

$$\begin{array}{r}
 c_4 \quad c_3 \quad c_2 \quad c_1 \quad c_0 \\
 0000 \\
 + 0110 \\
 \hline
 1000
 \end{array}$$

OV

$$\begin{array}{r}
 c_4 \quad c_3 \quad c_2 \quad c_1 \quad c_0 \\
 1101 \\
 + 1010 \\
 \hline
 0111
 \end{array}$$

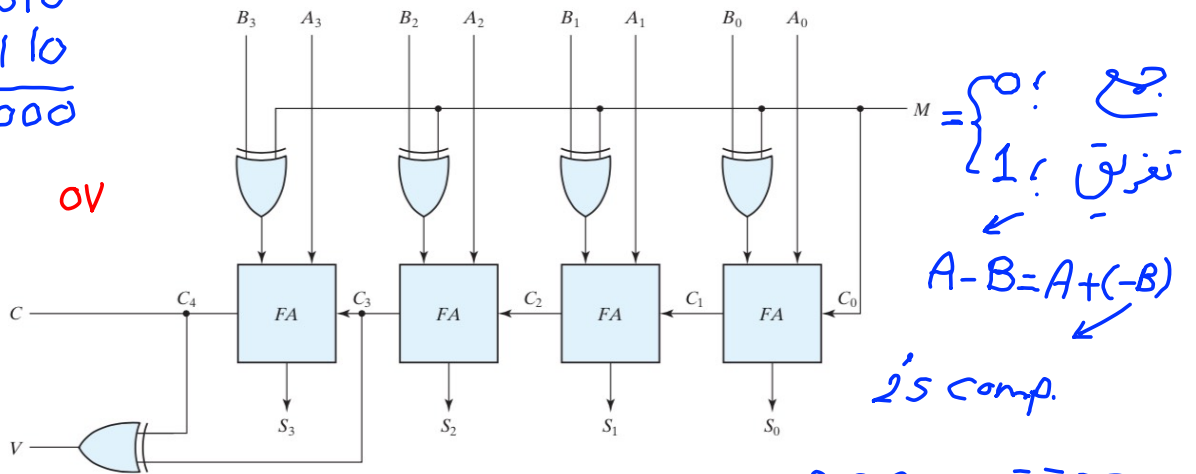


FIGURE 4.13

Four-bit adder-subtractor (with overflow detection)

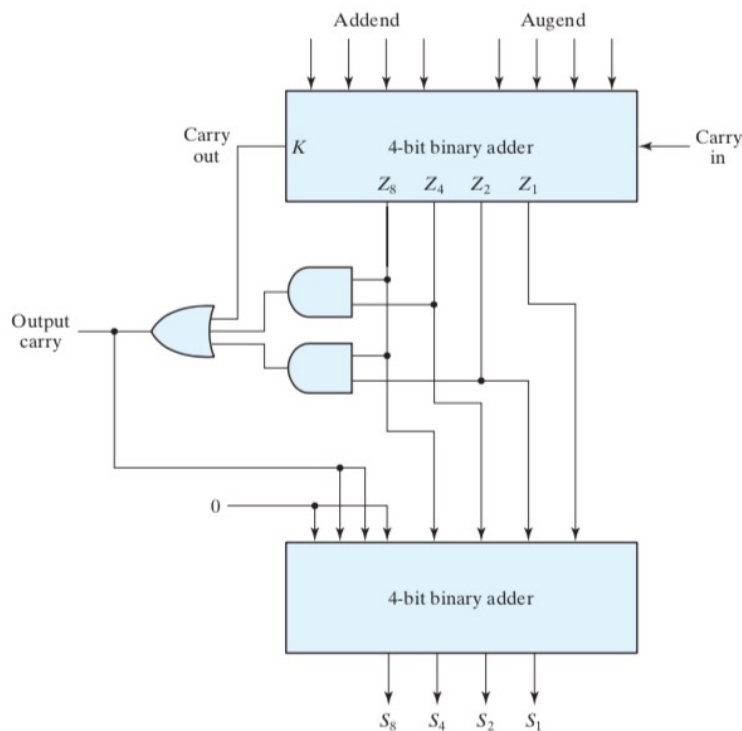
$$B_3 B_2 B_1 B_0 \rightarrow \bar{B}_3 \bar{B}_2 \bar{B}_1 \bar{B}_0 + 1$$

$$V = \bar{A}_3 \bar{B}_3 S_3 + A_3 B_3 \bar{S}_3$$

## BCD Adder

Binary Sum					BCD Sum					Decimal
K	Z <sub>8</sub>	Z <sub>4</sub>	Z <sub>2</sub>	Z <sub>1</sub>	C	S <sub>8</sub>	S <sub>4</sub>	S <sub>2</sub>	S <sub>1</sub>	
0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	2
0	0	0	1	1	0	0	0	1	1	3
0	0	1	0	0	0	0	1	0	0	4
0	0	1	0	1	0	0	1	0	1	5
0	0	1	1	0	0	0	1	1	0	6
0	0	1	1	1	0	0	1	1	1	7
0	1	0	0	0	0	1	0	0	0	8
0	1	0	0	1	0	1	0	0	1	9
0	1	0	1	0	1	0	0	0	0	10
0	1	0	1	1	1	0	0	0	1	11
0	1	1	0	0	1	0	0	1	0	12
0	1	1	0	1	1	0	0	1	1	13
0	1	1	1	0	1	0	1	0	0	14
0	1	1	1	1	1	0	1	0	1	15
1	0	0	0	0	1	0	1	1	0	16
1	0	0	0	1	1	0	1	1	1	17
1	0	0	1	0	1	1	0	0	0	18
1	0	0	1	1	1	1	0	0	1	19

$$C = K + Z_8 Z_4 + Z_8 Z_2$$



(comparator)

## مقایسه کنند

$a \rightarrow D \rightarrow G(a > b)$

مقایسه دو بیت  $a$  و  $b$

$a \rightarrow b \rightarrow L \ (a < b)$



$a \equiv b \iff [a=b]$

$$E = G + L$$

A hand-drawn diagram of a NAND gate. It has two input lines on the left labeled 'G' and 'L', and one output line on the right labeled 'E'. The gate symbol is a semi-circle with a small circle at its tip.

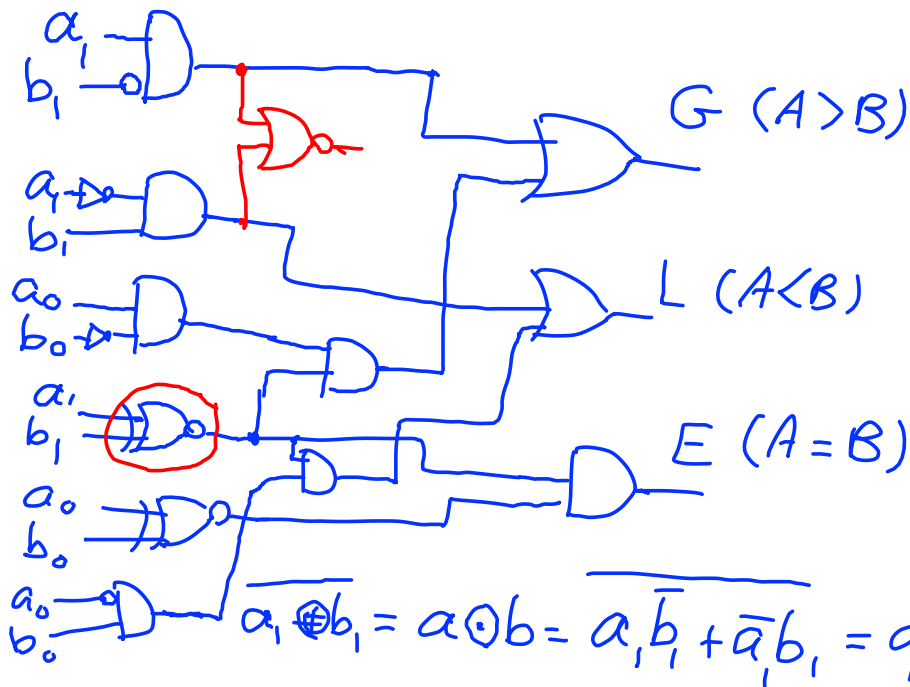
$$A = a, a_0$$

1000

0111

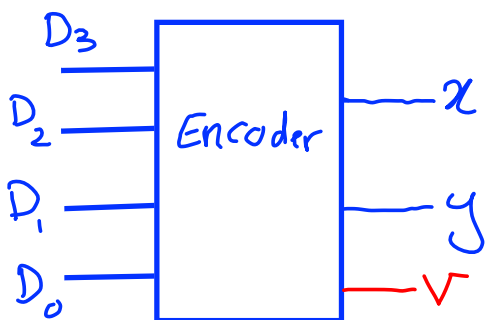
$$B = b, b_0$$

مقایسه کننده دویستی



Encoder (کدگذار)

## Decoder (دکڑا)



$$X = D_3 + D_2$$

$$y = D_3 + D_1$$

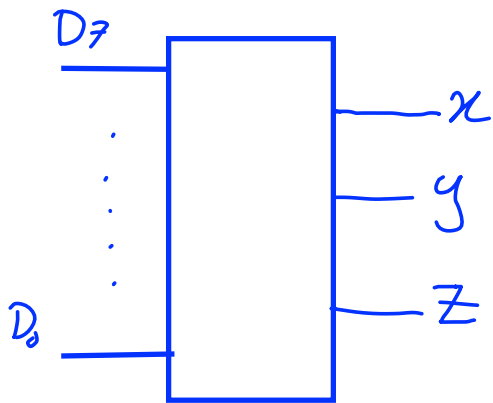
$$V = D_3 + D_2 + D_1 + D_0$$

$D_3 D_2 D_1 D_0$	$x$	$y$	$V$
1 0 0 0	1	1	1
0 1 0 0	1	0	1
0 0 1 0	0	1	1
0 0 0 1	0	0	1
0 0 0 0	X	X	0

## 8- Input encoder

۱ حالت بجاز (فقط یک ورودی فعال باشد)

۲۴۸ حالت غیر بجاز



$$x = D_7 + D_6 + D_5 + D_4$$

$$y = D_7 + D_6 + D_3 + D_2$$

$$z = D_7 + D_5 + D_3 + D_1$$

x	y	z
0	0	0

111

$$D_6, D_1 \quad x=1 \quad y=1 \quad z=1 \quad 111$$

$$D_6, D_2 \quad x=1 \quad y=1 \quad z=0 \quad 110$$

Priority Encoder (کدگذار اولویت دار)

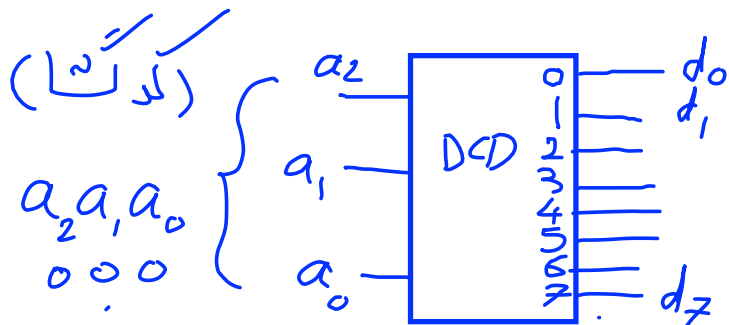
$$x = D_7 + D_6 + D_5 + D_4$$

$$y = D_7 + D_6 + D_3 \cdot (\bar{D}_5 \cdot \bar{D}_4) + D_2 \cdot (\bar{D}_5 \cdot \bar{D}_4)$$

$$z = D_7 + D_5 \cdot \bar{D}_6 + D_3 \cdot (\bar{D}_6 \cdot \bar{D}_4) + D_1 \cdot (\bar{D}_6 \cdot \bar{D}_4 \cdot \bar{D}_2)$$

$$V = D_7 + \dots + D_0$$

Decoder



فقط یک خروجی فعال (=1) می شود که متناظر با کد ورودی است

n ورودی،  $2^n$  خروجی

active high

2-to-4 decoder

$a_1 a_0$	$D_0$	$D_1$	$D_2$	$D_3$
00	1	0	0	0
01	0	1	0	0
10	0	0	1	0
11	0	0	0	1

