



Inspiring Excellence



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CSE 461

Introduction to Robotics

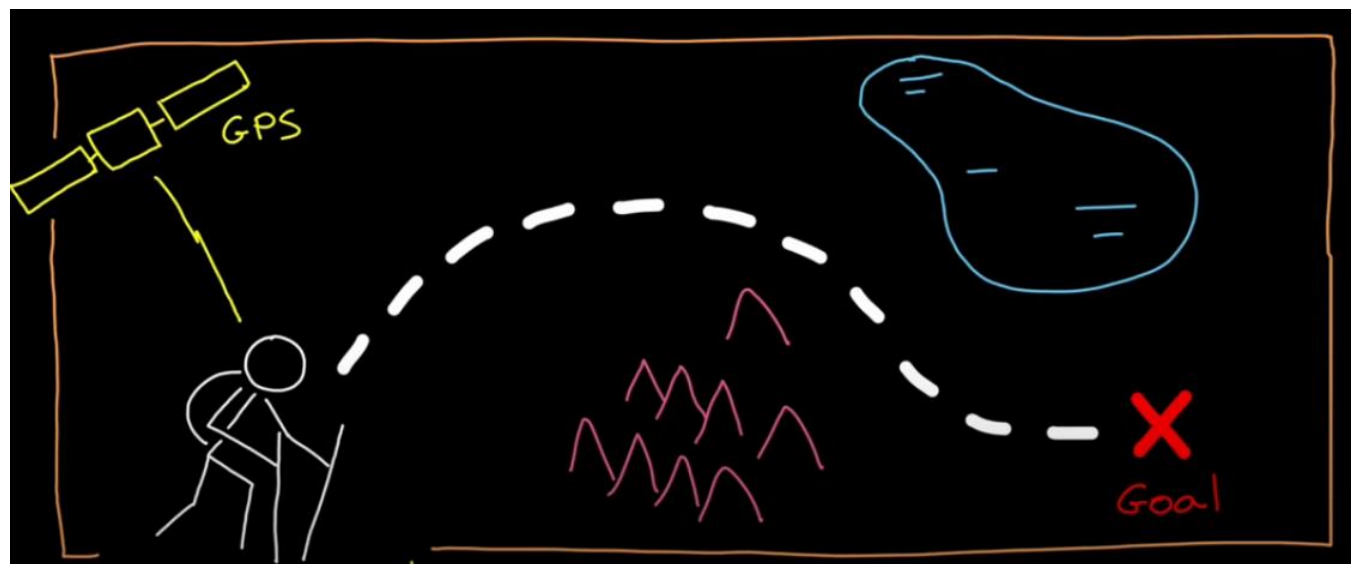
Navigation : Path planning, Localization, Mapping ,Exploration

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Navigation

- The act, activity, or process of finding the way to get to a place
- Navigation is the ability to determine your location and plan a path to some goal



Robot Navigation

For autonomous behavior, robots need the ability to navigate:

- Learn the environment->“Model”
- Estimate where it is in the environment->“Localize”
- Move to desired locations in the environment

Navigation Example



Scenarios

- Hospital Helper
(e.g. Diligent, Tugs)
- Office security or mail-delivery
(e.g. Cobalt, Savioke)
- Tour Guide robot in a museum (Minerva)
- Autonomous Car with GPS and Nav system

Biological analogies:

Humans, bees and ants, migrating birds, herds

Navigation Problem

Problem Characteristics

- Environments are Known versus Unknown
- Environments are Static versus Dynamic
- Environments are Structured versus Unstructured (Indoors versus Outdoors?)

Robots Navigating

- **Path Planning:** How I get to my Goal?
- **Localization:** Where am I?
- **Mapping:** Where have I been?
- **Exploration:** Where haven't I been?

What is Path Planning?

- Simple Question: **How do I get to my Goal?**
- Not a simple answer!
 - Can you see your goal?
 - Do you have a map?
 - Are obstacles unknown or dynamic?
 - Does it matter how fast you get there?
 - Does it matter how smooth the path is ?
 - How much compute power do you have?
 - How precise is your motion control?
- Path Planning is best thought of as a Collection of Algorithms
- 3 Things need to consider: Environment, Success metrics, Robot capability.

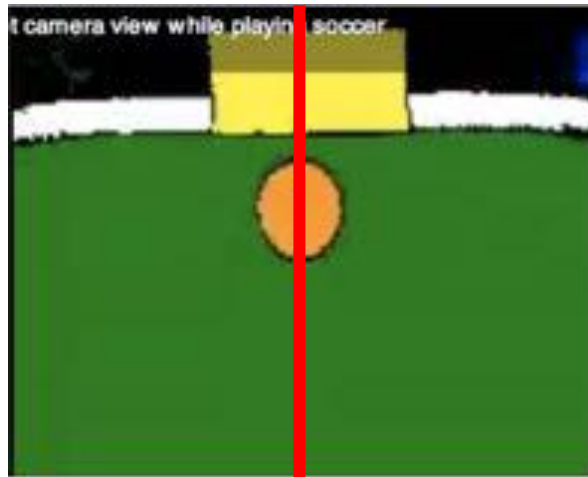
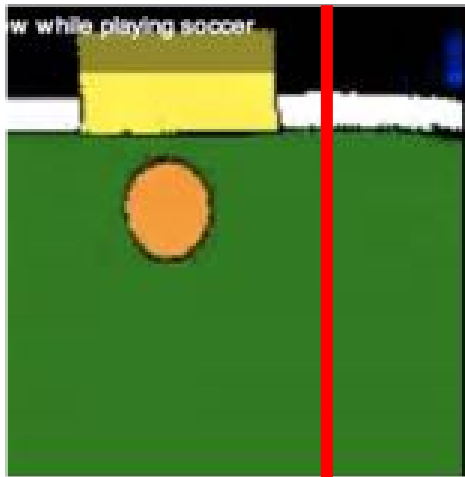
Types of Path Planning Approaches

- **Basics**
 - Visual homing (Purely local sensing and feedback control)
 - Inverse Kinematics (Turn-move-turn to get from A to B)
- **Bug-based Path Planning (mostly-local without a map)**
 - Robots can see the Goal (direction and distance)
 - But there are unknown obstacles in the way (No map)
- **Metric (A^*) Path Planning (global with a map)**
 - Assumes that you have a map (distance or graph) and you know where you and the goal are located in it.
 - Path is represented as a series of waypoints (directions)

Basics: Visual Homing

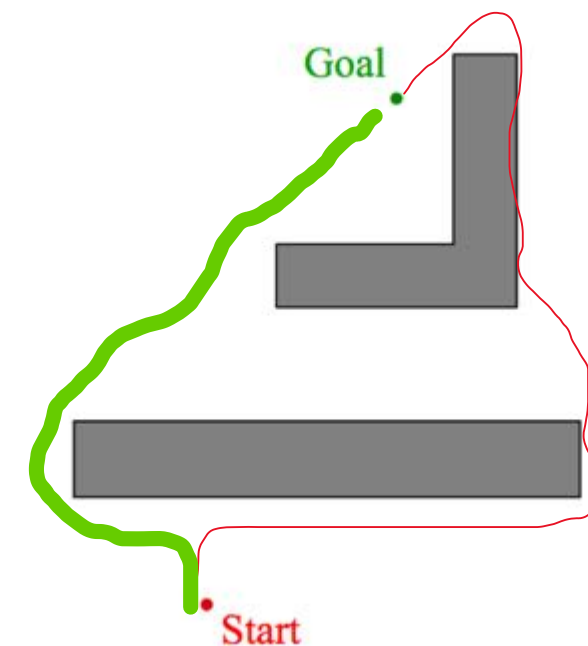
Purely Reactive Navigation

- Measure Visual (x,y) Position of Goal
- Move to bring goal to Visual Center
- Proportional Control (if you see the goal), Random walk (if you don't)



Bug-based Path Planning

- What if the Robot has obstacles in the way?
 - Always have Goal direction and/or distance (Global)
 - But No Map: Only local knowledge of environment (Local)
 - *Example Scenario:*
Outdoor robot knows GPS location of goal, but building in the way.
Indoor robot see goal location, but furniture in the way.
- “Bug” Algorithms depend on simple but provable behaviors!
 - Don’t need to build a map
 - *Simple Computation: Visual Homing + Wall-following + Odometry*
- Very intuitive class of algorithms – but surprisingly powerful



Metric/Global Path Planning

- **What if the Robot has Full Knowledge**
 - A map of the environment and robot + goal's locations
 - Goal: Find a “optimal” path (typically distance)

- **Two Components**
 - **Map Representation (“graph”):**
 - Feature based maps (office numbers, landmarks)
 - Grid based maps (cartesian, quadtrees)
 - Polygonal maps (geometric decompositions)
 - **Path Finding Algorithms:**
 - Shortest-Path Graph Algorithms (Breadth-First-Search, A* Algorithm)

Map Representation: Feature based

- Also known as a Topological or Landmark-based Map

- Features your robot can recognize:

- Includes both natural landmarks (corner, doorway, hallways) and artificial ones (office door numbers; or robot-friendly tags)

- Gateways are landmarks that represent decisions (e.g. intersection)

- Distinguishable places are unique landmarks

- World is a graph that connects landmarks

- Edges represent **actual motion**: how to get from landmark A to landmark B

- Usually visual/reactive navigation is possible along an edge*

- Edges can also keep **extra attributes**: distance, time it takes, etc.

- Google Maps are topological maps for humans (e.g. turn at intersection)

Path Finding Algorithms

- All Map Representations are a weighted “graph”
 - Nice part is that you only need to do this once
- Algorithm: Compute shortest paths in the graph
 - Path is represented by a series of waypoints
 - Single Path Search Algorithms: Find shortest path A to B
 - Breadth-First-Search (simple graphs);
 - A* search for large graphs (BFS + Heuristic)
 - Gradient Path Algorithms: Find *all paths* towards B
 - E.g. Fixed Base station: BFS, Dijkstra’s, Wavefront algorithms, etc.

Robots Navigating

- **Path Planning**: How to I get to my Goal?
- **Localization**: Where am I?
- **Mapping**: Where have I been?
- **Exploration**: Where haven't I been?

Localization

- **Simple Question:** *Where am I?*
- **Not a simple answer:**
 - Do you have a map?
 - Yes => a global position in the world
 - No => position in reference to other objects? Or your own past?
 - What can you sense?
 - Can you sense and record your own self-movement?
 - Can you sense external things like landmarks?
 - How certain are you about what you sense?
- **Localization is a “collection of algorithms”**

Localization Techniques

➤ **Dead-reckoning (motion)**

- Keep track of where you are without a map, by recording the series of actions that you made, using internal sensors. (also called Odometry, Path Integration)

➤ **Landmarks (sensing)**

- Triangulate your position geometrically, by measuring distance to one or more known landmarks
E.g. Visual beacons or features, Radio/Cell towers and signal strength, GPS!

➤ **State Estimation (uncertainty in motion & sensing)**

- *Probabilistic Reasoning*
 - **Kalman Filters** (combine both motion and sensing)
 - **Particle Filters** (also known as Monte Carlo Localization)

Dead-Reckoning

- Keep track of initial position and **the series of movements/actions** that you made.
- **Method: Take a “step”, compute new position.**
- Also called odometry or path integration

Example: Inertial navigation systems (INS)

- Complex motion (momentum, external effects)
- Include **accelerometers** and **gyroscopes** to provide better measurements of instantaneous velocity.
- Expensive systems very good
 - satellites, submarines
- But, low-cost IMU's increasingly available

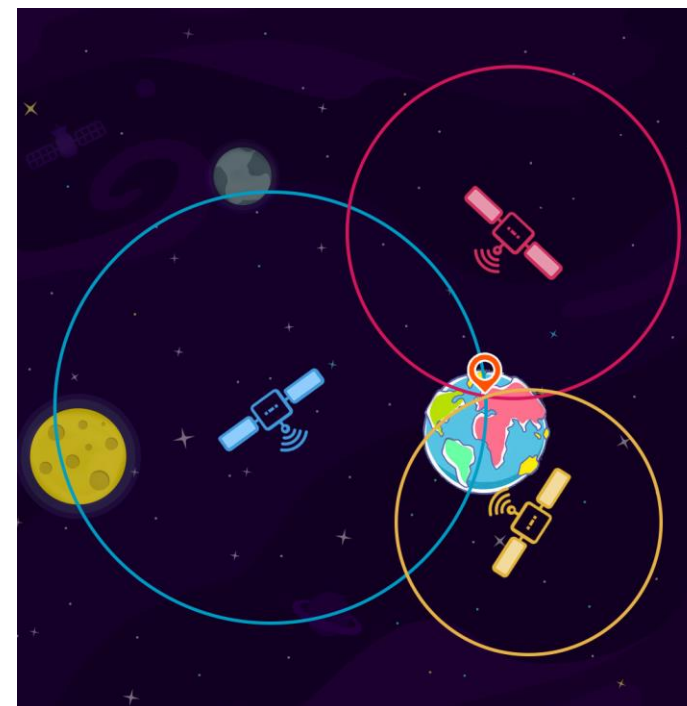
Land Mark

- **How it works**

- *Opposite of dead-reckoning!*
- Use measurements to external landmarks of known position
- Examples: visual landmarks, radio towers, GPS!

- **Example**

- ➤ GPS Satellites are your “landmarks”
- Continually transmits a message
- Message includes both time of transmission, and satellite position
- GPS Receiver
- Compute distance by measuring signal transmission time (speed of light)
- 3D: Lie on the intersection of 4 spheres!



State Estimation (uncertainty in motion & sensing)

- **Key Idea: Combine Motion and Sensing**
 - **(Dead-reckoning + uncertainty) + (Landmarks + uncertainty)**
 - Each has error, but the error can be complementary
- **Kalman Filters**
 - Take advantage of mathematics of **Gaussians** to model uncertainty
 - General method for state estimation (not just localization)
 - Applications: Car + GPS, Lawnmower + beacons, warehouse robots
- **Particle Filters (Monte Carlo Localization)**
 - Use a **discrete distribution of “Particles”** to represent uncertainty (think of sampling or histograms)
 - Useful when environment is complex and ambiguous
 - Application: A robot wandering in a building with a map

Robots Navigating

- **Path Planning**: How to I get to my Goal?
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Mapping and Exploration

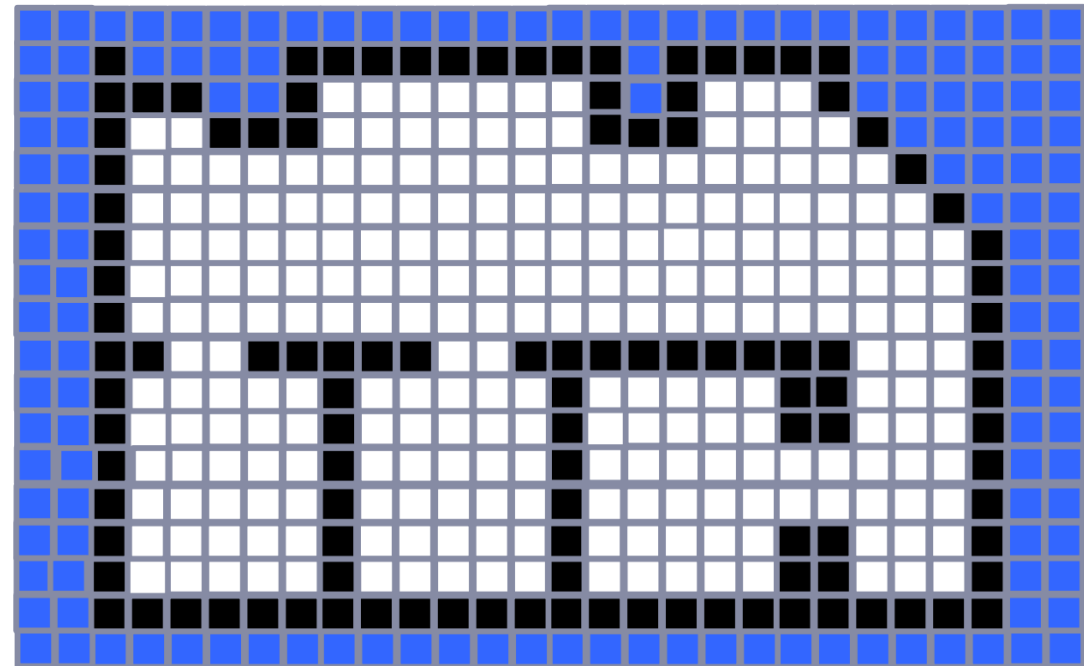
- **Question:**
 - You are roaming around in an unknown space, what can you learn about it?
- Two parts of the problem:
 - **Mapping:** As you roam around the world, how do you build a memory of the shape of the space you have moved through?
 - **Exploration:** Given that you don't know the shape or size of the environment, how to make sure you covered all of it?
- Both have many uses:
 - Returning back to home/charger after some task.
 - Cleaning a new room efficiently; Systematic search for survivors
 - Mapping a collapsed mine or building.
- **Mapping and Exploration are also “collections of algorithms”**
 - We will focus on “Occupancy Grid” algorithms

What is an Occupancy Grid?

- A way of representing a map as a gridded world where each cell is either “occupied” or “empty” or “unknown”.

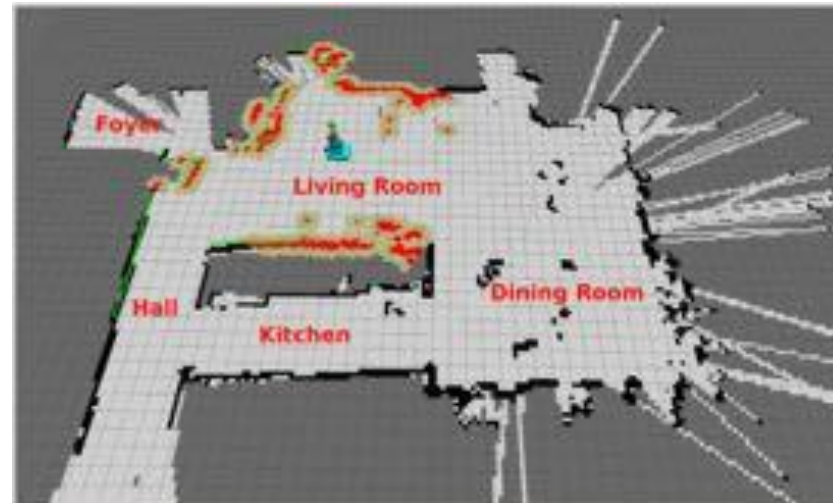
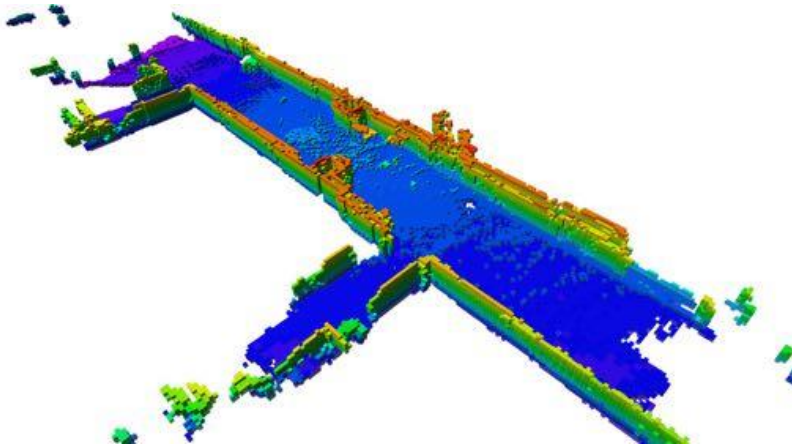
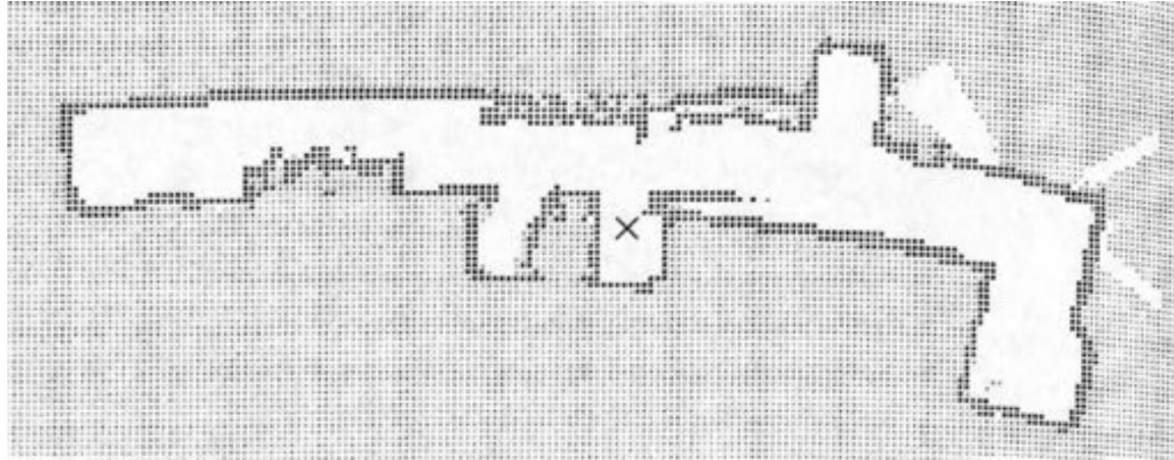


Your World



Grid generated by a Robot => boundary shape

Examples



What is a Sensor Model?

- **Constructing a Sensor Model**
 - A sensor measures *raw values* in an environment
 - You have to map that into a Grid Cell Value.
 - Robots can have very different sensors and configurations
 - Examples:
LIDAR/Depth Camera
Vs. a 360 degree vision/ranging system

Constructing a Sensor Model

- **Example: Depth Sensor Model**

R = maximum range, B = maximum angle

Let say the sensor at point p returns **distance** = " r "

Region 1 ($\text{dist} < r$, grid cell probably empty)

Region 2 ($\text{dist} = r$, grid cell probably obstacle)

Region 3 ($\text{dist} > r$, grid cell unknown/obscured)

- **Simplest Sensor Model**

Where I stand is Empty (white)

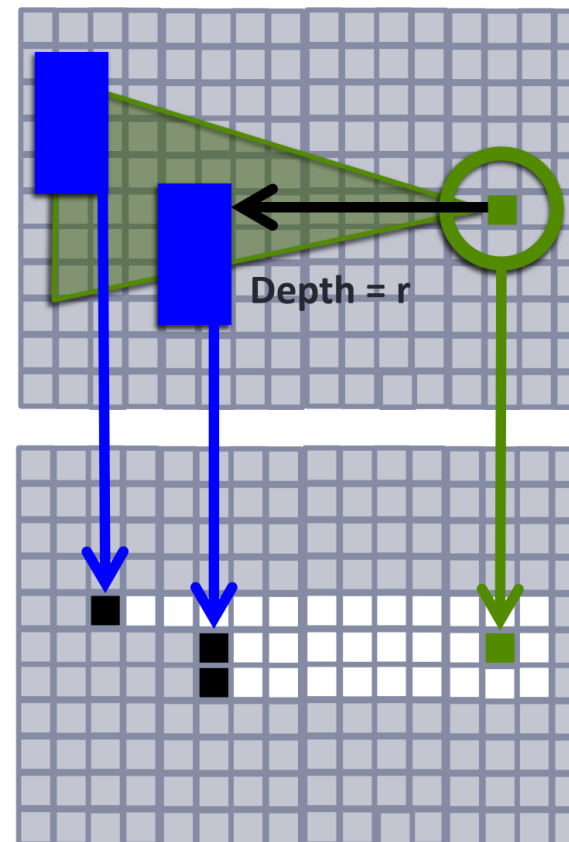
- **A Better Model**

Set Region 1 cells as Empty (white)

Set Region 2 cells as Occupied (black).

Pick a max range/angle where data is reliable

Rest is still Unknown (gray)



A Simple OG Mapping Algorithm

1. Initialize a Grid

- Set all locations as “unknown”, pick a start location and orientation

2. Update the Grid

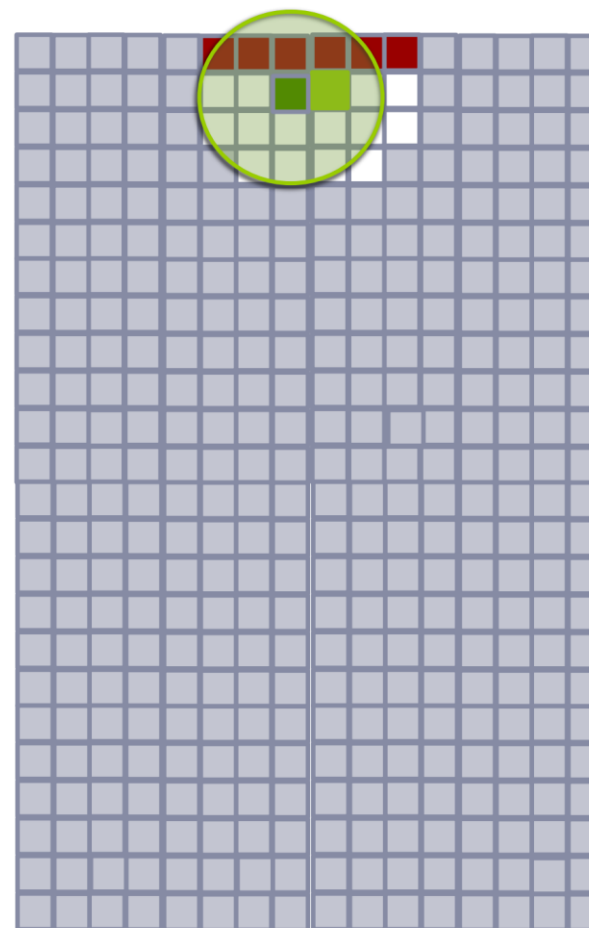
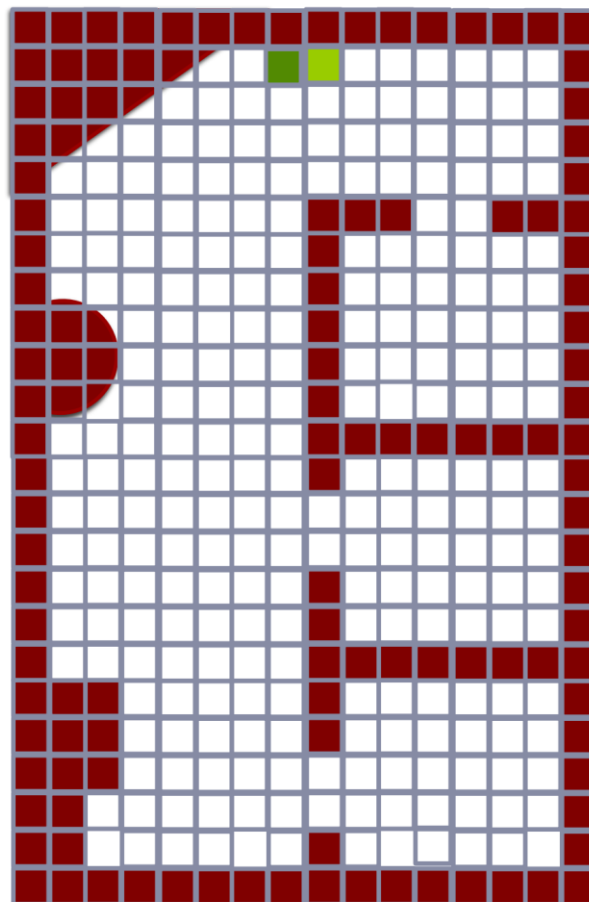
- *Mark your current grid position as “empty”*
- Using your better sensor model,
- *Mark all visible grid locations as “empty” or “occupied”*

3. Pick a Next Move

- Look at neighboring grid positions in your map
- Pick a neighboring grid location that is empty (randomly)
- Move to it and update your current position in the Grid

4. Loop forever

- Keep moving and updating the grid (unless you are “done”)



Exploration

- **Basic Concept in Robotics: Navigating a GRID Graph is different**
 - DFS works, but will still make a robot retrace steps
 - **Better choice: Frontier Based Exploration**

Exploration in Grid Worlds

- **Frontier Based Exploration**

- A common technique for building maps

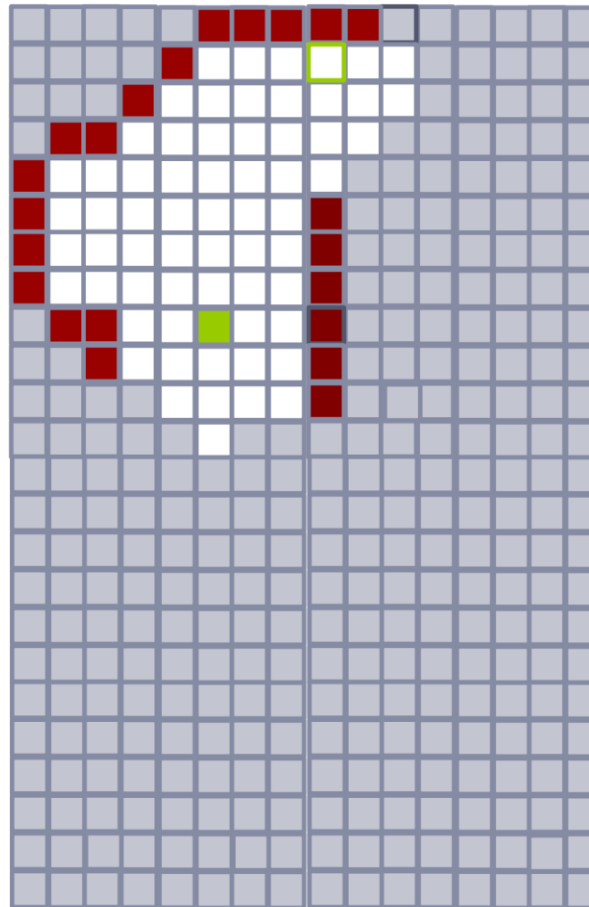
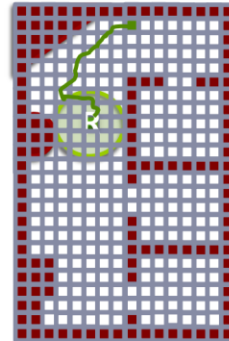
- **Key Idea:**

- Identify the “frontiers” between known and unknown
Frontier cell = a unknown cell with at least one empty cell
- Pick a frontier cell (e.g. the closest)
Plan a path to go explore it.

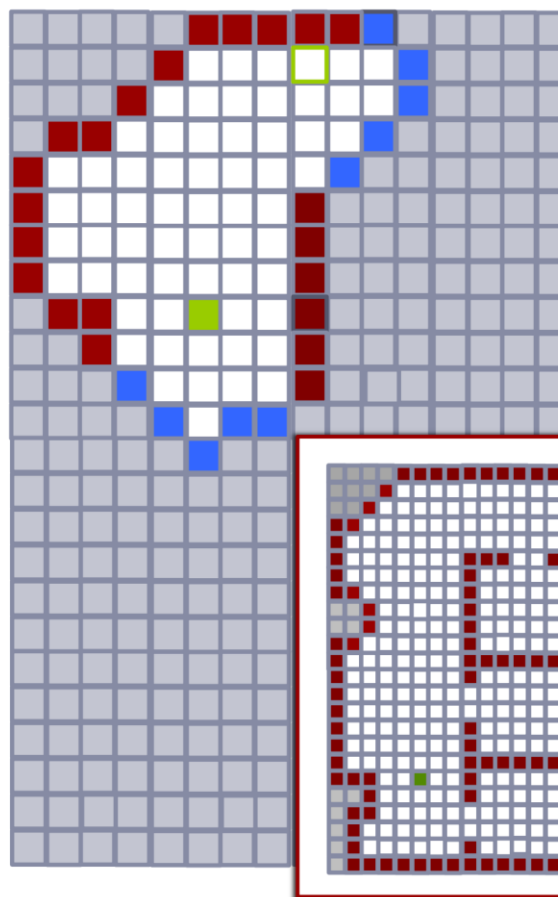
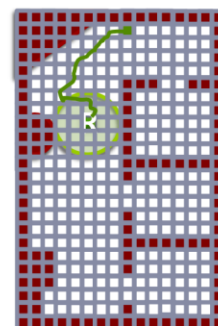
- **Done Condition:**

No more frontier nodes left => your map is Complete!

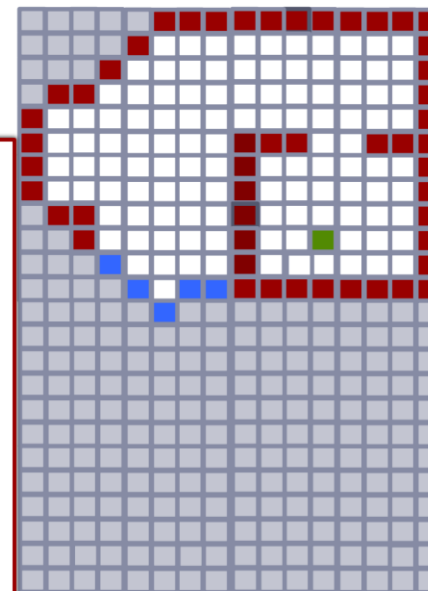
If finite world, then any algorithm that systematically explores frontier nodes is guaranteed to cover the whole world.



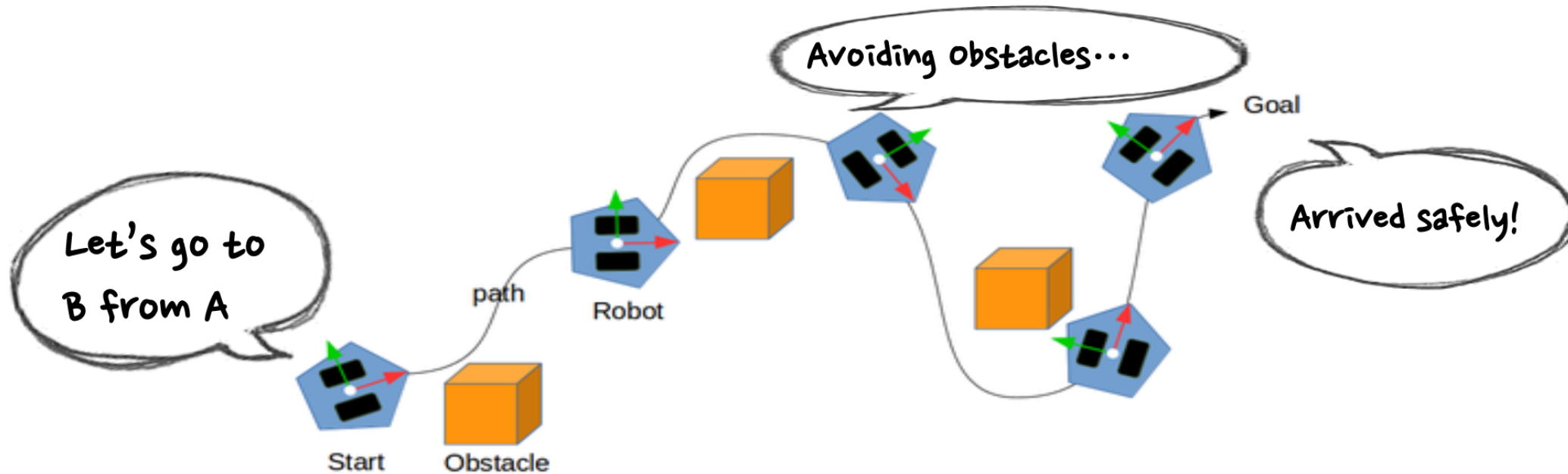
A **Frontier Node** is a
Gray node (Unknown)
next to a
White node (Empty)



A **Frontier Node** is a
Gray node (Unknown)
next to a
White node (Empty)



Summary



- ① **Position**: Measuring/estimating the robot's position
- ② **Sensing**: Measuring obstacles such as walls and objects
- ③ **Map**: Maps with road and obstacle information
- ④ **Path**: Calculate optimal path to the destination and follow the path

Summary

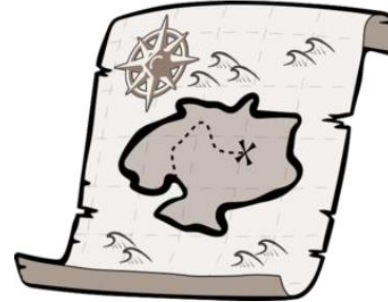
① **Position**



② **Sensing**



③ **Map**



④ **Path**



Position+Sensing → **Map**

SLAM

Simultaneous Localization And Mapping

Position+Sensing+Map → **Path**

Navigation