

# Experiment:- 6

**Objective:-** Solve Constraint Satisfaction Problem.

## **Theory:-**

A **Constraint Satisfaction Problem (CSP)** is a mathematical framework used to solve problems where a set of variables must be assigned values that satisfy specific constraints. CSPs are widely applied in Artificial Intelligence (AI) for tasks like scheduling, planning, resource allocation, and puzzle solving.

## **Key Components of CSP**

1. **Variables:** These represent the unknowns that need to be assigned values. For example, in Sudoku, each cell is a variable.
2. **Domains:** Each variable has a domain, which is the set of possible values it can take. For instance, in Sudoku, the domain for each cell is  $\{1, 2, \dots, 9\}$ .
3. **Constraints:** These are rules that restrict the values variables can take.

Constraints can be unary (affecting one variable), binary (involving two variables), or higher-order (involving multiple variables). For example, in Sudoku, no two cells in the same row can have the same value.

## **Solving CSPs**

CSPs are solved using algorithms that explore the search space while ensuring constraints are met. Common techniques include:

1. **Backtracking:** A depth-first search approach that assigns values to variables and backtracks when a constraint is violated.
2. **Forward Checking:** Enhances backtracking by eliminating inconsistent values from the domains of unassigned variables after each assignment.
3. **Constraint Propagation:** Enforces local consistency by propagating constraints across variables, reducing the search space.

## Types of Constraint Satisfaction Problems

CSPs can be classified into different types based on their constraints and problem characteristics:

1. **Binary CSPs:** In these problems each constraint involves only two variables. Like in scheduling problem constraints could specify that task A must be completed before task B.
2. **Non-Binary CSPs:** These problems have constraints that involve more than two variables. For instance in a seating arrangement problem a constraint could state that three people cannot sit next to each other.
3. **Hard and Soft Constraints:** Hard constraints must be strictly satisfied while soft constraints can be violated but at a certain cost. This is often used in real-world applications where not all constraints are equally important

## Program:-

### Solving Sudoku with Constraint Satisfaction Problem (CSP)

```
class SudokuSolver:
```

```
    def __init__(self, sudoku):
        self.sudoku = sudoku

        self.n = len(sudoku)

        self.sqrt_n = int(self.n ** 0.5)

    def solve_sudoku(self):
        if self.solve():
            return self.sudoku
        else:
            return None

    def solve(self):
        row, col = self.find_unassigned_space()
        if row
```

```

        -1 and col == num:
            return -1:

    return True # Puzzle solved

    for num in range(1, self.n + 1):
        if self.is_safe(row, col, num):
            self.sudoku[row][col] = num
            self.solve():
                return True
            self.sudoku[row][col] = 0 # Backtrack

    return False # Trigger backtracking

def find_unassigned_space(self):
    for row in range(self.n):
        for col in range(self.n):
            if self.sudoku[row][col] == 0:
                return row, col
    return -1, -1

def is_safe(self, row, col, num):
    #Row & Column check
    for i in range(self.n):
        if self.sudoku[row][i] == num or self.sudoku[i][col]
            return False
            == num:

```

```

# Subgrid check
subgrid_row_start = (row // self.sqrt_n) * self.sqrt_n
subgrid_col_start = (col // self.sqrt_n) * self.sqrt_n

for i in range(subgrid_row_start, subgrid_row_start + self.sqrt_n):
    for j in range(subgrid_col_start, subgrid_col_start + self.sqrt_n):
        if self.sudoku[i][j]
            == num:

            return False

return True

# Initial Sudoku Puzzle (0 means unfilled)
sudoku = [

        6],
[0, 0, 0, 0, 0, 0, 0, 7, [7, 0,
2, 9, 6, 0, 4, 5, 1],

```

```

]
[5, 3, 0, 0, 7, 1, 2, 8, 0],
[0, 7, 0, 0, 0, 6, 9, 2, 0],
[0, 0, 3, 8, 9, 0, 0, 4, 7],
[6, 0, 0, 0, 0, 0, 0, 1, 0],
[0, 0, 0, 6, 8, 2, 0, 0, 0],
[3, 6, 0, 5, 1, 4, 0, 9, 0],
[4, 2, 8, 7, 0, 9, 1, 0, 0]

# Solve it

solver = SudokuSolver(sudoku)
solution = solver.solve_sudoku()

# Display result

if solution:
    print("Sudoku solution:")
    for row in solution:

else:
    print(row)

    print("No solution exists.")

```

### Output:-

Sudoku solution:

[1, 4, 9, 2, 5, 8, 3, 7, 6]

[7, 8, 2, 9, 6, 3, 4, 5, 1]

[5, 3, 6, 4, 7, 1, 2, 8, 9] 3]

[8, 7, 5, 1, 4, 6, 9, 2,

[2, 1, 3, 8, 9, 5, 6, 4, 7]

[6, 9, 4, 3, 2, 7, 5, 1, 8]

[9, 5, 1, 6, 8, 2, 7, 3, 4]

[3, 6, 7, 5, 1, 4, 8, 9, 2]

[4, 2, 8, 7, 3, 9, 1, 6, 5]

