# Cara: An Isomorphism-Based #SAT Solver

This work is partially published in AAAI 2025

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To avoid redundant work

### Input CNF formula

$$\varphi$$
: ( $\mathbf{x_1} \lor x_2 \lor x_3$ )  $\land (\neg \mathbf{x_1} \lor x_2 \lor x_3)$ 

To avoid redundant work

### **Input CNF formula**

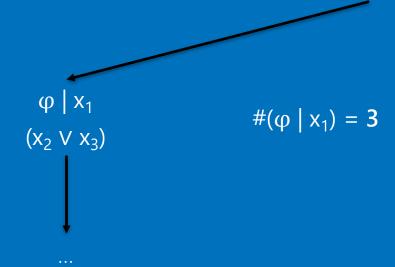
$$\varphi$$
:  $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$ 

$$\varphi \mid x_1$$
  $(x_2 \lor x_3)$ 

To avoid redundant work

### **Input CNF formula**

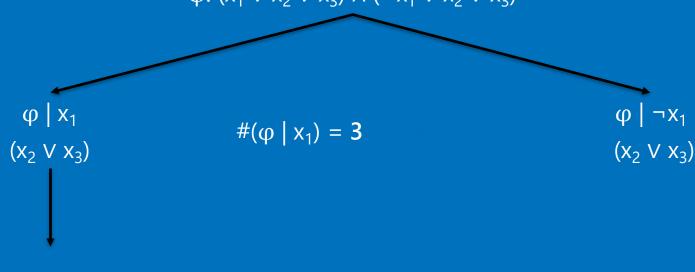
$$\varphi$$
:  $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$ 



To avoid redundant work



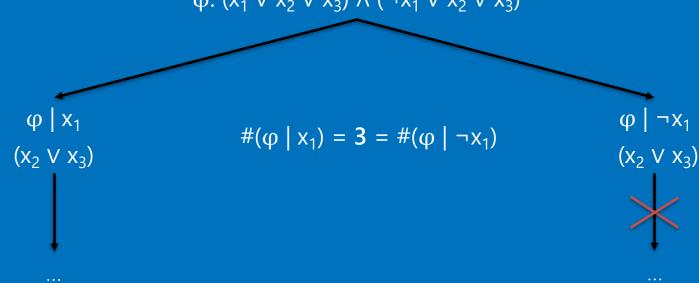
$$\varphi$$
:  $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$ 

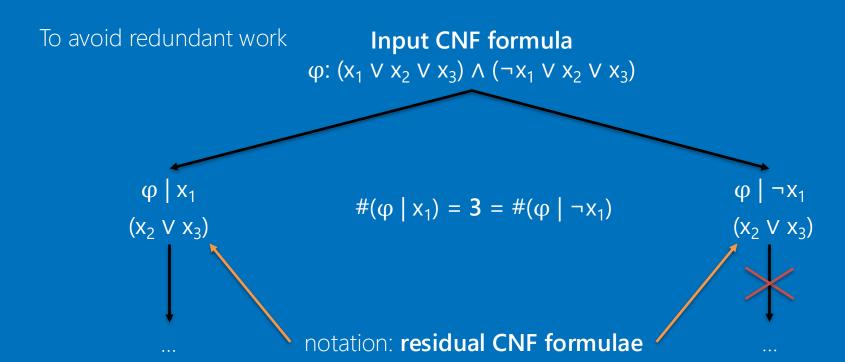


To avoid redundant work



$$\varphi$$
:  $(x_1 \lor x_2 \lor x_3) \land (\neg x_1 \lor x_2 \lor x_3)$ 











A caching scheme is **correct**<sup>1</sup> if  $\forall \psi_1, \psi_2 : (r(\psi_1) = r(\psi_2)) \Rightarrow (\psi_1 \Leftrightarrow \psi_2)$ 



<sup>&</sup>lt;sup>1</sup> LAGNIEZ, Jean-Marie; MARQUIS, Pierre. Enhanced Caching for# SAT Solving. 2020.



A caching scheme is **correct**<sup>1</sup> if  $\forall \psi_1, \psi_2$ :  $(r(\psi_1) = r(\psi_2)) \Rightarrow (\psi_1 \leftrightarrow \psi_2)$   $(\#\psi_1 = \#\psi_2)$ 



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**Key properties of a caching scheme:** strength of equivalence detection, representation size, computation time

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**Key properties of a caching scheme:** strength of equivalence detection, representation size, computation time

**Explicit representation:**  $standard (Cachet^2)$ , basic,  $i (D4^3)$ ,

**Implicit representation:** *hybrid* (*sharpSAT*<sup>4</sup>), *o*, *i*′,

probabilistic component caching (GANAK<sup>5</sup>)

<sup>&</sup>lt;sup>4</sup> THURLEY, Marc. sharp SAT-counting models with advanced component caching and implicit BCP. In: International Conference on Theory and Applications of Satisfiability Testing. Berlin, Heidelberg: Springer Berlin Heidelberg, 2006. p. 424-429.





<sup>&</sup>lt;sup>1</sup> LAGNIEZ, Jean-Marie; MARQUIS, Pierre. Enhanced Caching for# SAT Solving. 2020.

<sup>&</sup>lt;sup>2</sup> SANG, Tian, et al. Combining Component Caching and Clause Learning for Effective Model Counting. SAT, 2004, 4: 7th.

<sup>&</sup>lt;sup>3</sup> LAGNIEZ, Jean-Marie; MARQUIS, Pierre. An Improved Decision-DNNF Compiler. In: IJCAI. 2017. p. 667-673.

$$\varphi : (x_1 \lor x_2 \lor \neg x_4) \land (x_2 \lor x_3 \lor x_4) \land (x_1 \lor x_2 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$



$$\phi$$
:  $(x_1 \lor x_2 \lor \neg x_4) \land (x_2 \lor x_3 \lor x_4) \land (x_1 \lor x_2 \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$ 

$$\varphi \mid \neg x_2$$
:  $(x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underline{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}$  untouched clauses



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underbrace{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}_{\textbf{untouched clauses}}$$

$$r(\phi \mid \neg x_2) =$$

sorted residual variables

sorted touched residual clauses



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$\phi \mid \neg x_2 : (x_1 \lor \neg x_4) \land (x_3 \lor x_4) \land (x_1 \lor \neg x_4) \land \underbrace{(x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)}_{\textbf{untouched clauses}}$$

$$r(\phi \mid \neg x_2) = \underbrace{1, 3, 4, 5, 6, 0,}_{\text{sorted residual variables}} \underbrace{1, -4, 0, 1, -4, 0, 3, 4, 0}_{\text{residual clauses}}$$



$$\varphi : (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (\mathbf{x_2} \lor x_3 \lor x_4) \land (x_1 \lor \mathbf{x_2} \lor \neg x_4) \land (x_3 \lor x_4 \lor x_5) \land (x_1 \lor \neg x_6)$$

$$r(\phi \mid \neg x_2) = 1, 3, 4, 5, 6, 0, \frac{-1, -4, 0}{1, -4, 0}, 1, -4, 0, 3, 4, 0$$

sorted residual variables sorted touched non-redundant residual clauses



$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$ 

$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$  # $\psi_1 = 6$ 

$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$  # $\psi_1 = 6$ 

$$\psi_2$$
:  $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$ 

$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$  # $\psi_1 = 6$ 

$$\psi_2$$
:  $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$  # $\psi_2$  = **6**
variable names are NOT relevant

$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$  # $\psi_1 = 6$ 

$$\psi_2$$
:  $(x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8)$  # $\psi_2$  = 6 variable names are NOT relevant

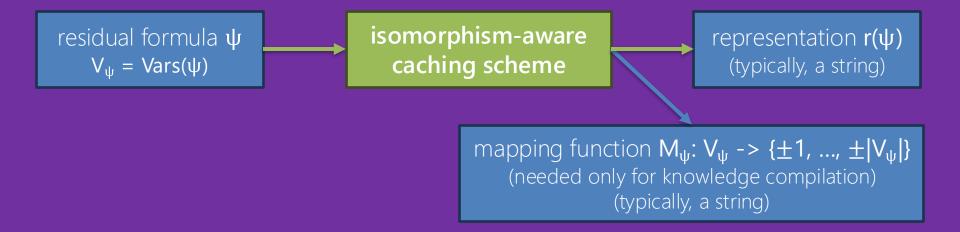
$$\psi_3 : (\neg x_1 \lor \neg x_2) \land (x_1 \lor \neg x_3) \land (\neg x_3 \lor x_4) \land (\neg x_1 \lor x_3 \lor \neg x_4)$$

$$\psi_1$$
:  $(x_1 \lor x_2) \land (\neg x_1 \lor x_3) \land (x_3 \lor \neg x_4) \land (x_1 \lor \neg x_3 \lor x_4)$  # $\psi_1 = 6$ 

$$\psi_2: (x_5 \lor x_6) \land (\neg x_5 \lor x_7) \land (x_7 \lor \neg x_8) \land (x_5 \lor \neg x_7 \lor x_8) \\ \text{variable names are NOT relevant} \\ \#\psi_2 = \mathbf{6}$$

$$\psi_3: (\neg x_1 \lor \neg x_2) \land (x_1 \lor \neg x_3) \land (\neg x_3 \lor x_4) \land (\neg x_1 \lor x_3 \lor \neg x_4) \qquad \#\psi_3 = \mathbf{6}$$
 literal polarity is NOT relevant

### Isomorphism-aware caching scheme





### Isomorphism-aware caching scheme



An isomorphism-aware caching scheme is **correct** if:

$$\forall \psi_1, \psi_2 : (r(\psi_1) = r(\psi_2)) \Rightarrow (M_{\psi_1}(\psi_1) \Leftrightarrow M_{\psi_2}(\psi_2)) \equiv (\#\psi_1 = \#\psi_2)$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$V_{\psi_1} = \{ 3, 4, 5, 6 \}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID$$

$$V_{\psi 1} = \{3, 4, 5, 6\}$$

$$C_I = \text{the number of }$$

$$\text{clauses containing } l$$

$$\mu_I = \text{the average size of }$$

$$\text{clauses containing } l$$

$$X_5 \quad C_x < C_{\neg x} = \text{sign flip}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$
 
$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID$$
 
$$V_{\psi 1} = \{\ 3,\ 4,\ 5,\ 6\ \}$$
 
$$C_I = \text{the number of }$$
 
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$$X_5 \quad C_x < C_{\neg x} = \text{sign flip}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (\underline{x_3} \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID$$

$$X_3 \qquad \qquad \qquad 3 \qquad \qquad C_I = \text{the number of }$$

$$\text{clauses containing } l$$

$$\mu_I = \text{the average size of }$$

$$\text{clauses containing } l$$

$$X_5 \qquad \qquad \qquad C_x < C_{\neg x} = \text{sign flip}$$











$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$clauses containing l$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad$$

$$x_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad$$

$$clauses containing l$$

$$\mu_1 = \text{the average size of }$$

$$clauses containing l$$

$$x_6 \quad 1 \quad 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \# \psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{ \ 3 \mapsto 2,$$

$$x_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad \text{pl} = \text{the average size of }$$

$$x_6 \quad 1 \quad 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip} \qquad 6 \mapsto 3 \}$$



$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$x_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$x_4 \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{ \ 3 \mapsto 2, \\ \mu_I = \text{the average size of } \quad 4 \mapsto 1, \\ 5 \mapsto 4, \\ x_6 \quad 1 < 2 \quad 3 \quad 2.5 \quad 6 \quad 3 \quad C_x < C_{\neg x} = \text{sign flip} \qquad 6 \mapsto -3 \, \}$$



#### Cara caching scheme<sup>1</sup>

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$C_{1} = \text{the number of }$$

$$C_{2} \quad C_{3} \quad C_{4} \quad C_{5} \quad C_{$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$



### Cara caching scheme<sup>1</sup>

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \#\psi_1 = ?$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_1 = \text{the number of }$$

$$C_1 \quad C_2 \quad C_3 \quad C_4 \quad C_5 \quad C_7 \quad C_8 \quad C_9 \quad$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$

$$r(\psi_1) = 1, 3, 0, -2, -4, 0, -1, 3, 4, 0, 2, -3, 4, 0$$

#### sorted residual clauses



### Cara caching scheme<sup>1</sup>

$$\psi_1 = (\neg x_3 \lor \neg x_5) \land (x_4 \lor \neg x_6) \land (x_3 \lor x_5 \lor x_6) \land (\neg x_4 \lor x_5 \lor \neg x_6) \qquad \# \psi_1 = \mathbf{5}$$

$$C_x \quad C_{\neg x} \quad \mu_x \quad \mu_{\neg x} \quad ID \quad Order$$

$$X_3 \quad 1 \quad 1 \quad 3 \quad 2 \quad 3 \quad 2 \quad C_I = \text{the number of }$$

$$C_{\mathbf{x}} \quad 1 \quad 1 \quad 2 \quad 3 \quad 4 \quad 1 \quad \text{clauses containing } l \quad M_{\psi 1} = \{3 \mapsto 2, \\ \mu_{\mathbf{i}} = \text{the average size of } \quad 4 \mapsto 1, \\ \mathbf{x}_5 \quad 2 \quad 1 \quad 3 \quad 2 \quad 5 \quad 4 \quad C_{\mathbf{x}} < C_{\neg x} = \text{sign flip}$$

$$M_{\psi 1} = \{3 \mapsto 2, \\ \mu_{\mathbf{i}} = \text{the average size of } \quad 4 \mapsto 1, \\ 5 \mapsto 4, \\ 6 \mapsto -3 \}$$

$$M_{\psi 1}(\psi_1) = (\neg x_2 \lor \neg x_4) \land (x_1 \lor x_3) \land (x_2 \lor x_4 \lor \neg x_3) \land (\neg x_1 \lor x_4 \lor x_3)$$
  
 $r(\psi_1) = 1, 3, 0, -2, -4, 0, -1, 3, 4, 0, 2, -3, 4, 0$  cache entry: key =  $r(\psi_1)$ , sorted residual clauses  $\forall x_1 \lor x_2 \lor x_4 \lor x_3 \lor x_4 \lor x_4 \lor x_3 \lor x_4 \lor x_4 \lor x_3 \lor x_4 \lor$ 



### Cara caching scheme<sup>1</sup> - key properties

- 1) Deterministic representations
- Syntactically identical (up to ordering) CNF formulae yield the same representation and mapping function
  - => everything detected by i is also detected by Cara
- 3) Additional moments can be used in tuples to enhance isomorphism detection
- 4) Construction is computationally expensive
- 5) Representations tend to be larger



# **Cara** caching scheme vs caching scheme **i**

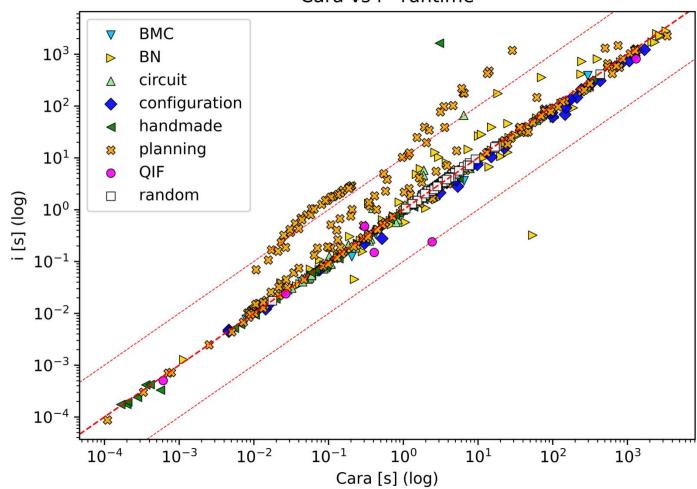


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved **3** times, and the given results are averages.

#solved runs	Cara	i
3/3	593	586
2/3	1	5
1/3	0	0
Total	594	591

#### Cara vs i - runtime

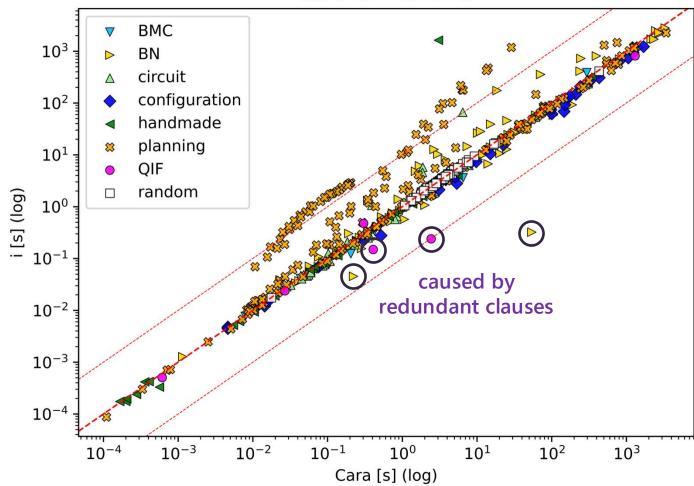


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

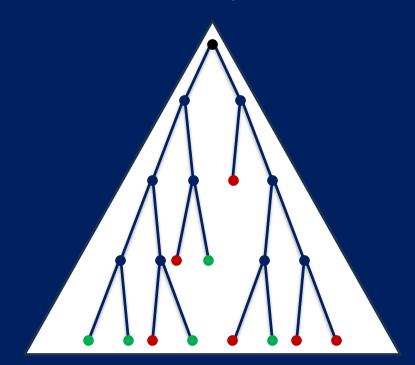
Each instance was solved **3** times, and the given results are averages.

#solved runs	Cara	i
3/3	593	586
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Total	594	591

#### Cara vs i - runtime

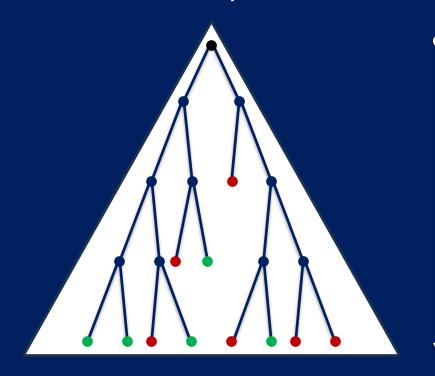


## Which caching scheme is better?





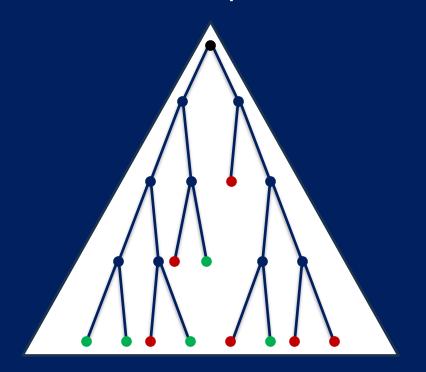
#### search space



larger residual formulae lower isomorphism detection more untouched clauses



#### search space

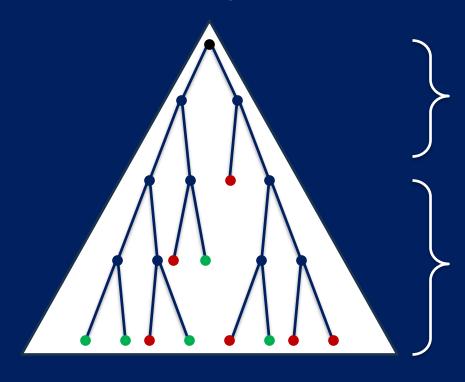


larger residual formulae lower isomorphism detection more untouched clauses

smaller residual formulaehigher isomorphism detectionfewer untouched clauses



#### search space

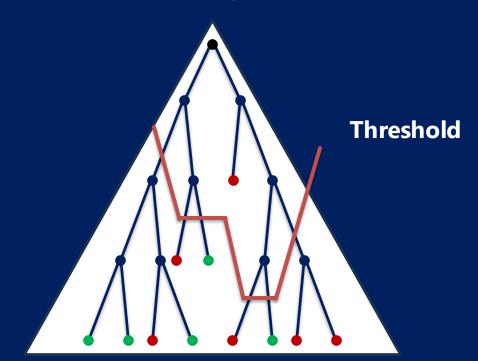


#### caching scheme

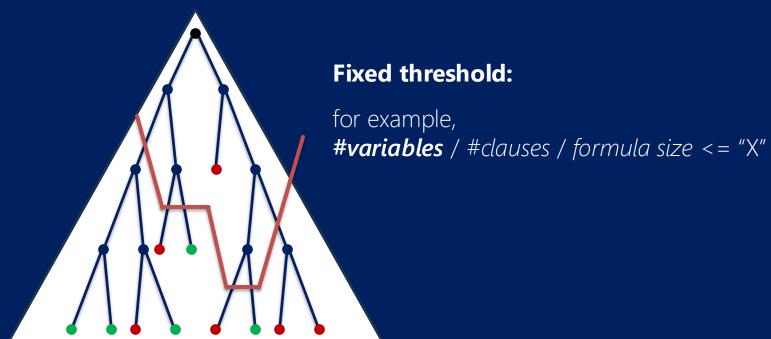
(standard, basic, i, hybrid, PCC, ...)

isomorphism-aware caching scheme (*Cara*, ...)

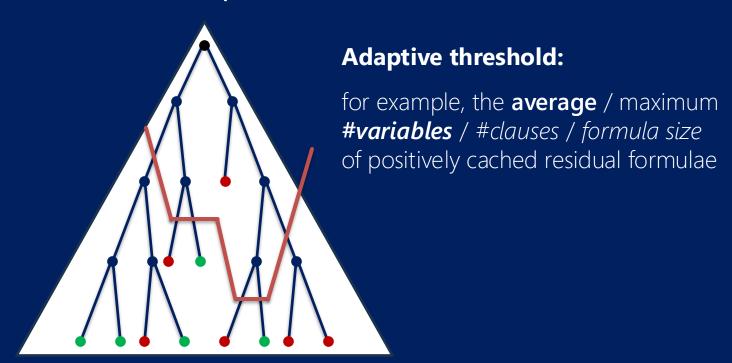






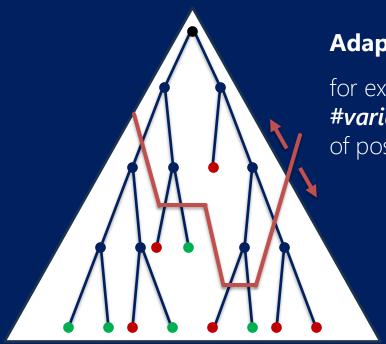








#### search space



#### **Adaptive threshold:**

for example, the **average** / maximum **#variables** / #clauses / formula size of positively cached residual formulae

Note: Invalid cache entries can be easily detected and removed when the next cache cleaning strategy is triggered.



## Cara<sup>1</sup> + Arjun<sup>\*2</sup> vs Ganak<sup>3</sup>

\* ensuring identical preprocessing



<sup>&</sup>lt;sup>2</sup> https://github.com/meelgroup/arjur



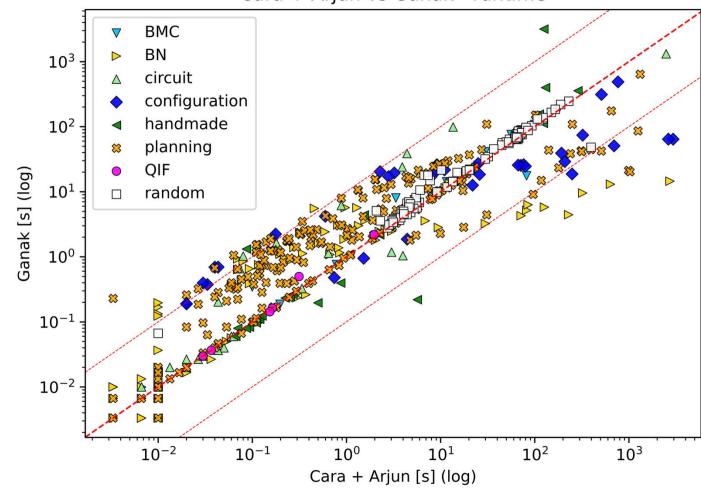
https://github.com/meelgroup/ganak

The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

#solved runs	Cara	Ganak
3/3	623	632
2/3	0	0
1/3	0	0
Total	623	632

Cara + Arjun vs Ganak - runtime

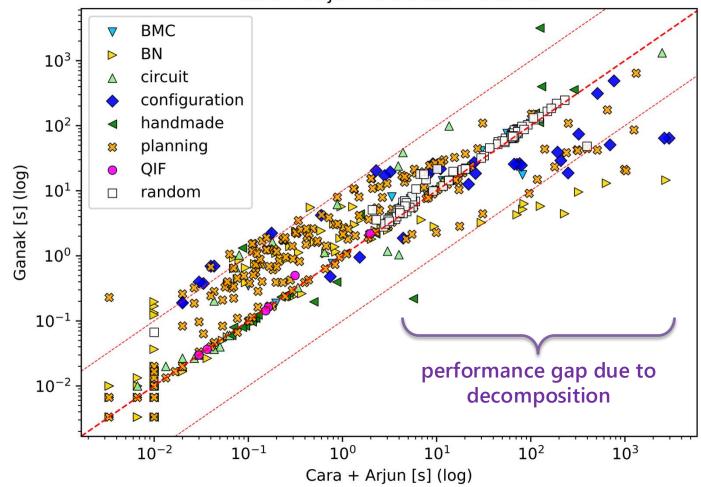


The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

#solved runs	Cara	Ganak
3/3	623	632
2/3	0	0
1/3	0	0
Total	623	632





# Cara<sup>1</sup> VS SymGanak\*2

\* no Arjun



https://github.com/Illner/carasolve

<sup>&</sup>lt;sup>2</sup> https://github.com/meelgroup/ganak

The time-out (resp. memory-out) was set to **1 hour** (resp. **32 GB**).

Each instance was solved 3 times, and the given results are averages.

#solved runs

3/3 593 512

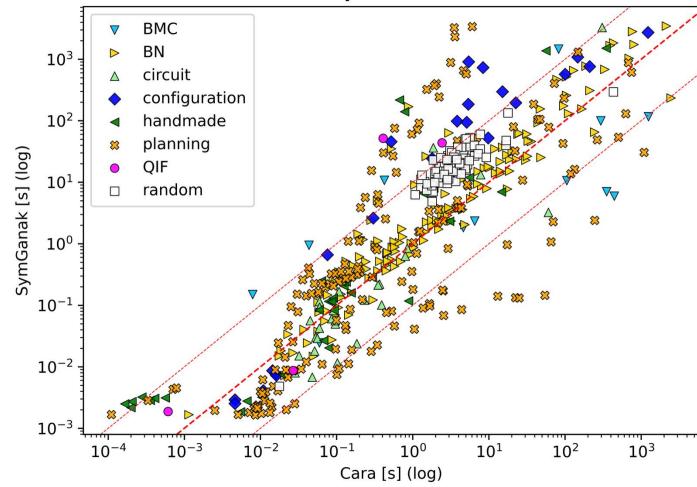
2/3 1 0

1/3 0 0

Total 594 512

\* strict dominance





## Functional pigeonhole principle (FPHP)

Instance <sup>1</sup>	#pigeons	#holes
fphp-010-020	10	20
fphp-015-020	15	20



<sup>1</sup> https://www.cril.univ-artois.fr/kc/benchmarks.htm

## Functional pigeonhole principle (FPHP)

Instance <sup>1</sup>	#pigeons	#holes
fphp-010-020	10	20
fphp-015-020	15	20

Instance1			Runtime	[s]		
Instance <sup>1</sup>	Cara <sup>2</sup>	Cara <sup>2</sup> + Arjun <sup>3</sup>	SymGanak <sup>4</sup>	Ganak <sup>4</sup>	SharpSAT-TD <sup>5</sup>	D4 <sup>6</sup>
fphp-010-020	3.04	124.81	2.37	3 176.17*	<u>—</u>	_
fphp-015-020	14.61	314.69	7.03	_	<u> </u>	_

<sup>\*</sup> invalid number of models



https://www.cril.univ-artois.fr/kc/benchmarks.html

<sup>&</sup>lt;sup>2</sup> https://github.com/Illner/carasolver

<sup>&</sup>lt;sup>3</sup> https://github.com/meelgroup/arjun

https://github.com/meelgroup/ganak

https://github.com/Laakeri/sharpsat-te

## N-Queens problem

N	Runtime [s]		
IN	<b>Cara</b> <sup>1</sup>	SymGanak <sup>2</sup>	
10	0.17	0.05	
11	0.62	0.47	
12	3.37	9.81	
13	25.89	92.09	
14	128.39	1858.32	
15	1264.51	_	



<sup>&</sup>lt;sup>1</sup> https://github.com/llher/carasolver <sup>2</sup> https://github.com/meelgroup/ganak

#### Future research

- 1) Adaptive balance of caching schemes
- 2) Replace the obsolete *MiniSat*<sup>1</sup>, which is used for satisfiability checks and implied literals at each inner node, with *CaDiCaL*<sup>2</sup>.
- 3) Integrate the decomposability approach used by *Ganak* and *SharpSAT-TD* into the adaptiveness framework.

