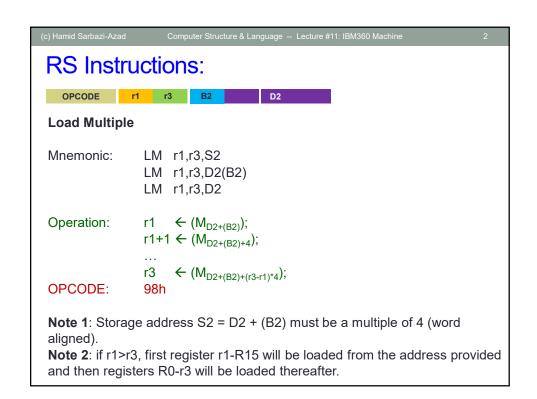
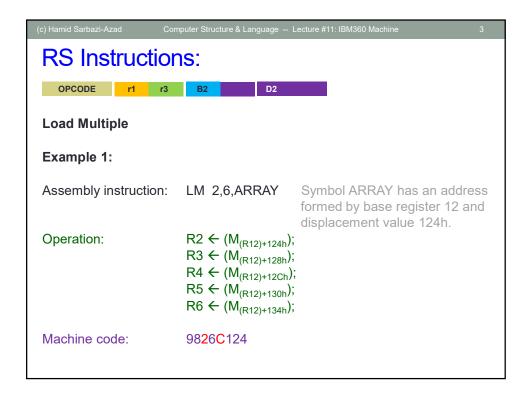
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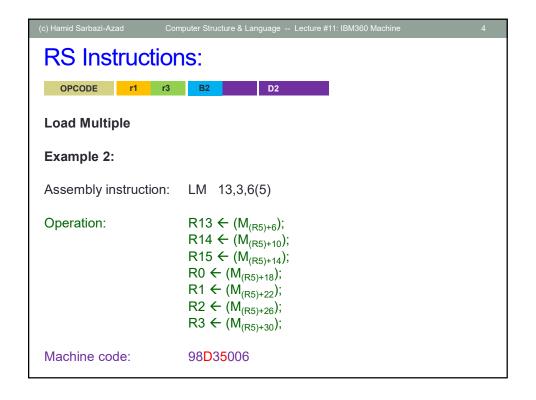
Hamid Sarbazi-Azad

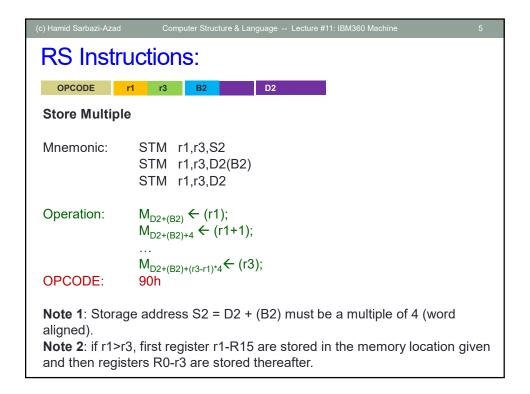
Department of Computer Engineering Sharif University of Technology (SUT) Tehran, Iran

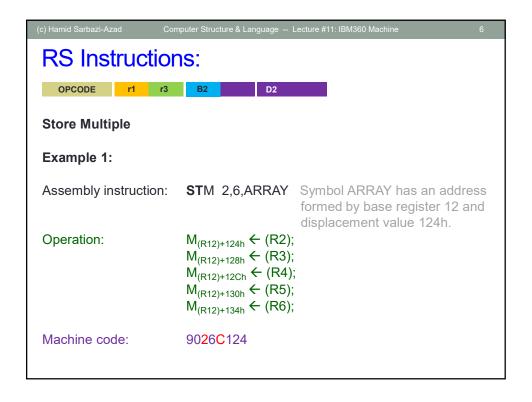


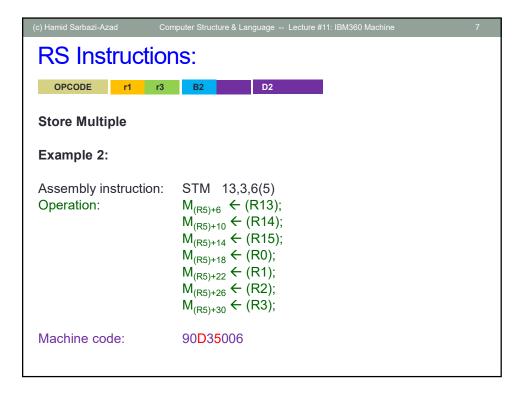


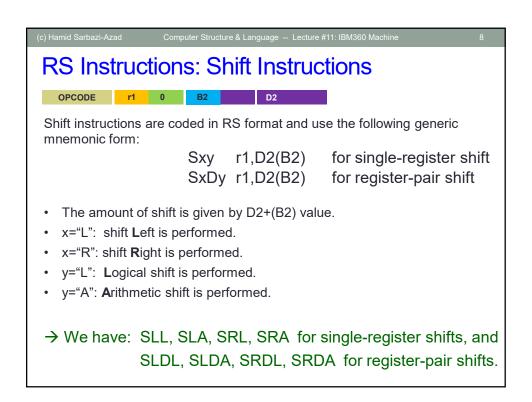


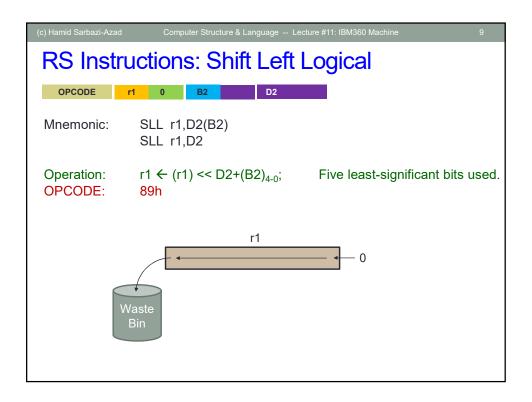


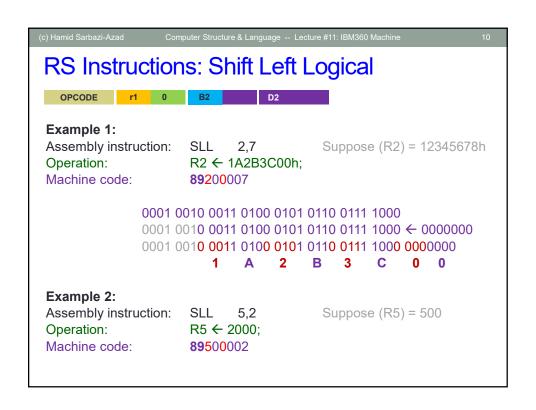


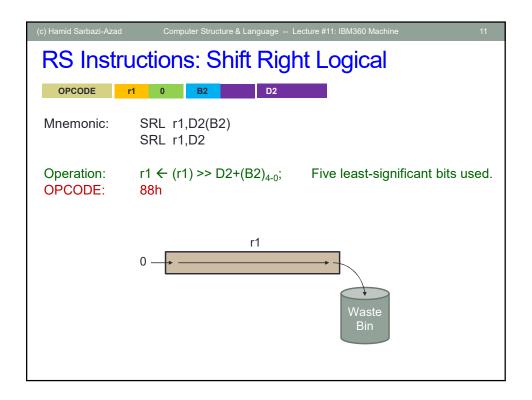


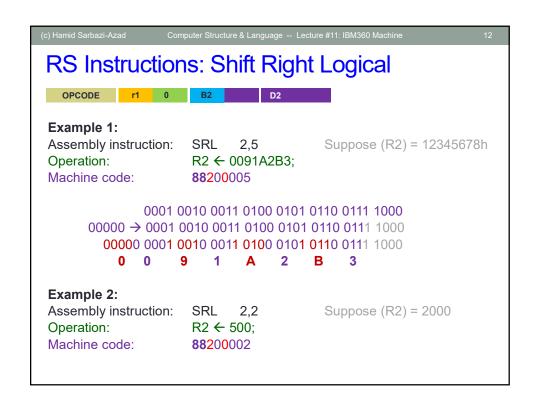


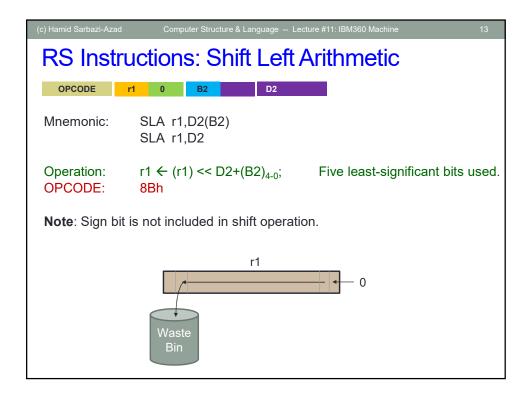


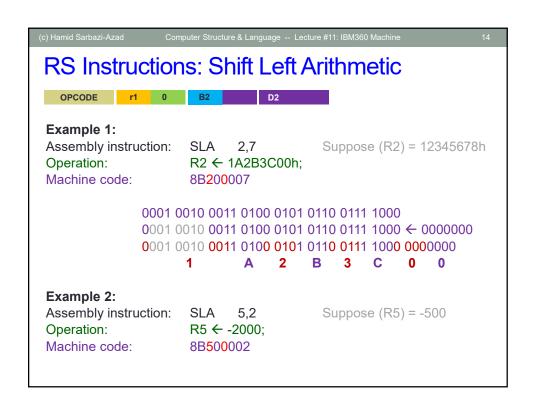


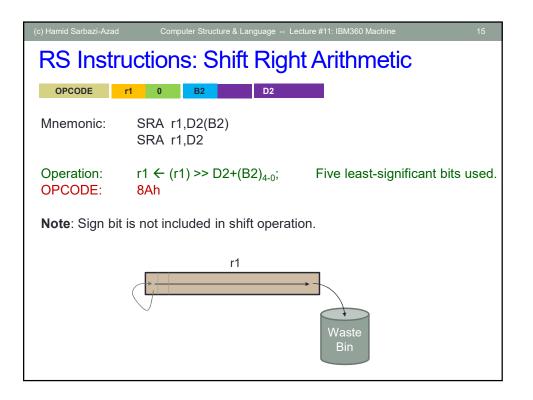


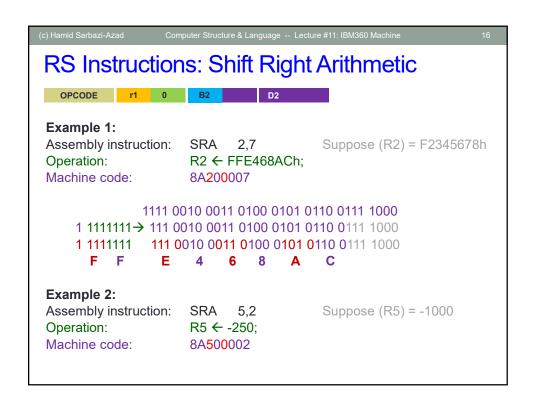


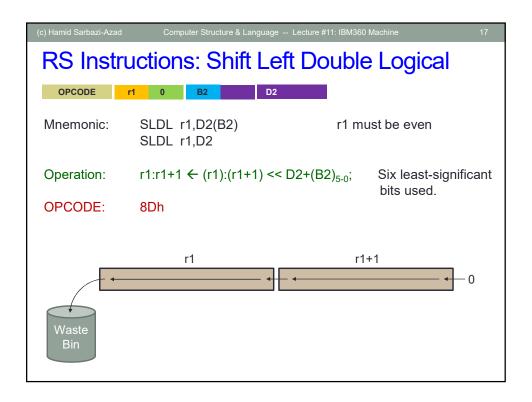


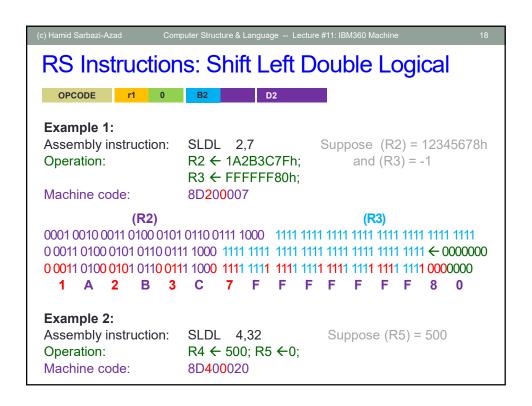


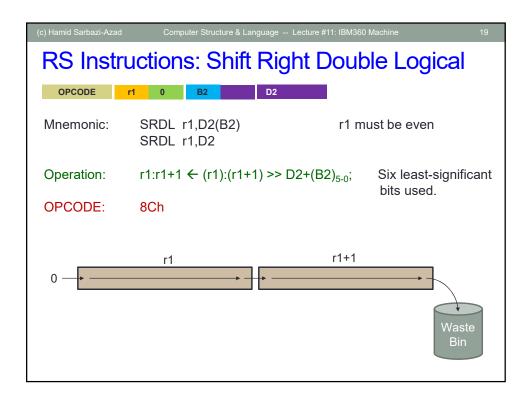


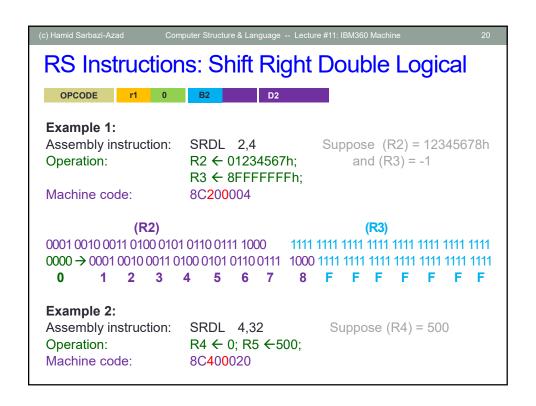


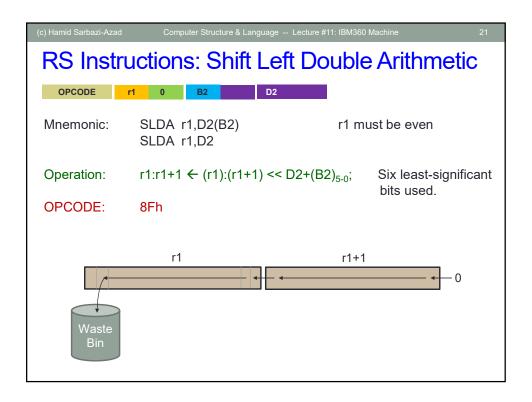


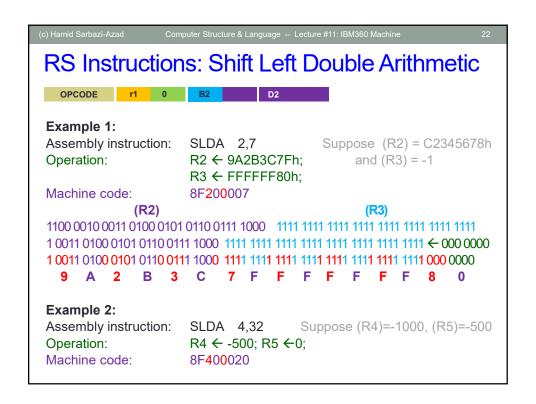


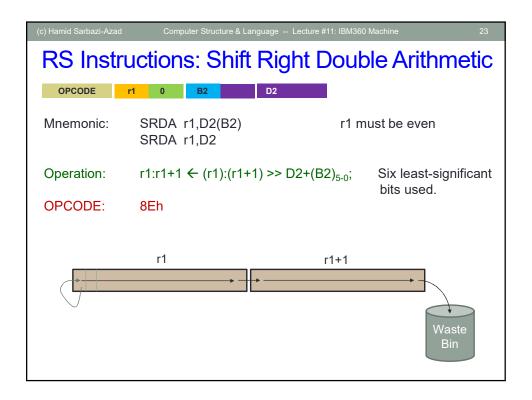


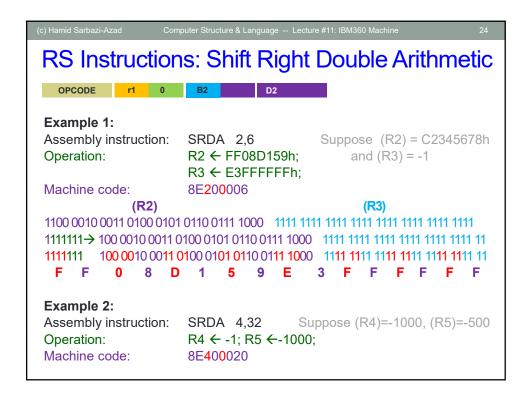


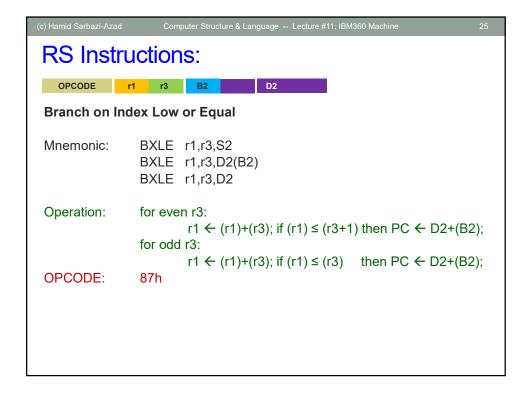


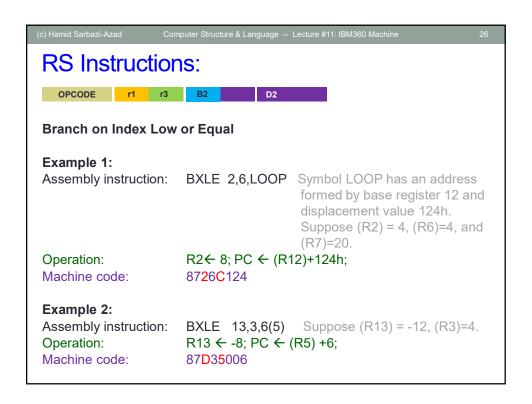


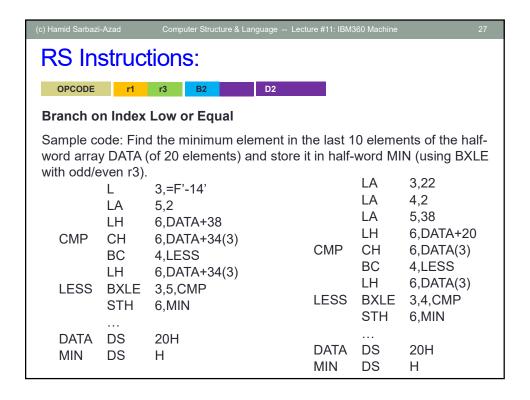


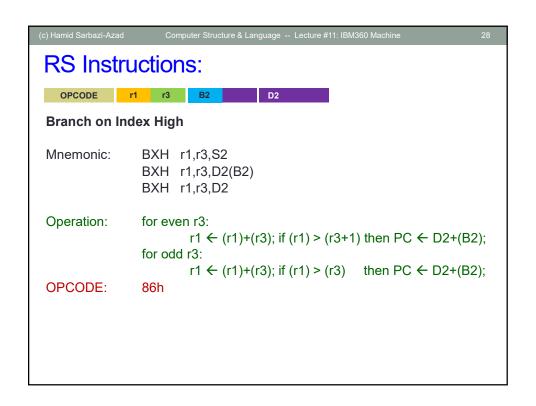


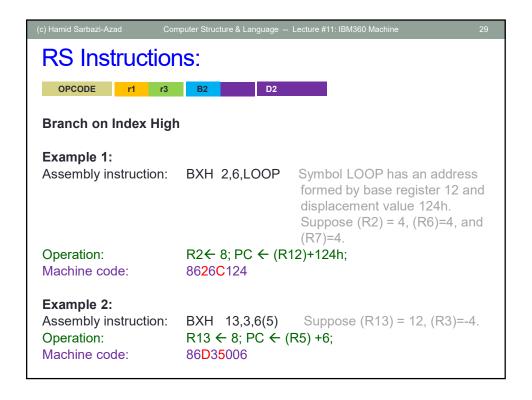


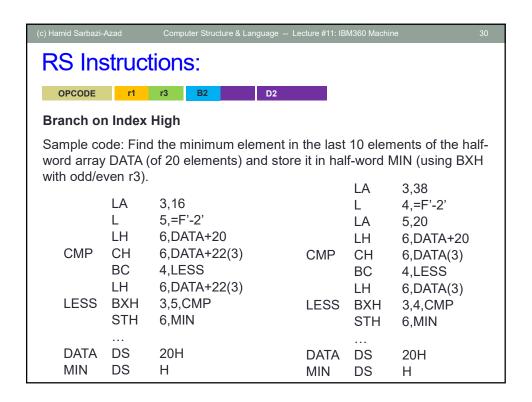












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3.

Binary Multiplication

Recall the pen and paper technique we use to multiply n-bit number A and m-bit number B to generate (m+n)-bit number $P = A \times B$.

$$A = a_{n-1} \cdots a_{1} a_{0}$$

$$B = b_{m-1} \cdots b_{1} b_{0}$$

$$M_{0} = a_{n-1} b_{0} \cdots a_{1} b_{0} a_{0} b_{0}$$

$$M_{1} = a_{n-1} b_{1} \cdots a_{1} b_{1} a_{0} b_{1}$$

$$\vdots$$

$$M_{m-1} = a_{n-1} b_{m-1} \cdots a_{1} b_{m-1} a_{0} b_{m-1}$$

$$p_{m+n-1} p_{m+n-2} \cdots p_{2} p_{1} p_{0}$$

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Binary Multiplication

Multiplication can be done in a serial manner.

Consider n-bit numbers $A(a_{n-1}a_{n-2}...a_0)$ and $B(b_{n-1}b_{n-2}...b_0)$.

We can write:

$$A \times B = (A \times 2^{n-1} \times b_{n-1}) + (A \times 2^{n-2} \times b_{n-2}) + \dots + (A \times 2^{1} \times b_{1}) + (A \times b_{0})$$

$$= [A \ll (n-1)] \times b_{n-1} + [A \ll (n-2)] \times b_{n-2} + \dots + [A \ll 1] \times b_{1} + [A \ll 0] \times b_{0}$$

$$= \sum_{i=0..n-1} [A \ll i] \times b_{i}$$

Shifting A for n-1 bits to the left we need a 2n-bit register to keep the partial products.

Alternatively, we can shift the accumulator, that accumulates the partial products, to the right. → a tricky circuit to save hardware ©

