

# Data Analysis 2: Foundations of Statistics

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# Types of Random Variables

- Continuous, takes values in any interval
  - i.e prices, temperature, grades...
- Discrete, countable number of values
  - i.e hotel stars, gender, number of rooms...

Each have their own distributions

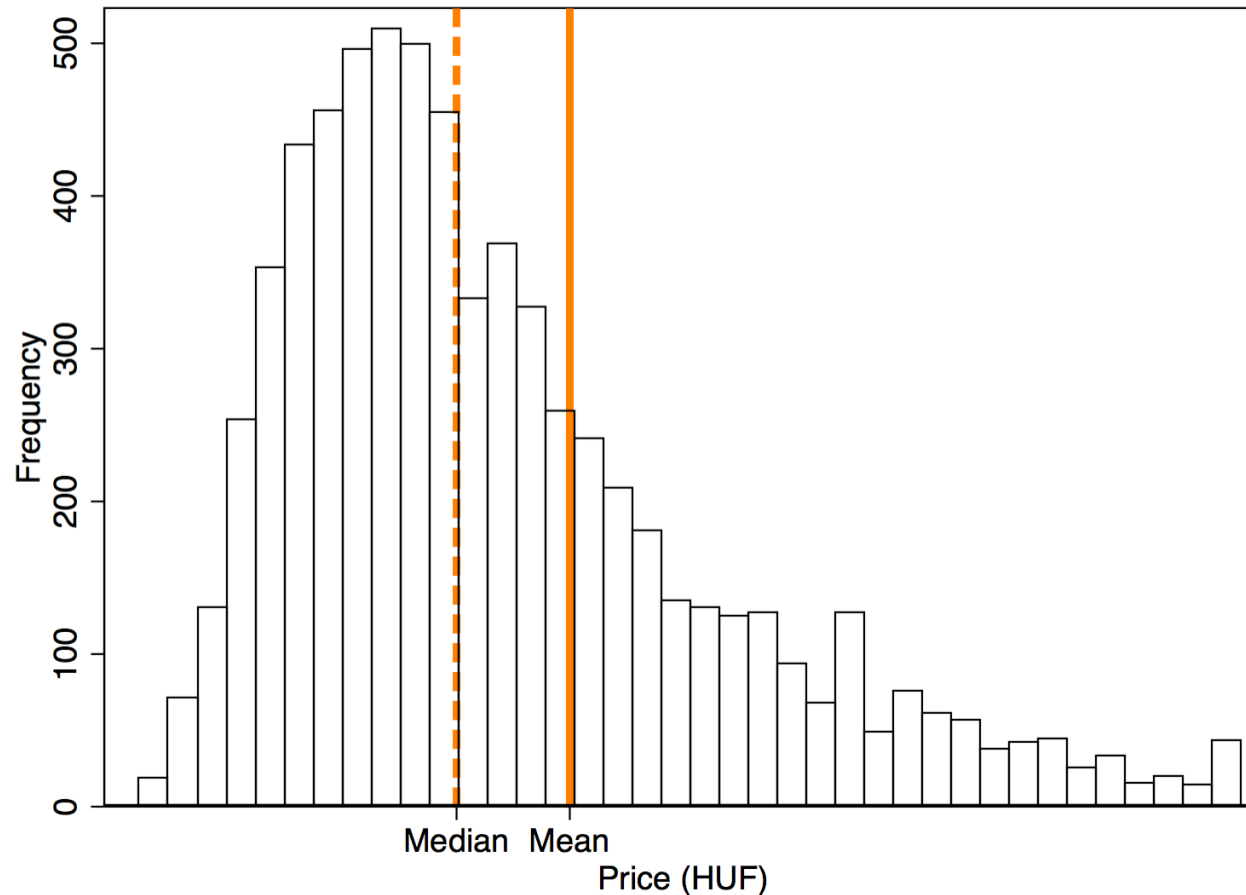
# Distributions in Practice

- The distribution of a variable tells the number of times each possible value of the variable occurs in the data
  - Can be expressed as frequency, percentage
- It does so in isolation from other variables.
  - It does not tell if certain values are more likely to occur when some other variable, or variables, take certain values

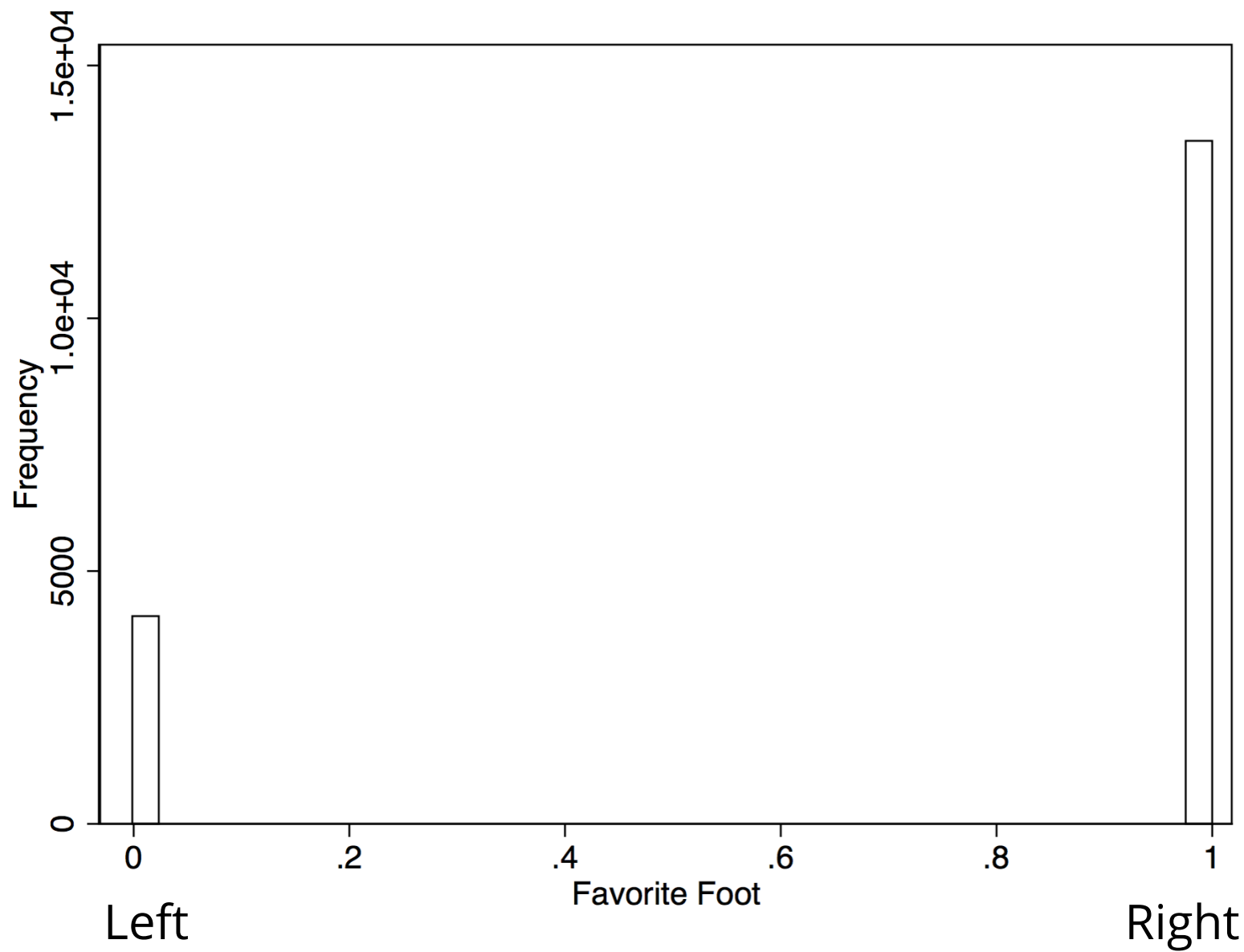
- The simplest way to visualize a distribution is through an histogram
- The histogram may takes on as many bars as the number of possible values
- From visual inspection of histograms we find out many interesting properties
  - the peaks, the immediate neighbourhood, if they have tails etc

**Let's go back to our hotel price example.  
What do we see?**

# Histograms in practice

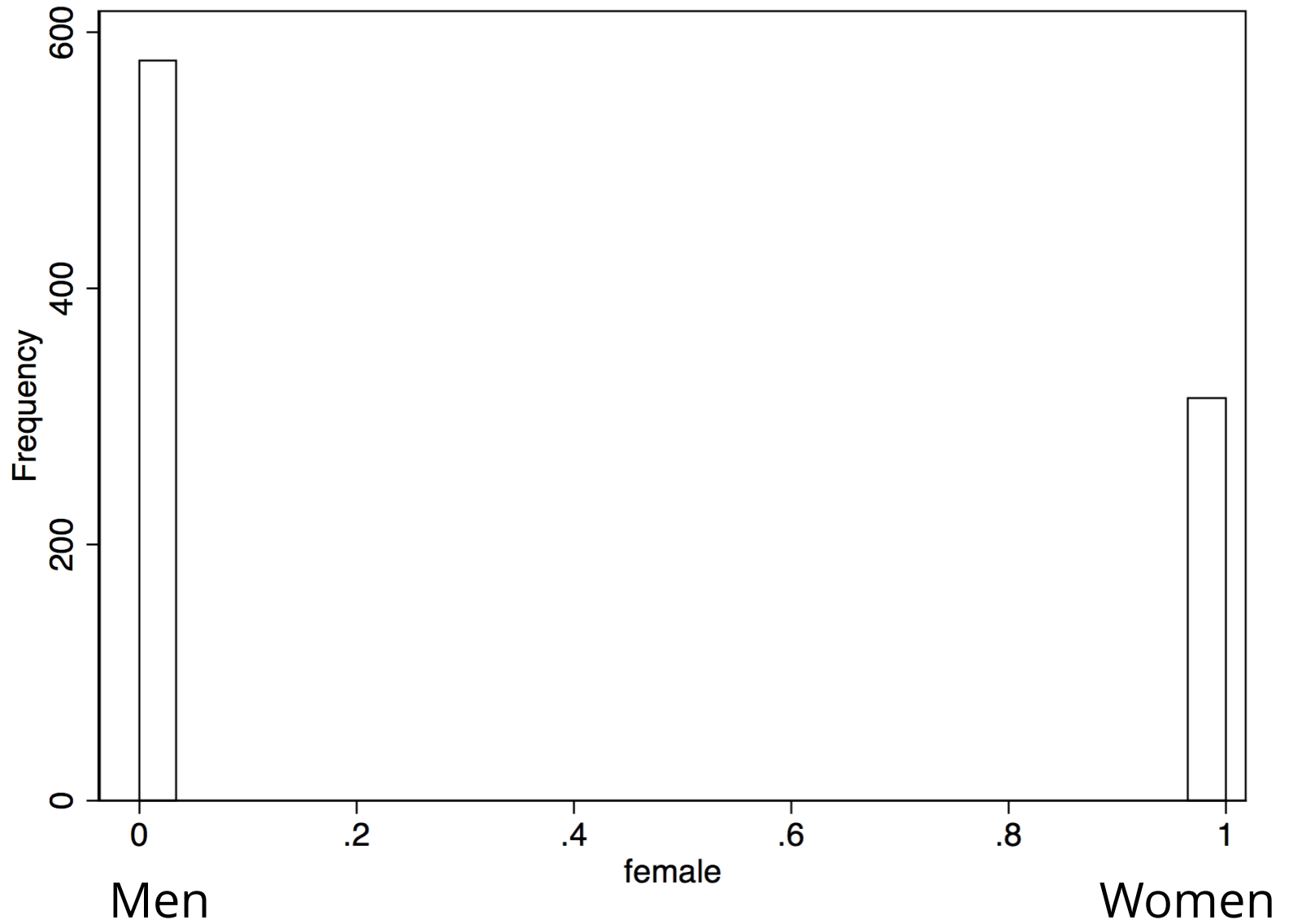


**If I tell you that football players have a  
favorite foot?**

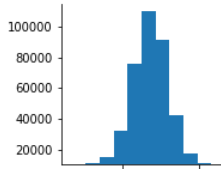




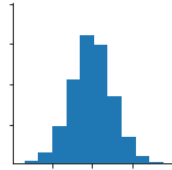
# Titanic passengers data



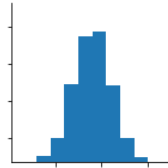
- Some of the properties of the distributions change if we change their bin size
  - Very wide bins may lump together multiple modes.
  - The statistical softwares you use, will compute the histogram with the default bin size
    - Try to figure out on your own the bin size that Stata or R use for their histograms.
    - Play with the simulations of distributions I provided you with by changing mean, variance, number of observations, and binsize
    - Is this also the case for discrete variables?



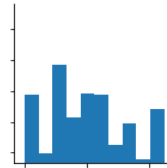
Average Area Income



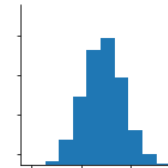
Average Area House age



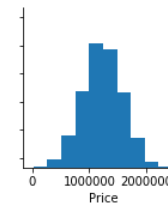
Number of rooms



Number of bedrooms

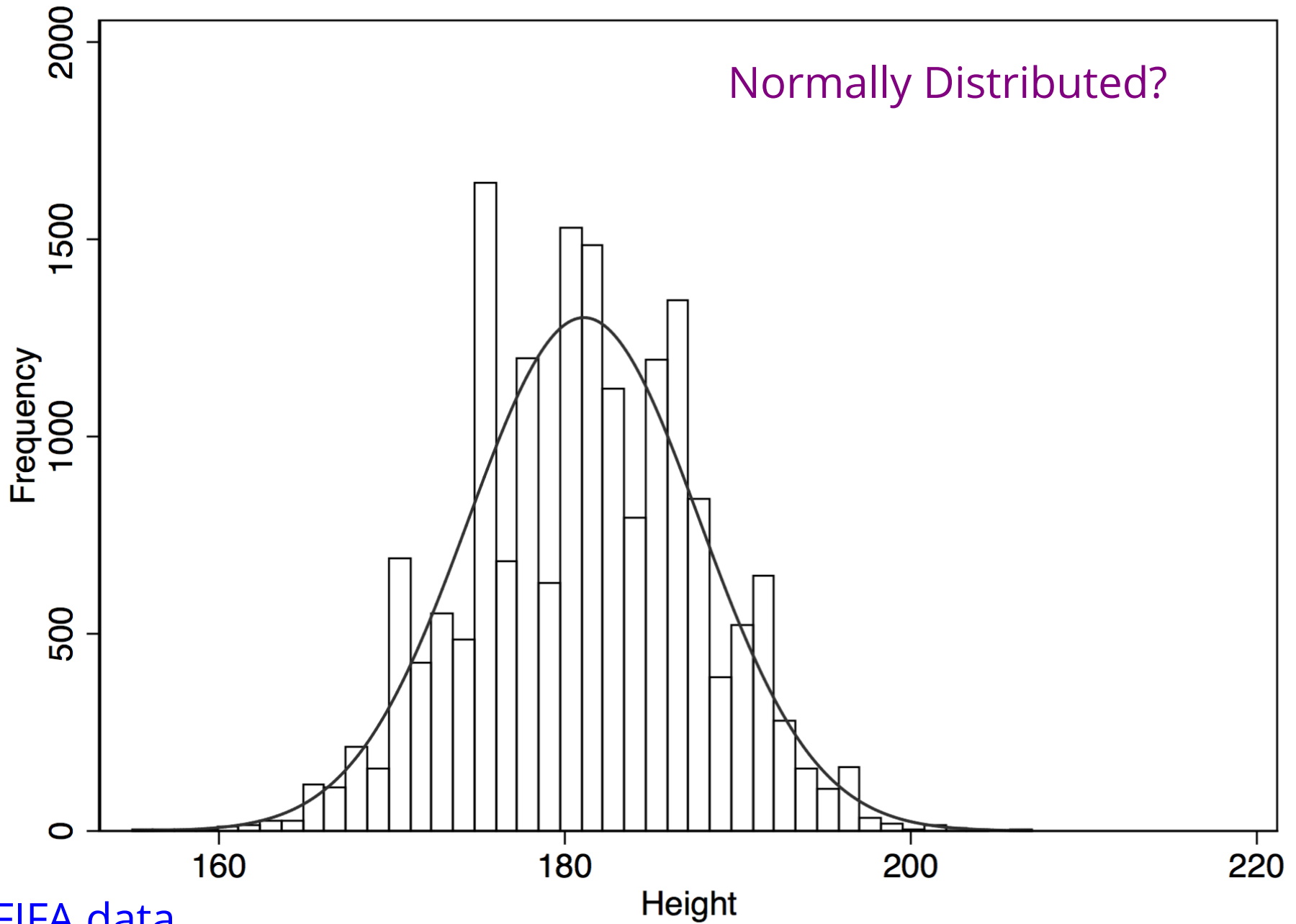


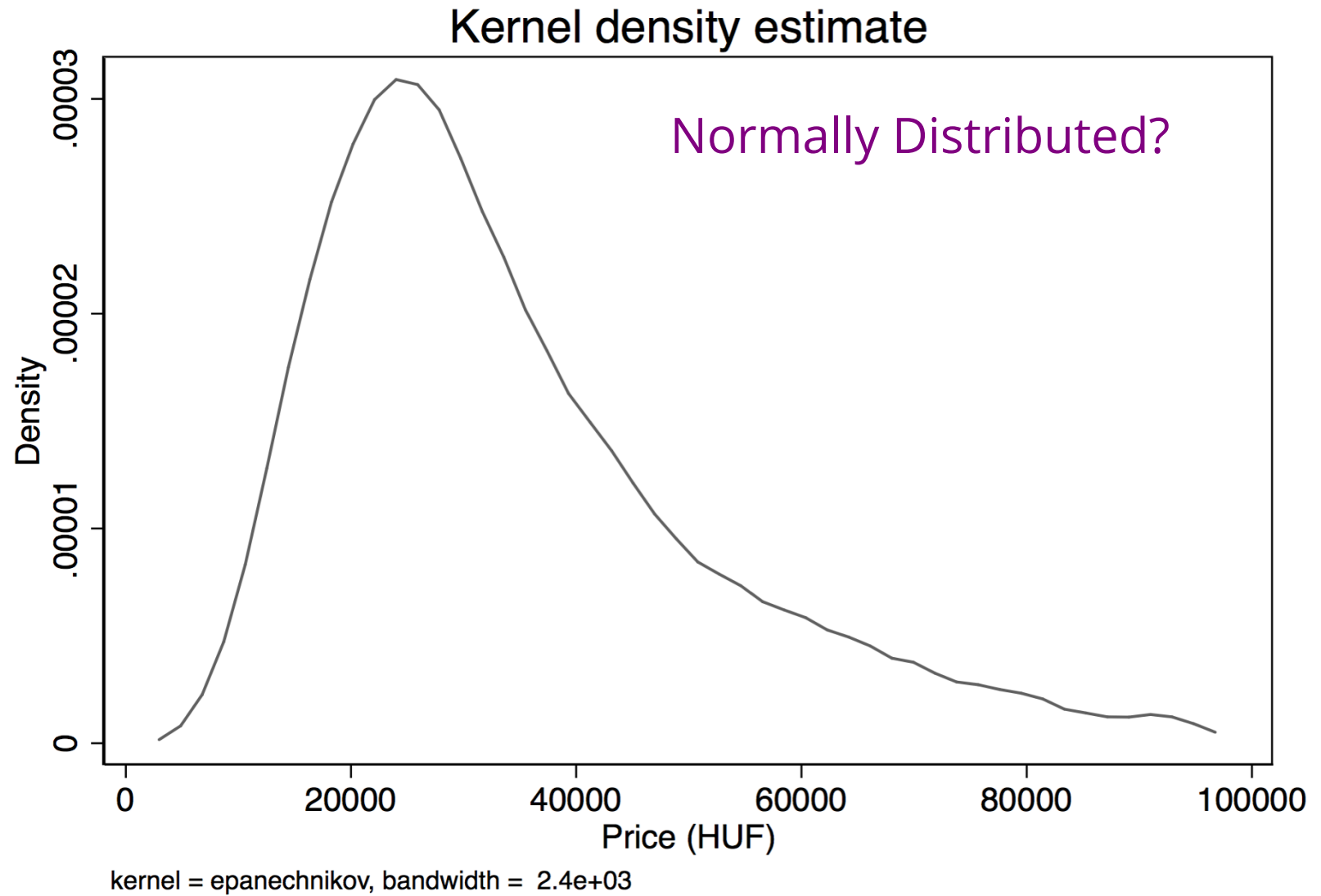
Area Population



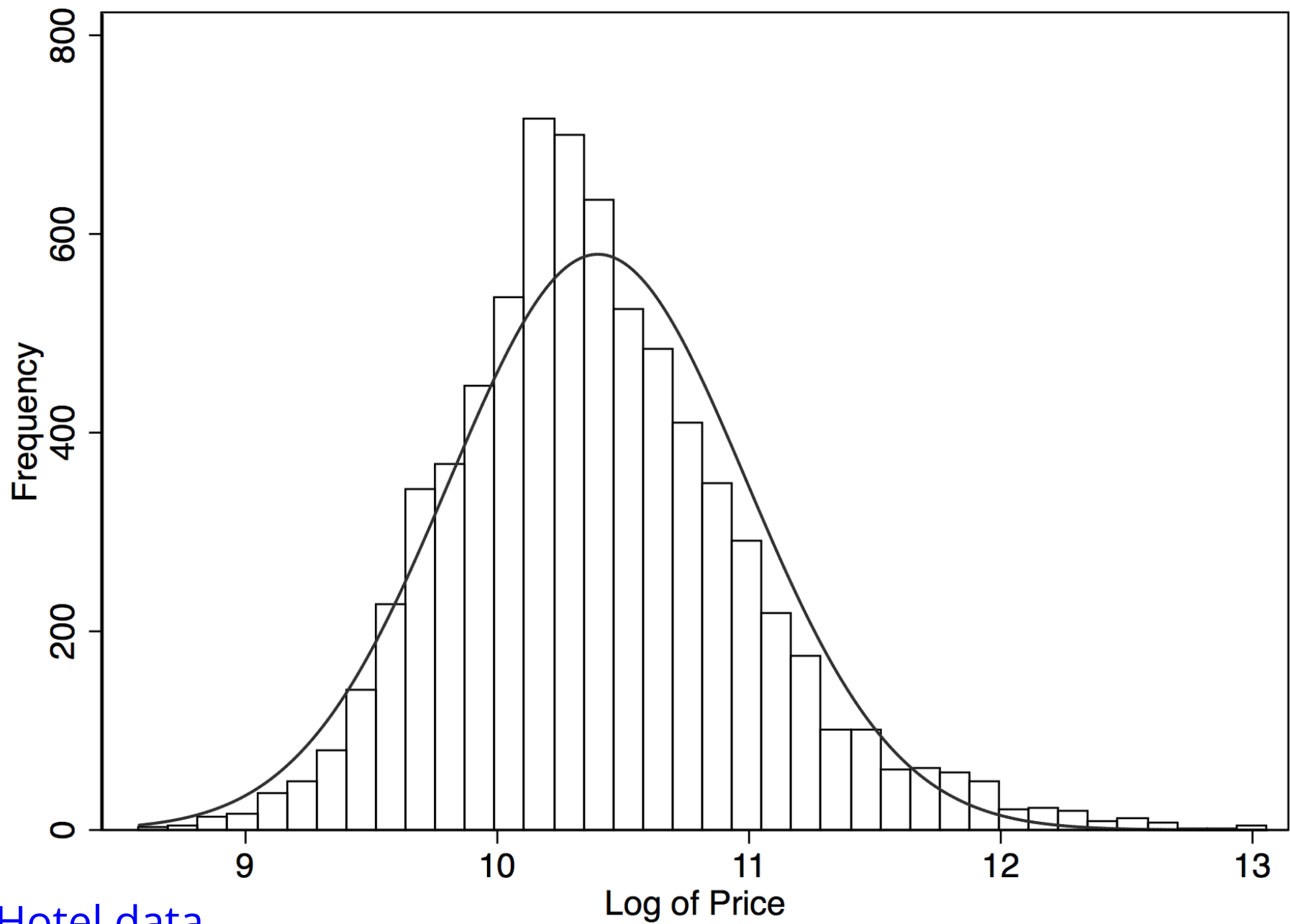
Price

- Kernel densities are an alternative way to histograms
  - for variables with many potential values
- A way to think about them is like curves that wrap around the corresponding histogram
- The most important parameter to set is the bandwidth, which is similar to setting the binsize in the histogram



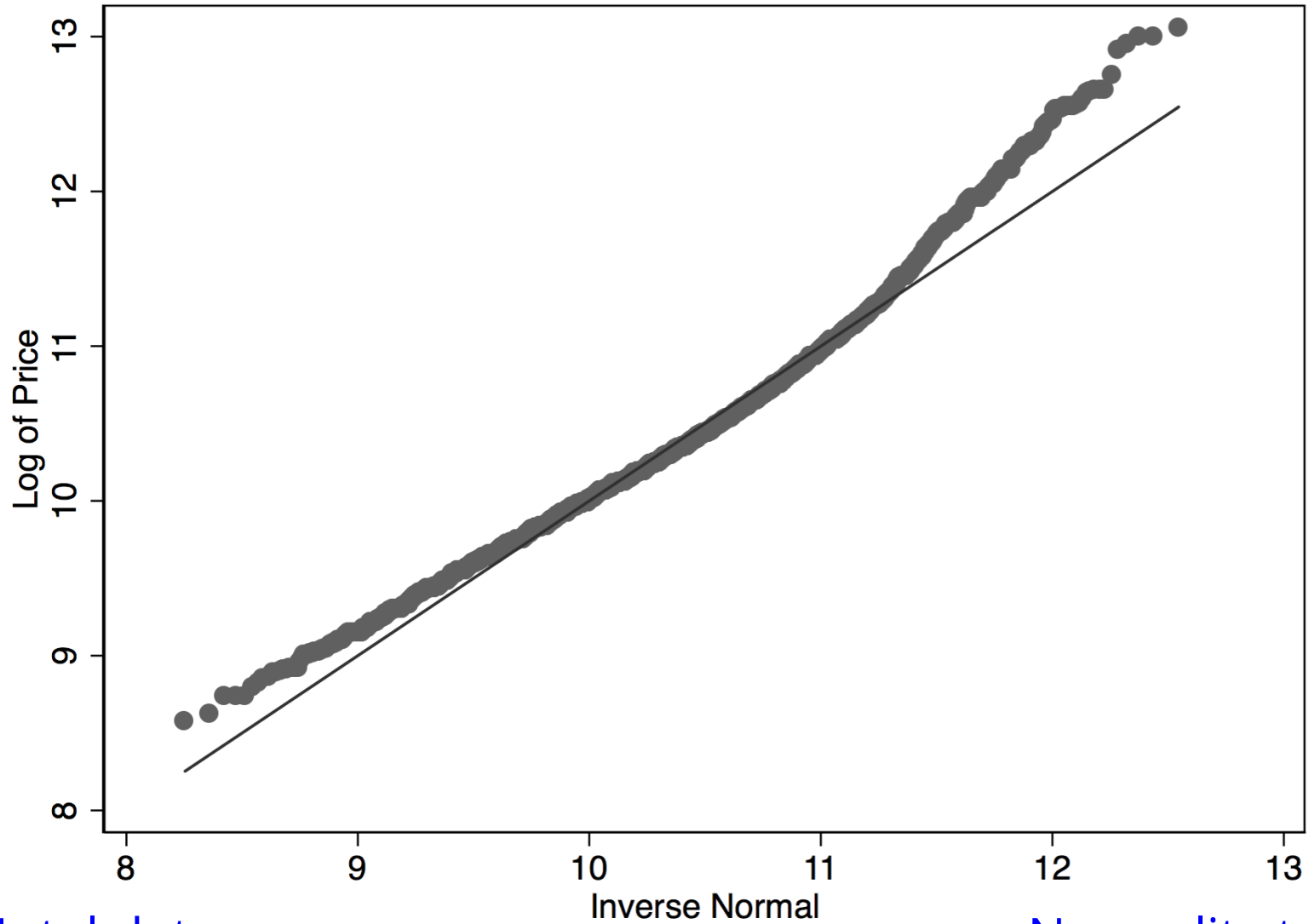


Hotel data



Hotel data





Hotel data

Normality test

# Joint Distributions

- In real life, we are often interested how variables that are related to each other. For example, number of rooms or bedrooms and average price of the house
  - The joint distribution shows the probabilities of each value combination of these variables we are interested in

# Conditional Distributions

- Conditional distributions are distributions of one variable for one (or more) values of the other variable

# Covariance

- It provides an indication of the dependence between two variables

$$Cov(x, y) = \frac{\sum_i (x_i - \bar{x})(y_i - \bar{y})}{n}$$

# Covariance

- In case:  $y_i = a + bx_i$

$$Cov(x, y) = \frac{b \sum_i (x_i - \bar{x})(x_i - \bar{x})}{n}$$

# Correlation

- Is computed by dividing the covariance by the standard deviation of each variable

$$\rho = \text{Corr}(x, y) = \frac{\text{Cov}(x, y)}{\text{Std}(x) \cdot \text{Std}(y)}$$

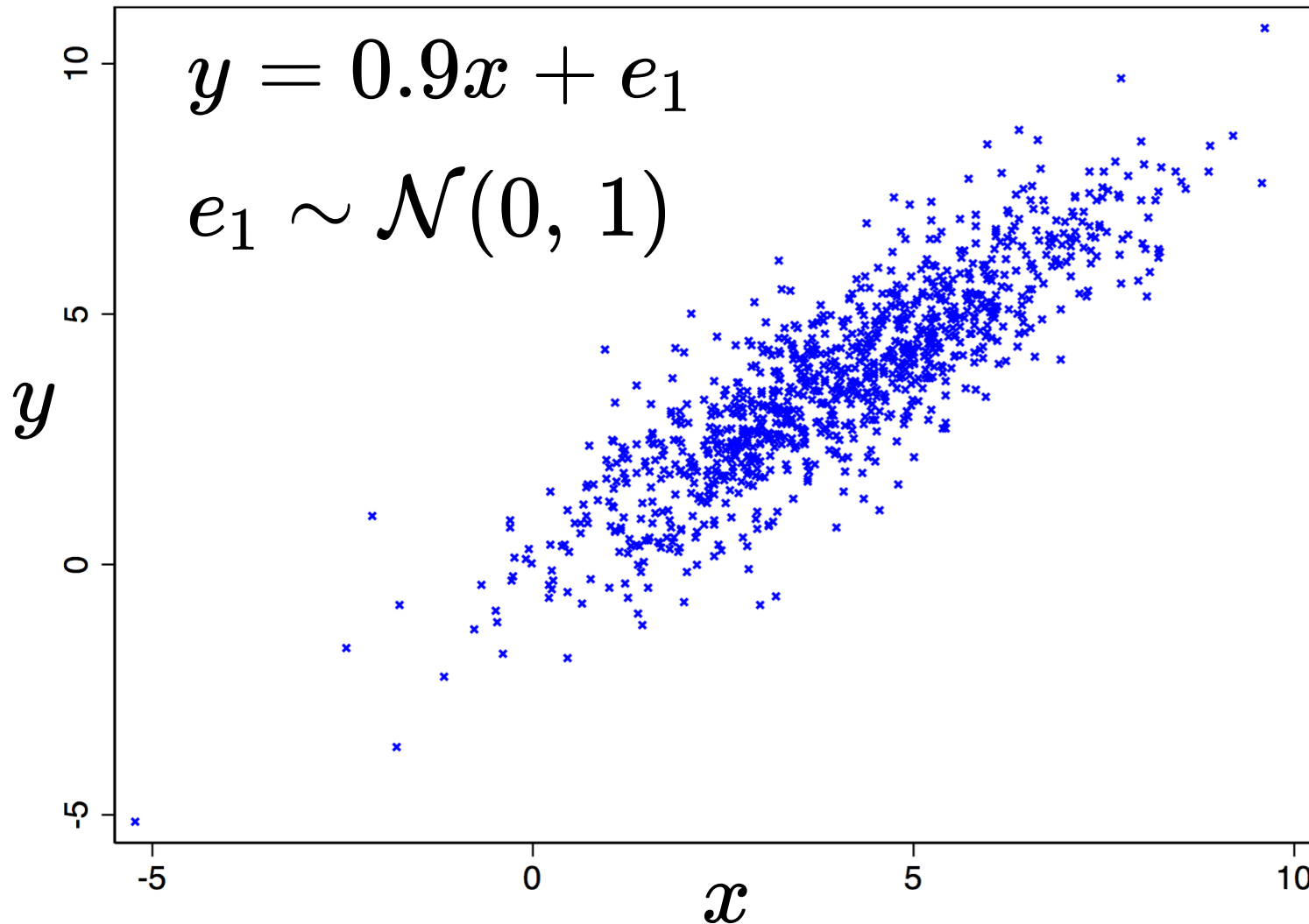
$$\rho \in [-1, 1]$$

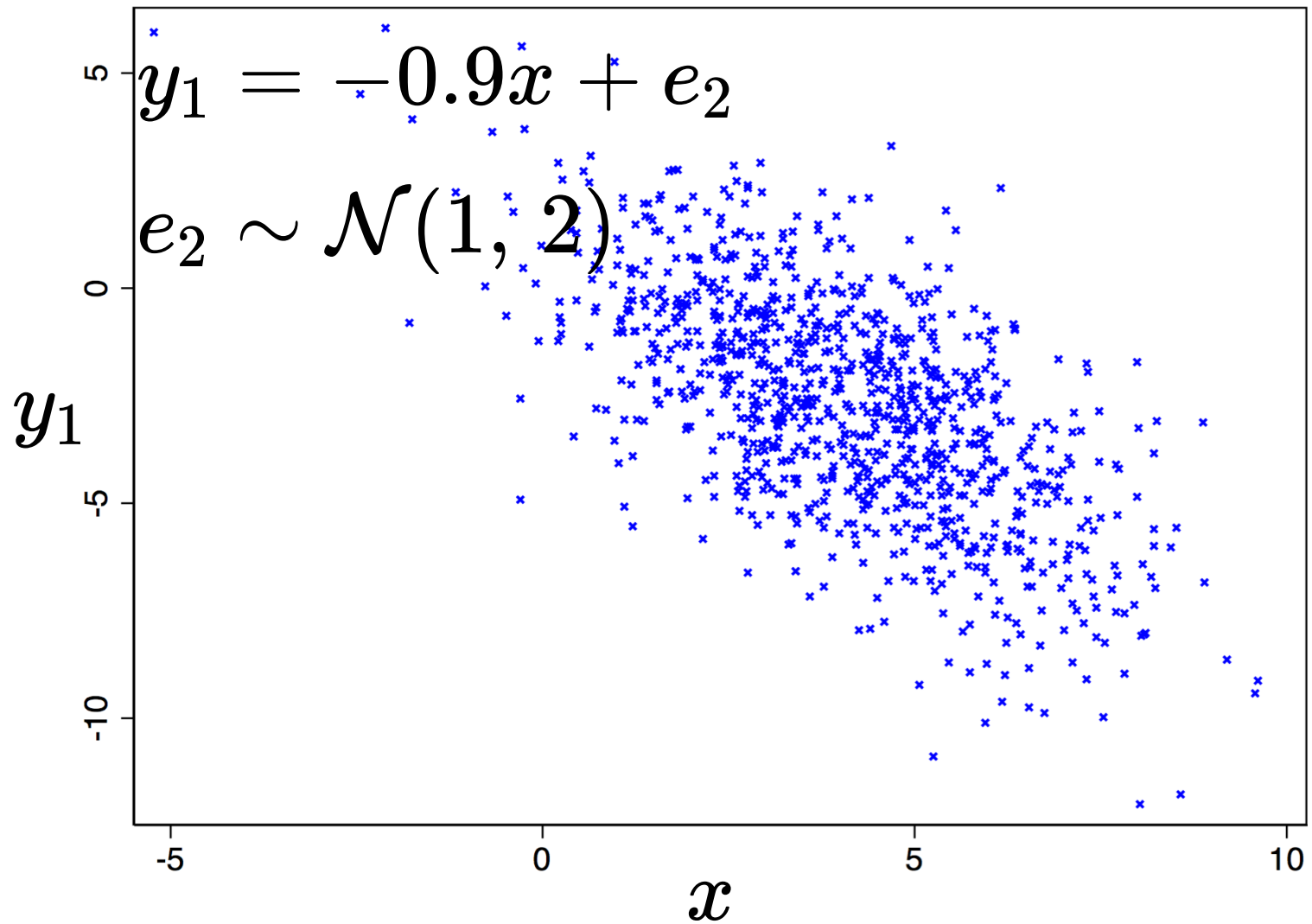
# Scatterplot

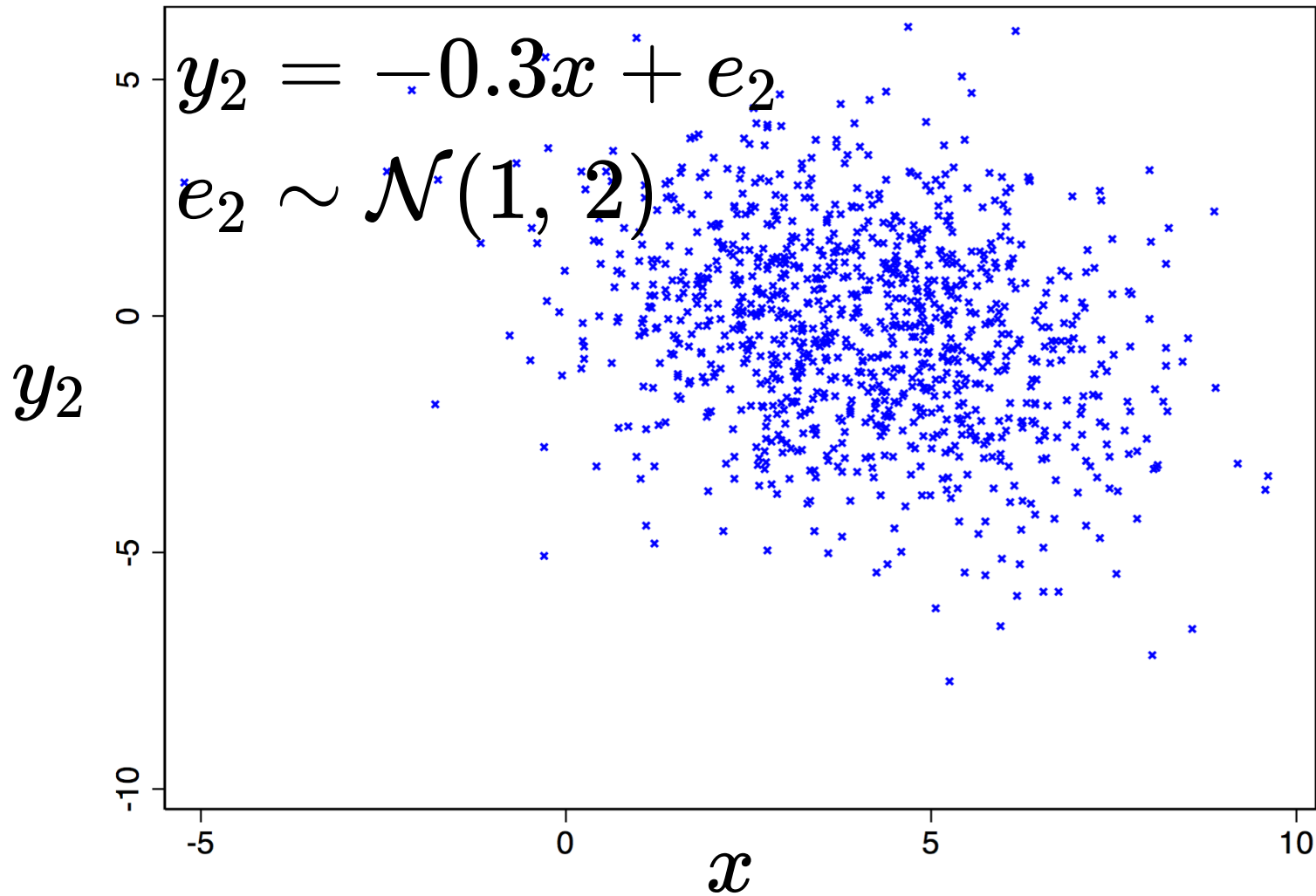
- Allows us to tell if there is a relationship among pairs of variables under consideration
  - We investigate if there is a linear relationship, nonlinear, or no relationship

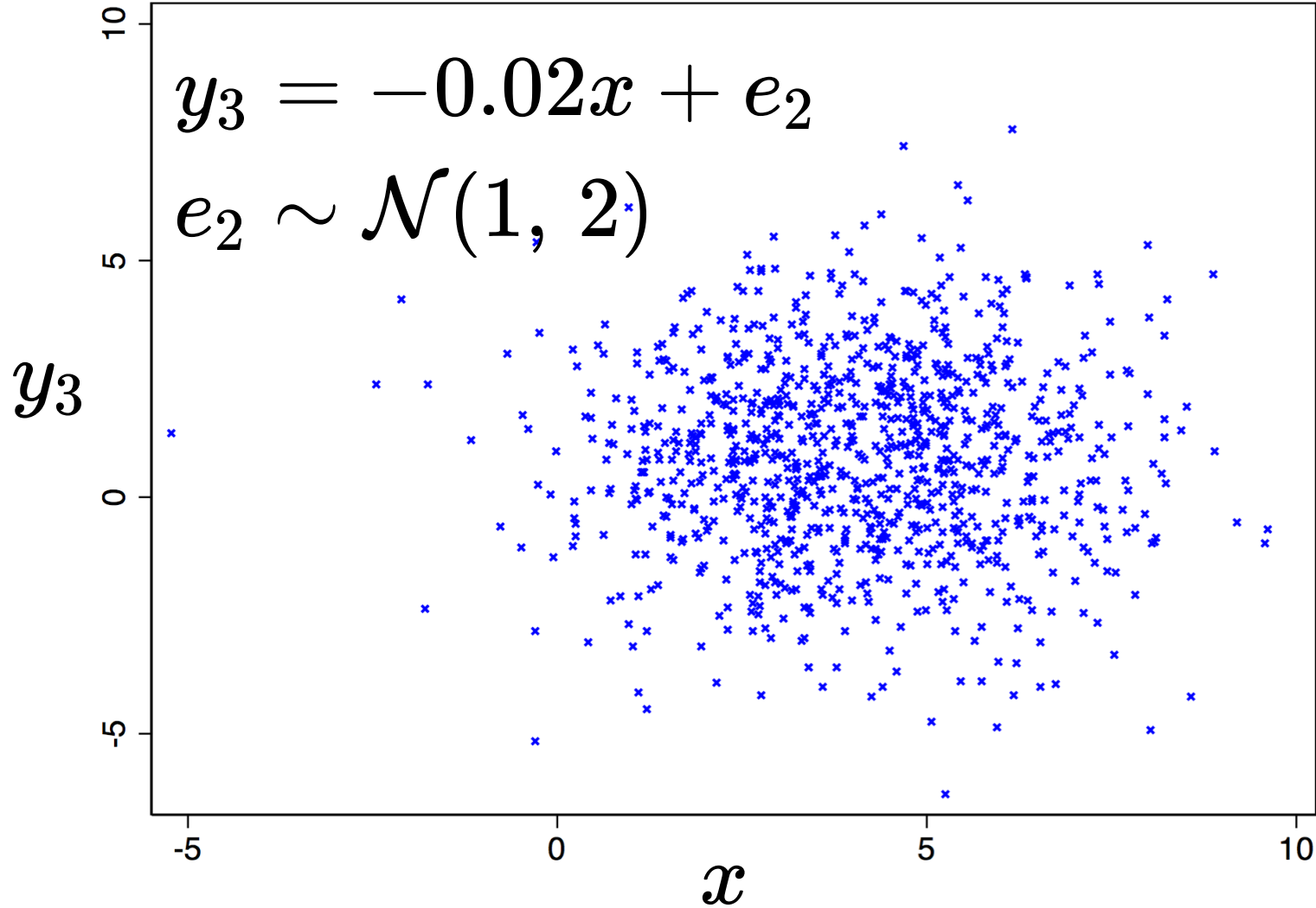
# Simulated data

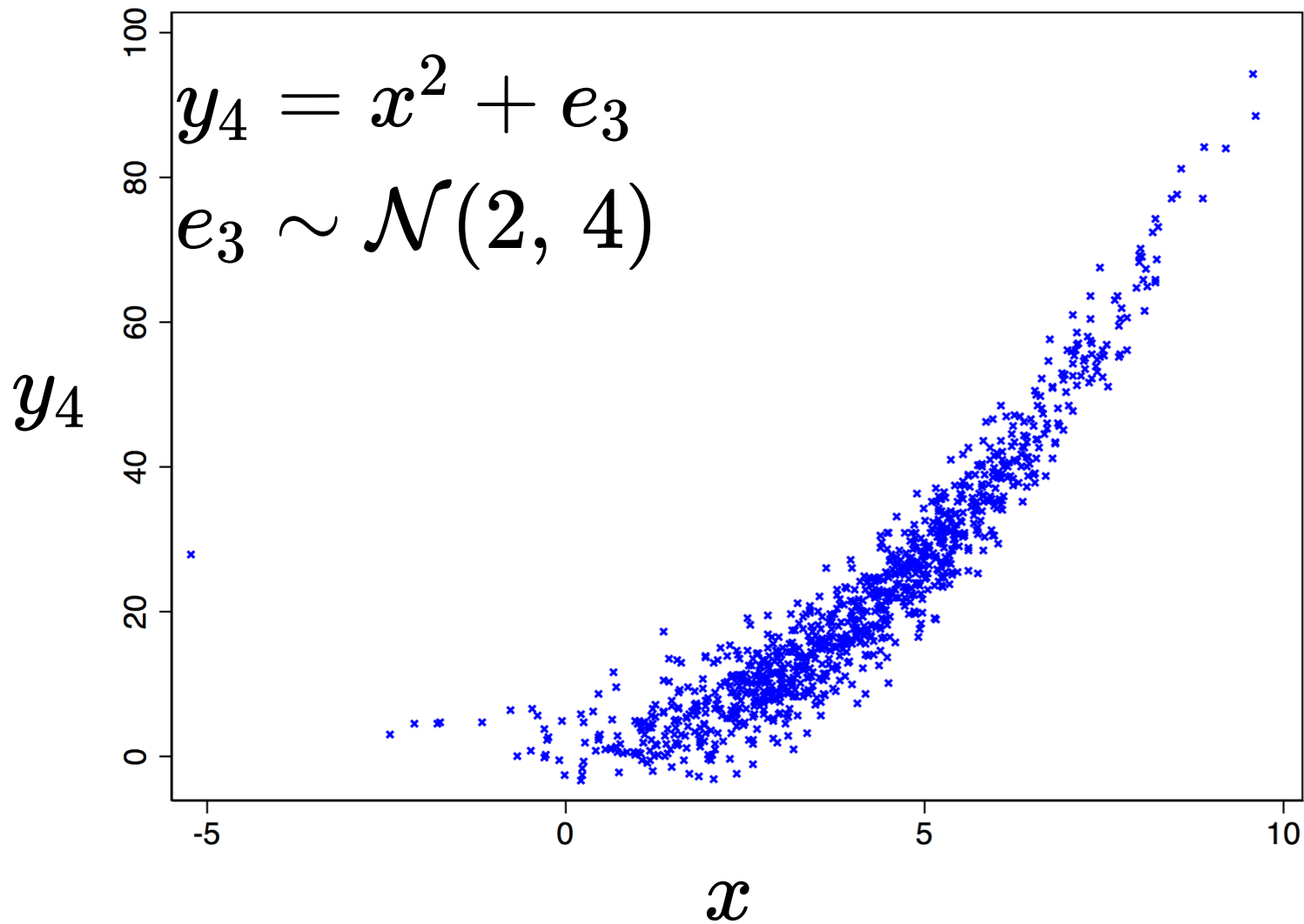


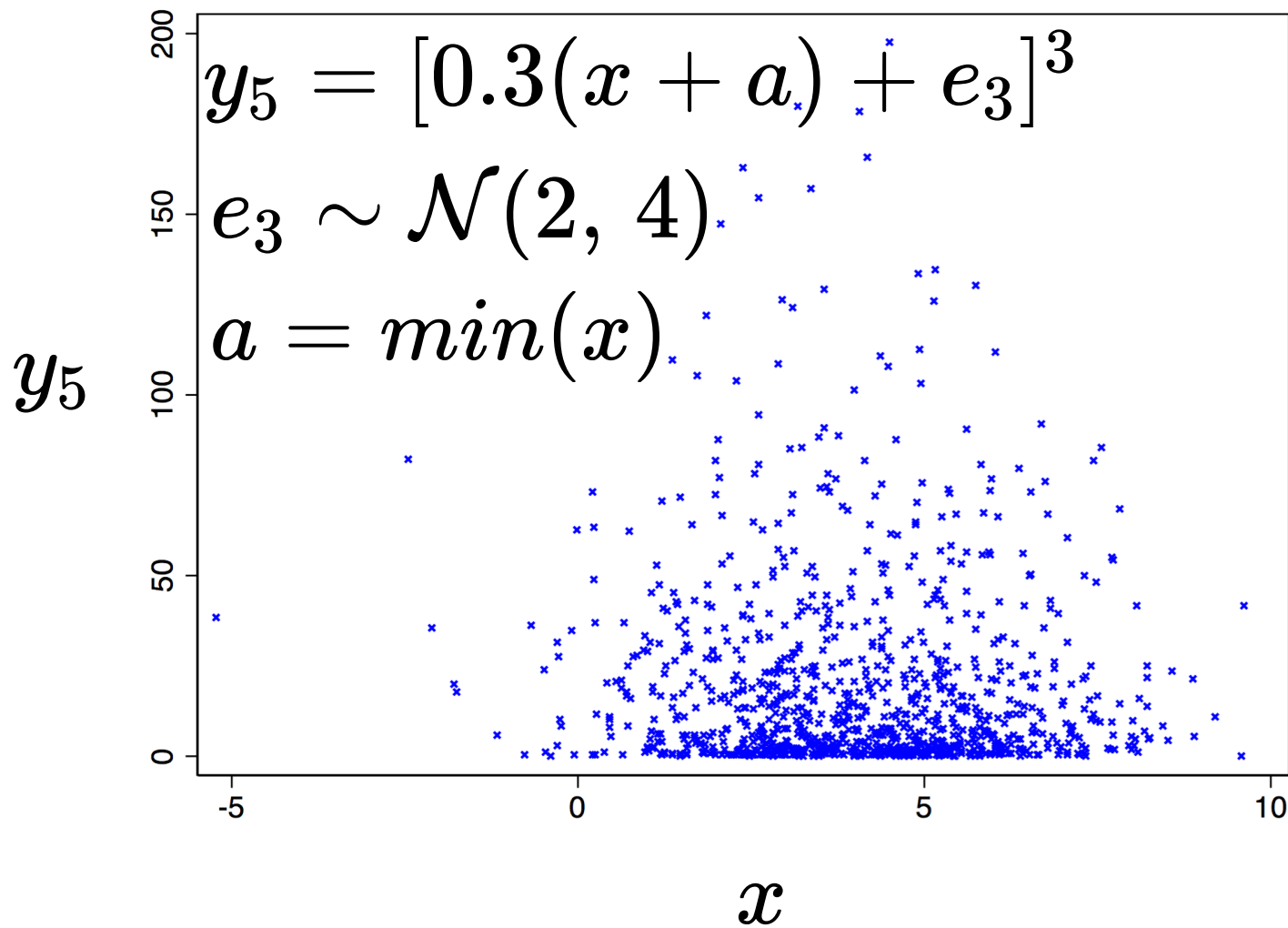




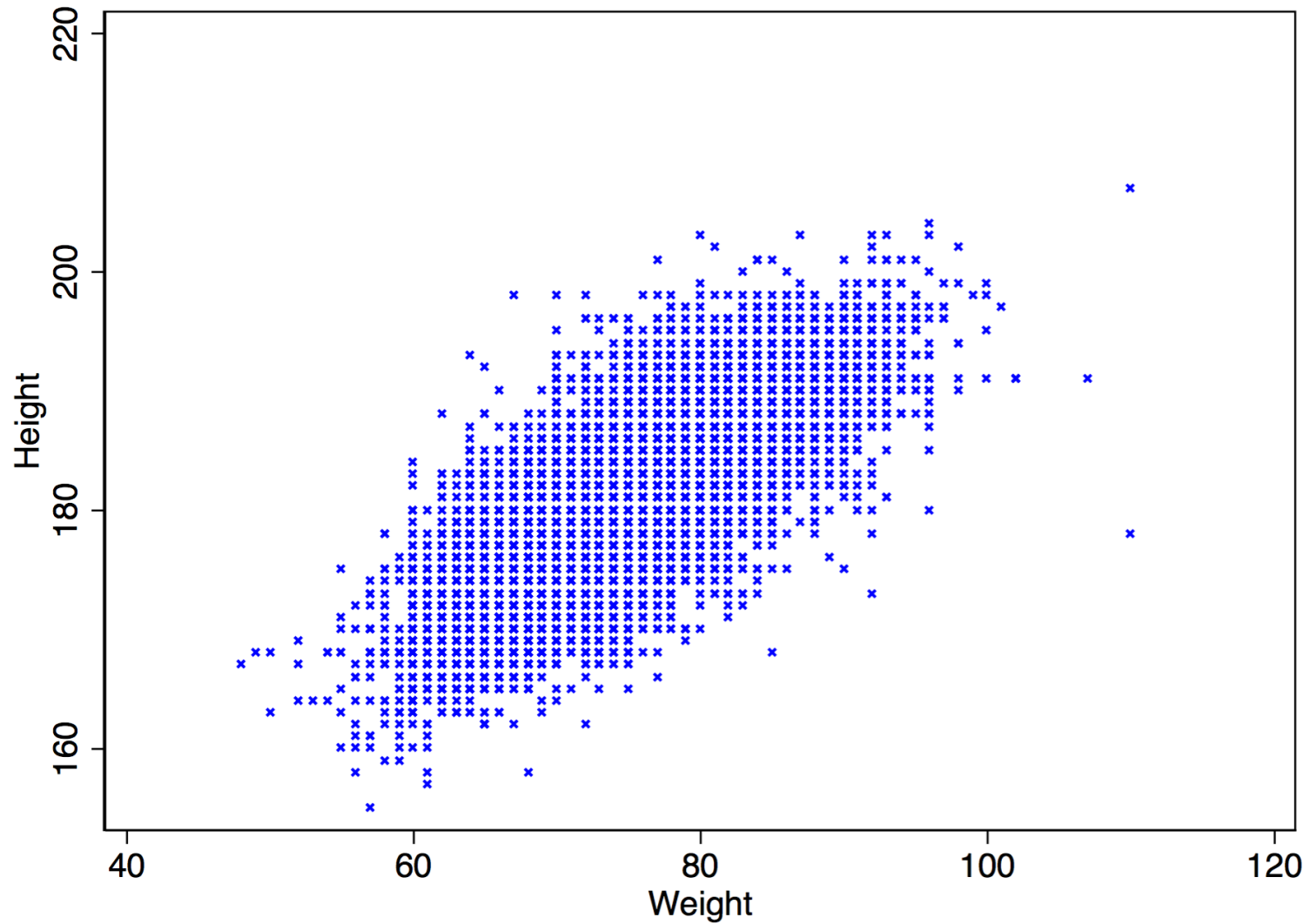




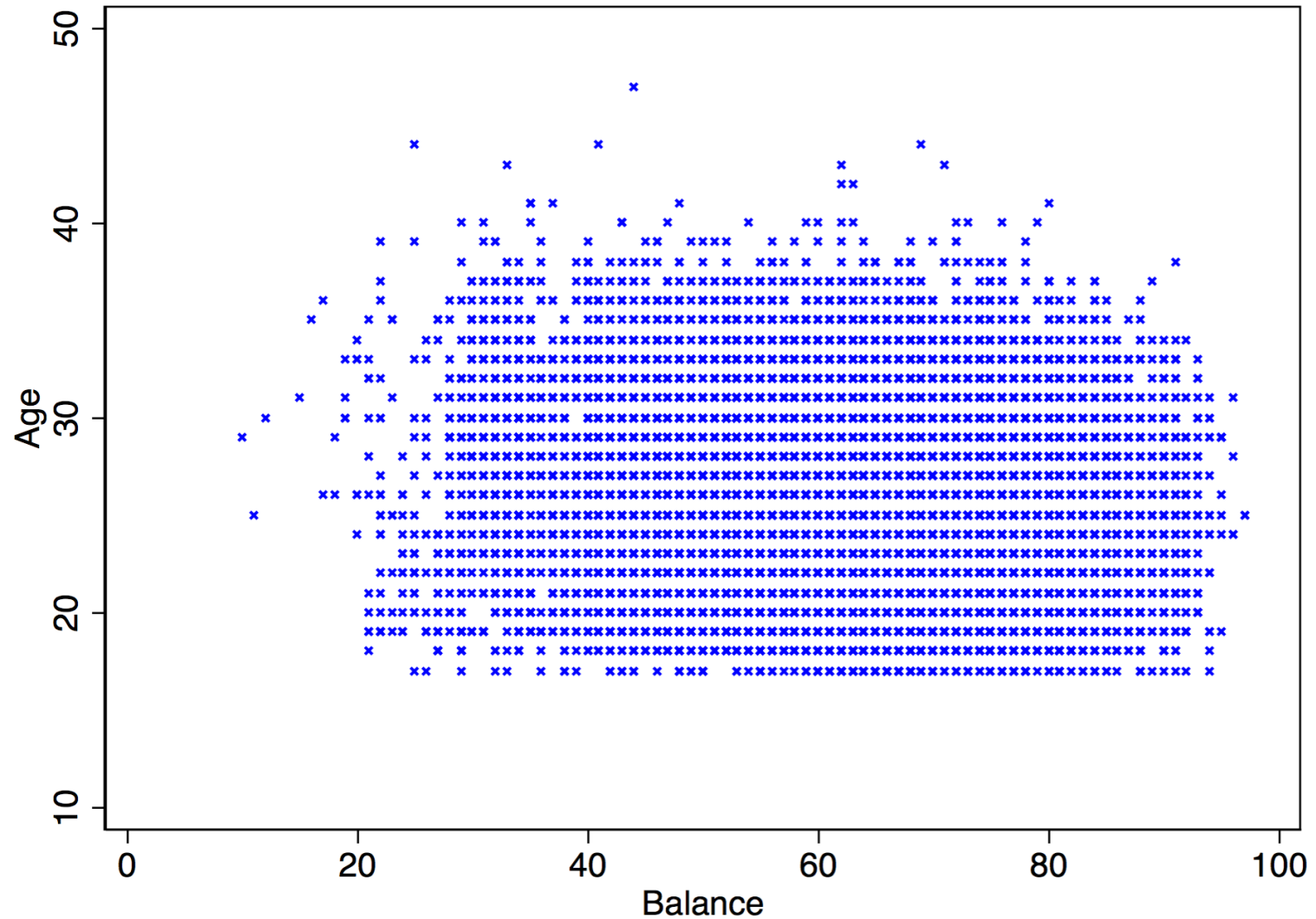


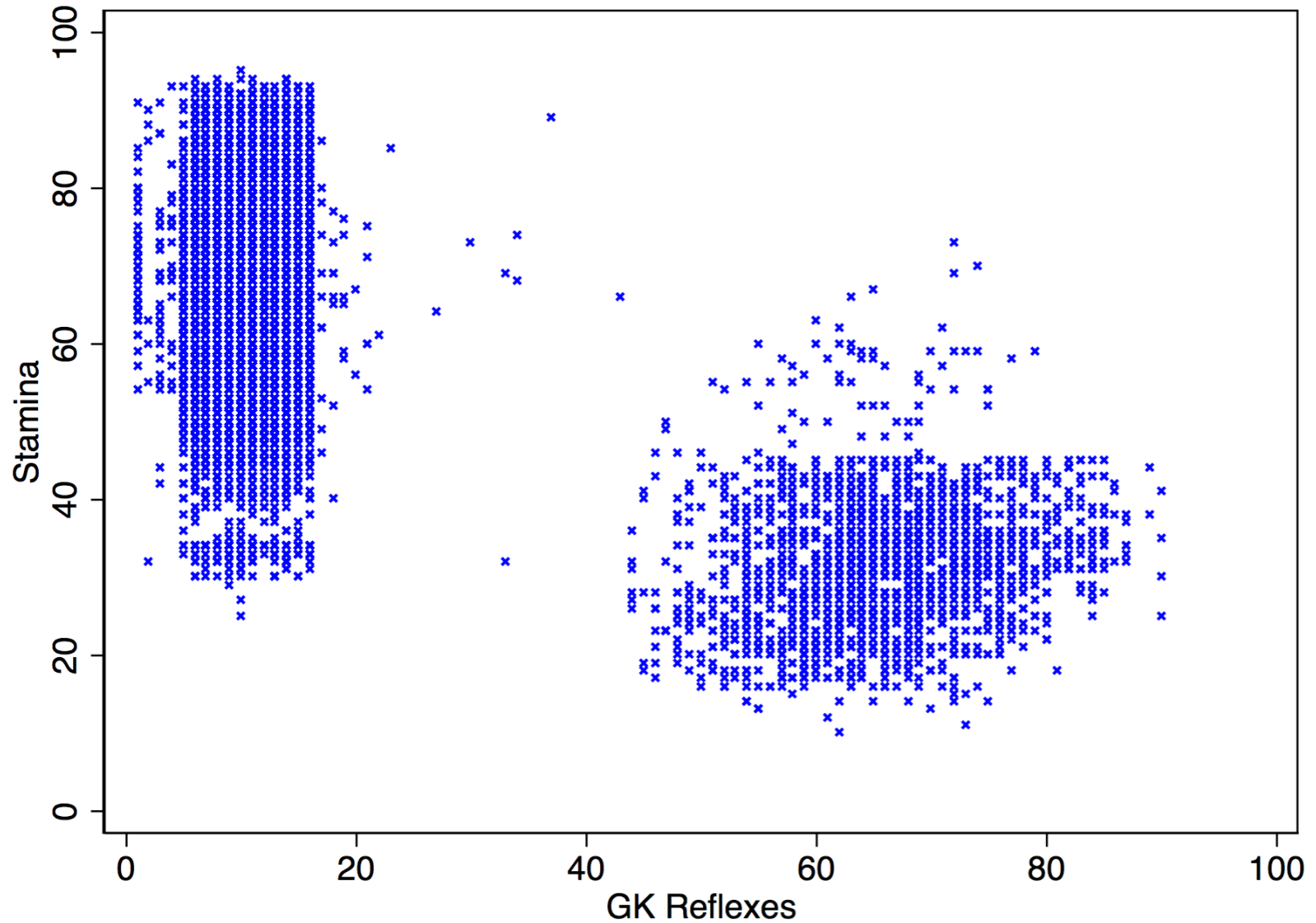


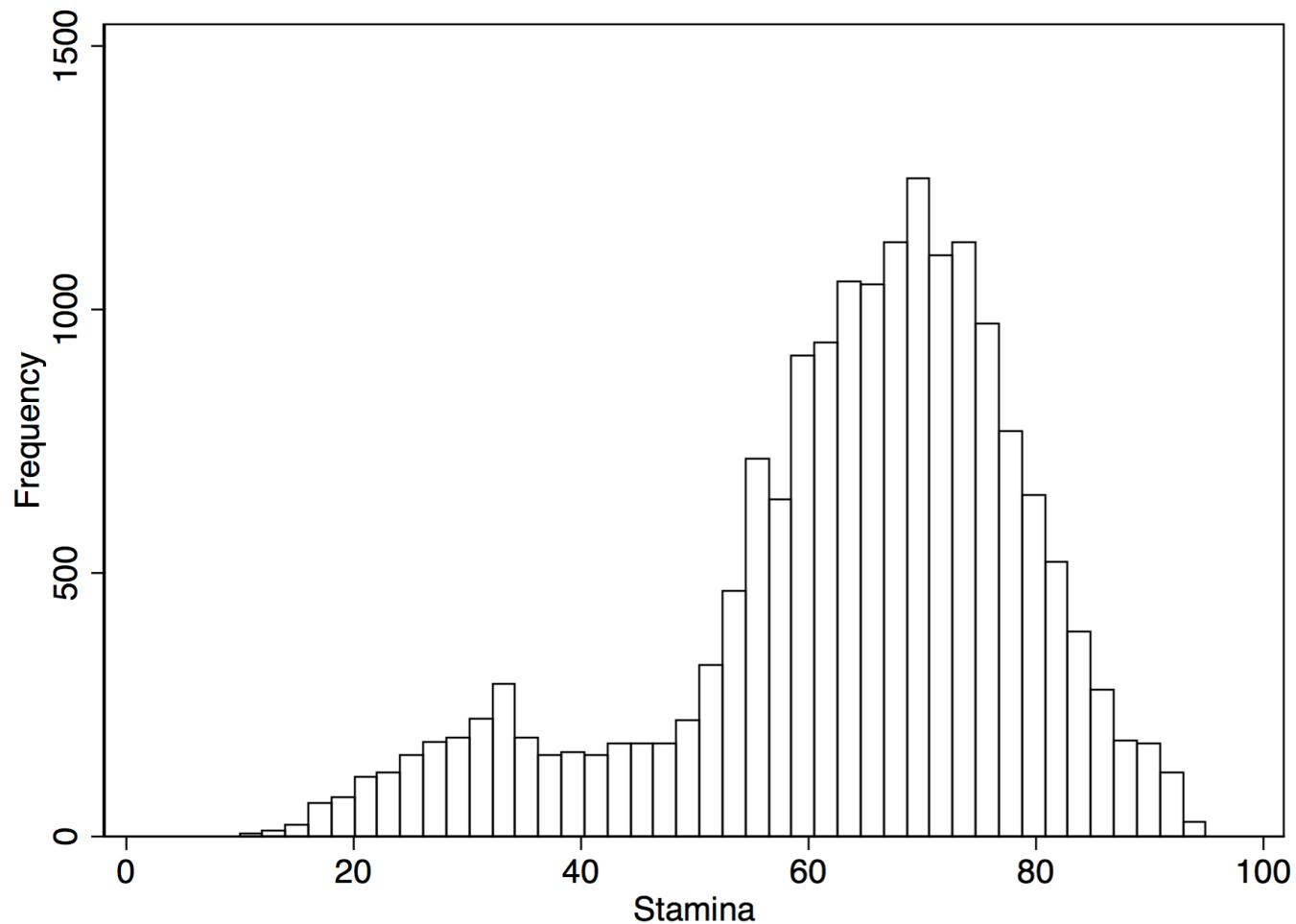
# FIFA data

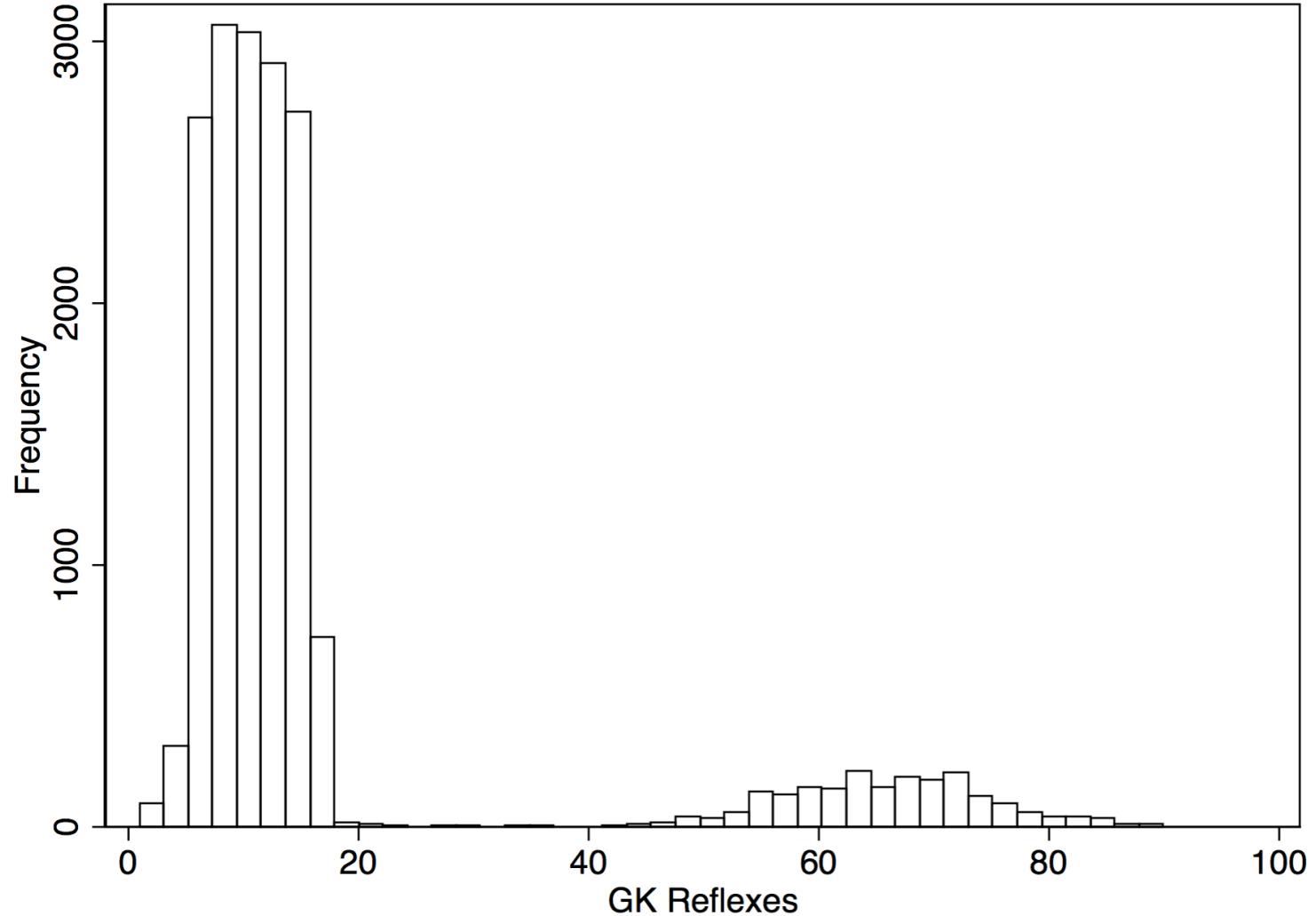


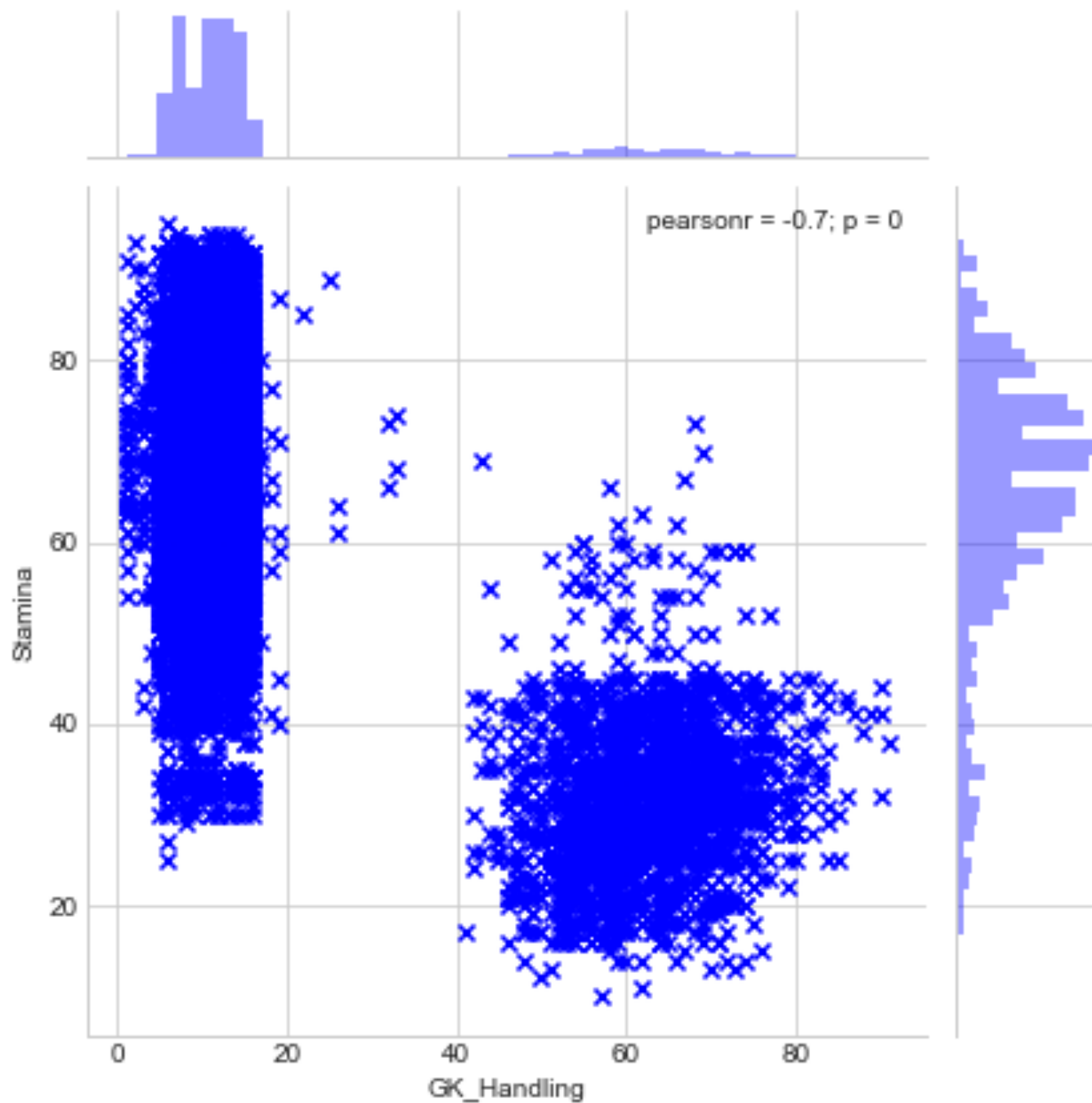


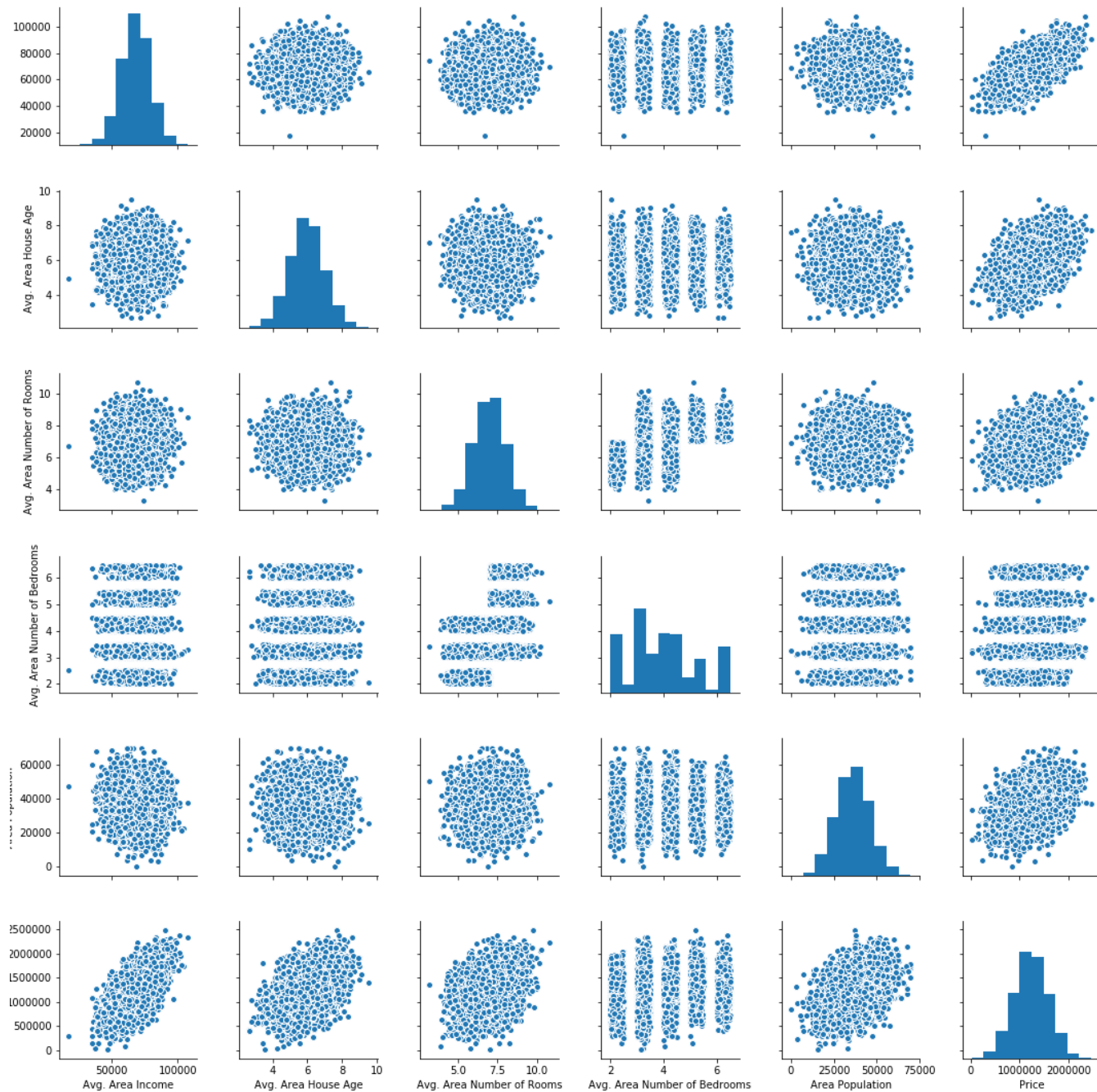




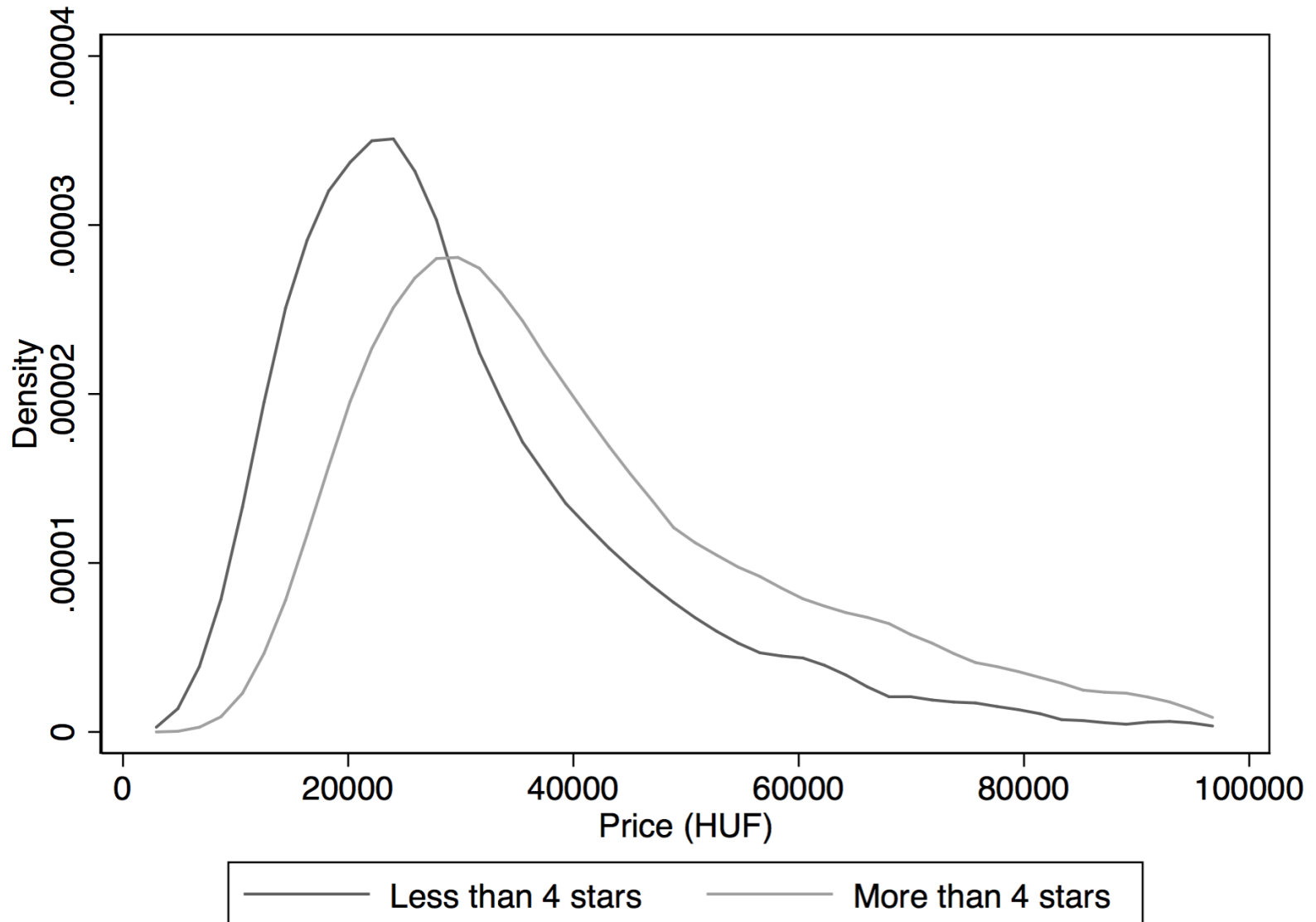




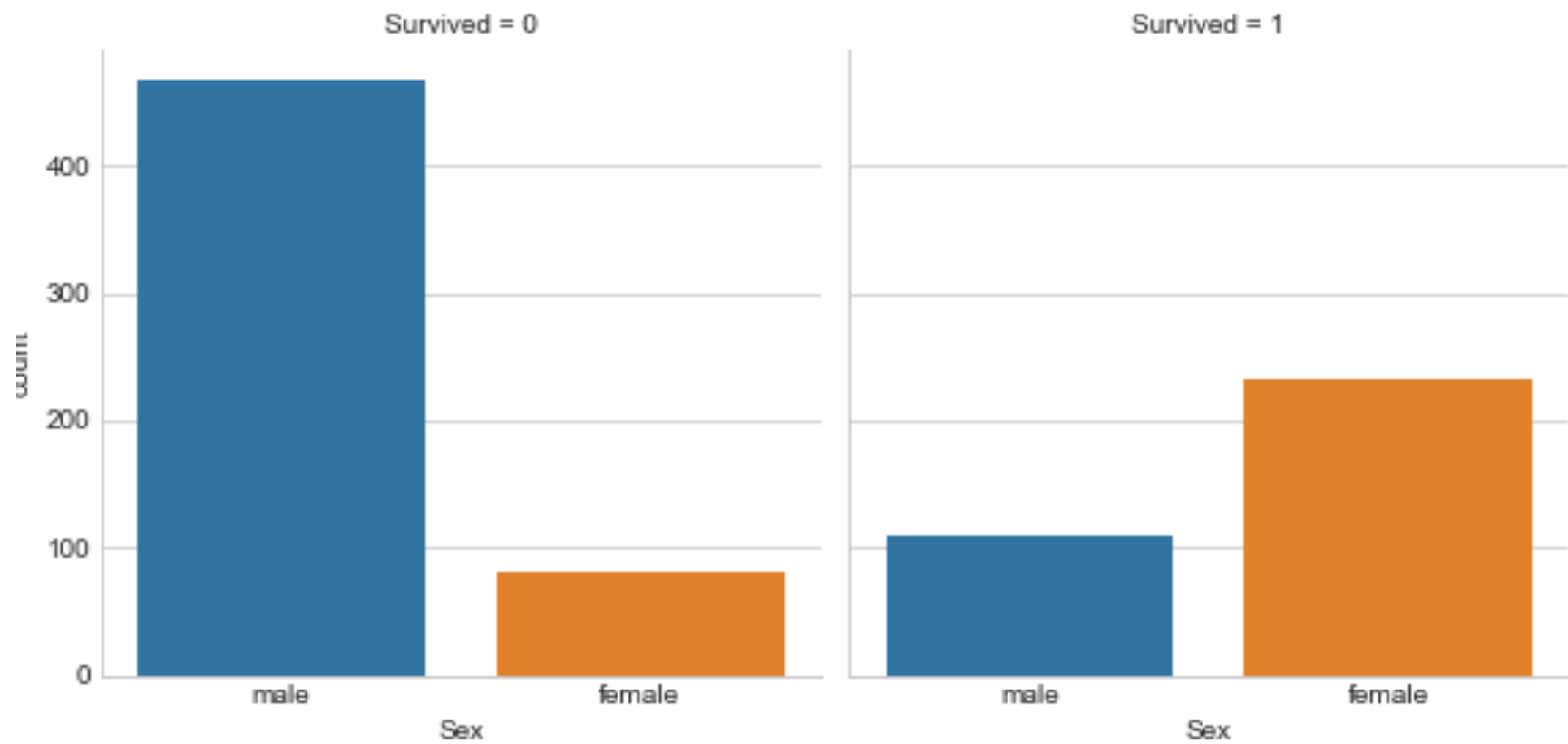


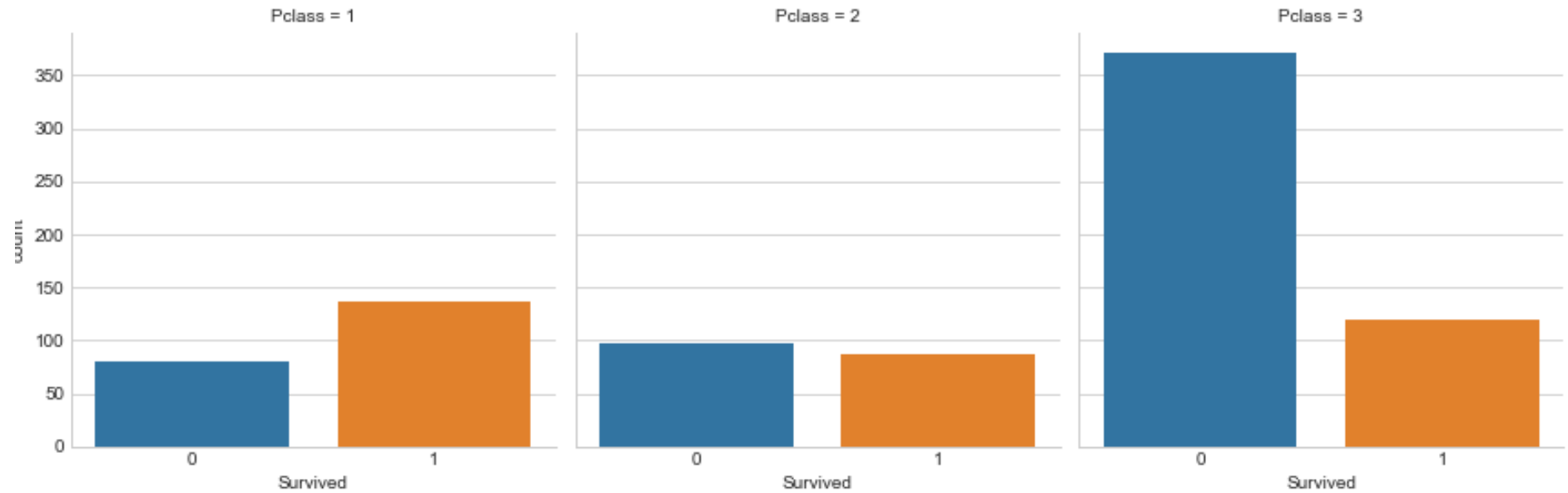


# Conditional Distributions in Practice

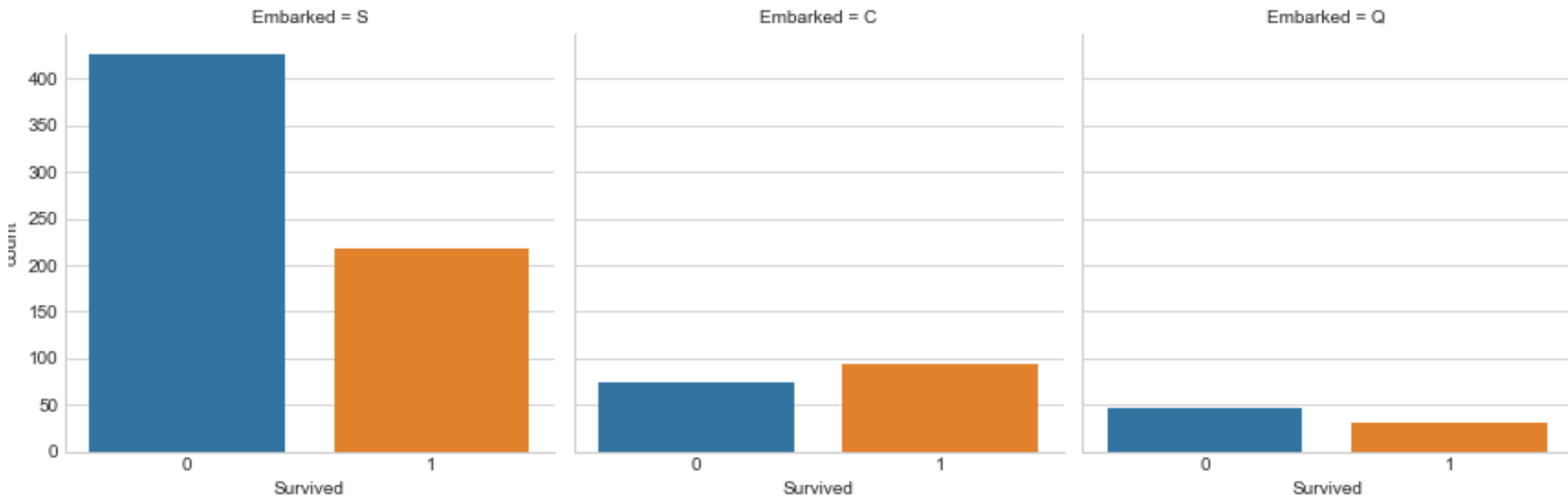






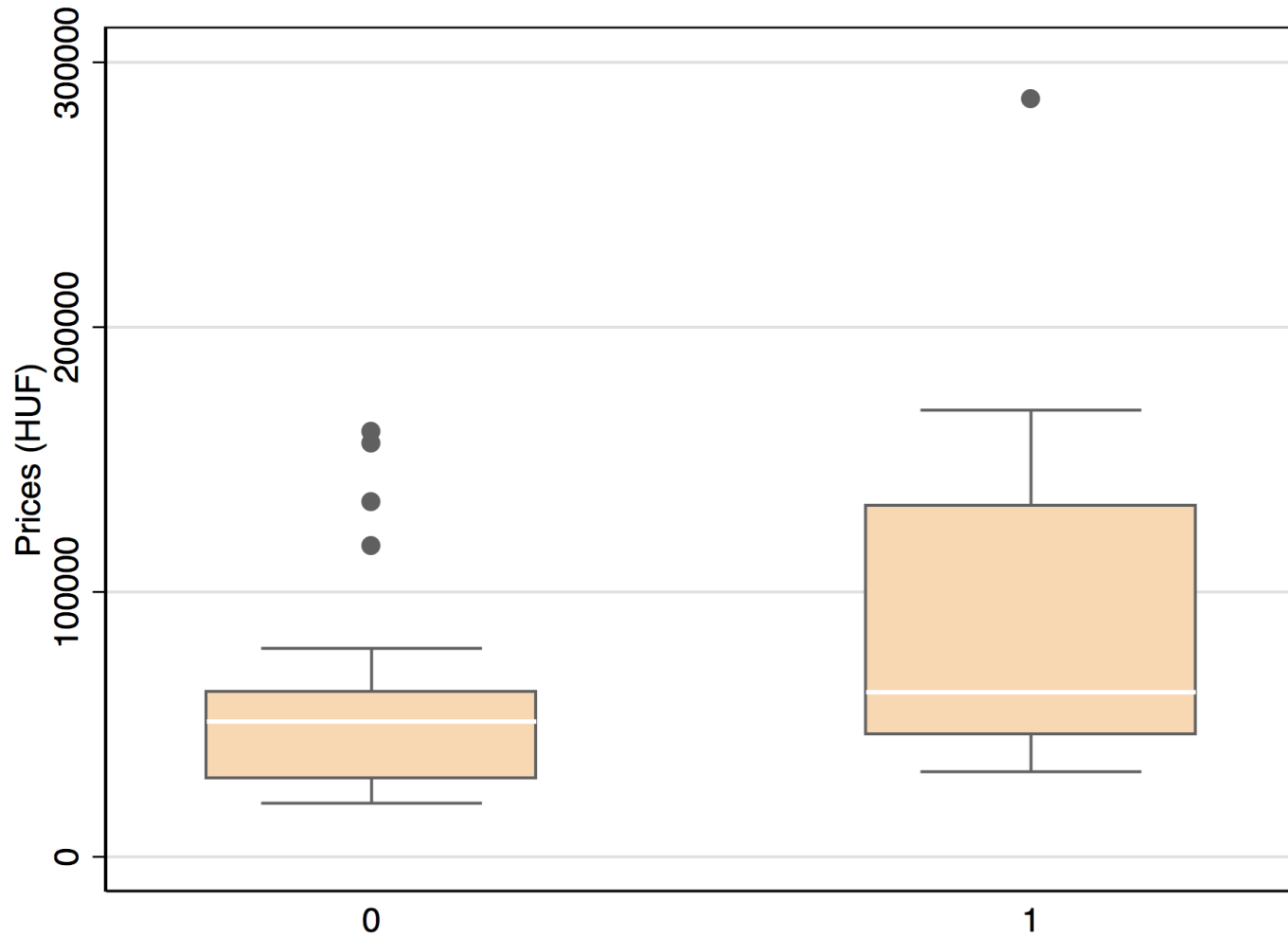


pclas=passanger class



Embarked=port of embarkation

# Vienna Hotel Prices (again)



## Sources of data used in these slides

- Hotel data, already available (only to be shared in Moodle)
- Simulated variables will be posted (Moodle and GitHub), try it on yourself, now you have the codes
- Fifa database and Titanic passengers database are going to also be posted (Moodle and GitHub).
  - Downloaded from Kaggle