Cara: An Isomorphism-Based #SAT Solver

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To avoid redundant work

Input CNF formula

$$\varphi$$
: ($\mathbf{x_1} \lor x_2 \lor x_3$) $\land (\neg \mathbf{x_1} \lor x_2 \lor x_3)$

To avoid redundant work

Input CNF formula

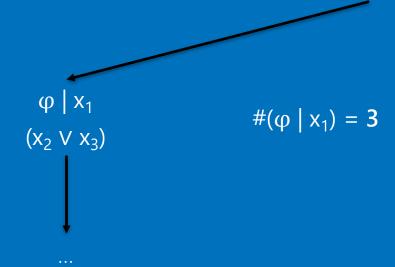
$$\varphi$$
: $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$

$$\varphi \mid x_1$$
 $(x_2 \lor x_3)$

To avoid redundant work

Input CNF formula

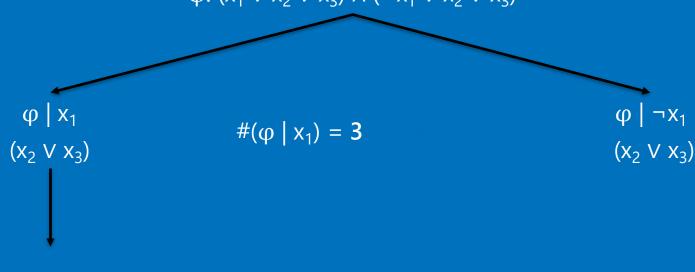
$$\varphi$$
: $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$



To avoid redundant work



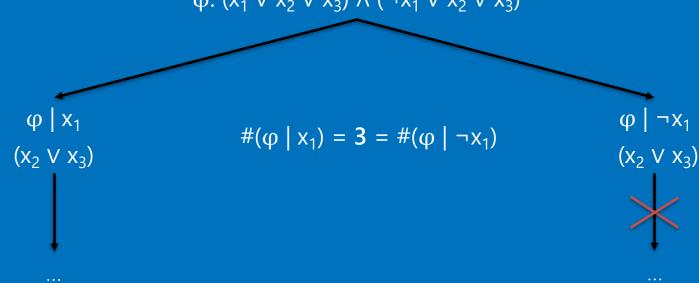
$$\varphi$$
: $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$

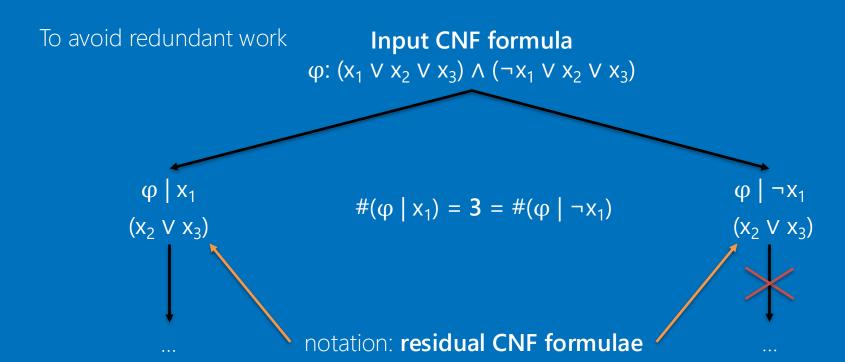


To avoid redundant work



$$\varphi$$
: $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$











A caching scheme is **correct**¹ if $\forall \psi_1, \psi_2 : (r(\psi_1) = r(\psi_2)) \Rightarrow (\psi_1 \Leftrightarrow \psi_2)$



¹ LAGNIEZ, Jean-Marie; MARQUIS, Pierre. Enhanced Caching for# SAT Solving. 2020.



A caching scheme is **correct**¹ if $\forall \psi_1, \psi_2$: $(r(\psi_1) = r(\psi_2)) \Rightarrow (\psi_1 \leftrightarrow \psi_2)$ $(\#\psi_1 = \#\psi_2)$



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A caching scheme is **correct**¹ if $\forall \psi_1, \psi_2$: $(r(\psi_1) = r(\psi_2)) \Rightarrow (\psi_1 \leftrightarrow \psi_2)$ $(\#\psi_1 = \#\psi_2)$

Key properties of a caching scheme: strength of equivalence detection, representation size, computation time

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Key properties of a caching scheme: strength of equivalence detection, representation size, computation time

Explicit representation: $standard (Cachet^2)$, basic, $i (D4^3)$,

Implicit representation: *hybrid* (*sharpSAT*⁴), *o*, *i*′,

probabilistic component caching (GANAK⁵)

⁴ THURLEY, Marc. sharp SAT-counting models with advanced component caching and implicit BCP. In: International Conference on Theory and Applications of Satisfiability Testing. Berlin, Heidelberg: Springer Berlin Heidelberg, 2006. p. 424-429.





¹ LAGNIEZ, Jean-Marie; MARQUIS, Pierre. Enhanced Caching for# SAT Solving. 2020.

² SANG, Tian, et al. Combining Component Caching and Clause Learning for Effective Model Counting. SAT, 2004, 4: 7th.

³ LAGNIEZ, Jean-Marie; MARQUIS, Pierre. An Improved Decision-DNNF Compiler. In: IJCAI. 2017. p. 667-673.

$$\varphi : (x_1 \lor x_2 \lor \neg x_4) \land (x_2 \lor x_3 \lor x_4) \land (x_1 \lor x_2 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$



$$\phi$$
: $(x_1 \lor x_2 \lor \neg x_4) \land (x_2 \lor x_3 \lor x_4) \land (x_1 \lor x_2 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$

$$\varphi \mid \neg x_2$$
: $(x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underline{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}$ untouched clauses



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underbrace{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}_{\textbf{untouched clauses}}$$

$$r(\phi \mid \neg x_2) =$$

sorted residual variables

sorted touched residual clauses



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underbrace{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}_{\textbf{untouched clauses}}$$

$$r(\phi \mid \neg x_2) = \underbrace{1, 3, 4, 5, 6, 0,}_{\text{sorted residual variables}} \underbrace{1, -4, 0, 1, -4, 0, 3, 4, 0}_{\text{residual clauses}}$$



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$r(\phi \mid \neg x_2) = 1, 3, 4, 5, 6, 0, \frac{-1, -4, 0}{1, -4, 0}, 1, -4, 0, 3, 4, 0$$

sorted residual variables sorted touched non-redundant residual clauses



$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$

$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ # $\psi_1 = 6$

$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ # $\psi_1 = 6$

$$\psi_2$$
: $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$

$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ # $\psi_1 = 6$

$$\psi_2$$
: $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$ # ψ_2 = **6**
variable names are NOT relevant

$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ # $\psi_1 = 6$

$$\psi_2$$
: $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$ # ψ_2 = 6 variable names are NOT relevant

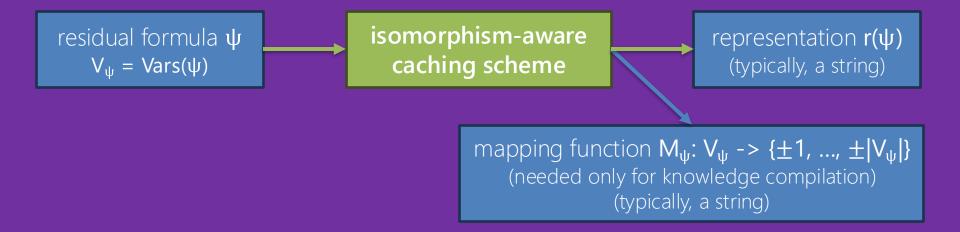
$$\psi_3 : (\neg x_1 \lor \neg x_2) \land (x_1 \lor \neg x_3) \land (\neg x_3 \lor x_4) \land (\neg x_1 \lor x_3 \lor \neg x_4)$$

$$\psi_1$$
: $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ # $\psi_1 = 6$

$$\psi_2: (x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8) \\ \text{variable names are NOT relevant} \\ \#\psi_2 = \mathbf{6}$$

$$\psi_3: (\neg x_1 \lor \neg x_2) \land (x_1 \lor \neg x_3) \land (\neg x_3 \lor x_4) \land (\neg x_1 \lor x_3 \lor \neg x_4) \qquad \#\psi_3 = \mathbf{6}$$
 literal polarity is NOT relevant

Isomorphism-aware caching scheme





Isomorphism-aware caching scheme



An isomorphism-aware caching scheme is **correct** if:

$$\forall \psi_1, \psi_2 : (r(\psi_1) = r(\psi_2)) \Rightarrow (M_{\psi_1}(\psi_1) \Leftrightarrow M_{\psi_2}(\psi_2)) \equiv (\#\psi_1 = \#\psi_2)$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$V_{\psi_1} = \{ 3, 4, 5, 6 \}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID$$

$$V_{\psi 1} = \{3, 4, 5, 6\}$$

$$C_I = \text{the number of }$$

$$\text{clauses containing } l$$

$$\mu_I = \text{the average size of }$$

$$\text{clauses containing } l$$

$$X_5 \quad C_x < C_{\neg x} = \text{sign flip}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

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$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (\underline{x_3} \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID$$

$$X_3 \qquad \qquad \qquad 3 \qquad \qquad C_I = \text{the number of }$$

$$\text{clauses containing } l$$

$$\mu_I = \text{the average size of }$$

$$\text{clauses containing } l$$

$$X_5 \qquad \qquad \qquad C_x < C_{\neg x} = \text{sign flip}$$











$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$clauses containing l$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad$$

$$x_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad$$

$$clauses containing l$$

$$\mu_1 = \text{the average size of }$$

$$clauses containing l$$

$$x_6 \quad 1 \quad 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \# \psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{ \ 3 \mapsto 2,$$

$$x_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad \text{pl} = \text{the average size of }$$

$$x_6 \quad 1 \quad 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip} \qquad 6 \mapsto 3 \}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{ \ 3 \mapsto 2, \\ \mu_I = \text{the average size of } \quad 4 \mapsto 1, \\ 5 \mapsto 4, \\ x_6 \quad 1 < 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip} \qquad 6 \mapsto -3 \, \}$$



Cara caching scheme¹

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$C_{1} = \text{the number of }$$

$$C_{2} \quad C_{3} \quad C_{4} \quad C_{5} \quad C_{$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$



Cara caching scheme¹

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$C_1 \quad C_2 \quad C_3 \quad C_4 \quad C_5 \quad C_7 \quad C_8 \quad C_9 \quad$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$

$$r(\psi_1) = 1, 3, 0, -2, -4, 0, -1, 3, 4, 0, 2, -3, 4, 0$$

sorted residual clauses



Cara caching scheme¹

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \# \psi_1 = \mathbf{5}$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$C_{\mathbf{x}} \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{3 \mapsto 2, \\ \mu_{\mathbf{i}} = \text{the average size of } \quad 4 \mapsto 1, \\ \mathbf{x}_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad C_{\mathbf{x}} < C_{\neg x} = \text{sign flip}$$

$$M_{\psi 1} = \{3 \mapsto 2, \\ \mu_{\mathbf{i}} = \text{the average size of } \quad 4 \mapsto 1, \\ 5 \mapsto 4, \\ 6 \mapsto -3 \}$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$

 $r(\psi_1) = 1, 3, 0, -2, -4, 0, -1, 3, 4, 0, 2, -3, 4, 0$ cache entry: key = $r(\psi_1)$, sorted residual clauses $\forall x_1 \lor x_2 \lor x_4 \lor x_3 \lor x_4 \lor x_4 \lor x_3 \lor x_4 \lor x_4 \lor x_3 \lor x_4 \lor$



Cara caching scheme¹ - key properties

- 1) Deterministic representations
- Syntactically identical (up to ordering) CNF formulae yield the same representation and mapping function
 - => everything detected by i is also detected by Cara
- 3) Additional moments can be used in tuples to enhance isomorphism detection
- 4) Construction is computationally expensive
- 5) Representations tend to be larger



Cara caching scheme vs caching scheme **i**

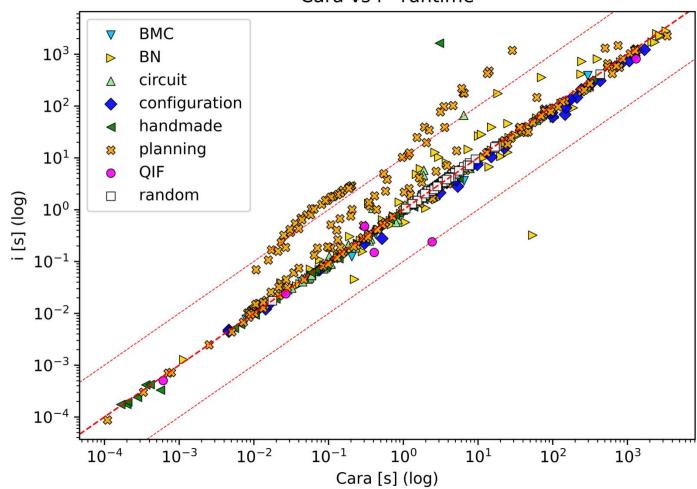


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved **3** times, and the given results are averages.

| #solved runs | Cara | i |
|--------------|------|-----|
| 3/3 | 593 | 586 |
| 2/3 | 1 | 5 |
| 1/3 | 0 | 0 |
| Total | 594 | 591 |

Cara vs i - runtime

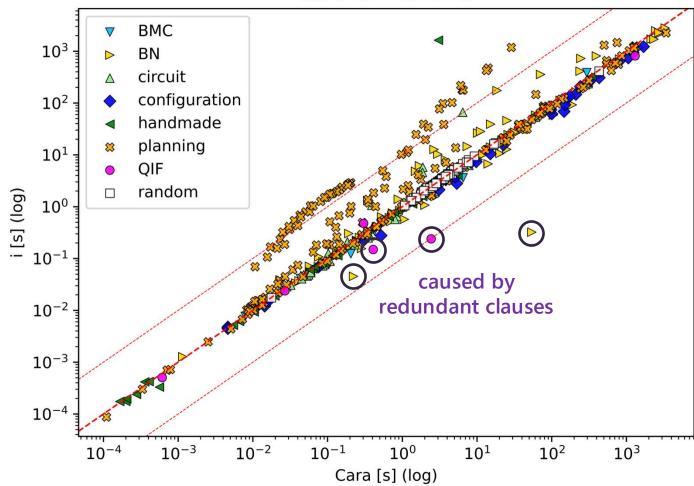


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

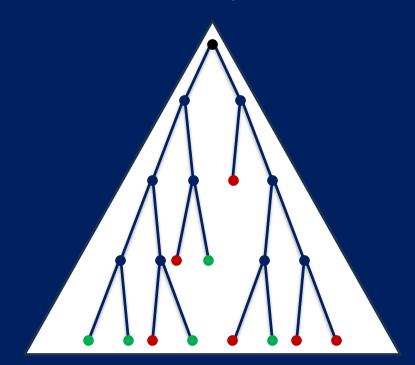
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Cara vs i - runtime

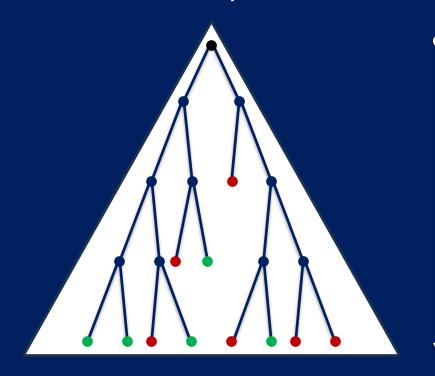


Which caching scheme is better?





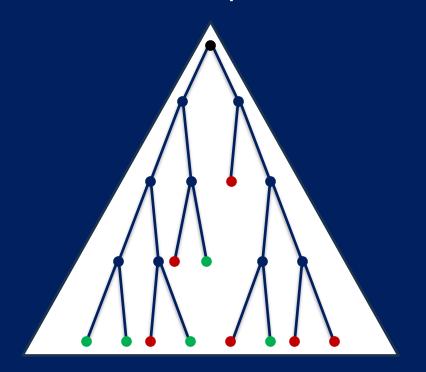
search space



larger residual formulae lower isomorphism detection more untouched clauses



search space

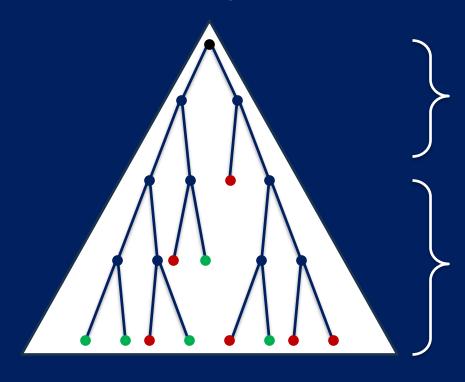


larger residual formulae lower isomorphism detection more untouched clauses

smaller residual formulaehigher isomorphism detectionfewer untouched clauses



search space

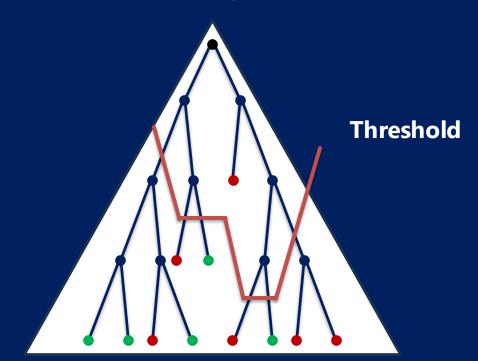


caching scheme

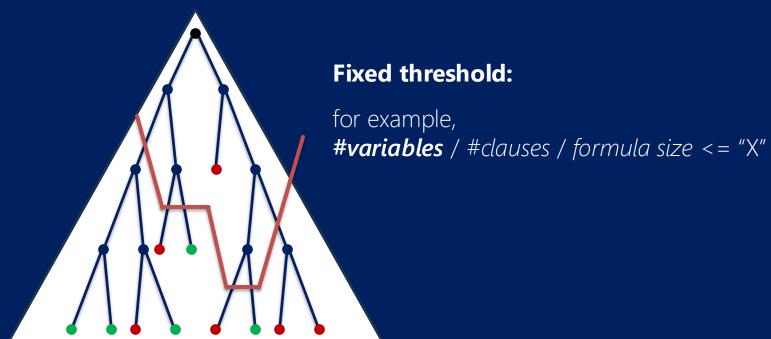
(standard, basic, i, hybrid, PCC, ...)

isomorphism-aware caching scheme (*Cara*, ...)

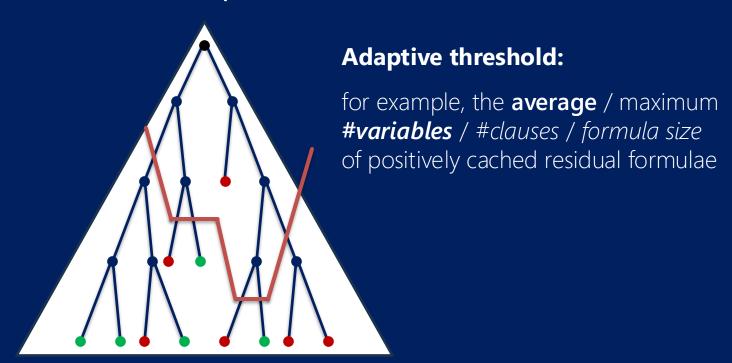






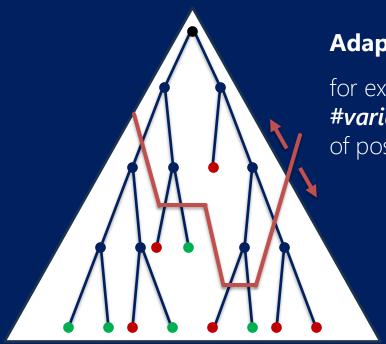








search space



Adaptive threshold:

for example, the **average** / maximum **#variables** / #clauses / formula size of positively cached residual formulae

Note: Invalid cache entries can be easily detected and removed when the next cache cleaning strategy is triggered.



Cara¹ + Arjun^{*2} vs Ganak³

* ensuring identical preprocessing



² https://github.com/meelgroup/arjur



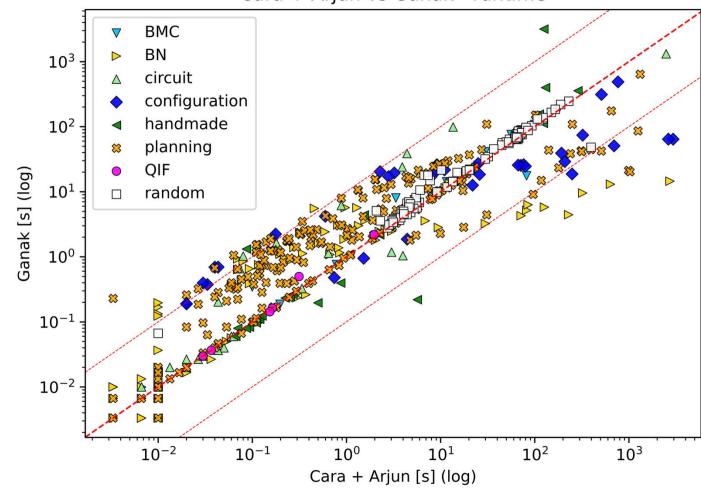
https://github.com/meelgroup/ganak

The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

| #solved runs | Cara | Ganak |
|--------------|------|-------|
| 3/3 | 623 | 632 |
| 2/3 | 0 | 0 |
| 1/3 | 0 | 0 |
| Total | 623 | 632 |

Cara + Arjun vs Ganak - runtime

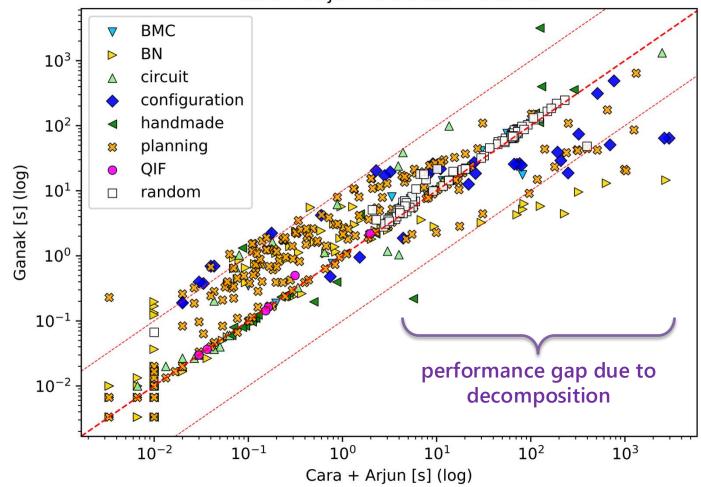


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

| #solved runs | Cara | Ganak | | |
|--------------|------|-------|--|--|
| 3/3 | 623 | 632 | | |
| 2/3 | 0 | 0 | | |
| 1/3 | 0 | 0 | | |
| Total | 623 | 632 | | |





Cara¹ VS SymGanak*2

* no Arjun



https://github.com/Illner/carasolve

² https://github.com/meelgroup/ganak

The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

#solved runs

3/3 593 512

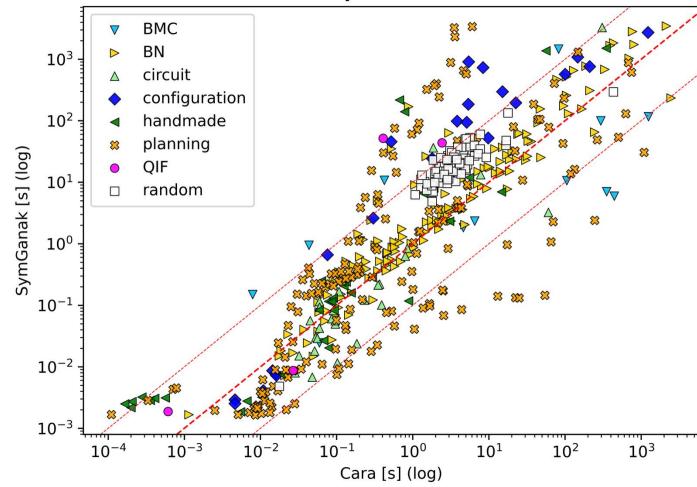
2/3 1 0

1/3 0 0

Total 594 512

* strict dominance





Functional pigeonhole principle (FPHP)

| Instance ¹ | #pigeons | #holes |
|-----------------------|----------|--------|
| fphp-010-020 | 10 | 20 |
| fphp-015-020 | 15 | 20 |



¹ https://www.cril.univ-artois.fr/kc/benchmarks.htm

Functional pigeonhole principle (FPHP)

| Instance ¹ | #pigeons | #holes |
|-----------------------|----------|--------|
| fphp-010-020 | 10 | 20 |
| fphp-015-020 | 15 | 20 |

| | Instance ¹ | | | Runtime | [s] | | |
|--|-----------------------|-------------------|--|-----------------------|--------------------|--------------------------|-----------------|
| | ilistance. | Cara ² | Cara ² + Arjun ³ | SymGanak ⁴ | Ganak ⁴ | SharpSAT-TD ⁵ | D4 ⁶ |
| | fphp-010-020 | 3.04 | 124.81 | 2.37 | 3 176.17* | <u>—</u> | _ |
| | fphp-015-020 | 14.61 | 314.69 | 7.03 | _ | <u> </u> | _ |

* invalid number of models



¹ https://www.cril.univ-artois.fr/kc/benchmarks.html

² https://github.com/Illner/carasolver

³ https://github.com/meelgroup/arjun

https://github.com/meelgroup/ganak

https://github.com/Laakeri/sharpsat-t

⁶ https://github.com/crillab/d4v

Future research

- 1) Adaptive balance of caching schemes
- 2) Replace the obsolete *MiniSat*¹, which is used for satisfiability checks and implied literals at each inner node, with *CaDiCaL*².
- 3) Integrate the decomposability approach used by *Ganak* and *SharpSAT-TD* into the adaptiveness framework.

