

# Exuberant and Uninformed: How Financial Markets (Mis-)Allocate Capital during Booms

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# Motivation

- Financial markets play an important role in the allocation of capital.
  - Growing concerns that markets do not always fulfill this role well:
- 1 Misallocation often increases during asset price booms. Example US Housing Boom
    - Gopinath et al. (2017), Doerr (2018), García-Santana et al. (2020), and Gorton and Ordoñez (2020).
  - 2 Which may lead to a slowdown in productivity growth. Example US
    - Borio et al. (2015): “disappointing US [pre-crisis] growth ... because of the [financial] boom.”
  - 3 Some argue that a decline in information production in financial markets is responsible. Literature
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# This Paper: Overview

- **This paper:** Study relationship between booms and misallocation through information production in financial markets.
- In the spirit of Hayek (1945), markets aggregate information:

Information Production  $\Rightarrow$  Capital Allocation  $\Rightarrow$  Overall Productivity

- To avoid Grossman-Stiglitz paradox: **Overconfidence**. Paradox
  - Common bias in a broad variety of settings. Literature
  - Yields a **tractable** macroeconomic framework.

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# This Paper: Framework

- Households (HH) save by investing in firms through stocks.
- **Information frictions:** HH do not know firm productivity; can acquire costly information.
- Two sources of firm-specific and aggregate fluctuations:
  - Fundamental (**Productivity**).
  - Non-Fundamental (**Sentiments as waves of optimism/pessimism**).
- In many ways, productivity and sentiment booms look similar:
  - They increase output, investment and asset prices.
  - Yet, they have different impacts on capital allocation.



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# Positive Results

- Relationship between asset price booms and misallocation depends on source of boom.
- Fundamental booms, e.g. which are driven by productivity, decrease misallocation.
  - Information production  $\uparrow \Rightarrow$  Endogenous TFP component  $\uparrow$
  - Productivity shocks get **amplified**.
- Non-fundamental booms, e.g. which are driven by sentiment, increase misallocation.
  - Information production  $\downarrow \Rightarrow$  Endogenous TFP component  $\downarrow$
  - Sentiment booms get **dampened**.

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# Normative Results

- Laissez-faire equilibrium is constrained inefficient.
  - Info production can be too high (rent-extracting behavior).
  - Info production can be too low (information spillover).
- Application: large scale asset purchases and sales.
  - Used intensively by central banks during past decade.
- Do large-scale asset purchases harm market efficiency?
  - They can distort prices and increase misallocation.
  - However, when used appropriately, asset purchases raise market efficiency.

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# Literature

- **Macro and Information:** Veldkamp (2005) and Van Nieuwerburgh and Veldkamp (2006), Peress (2014), David, Hopenhayn, and Venkateswaran (2016)
  - **New: Study two-way relationship between the cycle and information production.**
- **Credit Cycles:** Gorton and Ordoñez (2014), Asriyan, Laeven, and Martin (2019), Gorton and Ordoñez (2020)
  - **New information mechanism between booms and misallocation.**
- **Noisy Rational Expectations:** Grossman and Stiglitz (1980), Kyle (1985), Vives (2010), Albagli, Hellwig, and Tsyvinski (2011)
  - **Novel methodology: Overconfidence facilitates application to GE and macro.**



# Agents

- Infinite horizon OLG model.
- **Households**  $i \in [0, 1]$  live for two periods:

$$U_{it} = C_{it,t} + \delta \tilde{\mathbb{E}}_t \{C_{it,t+1}\} - \int_0^1 IA(\beta_{ijt}) dj.$$

- Consume during youth and old age, discount factor  $\delta \in (0, 1)$ .
- $\int_0^1 IA(\beta_{ijt}) dj$  are information production costs.
- Buy/issue bonds with return  $R_{t+1}$ .
- Household  $i$  is composed of a unit mass of **Traders**  $ij \in [0, 1] \times [0, 1]$ .
  - Endowed with one unit of labor, supplied inelastically during youth, earn  $W_t$ .
  - Buy stocks of firm  $j$  subject to position limits  $[0, 2]$ .
  - Choose information precision  $\beta_{ijt}$  to inform trading decision at cost  $IA(\beta_{ijt})$ :

$$IA(0) = 0 \quad IA'(0) = 0 \quad IA'(\cdot) \geq 0 \quad IA''(\cdot) > 0.$$

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# Final Good Producers

- Final good firms combine intermediate goods with labor to produce the final good,

$$Y_t = L^{1-\alpha} \left( \int_0^1 Y_{jt}^{\frac{\theta-1}{\theta}} dj \right)^{\frac{\alpha\theta}{\theta-1}}.$$

- $\alpha$  : Intermediate good share.
- $\theta$  : Elasticity of substitution between intermediate goods.
  - Linked to the cost of misallocation.

# Intermediate Good Sector

- Intermediate good firms indexed by  $j \in [0, 1]$ :

$$Y_{jt} = A_{jt-1}^{\frac{\theta}{\theta-1}} K_{jt}.$$

- Firm productivity/demand shifter  $\ln(A_{jt-1}) \stackrel{iid}{\sim} \mathcal{N}(a_{t-1}, \sigma_a^2)$ .
  - Firm capital  $K_{jt}$ , depreciates fully after production.
- Capital takes time to build: Investment in  $t$ , production in  $t + 1$ .
- As in Peress (2014), firms sell claims to firm revenue and invest proceeds,

$$K_{jt+1} = P_{jt}.$$

# Information Structure

- Trader  $ij$  receives the signal

$$s_{ijt} = a_{jt} + \frac{\eta_{ijt} + \varepsilon_{jt}}{\sqrt{\beta_{ijt}}}.$$

- Firm productivity  $a_{jt} = \ln A_{jt} \sim \mathcal{N}(a_t, \sigma_a^2)$ .
- Idiosyncratic noise  $\eta_{ijt} \sim \mathcal{N}(0, 1)$ .
- Firm-specific sentiment  $\varepsilon_{jt} \sim \mathcal{N}(\varepsilon_t, \sigma_\varepsilon^2)$ .
- Information precision  $\beta_{ijt}$ .

# Overconfidence

## Assumption (*Overconfidence*)

Trader  $ij$  believes the information structure to be

$$s_{ijt} = a_{jt} + \frac{\hat{\eta}_{ijt}}{\sqrt{\beta_{ijt}}}$$

$$s_{-ijt} = a_{jt} + \frac{\eta_{-ijt} + \varepsilon_{jt}}{\sqrt{\beta_{-ijt}}}.$$

- where  $\hat{\eta}_{ijt} \sim \mathcal{N}(0, 1)$ .
- Trader  $ij$  thinks that sentiment drives the beliefs of all traders except her own.
- Traders choose information precision  $\beta_{ijt}$  to maximize trading rents.

Overconfidence

# Two Aggregate Shocks: Productivity and Sentiment

- Aggregate productivity shock

$$a_{jt} \sim \mathcal{N}(a_t, \sigma_a^2).$$

- Aggregate sentiment shock

$$\varepsilon_{jt} \sim \mathcal{N}(\varepsilon_t, \sigma_\varepsilon^2).$$

- Captures phenomena such as herding, informational cascades, social learning, bubbles, liquidity trading, ... (see Kindleberger and Aliber, 2015; Shiller, 2015, 2017).
- For simplicity,  $a_t$  and  $\varepsilon_t$  are publicly observable.
  - What is crucial are the traders' expectations about aggregate shocks.

# Timing

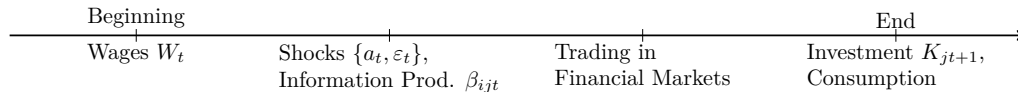


Figure: Information production takes place after aggregate shocks are revealed.



# Factor Market Clearing

- Prices for labor and intermediate goods are determined competitively,

$$W_t = \frac{\partial Y_t}{\partial L} = (1 - \alpha) \frac{Y_t}{L}$$

$$\rho_{jt} = \frac{\partial Y_t}{\partial Y_{jt}} = \alpha Y_t^{\alpha_Y} Y_{jt}^{-\frac{1}{\theta}},$$

where  $\alpha_Y = \frac{\alpha\theta - \theta + 1}{\alpha\theta}$ .

- Firm revenue is

$$\Pi_{jt} = \rho_{jt} Y_{jt}.$$

# Household $i$ 's Problem

- Household  $i$  chooses bond savings  $B_{it+1}$ :

$$\begin{aligned}
 \max_{B_{it+1}} \quad & C_{it,t} + \delta \tilde{\mathbb{E}}_t \{C_{it,t+1}\} - \int_0^1 \lambda A(\beta_{ijt}) dj \\
 \text{s.t.} \quad & C_{it,t} = W_t - \int_0^1 x_{ijt} P_{jt} dj - B_{it+1} \\
 & C_{it,t+1} = \int_0^1 x_{ijt} \Pi_{jt+1} dj + R_{t+1} B_{it+1} \\
 & C_{it,t}, C_{it,t+1} \geq 0.
 \end{aligned}$$

- Optimal saving decision:

$$B_{it+1} \begin{cases} = -\frac{\int_0^1 x_{ijt} \Pi_{jt+1} dj}{R_{t+1}} & \text{if } R_{t+1} < \frac{1}{\delta} \\ \in \left[ -\frac{\int_0^1 x_{ijt} \Pi_{jt+1} dj}{R_{t+1}}, W_t - \int_0^1 x_{ijt} P_{jt} dj \right] & \text{if } R_{t+1} = \frac{1}{\delta} \\ = W_t - \int_0^1 x_{ijt} P_{jt} dj & \text{if } R_{t+1} > \frac{1}{\delta} \end{cases}$$

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# Trader $ij$ 's Trading Problem

- Plugging  $B_{it+1}$  into the household's problem leads to trader  $ij$ 's trading problem:

$$\max_{x_{ijt} \in [0,2]} \tilde{\mathbb{E}} \left\{ x_{ijt} \left( \frac{1}{R_{t+1}} \Pi_{jt+1} - P_{jt} \right) \mid s_{ijt}, P_{jt} \right\}$$

- Trader  $ij$  buys two units whenever her valuation exceeds the prize,

$$x_{ijt} \begin{cases} = 0 & \text{if } \frac{1}{R_{t+1}} \tilde{\mathbb{E}} \{ \Pi_{jt+1} \mid s_{ijt}, P_{jt} \} < P_{jt} \\ \in [0, 2] & \text{if } \frac{1}{R_{t+1}} \tilde{\mathbb{E}} \{ \Pi_{jt+1} \mid s_{ijt}, P_{jt} \} = P_{jt} \\ = 2 & \text{if } \frac{1}{R_{t+1}} \tilde{\mathbb{E}} \{ \Pi_{jt+1} \mid s_{ijt}, P_{jt} \} > P_{jt} \end{cases}$$

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# Trader $ij$ 's Information Production Problem

- Optimal buying decision leads to information production problem:

$$\max_{\beta_{ijt}} \lambda_t \tilde{\mathbb{E}}_t \left\{ \underbrace{\mathcal{P}(x_{ijt} = 2)}_{\text{Probability of Buying}} \underbrace{\left( \frac{1}{R_{t+1}} \Pi_{jt+1} - P_{jt} \right)}_{\text{Rents}} \right\} - IA(\beta_{ijt}),$$

where  $\lambda_t = \max \{1, R_{t+1} \delta\}$ .

- Trader  $ij$ 's marginal benefit of increasing  $\beta_{ijt}$  is the central object of the model:

$$\widetilde{MB}(\beta_{ijt}, \beta_{jt}) \propto \tilde{\mathbb{E}}_t \left\{ \underbrace{\frac{\partial \mathcal{P}(x_{ijt} = 2)}{\partial \beta_{ijt}}}_{\text{Change in Probability of Buying}} \underbrace{\left( \frac{1}{R_{t+1}} \Pi_{jt+1} - P_{jt} \right)}_{\text{Rents}} \right\}.$$

- Producing more precise information makes buying more likely when rents are large.

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# Financial Market Clearing, Intuition

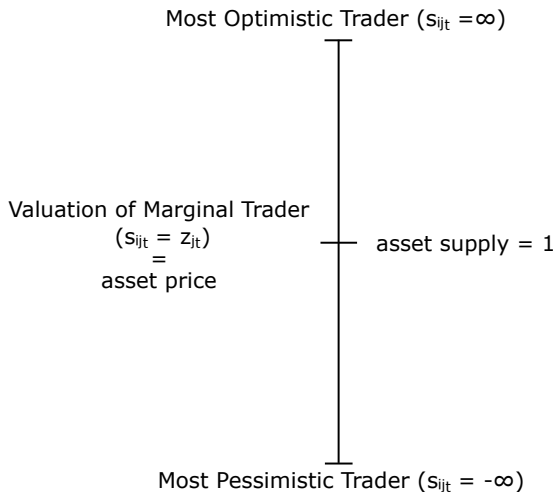


Figure: Price  $P_{jt}$  is equal to the marginal trader's valuation, who is indifferent between buying or not.



# Financial Market Clearing, Formal

- In eq ( $\forall i : \beta_{ijt} = \beta_{jt}$ ), trader  $ij$  demands two shares when  $s_{ijt}$  is above a threshold  $z_{jt}$ ,

$$x_{ijt} = 2 \iff s_{ijt} > z_{jt}.$$

- Market clearing

$$2 \left[ 1 - \Phi \left( \sqrt{\beta_{jt}} (z_{jt} - a_{jt}) - \varepsilon_{jt} \right) \right] = 1.$$

- Price signal

$$z_{jt} = a_{jt} + \frac{\varepsilon_{jt}}{\sqrt{\beta_{jt}}}.$$

- Price equal to the valuation of the marginal trader ( $s_{ijt} = z_{jt}$ ),

$$P_{jt} = \frac{1}{R_{t+1}} \mathbb{E} \{ \Pi_{jt+1} | s_{ijt} = z_{jt}, z_{jt} \}.$$

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# Productivity and Allocative Efficiency

## Proposition (Market Allocation)

(i) Firm-capital is given by

$$K_{jt+1} = \frac{\tilde{\mathbb{E}} \{A_{jt} | s_{ijt} = z_{jt}, z_{jt}\}^\theta}{\int_0^1 \tilde{\mathbb{E}} \{A_{jt} | s_{ijt} = z_{jt}, z_{jt}\}^\theta dj} K_{t+1}.$$

(ii) The aggregate production function is

$$Y_t = A(a_{t-1}, \beta_{t-1}) K_t^\alpha$$

with total factor productivity

$$\ln A(a_{t-1}, \beta_{t-1}) = \underbrace{A^{\text{ex}}(a_{t-1})}_{\text{exogenous}} + \underbrace{A^{\text{end}}(\beta_{t-1})}_{\text{allocative efficiency}}.$$

(iii)  $A(a_{t-1}, \beta_{t-1})$  is monotonically increasing in  $\beta_{t-1}$  if  $\sigma_\varepsilon^2$  is small enough.

Assumption

Non-monotonic TFP

# Productivity and Allocative Efficiency

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Non-monotonic TFP

# Productivity Shocks and Information

## Proposition

*Productivity booms decrease misallocation by encouraging information production.*

- Positive productivity shocks make all trades proportionally more valuable.
- Productivity-driven booms increase information production and TFP's endogenous component.

# Productivity Shock with fixed Info

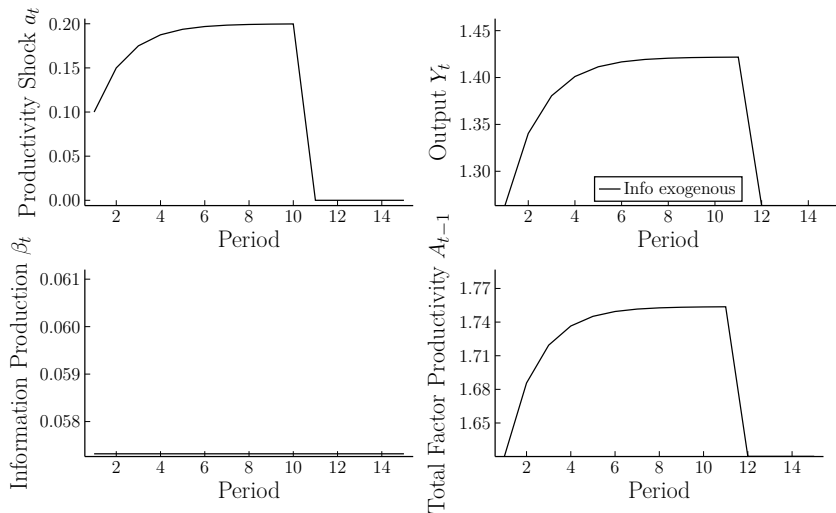
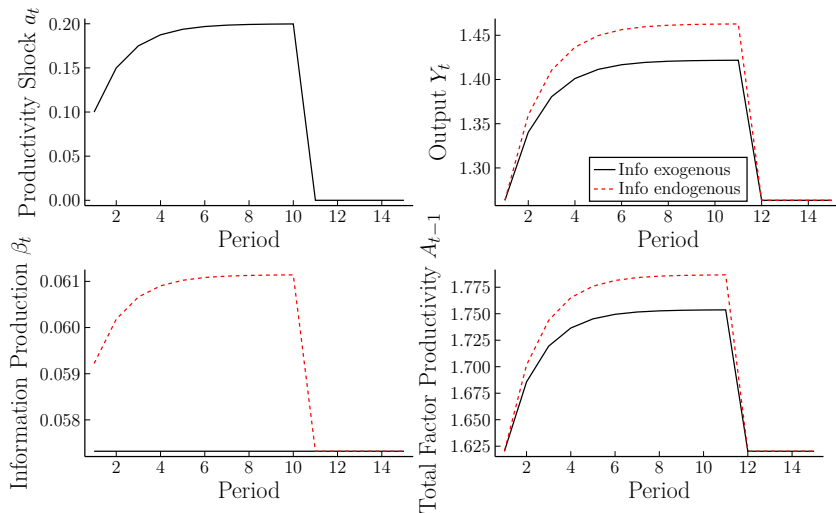


Figure: Productivity shocks increase exogenous TFP and investment.

# Productivity Booms are Amplified by Information Production



**Figure:** Productivity booms encourage information production, which amplifies the boom.

Detail

Misallocation

# Sentiment Shocks crowd out Information Production

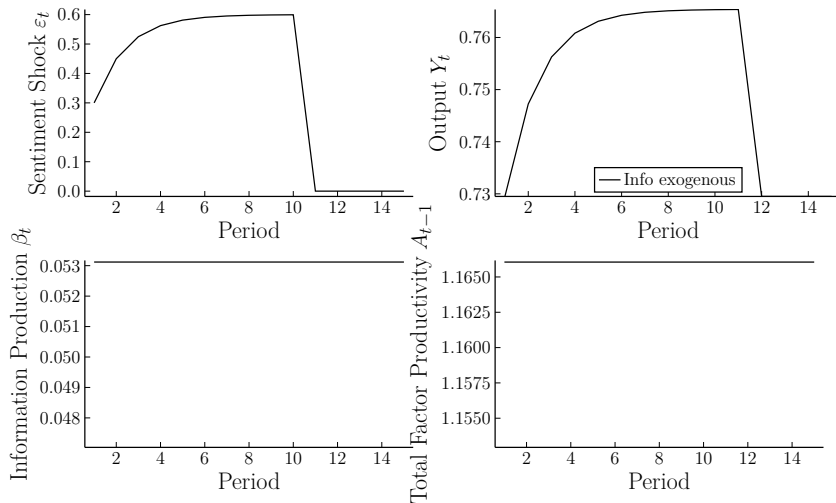
## Proposition

*Sentiment shocks, whether positive or negative, tend to increase misallocation by discouraging information production.*

- Private information becomes less likely to guide the trading decision.
- Sentiment booms decrease information production and TFP's endogenous component.

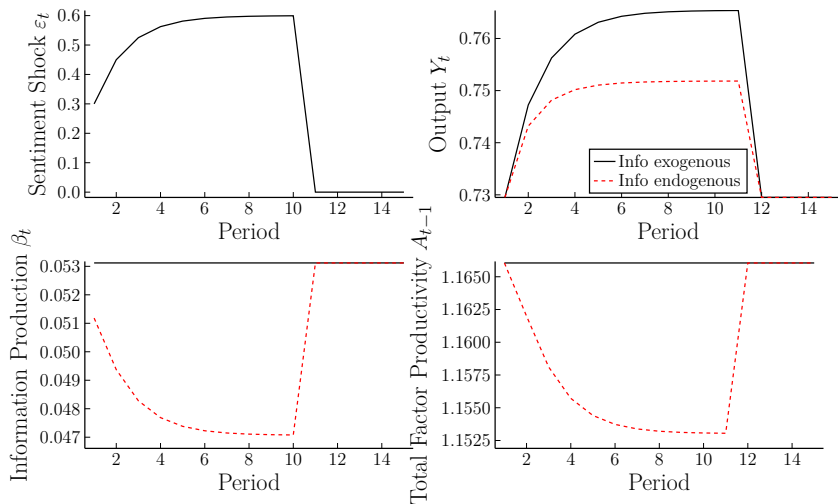


# Sentiment Booms with fixed Info leave TFP unaffected



**Figure:** Sentiment booms increase investment and output.

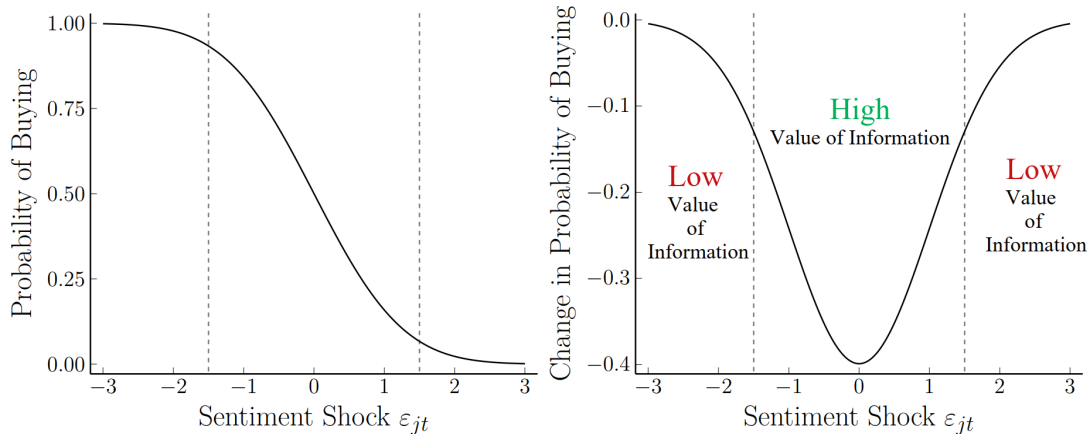
# Sentiment Booms are Dampened by Information Production



**Figure:** Sentiment booms increase misallocation by discouraging information production, which dampens the boom.

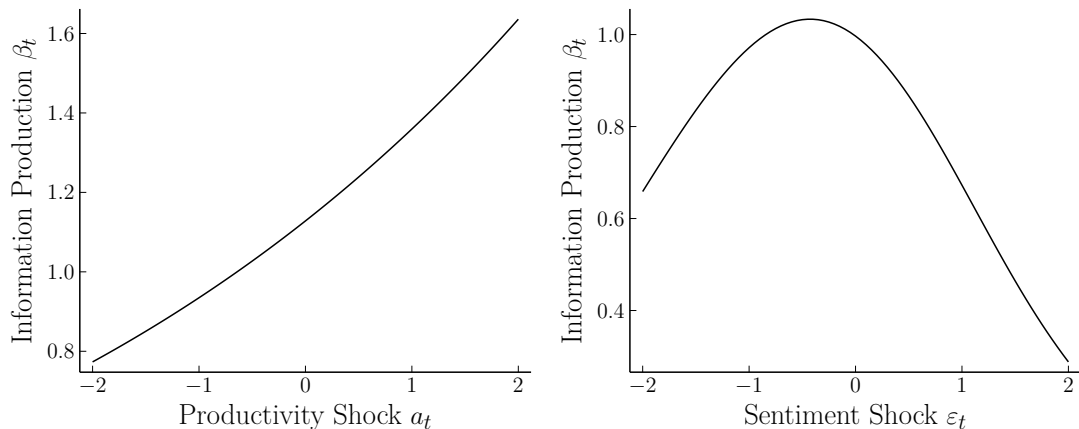
[Detail](#)
[Misallocation](#)

# Sentiment Shocks make Trading less information-sensitive



**Figure:** Positive and negative sentiment shocks make assets more mispriced.

# Information Production depending on Aggregate Shocks



**Figure:** Productivity booms *crowd in* information. Sentiment shocks (positive or negative) *crowd out* information.

[Detail Sentiment](#)

# Taking Stock

- Information plays a key role in the allocation of capital.
  - Two forces at firm-level: **Productivity** and **Sentiment**.
  - More information improves capital allocation among firms  $\Rightarrow$  higher TFP.
- Similarly, aggregate booms can be driven by these two forces.
  - **Productivity-Booms** *crowd in* information and increase TFP, **amplifying** the initial shock.
  - **Sentiment-Booms** *crowd out* information and decrease TFP, **dampening** the shock.
  - Rationalizes evidence for “good” and “bad” booms (Gorton and Ordoñez, 2020).
- Can the social planner improve on the laissez-faire equilibrium? Yes!

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# Social Planner's Two-Period Problem

- Two-period problem to abstract from inter-generational trade-offs.
- Focus on information frictions. Full Planner Problem
- Social planner dictates information production for each trader:

$$\begin{aligned}
 & \max_{\{\beta_{ij0}\}} \quad C_0 + \delta C_1 - \int_0^1 IA(\beta_{ij0}) \, dj \\
 s.t. \quad & C_1 = A_0(\{\beta_{ij0}\}) K_1^\alpha \\
 & C_0 = W_0 - K_1 \\
 & K_1 \text{ is determined competitively} \\
 & \beta_{ij0} \geq 0.
 \end{aligned}$$



# Information Production: Planner vs. Market

- **Rent-Extracting Behavior:** Produce info to extract rents from other traders:

Gain of Trader  $ij$  = Loss of other Traders (Rent Extraction).

- **Information Spillover:** *Collective* info production improves productivity:

$$\frac{\partial A_0(\beta_0)}{\partial \beta_0} > 0.$$

# Information Production: Planner vs. Market

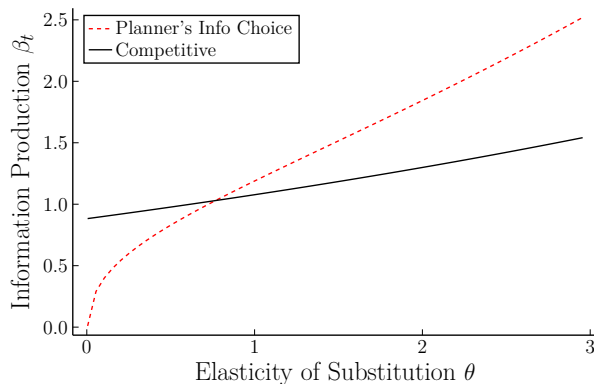
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# Planner vs. Laissez-faire Information Production



**Figure:** Low elasticity: Too much information production. High elasticity: Too little information production.

# No substitution: Information Unimportant for Allocation

- No substitution ( $\theta \rightarrow 0$ ):

$$\lim_{\theta \rightarrow 0} Y_t = L^{1-\alpha} (\inf K_{jt+1})^\alpha \Rightarrow K_{jt+1} = K_{t+1}.$$

- Information has **very little social value**.
- Yet, traders produce information as rents depend on  $A_{jt}$ :

$$\Pi_{jt+1} = \alpha Y_{t+1}^{\alpha_Y} A_{jt} K_{jt+1}^{\frac{\theta-1}{\theta}}.$$

# Perfect Substitution: Information Very Important for Allocation

- Perfect substitution ( $\theta = \infty$ ):

$$\lim_{\theta \rightarrow \infty} Y_t = L^{1-\alpha} \int_0^1 A_{jt} K_{jt+1} dj \Rightarrow \text{all capital to most prod. firm.}$$

- Information has **very high social value**.
- Yet, traders do not incorporate the social value of information.
- Bottom line: Traders produce too little information when capital allocation is important.

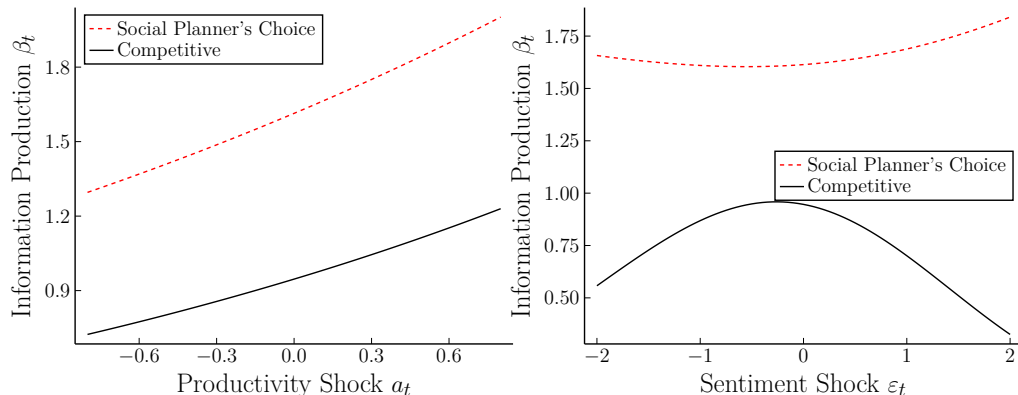
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# High $\theta$ : Planner's Response to Shocks



**Figure:** Social planner increases info production in response to productivity booms. In contrast, social planner increases information production in response to positive and negative sentiment shocks. [Implementation](#)

# Application: Asset Purchases

- In the past decade, asset purchases have been repeatedly used to stabilize financial markets and stimulate growth and inflation:
  - US: QE1 - QE4, Government bonds and mortgage backed securities.
  - UK, Eurozone: Government and corporate bonds.
  - Japan: Variety of assets, also stock ETFs (Okimoto, 2019).
- This raised concerns that asset purchases lift asset prices and growth, but destroy market efficiency.
  - DNB (2017): *"The large-scale purchase programmes and the flood of liquid assets has set the risk compass in financial markets spinning, with misallocations as a result."*
  - Model confirms this concern: asset purchases can decrease market efficiency.
  - But: Asset purchases, when used appropriately, can increase market efficiency. Problem



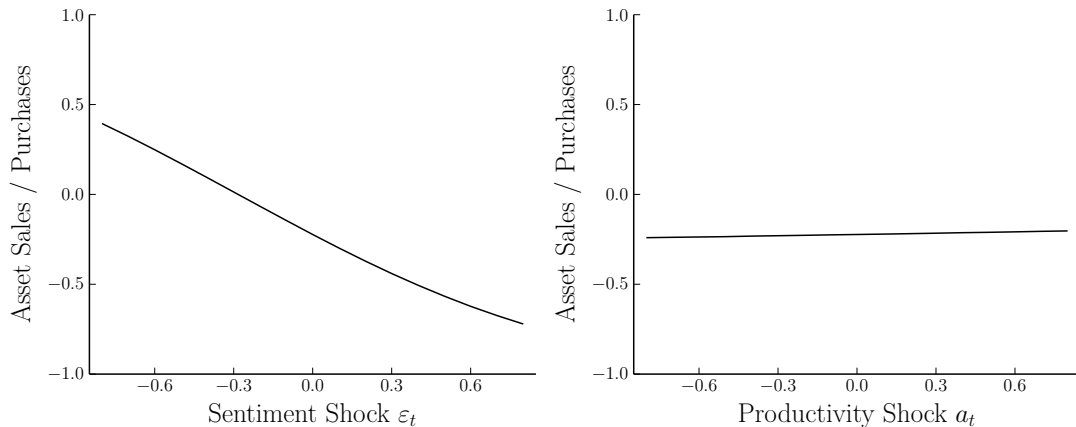
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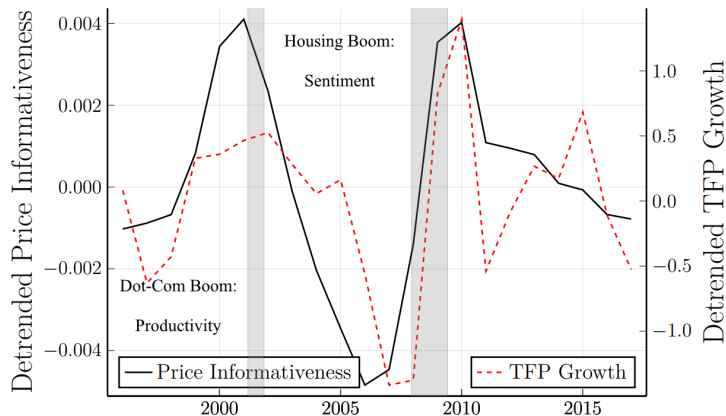
# Optimal Asset Purchases: Leaning against Sentiment



**Figure:** Social planner buys (sells) assets in response to negative (positive) sentiment shocks.

[Mechanism](#)[Uncertainty](#)

# Positive Co-Movement between Price Informativeness and TFP growth



**Figure:** Detrended Price Informativeness (Dávila and Parlatore, 2020) and TFP growth (San Francisco Fed) for the US.

Not Detrended

Dispersion

Derivation

Source TFP

# Conclusion

- I develop a tractable macroeconomic model with info production in financial markets.
  - Information is important for the allocation of capital and productivity.
- Booms have different effects on misallocation depending on their source.
  - Productivity booms *decrease misallocation by encouraging info production*.
  - Sentiment booms *increase misallocation by discouraging info production*.
- Dichotomy of “good” and “bad” booms as in Gorton and Ordoñez (2020).
- Information production in markets constrained inefficient:
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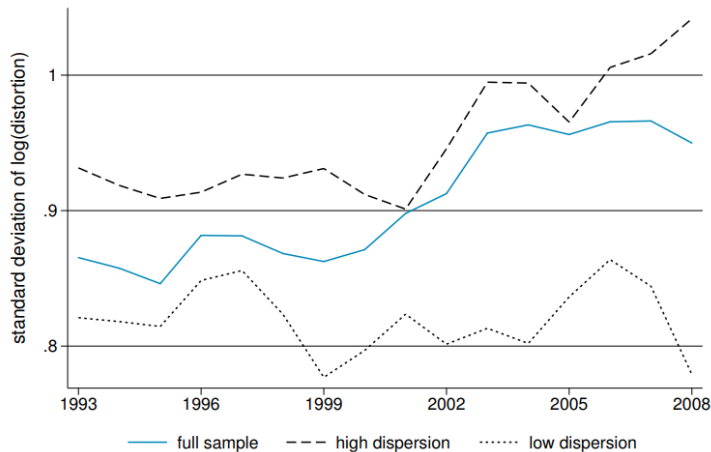


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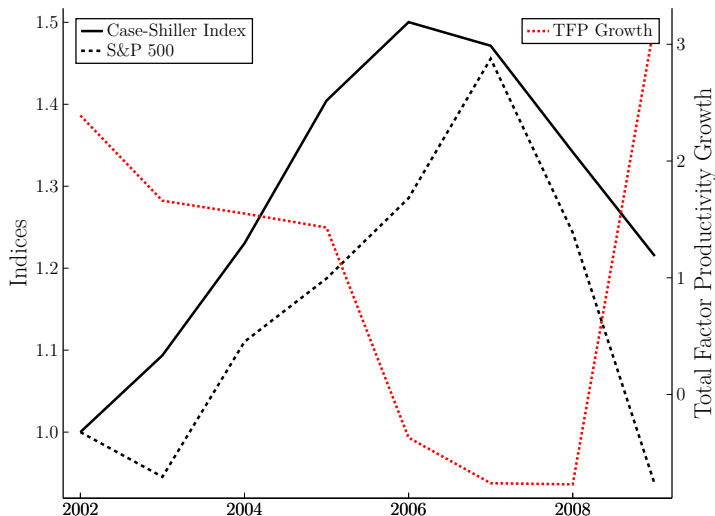
Gorton, Gary and Guillermo Ordoñez (2020). “Good Booms, Bad Booms.” In: *Journal of the European Economic Association* 18.2, pp. 618–665.

# Factor Misallocation increased during the US Housing Boom



**Figure:** “Yearly median of within industry-year standard deviation of log distortions.  $\log(\text{distortions})$  refers to the residual of a regression of  $\ln(k/I)$  on industry-year dummies. *dispersion* stands for dispersion in initial real estate value, split into top and bottom tercile.” Source: Doerr (2018). [Back](#)

# US experienced a Decline in Productivity during pre-crisis Boom



**Figure:** Asset price boom during slowdown in total factor productivity growth.

[Spain](#)
[Source TFP](#)
[Back](#)

# Similar experience in Southern Europe, for example Spain

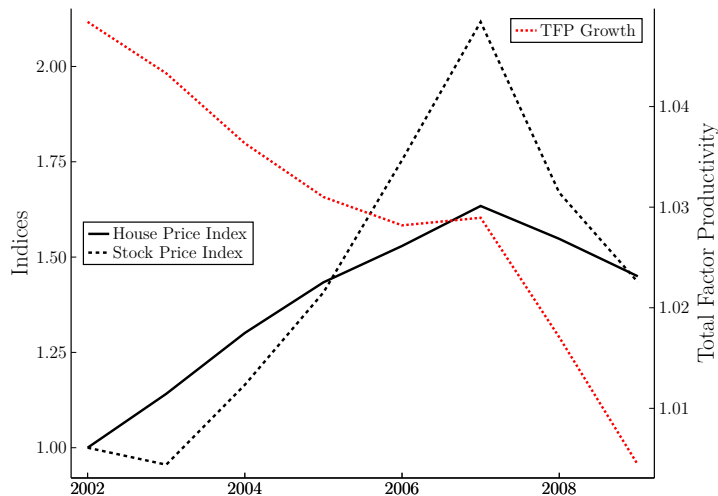


Figure: Total factor productivity declined, although asset prices were booming.

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# Decline in Information Production

- Asea and Blomberg (1998):
  - **Sample:** Panel dataset of 2 million loans by 580 banks between 1977-1993.
  - **Finding:** Banks systematically change their lending behavior from tight to lax over the cycle.
  - **Conclusion:** Banks decrease screening efforts / provide credit on easier terms during expansions.
- Keys et al. (2010):
  - **Sample:** Securitized subprime mortgage loan contracts in the US.
  - **Finding:** Portfolios that are easier to securitize default 10%-25% more often.
  - **Conclusion:** Incentives for screening declined during US housing boom because of securitization.
- Becker, Bos, and Roszbach (2020):
  - **Sample:** Credit, internal ratings by one of the four largest Swedish cross-border banks + external ratings from a credit bureau.
  - **Finding:** Internal credit rating more predictive of default during recessions.
  - **Conclusion:** The bank has worse info / info frictions are more severe during expansions.

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# Utilization-Adjusted TFP

- Source: San Francisco FED.
- Both labor and capital inputs are utilization adjusted following Basu, Fernald, and Kimball (2006).
- Industry-level production function: [Back Intro](#) [Back Empirical](#)

$$Y_i = F^i \left( \underbrace{A_i}_{\text{utilization}}, \underbrace{K_i}_{\text{capital}}, \underbrace{E_i}_{\text{effort}}, \underbrace{H_i}_{\text{hours}}, \underbrace{N_i}_{\text{labor}}, \underbrace{M_i}_{\text{inputs}}, \underbrace{Z_i}_{\text{technology}} \right)$$

# Overconfidence

- Overconfidence is one of the [most-studied behavioral biases](#). (Glaser and M. Weber, 2010; Daniel and Hirshleifer, 2015). [Back Results](#) [Back Overconfidence](#)
- Has been observed
  - with [managers in financial companies](#) (Ben-David, Graham, and Harvey, 2013),
  - with [traders and investment bankers](#) (Glaser, Langer, and M. Weber, 2013),
  - [in experimental settings](#) (Biais et al., 2005; Huffman, Raymond, and Shvets, 2019).
- Similar to correlation neglect due to imperfect understanding of signals' correlation structure.
  - Generally agents put [too much weight on correlated signals](#).
  - Chandrasekhar, Larreguy, and Xandri (2012), Brandts, Giritligil, and R. A. Weber (2015), Eyster et al. (2018), Grimm and Mengel (2018), and Enke and Zimmermann (2019).

# Grossman-Stiglitz Paradox in one Slide

- Following Grossman and Stiglitz (1980):

- Assume asset prices reflect all available information.
- Then, investors do not have any incentive to produce private information.
- However, if investors are uninformed, prices cannot reflect any information.

⇒ To incentivize information production, financial markets have to be imperfect.

- Some source of noise/irrationality is necessary.

- Most literature: noise traders.

- My paper: “micro-found” noise via overconfidence.

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# Entrepreneur's Problem

## Assumption

*Entrepreneurs can only sell claims to a fraction  $\lambda_{jt} \in [0, 1]$  of firm-revenue.*

- The entrepreneur solves

$$\begin{aligned} \max_{\lambda_{jt}, K_{jt+1}} \quad & \mathbb{E} \{ \Pi(a_{jt}, K_{jt+1}, Y_{t+1}) - D(a_{jt}, K_{jt+1}, Y_{t+1}) | P_{jt} \} \\ D(a_{jt}, K_{jt+1}, Y_{t+1}) = & \lambda_{jt} \Pi(a_{jt}, K_{jt+1}, Y_{t+1}) \\ 0 \leq K_{jt+1} \leq & P_{jt}, \end{aligned} \quad (P2)$$

where

$$\Pi(a_{jt}, K_{jt+1}, Y_{t+1}) = \rho_{jt+1} Y(a_{jt}, K_{jt+1}, Y_{t+1})$$

- The optimal decision by the entrepreneur is to choose  $K_{jt+1} = P_{jt}$  and  $\lambda^* = \frac{\theta-1}{\theta}$ . [Back](#)

# Equilibrium Definition

## Definition

*A symmetric, competitive equilibrium consists of prices  $\{W_t, \rho_{jt+1}, P_{jt}, P_t, R_{t+1}\}$  and allocations  $\{B_{it+1}, x_{ijt}, \beta_{ijt}, K_{jt+1}\}$  such that:*

- ① *Given prices  $\{W_t, \rho_{jt+1}, P_{jt}, R_{t+1}\}$  and allocations  $\{x_{ijt}, \beta_{ijt}\}$ ,  $B_{it+1}$  solves the household's problem.*
- ② *Given prices  $\{P_{jt}, R_{t+1}\}$  and allocations  $\{B_{it+1}, \beta_{jt}, K_{jt+1}\}$ ,  $\{x_{ijt}, \beta_{ijt}\}$  solve the trader's problem.*
- ③ *Prices are such that markets for shares, labor, intermediate goods, bonds and capital clear.*

# Assumption: Information increases TFP and Investment

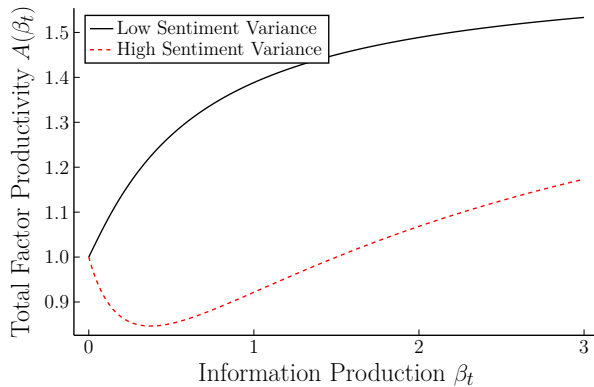
## Assumption

*The variance of firm-specific sentiment shocks  $\sigma_\varepsilon^2$  is low enough such that*

(i)  $\frac{\partial A(a_t, \beta_t)}{\partial \beta_t} > 0$ .

(ii) for  $\varepsilon_t = 0$ :  $\frac{\partial K_{t+1}(\beta_t)}{\partial \beta_t} \geq 0$ . [Back](#)

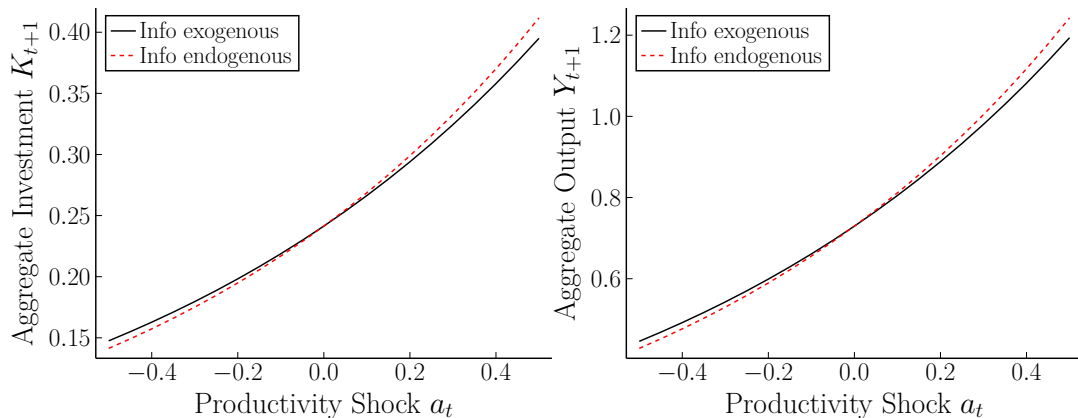
## TFP



**Figure:** Total factor productivity can be locally decreasing in  $\beta_t$  under the market allocation.

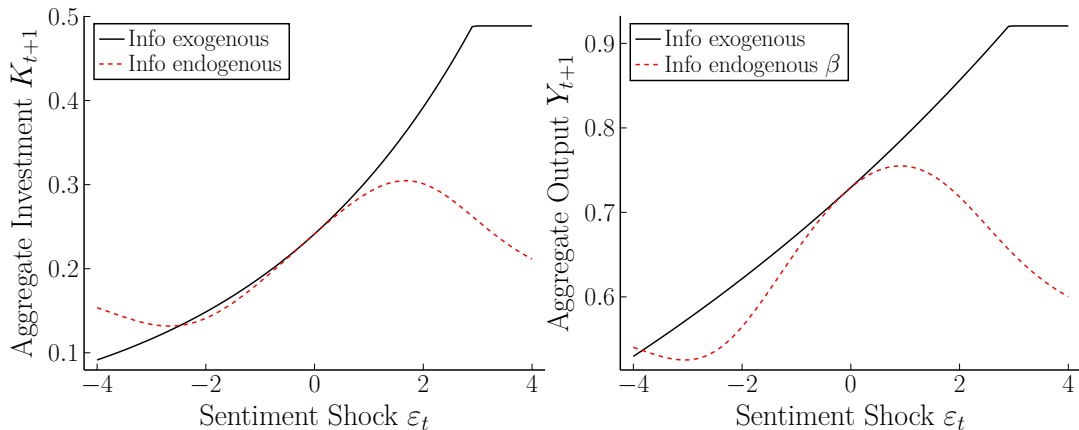
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# Amplification - Productivity Shock



**Figure:** Information production amplifies productivity shocks. [Back](#)

# Dampening - Sentiment Shock



**Figure:** Information production dampens positive sentiment shocks.

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# Dampening - Sentiment Shock

## Proposition

- (i) If  $\theta > \frac{1}{1-\alpha}$  and  $\beta^* < \frac{\sigma_a^{-2}}{1+\sigma_\varepsilon^{-2}}$ , information production dampens positive sentiment shocks.
- (ii) If  $\lim_{\varepsilon_t \rightarrow \infty} \sqrt{\beta_t(\varepsilon_t)}\varepsilon_t = 0$ , large positive sentiment shocks eventually lead to a decrease in aggregate investment.

- Direct effect: sentiment shocks increase investment.
  - But two indirect effects of decrease in info acq:
- 1 TFP  $\downarrow \Rightarrow$  investment  $\downarrow$ .
  - 2 Do beliefs get more or less noisy?

[Back](#)

# Rational and Noise Traders, building on Albagli, Hellwig, and Tsyvinski (2017)

- 1 Noise traders/mutual funds have demand  $\Phi(u_{jt})$ , where the noise trader shock  $u_{jt}$  is *iid* across time and markets.
- 2 Rational traders receive a signal  $s_{ijt} = a + \frac{\eta_{ijt}}{\sqrt{\beta_{ijt}}}$ , where  $\eta_{ijt} \sim \mathcal{N}(0, 1)$ . They can lend and borrow between each other at interest rate  $R_{t+1}$ 
  - 1 Position limits are given by  $x_{ijt} \in [0, 1]$ , and the equilibrium strategy is

$$x_{ijt} = 1 \iff s_{ijt} \geq z_{jt} \iff \frac{1}{R_{t+1}} \mathbb{E} \left\{ \Pi_{jt+1} | s_{ijt}, P_{jt} \right\} \geq P_{jt}(z_{jt}).$$

- 3 The market clearing condition in the symmetric equilibrium is

$$1 - \Phi\left(\sqrt{\beta_{jt}}(z_{jt} - a_{jt})\right) + \Phi(u_{jt}) = 1.$$

$$z_{jt} = a_{jt} + \frac{u_{jt}}{\sqrt{\beta_{jt}}}$$

- 4 Households allocate  $\gamma_t W_t$  to mutual funds

$$\gamma_t W_t = \int_0^1 \Phi(u_{jt}) P(z_{jt}) dj.$$

- 5 Households manage the remaining  $(1 - \gamma_t) W_t$  themselves, choosing  $\beta_{ijt}$  and positions  $x_{ijt}$ .

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# Sentiment Shocks II

- Marginal benefit of increasing  $\beta_{ijt}$  can be expressed as Analytical

$$\widetilde{MB}(\beta_{ijt}, \beta_{jt}) \Big|_{\beta_{ijt}=\beta_{jt}} \propto \tilde{\mathbb{E}}_t \left\{ \underbrace{\frac{\partial \mathcal{P}\{x_{ijt}=2\}}{\partial \beta_{ijt}} \Big|_{\beta_{ijt}=\beta_{jt}}}_{\text{Information-Sensitivity}} \left( \frac{K_{jt+1}}{K_{t+1}} \right)^{\frac{\theta-1}{\theta}} K_{t+1}^{\alpha} \left( A_{jt} - \tilde{\mathbb{E}}\{A_{jt} | s_{ijt} = z_{jt}, z_{jt}\} \right) \right\}$$

- There are three mechanisms:
  - 1 **Information-Sensitivity**: How likely is the private signal to change the trading decision?
  - 2 **Relative Size**: How large are firms for which information is valuable ( $\varepsilon_{jt} \approx 0$ )?
  - 3 **Absolute Size**: How large are firms on average? Back

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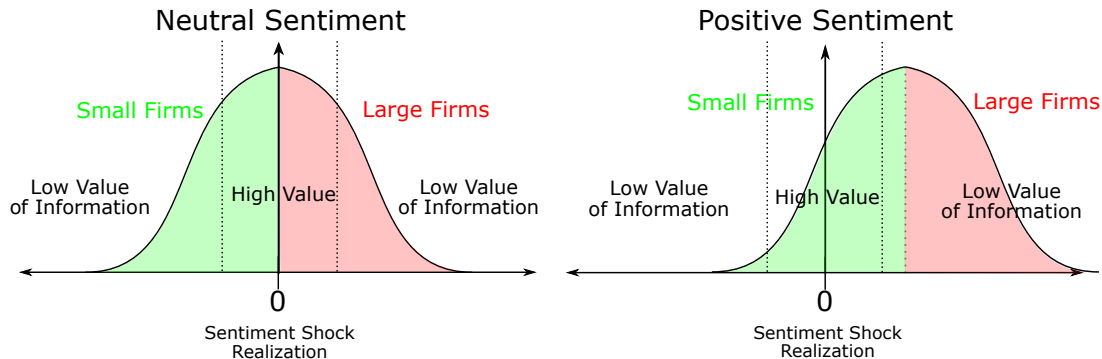
# Sentiment Shocks II: Analytical Expressions

- Marginal benefit of increasing  $\beta_{ijt}$  can be expressed as

$$\widetilde{MB}(\beta_{ijt}, \beta_{jt}) \Big|_{\beta_{ijt}=\beta_{jt}} \propto \exp \left\{ \underbrace{-\frac{\varepsilon_t^2}{2(1+\sigma_\varepsilon^2)}}_{\text{Information-Sensitivity}} \underbrace{-(\theta-1)\omega_{s\varepsilon}\varepsilon_t}_{\text{Relative Size}} + \underbrace{\frac{\alpha}{1-\alpha}\omega_{s\varepsilon}\varepsilon_t}_{\text{Absolute Size}} \right\}$$

- There are three mechanisms that drive this result:
  - 1 Information-Sensitivity: How likely is the private signal to change the trading decision?
  - 2 Relative Size: How large are firms for which information is valuable ( $\varepsilon_{jt} \approx 0$ )?
  - 3 Absolute Size: How large are firms on average? [Back](#)

# Relative Size



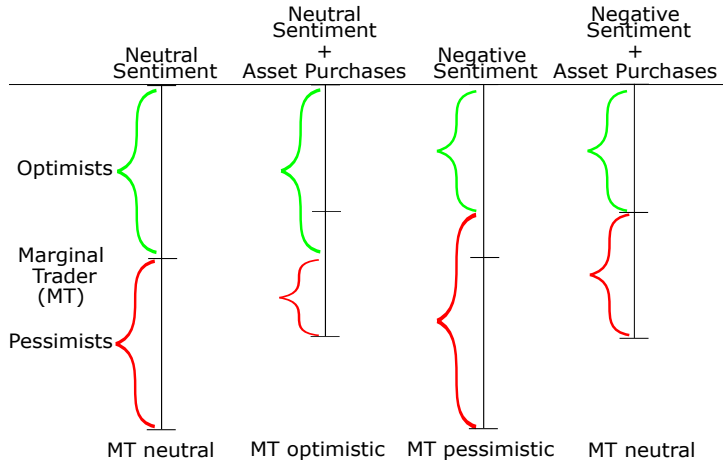
**Figure:** Firms with  $\varepsilon_{jt} \approx 0$  must appear unproductive when  $\varepsilon_t > 0$ .

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# Asset Purchases

- Asset purchases affect **investment and info production**.
  - Exploit **dispersed information**; changes to asset supply change the identity of marginal trader.
  - Decrease in asset supply makes the marginal trader more optimistic.
  - Introduces a bias in asset prices.
- Therefore, model supports arguments for and against asset purchases:
  - Purchases can counter negative sentiment shocks (negative bias + positive bias = no bias).
  - However, asset purchases also source of bias in absence of sentiment shocks.
- **Non-Ricardian effect**: Asset purchases can increase investment. [Back](#)

# Asset Purchases



**Figure:** Asset purchases introduce a positive bias in asset prices and can therefore offset negative sentiment shocks. [Back](#)

# Uncertainty: Revelation after Info Production

- Aggregate shocks get revealed after information production. [Back](#)
  - [Traders' expectations](#) about sentiment shocks distort information production.
  - Social planner can intervene perfectly if she shares same information set.
  - Contingent taxes/subsidies can fix investment.
- Surveys can be used to measure expectations about sentiment among traders.
  - “Do you expect markets to be driven by sentiment?”
- Similarly, dispersion of asset prices can be used to disentangle productivity and sentiment booms.
  - Asset prices increase and [firms appear more similar](#) → [sentiment boom](#).
  - Asset prices increase and [firms appear less similar](#) → [productivity boom](#).



# Uncertainty: Revelation only ex-post

- Aggregate shocks get revealed ex-post. [Back](#)
- Interventions must balance costs and benefits due to uncertainty.
- Aggregate prices send signal  $z_t = a_t + \frac{\varepsilon_t}{\sqrt{\beta_t}}$ . Prior on  $\{a_t, \varepsilon_t\}$  important when interpreting  $z_t$ .
- Info production can be used to dampen impact of sentiment shocks.

# Social Planner's Two-Period Problem

- Two-period problem to abstract from inter-generational trade-offs: [Back](#)

$$\begin{aligned}
 & \max_{K_{j1}, C_0, C_1, \beta_{j0}} \quad C_0 + \delta \mathbb{E}_0 \{C_1 | \{z_{j0}\}\} - \int_0^1 IA(\beta_{j0}) dj \\
 & s.t. \quad K_1 = W_0 - C_0 \\
 & \quad \quad C_1 \leq Y_1(\{K_{j1}\}, \{\beta_{j0}\}) \\
 & \quad \quad C_0 \leq W_0 \\
 & \quad \quad C_0, C_1, \beta_{j0}, K_{j1} \geq 0.
 \end{aligned}$$

# Constraint-Efficient Capital Allocation

- Firm capital is given by Price Distortion

$$K_{j1}^{SP} = \frac{\mathbb{E} \{A_{j0}|z_{j0}\}^\theta}{\int_0^1 \mathbb{E} \{A_{j0}|z_{j0}\}^\theta dj} K_1^{SP}.$$

- Does not overreact to  $z_{j0}$  as market allocation,

$$K_{j1}^{CE} = \frac{\tilde{\mathbb{E}} \{A_{j0}|x_{ij0} = z_{j0}, z_{j0}\}^\theta}{\int_0^1 \tilde{\mathbb{E}} \{A_{j0}|x_{ij0} = z_{j0}, z_{j0}\}^\theta dj} K_1^{CE}.$$

- Aggregate output and productivity are given by

$$Y_1^{SP} = A_0^{SP} (K_1^{SP})^\alpha \quad \text{with } A_0^{SP} = \left( \int_0^1 \mathbb{E} \{A_{j0}|z_{j0}\}^\theta dj \right)^{\frac{\alpha}{\theta-1}}.$$

- Where  $A_0^{SP} > A_0^{CE}$  for interior values of  $\beta_0$ . Back

## Wedge

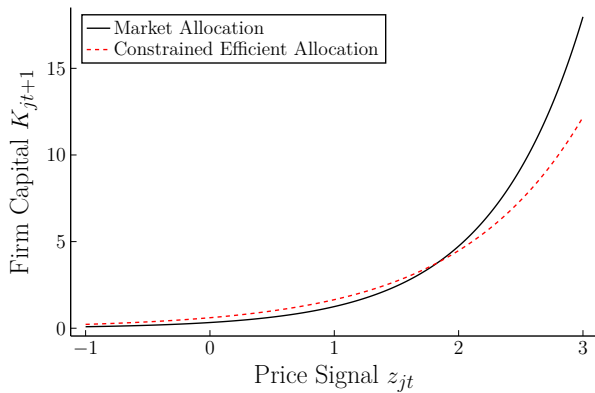


Figure: Market allocation of capital and the constrained-efficient allocation.

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# Decentralized Implementation: Investment

- A combination of taxes and subsidies can be used to implement the social planner's allocation.
  - Taxes are collected lump-sum from young generation.
  - Revenue is rebated lump-sum to same generation when old.
- Tax/subsidy on dividends:

$$\Pi_{j1}^{DE} = \tau^{Bias}(z_{j0}) \Pi_{j1}, \quad \text{where } \tau^{Bias}(z_{j0}) = \frac{\mathbb{E}\{A_{j0}|z_{j0}\}}{\tilde{\mathbb{E}}\{A_{j0}|x_{ij0} = z_{j0}, z_{j0}\}}.$$

- 1 Redistributes capital from large to small firms.
- 2 Tax on investment when sentiment is positive.

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# Decentralized Implementation: Information

- Tax/subsidy on information production:

$$\frac{\partial IA^{DE}(\beta_{ij0})}{\partial \beta_{ij0}} = \tau^{Info}(\beta_{ij0}) \frac{\partial IA(\beta_{ij0})}{\partial \beta_{ij0}}, \quad \tau^{Info}(\beta_{ij0}) = \frac{\widetilde{MB}^{CE}(\beta_{ij0}, \beta_{j0}) \Big|_{\beta_{ij0}=\beta_{j0}}}{\delta \frac{\partial A_0}{\partial \beta_0} K_1^\alpha}.$$

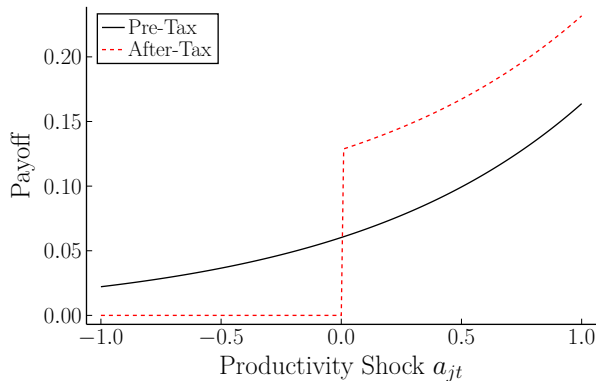
- 1 Makes traders target TFP when acquiring information.
- 2 Subsidize information production when sentiment shock hits.

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# Implementation of Social Planner's Information Choice

- ① Direct subsidies/taxes on information production.
  - For example, tax credits for expenses related to info acq.
- ② Use subsidies/taxes to make buying assets riskier/safer:
  - Taxes on profits and deductions for losses → flatten payoff function.
  - Taxes on losses and subsidies for profits → steepen payoff function.

# Implementing more Info Production



**Figure:** Tax/subsidy scheme incentivizes info production by increasing exposure to productivity shock.

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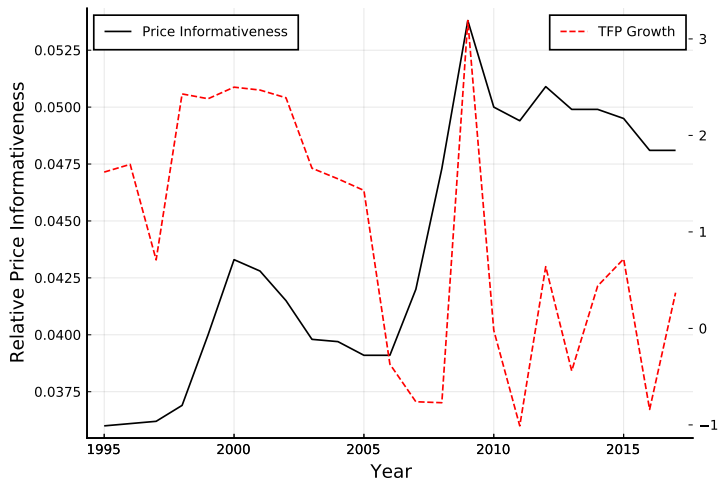


# Planner's Problem: Asset Purchases and Sales

- Let social planner use asset purchases / sales: [Back](#)

$$\begin{aligned}
 & \max_{x_0^{SP} \in (-1,1)} C_0 + \delta C_1 - \int_0^1 IA(\beta_{j0}) dj \\
 \text{s.t. } & C_{i0} = W_0 - \int_0^1 x_{ij0} P_{j0} dj - B_{i1} - x_0^{SP} \int_0^1 P_{j0} dj \\
 & C_{i1} = \int_0^1 x_{ij0} \Pi_{j1} dj + R_1 B_{i1} + x_0^{SP} \int_0^1 \Pi_{j1} dj \\
 & C_0, C_1 \geq 0. \\
 & x_{ij0}, B_{i1}, P_{j0}, \beta_{j0} \text{ are determined competitively.}
 \end{aligned}$$

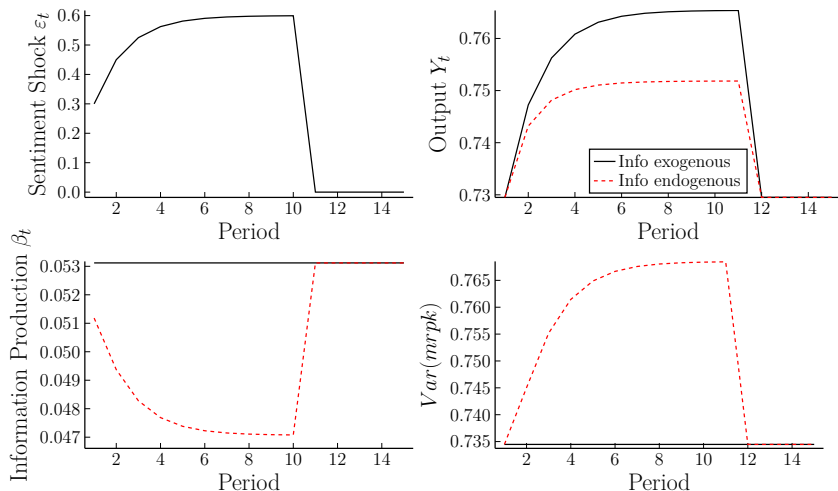
# Price Informativeness and TFP growth for the US



**Figure:** There is positive co-movement between price informativeness and TFP growth.

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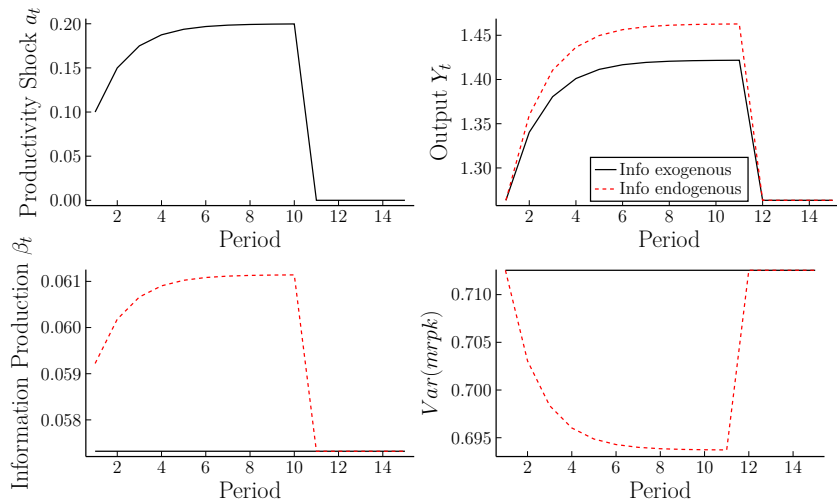
# Dispersion in $mrpk$ increase during Sentiment Boom



**Figure:** Capital becomes increasingly misallocated during a sentiment boom.

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# Dispersion in $mrpk$ decreases during Productivity Boom



**Figure:** Capital becomes less misallocated during a productivity boom.

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# Price Informativeness: How informative are Prices about Earnings Tomorrow?

- Relative price informativeness in my model is

$$\frac{\beta (1 + \sigma_{\varepsilon}^{-2})}{\sigma_a^{-2} + \beta (1 + \sigma_{\varepsilon}^{-2})}.$$

- Dávila and Parlato (2020) run two regressions at the firm level:

$$\Delta p_t = \bar{\beta} + \beta_0 \Delta x_t + \beta_1 \Delta x_{t+1} + e_t \quad (R1)$$

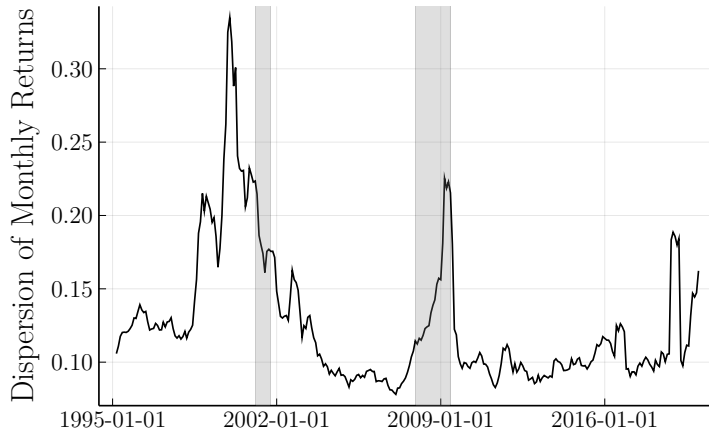
$$\Delta p_t = \bar{\zeta} + \zeta_0 \Delta x_t + e_t^{\zeta} \quad (R2)$$

- Relative price informativeness is then derived as

$$\frac{R_{\Delta x, \Delta x'}^2 - R_{\Delta x}^2}{1 - R_{\Delta x}^2}.$$

- where  $R_{\Delta x, \Delta x'}^2$  belongs to (R1) and  $R_{\Delta x}^2$  to (R2). [Back](#)

# Alternative Measure of Information: Return Dispersion



**Figure:** Return dispersion was high during dot-com boom leading up to 2001, but low during the housing boom.

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