delimited by quotes: "...".

Format strings

Format strings are delimited by: f"...". A formatter can be inserted in a format string with %(value)

Booleans

true, false

Type system

Types

`<tlit> : int | bool | string | unit | html | db`

$\alpha, \beta, \dots ::= \alpha \rightarrow \beta \mid \alpha \times \beta$

Typing rules

$$\begin{array}{c} \frac{\Gamma \vdash e : \alpha \quad \Gamma, x : \alpha \vdash e' : \beta}{\Gamma \vdash \text{let } x = e \text{ in } e' : \beta} \quad \frac{\Gamma, x : \alpha \vdash e : \beta}{\Gamma \vdash \text{fun } x \rightarrow e : \alpha \rightarrow \beta} \quad \frac{\Gamma, f : \alpha \rightarrow \beta, x : \alpha \vdash e : \beta}{\Gamma \vdash \text{fixfun } f \ x \rightarrow e : \alpha \rightarrow \beta} \\ \frac{\Gamma \vdash e : \alpha \rightarrow \beta \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e \ e' : \beta} \quad \frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e' : \alpha \quad \Gamma \vdash e'' : \alpha}{\Gamma \vdash \text{if } e \text{ then } e' \text{ else } e'' : \alpha} \quad \frac{\Gamma \vdash e : \text{unit} \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e; e' : \alpha} \\ \textcircled{\otimes} : +, -, *, /, \text{ or } ^ \quad \frac{\Gamma \vdash e : \text{int} \quad \Gamma \vdash e' : \text{int}}{\Gamma \vdash e \ \textcircled{\otimes} \ e' : \text{int}} \quad \textcircled{\otimes} : >, <, >=, <=, = \text{ or } <> \quad \frac{\Gamma \vdash e : \alpha \quad \Gamma \vdash e' : \alpha}{\Gamma \vdash e \ \textcircled{\otimes} \ e' : \text{bool}} \\ \textcircled{\otimes} : \&\& \text{ or } || \quad \frac{\Gamma \vdash e : \text{bool} \quad \Gamma \vdash e' : \text{bool}}{\Gamma \vdash e \ \textcircled{\otimes} \ e' : \text{bool}} \quad \frac{\Gamma \vdash e : \text{bool}}{\Gamma \vdash \text{not } e : \text{bool}} \quad \frac{\Gamma(x) = \alpha}{\Gamma \vdash x : \alpha} \\ \frac{}{\Gamma \vdash b : \text{bool}} \quad \frac{}{\Gamma \vdash n : \text{int}} \quad \frac{}{\Gamma \vdash \text{<(f)string literal> : string}} \quad \frac{}{\Gamma \vdash \text{<[html code]> : html}} \\ \frac{\Gamma \vdash e : \alpha \quad \Gamma \vdash e' : \beta}{\Gamma \vdash (e, e') : \alpha \times \beta} \quad \frac{}{\Gamma \vdash \text{fst} : \alpha \times \beta \rightarrow \alpha} \quad \frac{}{\Gamma \vdash \text{snd } e : \alpha \times \beta \rightarrow \beta} \quad \frac{}{\Gamma \vdash () : \text{unit}} \\ \frac{}{\Gamma \vdash \text{sqlite_opendb} : \text{string} \rightarrow \text{db}} \quad \frac{}{\Gamma \vdash \text{sqlite_closedb} : \text{db} \rightarrow \text{bool}} \\ \hline \Gamma \vdash \text{sqlite_exec} : \text{db} \rightarrow (\text{html} \rightarrow \text{html} \rightarrow \text{html}) \rightarrow (\text{html} \rightarrow \text{string} \rightarrow \text{string} \rightarrow \text{html}) \rightarrow \text{bool} \end{array}$$

Program semantics

Values

values: $v, v', \dots ::= \langle E, \text{<function>} \rangle \mid n \mid \text{true} \mid \text{false} \mid \text{<string literal>} \mid (v, v') \mid \text{<vdb>} \mid \text{pure_html_code} \mid \boxed{\text{evald_page}}$

function: $\text{fun } x \rightarrow e \mid \text{fixfun } x \rightarrow e$

evald_page: $[v_1; v_2; \dots; v_n]$  it's a list in the meta-language.

vdb: a value representing a database in the language

An evaluated webpage can be injected in a value (via the frame). This happens when we evaluate, e.g.

`<{ <[htmlcode <{let x = 1 in x}> somemorehtmlcode]> }>`

Evaluation rules

A dynamic webpage to evaluate is seen as a list of either:

- Pure html code ;
- An expression ;
- A global declaration.

The top-level interpreted page is a dynamic webpage, as well as the content between HTML opening/closing bracket.

The interpreter evaluates following a big-step call-by-value semantics. We define two mutually recursive relations to evaluate expressions and dynamic webpages.

Expression

$$\begin{array}{c} \frac{}{E \vdash n \Downarrow n} \quad \frac{}{E \vdash \text{true} \Downarrow \text{true}} \quad \frac{}{E \vdash \text{false} \Downarrow \text{false}} \quad \frac{}{E \vdash \text{"<string>"} \Downarrow \text{"<string>"} } \\ \frac{}{E \vdash \text{fun } x \rightarrow e \Downarrow \langle E, \text{fixfun } f \ x \rightarrow e \rangle} \quad \frac{}{E \vdash \text{fixfun } f \ x \rightarrow e \Downarrow \langle E, \text{fun } x \rightarrow e \rangle} \end{array}$$

$$\begin{array}{c}
\frac{E \vdash e \Downarrow v \quad E \vdash e' \Downarrow v'}{E \vdash (e, e') \Downarrow (v, v')} \quad \frac{E \vdash e \Downarrow n \quad E \vdash e' \Downarrow m}{E \vdash e \otimes e' \Downarrow n \otimes n'} \quad \frac{E \vdash e \Downarrow n}{E \vdash -e \Downarrow -n} \quad \frac{E \vdash e \Downarrow b \quad E \vdash e' \Downarrow b'}{E \vdash e \otimes e' \Downarrow b \otimes b'} \\
\frac{E \vdash e \Downarrow b}{E \vdash \text{not } e \Downarrow \neg b} \quad \frac{E \vdash e \Downarrow s \quad E \vdash e' \Downarrow s'}{E \vdash e \# e' \Downarrow s \# s'} \\
\frac{E \vdash e \Downarrow \langle E', \text{fun } x \rightarrow e_f \rangle \quad E \vdash e' \Downarrow v \quad E', x \mapsto v \vdash e_f \Downarrow v'}{E \vdash e e' \Downarrow v'} \quad \frac{E \vdash e' \Downarrow v' \quad E, x \mapsto v' \vdash e' \Downarrow v}{E \vdash \text{let } x = e \text{ in } e' \Downarrow v} \\
\frac{E \vdash e \Downarrow \langle E', \text{fixfun } f x \rightarrow e_f \rangle \quad E \vdash e' \Downarrow v \quad E, f \mapsto \text{fixfun } f x \rightarrow e_f, x \mapsto v \vdash e_f \Downarrow v'}{E \vdash e e' \Downarrow v'} \\
\frac{E \vdash e \Downarrow v \quad E \vdash e' \Downarrow v'}{E \vdash e; e' \Downarrow v'} \quad \frac{E \vdash e \Downarrow \text{true} \quad E \vdash e' \Downarrow v'}{E \vdash \text{if } e \text{ then } e' \text{ else } e'' \Downarrow v'} \quad \frac{E \vdash e \Downarrow \text{false} \quad E \vdash e'' \Downarrow v''}{E \vdash \text{if } e \text{ then } e' \text{ else } e'' \Downarrow v''} \\
\frac{E \vdash e \Downarrow (v, v')}{E \vdash \text{fst } e \Downarrow v} \quad \frac{E \vdash e \Downarrow (v, v')}{E \vdash \text{snd } e \Downarrow v'} \quad E(x) = v \frac{E \vdash e \Downarrow x}{E \vdash e \Downarrow v} \quad \frac{E \vdash \text{dynamic_webpage} \Downarrow \text{evald_page}}{E \vdash \langle \text{dynamic_webpage} \rangle \Downarrow \boxed{\text{evald_page}}}
\end{array}$$

vdb is a projection within the language of the db at path s $\frac{E \vdash e \Downarrow s}{E \vdash \text{sqlite_opendb } e \Downarrow \text{vdb}}$

If the corresponding db could be closed $\frac{E \vdash e \Downarrow \text{vdb}}{E \vdash \text{sqlite_closedb } e \Downarrow \text{true}}$

If the corresponding db couldn't be closed (it remains open) $\frac{E \vdash e \Downarrow \text{vdb}}{E \vdash \text{sqlite_closedb } e \Downarrow \text{true}}$

$\frac{E \vdash e \Downarrow \text{vdb} \quad E \vdash \text{a closure for function } f1 \Downarrow \text{vdb} \quad E \vdash \text{a closure for function } f2 \Downarrow \text{vdb} \quad E \vdash e' \Downarrow s}{E \vdash \text{sqlite_exec } e \text{ } f1 \text{ } f2 \text{ } e' \Downarrow \text{processed } s^*}$

*The semantic of exec is as follows: s is a string corresponding to a SQL command, which is executed on the database vdb. If it has query statements, then sqlite_exec allow to process the result with a double fold left function applied on the resulting table i.e. let:

| | | |
|----------|-----|----------|
| header_1 | ... | header_n |
| data_1 | ... | data_n |

be a line of the resulting table of the query. We first allow to process one line in the following manner: the value line_i corresponding to the table above is: fc (... (fc EmptyHtmlCode header_1 data_1) ...) header_n data_n.

Similarly, the result of each line is combined in the following manner to form processed s:
processed s = fl (... (fl EmptyHtmlCode line_1) ...) line_n

See here for reason the db couldn't be closed, and more specifications of the sqlite functions.

Dynamic webpage

$$\frac{E \vdash e \Downarrow v \quad E, x \mapsto v \vdash \text{page} \Downarrow \text{evald}}{E \vdash (\text{let } x = e) :: \text{page} \Downarrow \text{evald}} \quad \frac{E \vdash \text{page} \Downarrow \text{evald}}{E \vdash \text{pure_html} :: \text{page} \Downarrow \text{pure_html} :: \text{evald}} \\
\frac{E \vdash e \Downarrow v \quad E \vdash \text{page} \Downarrow \text{evald}}{E \vdash e :: \text{page} \Downarrow v :: \text{evald}}$$

TODO

- ☐ Implement fstrings
- ☐ See why special characters passed as argument of GET/POST requests is displayed weirdly.
- ☐ Don't lex ml located in html comment
- ☐ Add comments within ML
- ☒ Allow HTML brackets to contain any dynpage e.g. `<[somehtml <{"coucou"}> somemorehtml]>`
- ☐ Add syntactic sugar for multiple variables functions.
- ☐ Add t-uples
- ☐ Add pattern-matching
- ☒ Add superglobal variables (e.g. given in argument of the interpreter in a yaml format)
- ☒ Add user-defined global variables
- ☐ Add user-defined types
- ☐ Once it's done, implement basic types such as list directly within the language.
- ☐ Allow type annotations from the user
- ☐ Allow importing other ml files (as modules ?)
- ☐ Keep line number information on parsed term for better typing error messages (?)