Social network Graph Link Prediction - Facebook Challenge

```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import warnings
        warnings.filterwarnings("ignore")
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xqboost: pip3 install xqboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import pickle
        from pandas import HDFStore,DataFrame
        from pandas import read hdf
        from scipy.sparse.linalg import svds, eigs
        import gc
        from tadm import tadm
```

1. Reading Data

```
In [2]: if os.path.isfile('data/after_eda/train_pos_after_eda.csv'):
            train_graph=nx.read_edgelist('data/after_eda/train_pos_after_eda.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=int)
            print(nx.info(train_graph))
        else:
            print("please run the FB EDA.ipynb or download the files from drive")
        Name:
        Type: DiGraph
        Number of nodes: 1780722
        Number of edges: 7550015
        Average in degree: 4.2399
        Average out degree: 4.2399
```

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

```
In [3]: #for followees
        def jaccard for followees(a,b):
            try:
                if len(set(train_graph.successors(a))) == 0 | len(set(train_graph.successors(b))) == 0:
                sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
                                            (len(set(train graph.successors(a)).union(set(train graph.successors(b)))))
            except:
                return 0
            return sim
In [4]: #one test case
        print(jaccard_for_followees(273084,1505602))
        0.0
In [5]: #node 1635354 not in graph
        print(jaccard for followees(273084,1505602))
        0.0
```

```
In [6]: #for followers
        def jaccard_for_followers(a,b):
                if len(set(train_graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
                    return 0
                sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b)))))/\
                                         (len(set(train graph.predecessors(a)).union(set(train graph.predecessors(b)))))
                return sim
            except:
                return 0
In [7]: print(jaccard for followers(273084,470294))
        0
In [8]: #node 1635354 not in graph
        print(jaccard_for_followees(669354,1635354))
        2.2 Cosine distance
                                                                     CosineDistance =
In [9]: #for followees
        def cosine for followees(a,b):
            try:
                if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
                    return 0
                sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))))/\
                                            (math.sqrt(len(set(train graph.successors(a)))*len((set(train graph.successors(b))))))
                return sim
            except:
                return 0
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html (https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

```
In [15]: if not os.path.isfile('data/fea_sample/page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr,open('data/fea_sample/page_rank.p','wb'))
else:
    pr = pickle.load(open('data/fea_sample/page_rank.p','rb'))
```

```
In [16]: print('min',pr[min(pr, key=pr.get)])
    print('max',pr[max(pr, key=pr.get)])
    print('mean',float(sum(pr.values())) / len(pr))

min 1.6556497245737814e-07
    max 2.7098251341935827e-05
    mean 5.615699699389075e-07

In [17]: #for imputing to nodes which are not there in Train data
    mean_pr = float(sum(pr.values())) / len(pr)
    print(mean_pr)
```

5.615699699389075e-07

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [18]: #if has direct edge then deleting that edge and calculating shortest path
def compute_shortest_path_length(a,b):
    p=-1
    try:
        if train_graph.has_edge(a,b):
             train_graph.remove_edge(a,b)
             p= nx.shortest_path_length(train_graph,source=a,target=b)
             train_graph.add_edge(a,b)
    else:
        p= nx.shortest_path_length(train_graph,source=a,target=b)
        return p
    except:
        return -1
```

```
In [19]: #testing
    compute_shortest_path_length(77697, 826021)
Out[19]: 10
In [20]: #testing
    compute_shortest_path_length(669354,1635354)
Out[20]: -1
```

4.2 Checking for same community

```
In [21]: #getting weekly connected edges from graph
         wcc=list(nx.weakly_connected_components(train_graph))
         def belongs_to_same_wcc(a,b):
             index = []
             if train_graph.has_edge(b,a):
                 return 1
             if train graph.has edge(a,b):
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if (b in index):
                         train_graph.remove_edge(a,b)
                         if compute_shortest_path_length(a,b)==-1:
                             train_graph.add_edge(a,b)
                             return 0
                         else:
                             train_graph.add_edge(a,b)
                             return 1
                     else:
                         return 0
             else:
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if(b in index):
                         return 1
                     else:
                         return 0
In [22]: belongs_to_same_wcc(861, 1659750)
Out[22]: 0
In [23]: belongs to same wcc(669354,1635354)
```

4.3 Adamic/Adar Index:

Out[23]: 0

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x, y) = \sum_{u \in N(x) \cap N(y)} \frac{1}{log(|N(u)|)}$$

```
In [24]: |#adar index
         def calc_adar_in(a,b):
             sum=0
             try:
                 n=list(set(train graph.successors(a)).intersection(set(train graph.successors(b))))
                 if len(n)!=0:
                     for i in n:
                         sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
                     return sum
                 else:
                     return 0
             except:
                 return 0
In [25]: calc_adar_in(1,189226)
Out[25]: 0
In [26]: calc_adar_in(669354,1635354)
Out[26]: 0
         4.4 Is persion was following back:
In [27]: def follows_back(a,b):
             if train_graph.has_edge(b,a):
                 return 1
             else:
                 return 0
In [28]: follows_back(1,189226)
Out[28]: 1
In [29]: follows_back(669354,1635354)
```

4.5 Katz Centrality:

Out[29]: 0

https://en.wikipedia.org/wiki/Katz centrality (https://en.wikipedia.org/wiki/Katz centrality)

https://www.geeksforgeeks.org/katz-centrality-measure/ (https://www.geeksforgeeks.org/katz-centrality-measure/) Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i

 $x_i = \alpha \sum_j A_{ij} x_j + \beta,$

where A is the adjacency matrix of the graph G with eigenvalues

λ

The parameter

β

controls the initial centrality and

$$\alpha < \frac{1}{\lambda_{max}}$$

```
In [30]: if not os.path.isfile('data/fea_sample/katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('data/fea_sample/katz.p','wb'))
else:
    katz = pickle.load(open('data/fea_sample/katz.p','rb'))

In [31]: print('min',katz[min(katz, key=katz.get)])
    print('max',katz[max(katz, key=katz.get)])
    print('mean',float(sum(katz.values())) / len(katz))

min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018

In [32]: mean_katz = float(sum(katz.values())) / len(katz)
    print(mean_katz)
```

4.6 Hits Score

0.0007483800935562018

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm (https://en.wikipedia.org/wiki/HITS_algorithm)

```
In [33]: if not os.path.isfile('data/fea_sample/hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('data/fea_sample/hits.p','wb'))
else:
    hits = pickle.load(open('data/fea_sample/hits.p','rb'))
```

```
In [34]: print('min',hits[0][min(hits[0], key=hits[0].get)])
    print('max',hits[0][max(hits[0], key=hits[0].get)])
    print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
    max 0.004868653378780953
    mean 5.615699699344123e-07
```

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
In [35]: import random
         if os.path.isfile('data/after eda/train after eda.csv'):
             filename = "data/after eda/train after eda.csv"
             # you uncomment this line, if you dont know the lentqh of the file name
             # here we have hardcoded the number of lines as 15100030
             # n train = sum(1 for line in open(filename)) #number of records in file (excludes header)
             n train = 15100028
             s = 100000 #desired sample size
             skip train = sorted(random.sample(range(1,n_train+1),n_train-s))
             #https://stackoverflow.com/a/22259008/4084039
In [36]: if os.path.isfile('data/after_eda/train_after_eda.csv'):
             filename = "data/after eda/test after eda.csv"
             # you uncomment this line, if you dont know the lentgh of the file name
             # here we have hardcoded the number of lines as 3775008
             # n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
             n test = 3775006
             s = 50000 #desired sample size
             skip_test = sorted(random.sample(range(1,n_test+1),n_test-s))
             #https://stackoverflow.com/a/22259008/4084039
```

```
In [37]: print("Number of rows in the train data file:", n train)
         print("Number of rows we are going to elimiate in train data are",len(skip train))
         print("Number of rows in the test data file:", n test)
         print("Number of rows we are going to elimiate in test data are",len(skip test))
         Number of rows in the train data file: 15100028
         Number of rows we are going to elimiate in train data are 15000028
         Number of rows in the test data file: 3775006
         Number of rows we are going to elimiate in test data are 3725006
In [38]: df final train = pd.read csv('data/after eda/train after eda.csv', skiprows=skip train, names=['source node', 'destination node'])
         df final train['indicator link'] = pd.read csv('data/train y.csv', skiprows=skip train, names=['indicator link'])
         print("Our train matrix size ",df final train.shape)
         df final train.head(2)
         Our train matrix size (100002, 3)
Out[38]:
             source_node destination_node indicator_link
          0
                 273084
                               1505602
          1
                1492633
                               1370536
In [39]: df_final_test = pd.read_csv('data/after_eda/test_after_eda.csv', skiprows=skip_test, names=['source_node', 'destination_node'])
         df final test['indicator link'] = pd.read csv('data/test y.csv', skiprows=skip test, names=['indicator link'])
         print("Our test matrix size ",df final test.shape)
         df final test.head(2)
         Our test matrix size (50002, 3)
Out[39]:
             source_node destination_node indicator_link
                 848424
                                784690
                1054634
          1
                                332605
```

5.2 Adding a set of features

we will create these each of these features for both train and test data points

- 1. jaccard followers
- 2. jaccard followees
- 3. cosine followers
- 4. cosine followees
- 5. num followers s

```
6. num_followees_s
7. num_followers_d
8. num_followees_d
9. inter_followers
10. inter_followees
```

```
In [40]: if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
             #mapping jaccrd followers to train and test data
             df final train['jaccard followers'] = df final train.apply(lambda row:
                                                     jaccard for followers(row['source node'],row['destination node']),axis=1)
             df final test['jaccard followers'] = df final test.apply(lambda row:
                                                     jaccard_for_followers(row['source_node'],row['destination_node']),axis=1)
             #mapping jaccrd followees to train and test data
             df final train['jaccard followees'] = df final train.apply(lambda row:
                                                     jaccard_for_followees(row['source_node'],row['destination_node']),axis=1)
             df final test['jaccard followees'] = df final test.apply(lambda row:
                                                     jaccard for_followees(row['source_node'],row['destination_node']),axis=1)
                 #mapping jaccrd followers to train and test data
             df final train['cosine followers'] = df final train.apply(lambda row:
                                                     cosine_for_followers(row['source_node'],row['destination_node']),axis=1)
             df_final_test['cosine_followers'] = df_final_test.apply(lambda row:
                                                     cosine_for_followers(row['source_node'],row['destination_node']),axis=1)
             #mapping jaccrd followees to train and test data
             df final train['cosine followees'] = df final train.apply(lambda row:
                                                     cosine for followees(row['source node'],row['destination node']),axis=1)
             df final test['cosine followees'] = df final test.apply(lambda row:
                                                     cosine for_followees(row['source_node'],row['destination_node']),axis=1)
```

```
In [41]: def compute features stage1(df final):
             #calculating no of followers followees for source and destination
             #calculating intersection of followers and followees for source and destination
             num_followers_s=[]
             num followees s=[]
             num followers d=[]
             num followees d=[]
             inter followers=[]
             inter followees=[]
             for i,row in df final.iterrows():
                 try:
                     s1=set(train_graph.predecessors(row['source_node']))
                     s2=set(train graph.successors(row['source node']))
                 except:
                     s1 = set()
                     s2 = set()
                 try:
                     d1=set(train graph.predecessors(row['destination node']))
                     d2=set(train_graph.successors(row['destination_node']))
                 except:
                     d1 = set()
                     d2 = set()
                 num_followers_s.append(len(s1))
                 num followees s.append(len(s2))
                 num followers d.append(len(d1))
                 num followees d.append(len(d2))
                 inter followers.append(len(s1.intersection(d1)))
                 inter followees.append(len(s2.intersection(d2)))
             return num_followers_s, num_followers_d, num_followees_s, num_followees_d, inter_followers, inter_followees
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
In [43]: if not os.path.isfile('data/fea sample/storage sample stage2.h5'):
            #mapping adar index on train
            df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node'],row['destination node']),axis=1)
            #mapping adar index on test
            df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],row['destination node']),axis=1)
            #mapping followback or not on train
            df final train['follows back'] = df final train.apply(lambda row: follows back(row['source node'],row['destination node']),axis=1)
            #mapping followback or not on test
            df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node'],row['destination node']),axis=1)
            #mapping same component of wcc or not on train
            df final train['same comp'] = df final_train.apply(lambda row: belongs_to_same_wcc(row['source_node'],row['destination_node']),axis=1)
            ##mapping same component of wcc or not on train
            df final test['same comp'] = df final test.apply(lambda row: belongs to same wcc(row['source node'],row['destination node']),axis=1)
            #-----
            #mappina shortest path on train
            df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path_length(row['source_node'],row['destination_node']),axis=1
            #mapping shortest path on test
            df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['source node'],row['destination node']),axis=1)
            hdf = HDFStore('data/fea sample/storage sample stage2.h5')
            hdf.put('train df',df final train, format='table', data columns=True)
            hdf.put('test df',df final test, format='table', data columns=True)
            hdf.close()
         else:
            df final train = read hdf('data/fea sample/storage sample stage2.h5', 'train df',mode='r')
            df final test = read hdf('data/fea sample/storage sample stage2.h5', 'test df',mode='r')
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - weight of incoming edges
 - weight of outgoing edges
 - · weight of incoming edges + weight of outgoing edges
 - weight of incoming edges * weight of outgoing edges
 - 2*weight of incoming edges + weight of outgoing edges
 - · weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source

- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1 + |X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
In [44]: #weight for source and destination of each link
Weight_in = {}
Weight_out = {}
for i in tqdm(train_graph.nodes()):
    s1=set(train_graph.predecessors(i))
    w_in = 1.0/(np.sqrt(1+len(s1)))
    Weight_in[i]=w_in

    s2=set(train_graph.successors(i))
    w_out = 1.0/(np.sqrt(1+len(s2)))
    Weight_out[i]=w_out

#for imputing with mean
mean_weight_in = np.mean(list(Weight_in.values()))
mean_weight_out = np.mean(list(Weight_out.values()))
```

| 1780722/1780722 [00:26<00:00, 67788.51it/s]

```
In [45]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
             #mapping to pandas train
             df_final_train['weight_in'] = df_final_train.destination_node.apply(lambda x: Weight_in.get(x,mean_weight_in))
             df final train['weight out'] = df final train.source node.apply(lambda x: Weight out.get(x,mean weight out))
             #mapping to pandas test
             df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x,mean weight in))
             df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x,mean weight out))
             #some features engineerings on the in and out weights
             df final train['weight f1'] = df final train.weight in + df final train.weight out
             df final train['weight f2'] = df final train.weight in * df final train.weight out
             df final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
             df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
             #some features engineerings on the in and out weights
             df final test['weight f1'] = df final test.weight in + df final test.weight out
             df final test['weight f2'] = df final test.weight in * df final test.weight out
             df final test['weight f3'] = (2*df final test.weight in + 1*df final test.weight out)
             df final test['weight f4'] = (1*df final test.weight in + 2*df final test.weight out)
```

```
In [46]: if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
            #page rank for source and destination in Train and Test
            #if anything not there in train graph then adding mean page rank
           df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
           df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr))
            df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
            df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
            #-----
            #Katz centrality score for source and destination in Train and test
            #if anything not there in train graph then adding mean katz score
           df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x,mean katz))
            df final train['katz d'] = df final train.destination node.apply(lambda x: katz.get(x,mean katz))
            df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
            df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
            #Hits algorithm score for source and destination in Train and test
           #if anything not there in train graph then adding 0
            df final train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x,0))
            df final train('hubs d') = df final train.destination node.apply(lambda x: hits[0].get(x,0))
            df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].get(x,0))
           df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
            #-----
            #Hits algorithm score for source and destination in Train and Test
            #if anything not there in train graph then adding 0
            df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x,0))
           df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x,0))
            df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
            df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
            hdf = HDFStore('data/fea sample/storage sample stage3.h5')
           hdf.put('train df',df final train, format='table', data columns=True)
           hdf.put('test df',df final test, format='table', data columns=True)
           hdf.close()
        else:
            df final train = read hdf('data/fea sample/storage sample stage3.h5', 'train df',mode='r')
            df final test = read hdf('data/fea sample/storage sample stage3.h5', 'test df',mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [47]: def svd(x, S):
             try:
                 z = sadj_dict[x]
                 return S[z]
             except:
                 return [0,0,0,0,0,0]
In [48]: #for svd features to get feature vector creating a dict node val and inedx in svd vector
         sadj col = sorted(train graph.nodes())
         sadj dict = { val:idx for idx,val in enumerate(sadj col)}
In [49]: Adj = nx.adjacency_matrix(train_graph,nodelist=sorted(train_graph.nodes())).asfptype()
In [50]: U, s, V = svds(Adj, k = 6)
         print('Adjacency matrix Shape',Adj.shape)
         print('U Shape',U.shape)
         print('V Shape', V.shape)
         print('s Shape',s.shape)
         Adjacency matrix Shape (1780722, 1780722)
         U Shape (1780722, 6)
         V Shape (6, 1780722)
         s Shape (6,)
```

```
In [51]: if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
          #-----
          df_final_train[['svd_u_s_1', 'svd_u_s_2','svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6']] = \
          df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
          df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5', 'svd_u_d_6']] = \
          df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
          df_{final_train[['svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]] = \
          df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
          df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6']] = \
          df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
          #=-----
          df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
          df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
          df final test[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
          df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
          #-----
          df final test[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
          df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
          df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6']] = \
          df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
          #_____
          hdf = HDFStore('data/fea sample/storage sample stage4.h5')
          hdf.put('train df', df final train, format='table', data columns=True)
          hdf.put('test df',df final test, format='table', data columns=True)
          hdf.close()
```

In [52]: # prepared and stored the data from machine learning models
pelase check the FB Models.ipynb