N	а	m	Δ

Standard Equation

Features

Graph

Ellipsoid

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

All traces are ellipses.

Elliptic paraboloid

$$z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

Traces with $z = z_0 > 0$ are ellipses.

Traces with $x = x_0$ or $y = y_0$ are parabolas.



Hyperboloid of one sheet

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

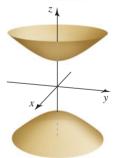
Traces with $z = z_0$ are ellipses for all z_0 . Traces with $x = x_0$ or $y = y_0$ are hyperbolas.



Hyperboloid of two sheets

$$-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

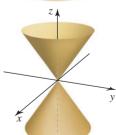
 $-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ Traces with $z = z_0$ with $|z_0| > |c|$ are ellipses. Traces with $z = x_0$ and $z = y_0$ are hyperbolas.



Elliptic cone

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = \frac{z^2}{c^2}$$

Traces with $z = z_0 \neq 0$ are ellipses. Traces with $x = x_0$ or $y = y_0$ are hyperbolas or intersecting lines.



Hyperbolic paraboloid

$$z = \frac{x^2}{a^2} - \frac{y^2}{b^2}$$

Traces with $z = z_0 \neq 0$ are hyperbolas.

Traces with $x = x_0$ or $y = y_0$ are parabolas.

