

Unique Paths:

```
class Solution {
public:
    int countPaths(int i, int j, int m, int n) {
        //base case
        if (i == m - 1 && j == n - 1) {
            return 1;
        }

        //edge case
        if (i >= m || j >= n) {
            return 0;
        }

        int downPaths = countPaths(i + 1, j, m, n);
        int rightPaths = countPaths(i, j + 1, m, n);
        return (downPaths + rightPaths) % (2 * 1e9);
    }
    int uniquePaths(int m, int n) {
        int i = 0;
        int j = 0;
        int paths = countPaths(i, j, m, n);
        return paths % (2 * 1e9);
    }
};
```

Time: $O(2^{n*m})$ (Exponential) (for every $m*n$ cell you were having two recursive calls so)

Space: Recursive Stack Space

Unique Paths-2:

```
class Solution {
public:
    int countPaths(int i, int j, int m, int n, vector<vector<int>>&
obstacleGrid) {
        //base case
        if (i == m - 1 && j == n - 1) {
            return 1;
        }

        //edge case
        if (i >= m || j >= n || obstacleGrid[i][j] == 1) {
            return 0;
        }
    }
};
```

```

    }

    int downPaths==countPaths(i+1,j,m,n,obstacleGrid);
    int rightPaths==countPaths(i,j+1,m,n,obstacleGrid);
    return (downPaths+rightPaths)%(2*1e9);
}

int uniquePathsWithObstacles(vector<vector<int>>& obstacleGrid) {
    int m=obstacleGrid.size();
    int n=obstacleGrid[0].size();
    int i=0;
    int j=0;
    int paths=countPaths(i,j,m,n,obstacleGrid);
    return paths%(2*1e9);
}
};

```

Time: $O(2^{n*m})$ (Exponential)(for every $m*n$ cell you were having two recursive calls so)

Space:Recursive Stack Space

Climb Stairs:

```

#include <iostream>
#include<vector>
using namespace std;

void climbStairs(int n,vector<int>&ans){
    //base case
    if(n==0){
        for(int x:ans){
            cout<<x<<" ";
        }
        cout<<endl;
        return;
    }

    //edge case
    if(n==1){
        return;
    }

    //one step down
    ans.push_back(1);
    climbStairs(n-1,ans);
    ans.pop_back();
}

```

```

//two step down
ans.push_back(2);
climbStairs(n-2,ans);
ans.pop_back();

}
int main() {
    int n=2;
    vector<int>ans;
    climbStairs(n,ans);
    return 0;
}

```

Time:O(n)

Space:Recursive stack space and vector space won't be counted because it is asked in question to use vector we haven't used any extra space

Print Maze Paths:

```

#include <iostream>
#include<vector>
using namespace std;

void printPaths(int i,int j,int m,int n,vector<char>&ans){
    //base case
    if(i==m-1&&j==n-1){
        for(char x:ans){
            cout<<x<<" ";
        }
        cout<<endl;
    }

    //edge case
    if(i>=m||j>=n){
        return;
    }

    //down
    ans.push_back('D');
    printPaths(i+1,j,m,n,ans);
    ans.pop_back();

    //right
    ans.push_back('R');
    printPaths(i,j+1,m,n,ans);
}

```

```

        ans.pop_back();
    }

int main() {
    int m=3;
    int n=2;
    int i=0;
    int j=0;
    vector<char>ans;
    printPaths(i,j,m,n,ans);

    return 0;
}

```

Time: $O(2^{n*m})$ (Exponential)(for every $m*n$ cell you were having two recursive calls so)

Space:Recursive Stack Space

Print All Subsequences:

```

#include <iostream>
#include<vector>
using namespace std;

void printSubsequences(int i,string s,vector<char>&ans){
    //base case
    if(i==s.size()){
        for(char ch:ans){
            cout<<ch<<" ";
        }
        cout<<endl;
        return;
    }

    //pick
    ans.push_back(s[i]);
    printSubsequences(i+1,s,ans);
    ans.pop_back();

    //not pick
    printSubsequences(i+1,s,ans);
}

int main() {
    string s="abc";
    int i=0;
    vector<char>ans;
}

```

```

    printSubsequences(i,s,ans);

    return 0;
}

```

Time: $O(2^n)$, where n is size of string (Exponential) (for every n array elements you were having two recursive calls of pick and not pick so)
Space: Recursive Stack Space

Climbing Stairs:

```

class Solution {
public:
    int climbStairs(int n) {
        //base case
        if (n==0 || n==1) {
            return 1;
        }

        int xwaysToReachGroudBy1step=climbStairs(n-1);
        int ywaysToReachGroudBy2step=climbStairs(n-2);
        return xwaysToReachGroudBy1step+ywaysToReachGroudBy2step;
    }
};

```

Time: $O(n)$

Space: recursive Stack Space (function calls that are stored in stack order)