

# Generative models for human activity recognition

Ilya Zharikov, Roman Isachenko, Artem Bochkarev

## Introduction

This project is dedicated to multiclass classification of complex-structured objects (for which we don't have explicit features). The problem arises in many applications such as image recognition, signal processing or time series classification. We will focus on multiclass multivariate time series classification. In this setup time series are regarded as complex-structured objects without explicit feature description. This is reasonable because we can't operate with original features as time series might be of different size and not aligned [1].

We investigate classification of accelerometer time series [2]. The data is time series of acceleration from three axis, which is sensed by mobile phone or other portable device with accelerometer. The task is to predict the activity a person is performing. List of activities might include walking, running, sitting or walking up/down the stairs.

In general the problem of classifying complex-structured objects can be split in two distinctive procedures. First, we need to extract informative features, and then we use those features as input to some classifier to obtain final model. For simplicity, we assume that these two procedures can be built and analyzed separately. In our project we focused mainly on comparing different methods of feature generation [3, 4]. Extracted features can be later used for building classifiers and feature selection algorithms.

The first approach for feature generation is calculating expertly defined functions of time series [5]. These functions include average value, standard deviation,

mean absolute deviation and distribution for each component. We consider this approach a baseline, as it is the simplest method we use.

We compare baseline with more sophisticated parametric feature generation methods. One of them is autoregressive model [6]. For each time series we build parametric model and use those parameters as features for classification. We also consider the model of singular spectrum analysis of time series [7]. We use eigenvalues of trajectory matrix as features for building classifier.

In the first part of these report we give definitions and make problem statement. In the second part we describe all of the proposed approaches in more detail. Last, we make the experiment on real accelerometer datasets [8, 9], compare all methods and give conclusions and recommendations for practical use.

## Problem Statement

Let  $\mathcal{S}$  be a space of complex-structured objects,  $Y$  is a finite set of class labels. Denote by  $\mathfrak{D} = \{(s_i, y_i)\}_{i=1}^m$  – given sample, where  $s_i \in \mathcal{S}$  and  $y_i \in Y$ .

We consider the problem of recovering the function  $f : \mathcal{S} \rightarrow Y$

$$y = f(s).$$

Let  $L(f, \mathfrak{D})$  be an error function which expresses the classification error of the function  $f$  over the sample  $\mathfrak{D}$ . Our goal is to determine function  $f^*$  which minimizes the error

$$f^* = \arg \min_f L(f, \mathfrak{D}). \quad (1)$$

We assume that the target function  $f^*$  belongs to the class of function compositions  $f = g \circ h$ , where

- $h : \mathcal{S} \rightarrow H$  is a map from the original space  $\mathcal{S}$  to the feature space  $H \in \mathbb{R}^n$ ;
- $g : H \times \Theta \rightarrow Y$  is a parametric map from feature space  $H$  to the space of class labels  $Y$ . The function  $g$  is parametrized by a vector parameter  $\theta \in \Theta$ .

The determining of the function  $f^*$  is equivalent to determining the functions  $h^*$  and  $g^*$ .

In this project we consider the following ways of generating the feature space  $H$ :

- expert functions based on prior knowledge of the original objects. These functions can be expressed as a set of statistics  $\{h_i\}_{i=1}^n$ . Thus, the description  $\mathbf{h}$  of the object  $s$  is the value of these statistics on the object

$$\mathbf{h} = h(s) = (h_1(s), \dots, h_n(s)).$$

- hypothesis of data generation. In this case the features are the estimated parameters of the considered hypothesis. Let  $S(s, \mathbf{h}, \boldsymbol{\lambda})$  be the error function which specifies the hypothesis, e.g. one could define the function  $S$  as negative log-likelihood function [to do link]. The optimal parameters  $\hat{\mathbf{h}}$  for object  $s$  is obtained by

$$\hat{\mathbf{h}} = \arg \min_{\mathbf{h}} S(s, \mathbf{h}, \boldsymbol{\lambda}). \quad (2)$$

The parameter  $\boldsymbol{\lambda}$  is external structural parameter for the function  $S$ . The equation (2) determines the feature map  $h : \mathcal{S} \rightarrow H$ .

Given appropriate feature space  $H$  and feature map  $h$  we transform our original sample  $\mathfrak{D} = \{s_i, y_i\}_{i=1}^m$  to the  $\mathfrak{D}_H = \{\mathbf{h}_i, y_i\}_{i=1}^m$ , where  $\mathbf{h}_i = h(s_i)$ . The function  $g(\mathbf{h}, \theta)$  is defined by its parameters vector  $\theta \in \Theta$ . The optimal parameters  $\hat{\theta}$  are given by

$$\hat{\theta} = \arg \min_{\theta} L(g(\cdot, \theta), \mathfrak{D}_H),$$

where  $L(\cdot, \cdot)$  is an analogue of the function (1).

In our project we consider accelerometer time series as a complex objects. Time series is represented in following way:

$$s_i = \{x_1, \dots, x_T\},$$

where  $T$  denotes the length of time series. Now let us expand on different approaches of feature generation.

# Feature generation approaches

## Expert functions

Given a set of complex objects  $\{s_i\}_{i=1}^m$  we can extract features in a non-parametric way with a set of expert functions  $\{h_i\}_{i=1}^n$ . For time series, these functions could be mean, standard deviations, mean average deviations and distributions of the values. The main drawback of this approach is that we are restricted by our choice of expert functions and for some types of data these functions might be impossible to derive.

## Model of autoregression

In this method we assume autoregressive model of the order  $n$  as a hypothesis for generation of time series  $s$ . Here,  $n$  is a structural parameter and  $\lambda = n$ . We have

$$x_t = \theta_0 + \sum_{j=1}^n \theta_j x_{t-j} + \varepsilon_t.$$

Optimal parameters of autoregressive model  $\hat{\theta}_i = \mathbf{h}_i$  for time series  $s_i$  are found by minimizing mean squared error:

$$\mathbf{h}_i = \arg \min_{\theta \in \Theta} S(s_i, \theta, \lambda) = \arg \min_{\theta \in \Theta} \left( \sum_{t=1}^T \|x_i - \hat{x}_i\| \right),$$

where

$$\hat{x}_i = \theta_0 + \sum_{j=1}^n \theta_j x_{t-j}$$

## References

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