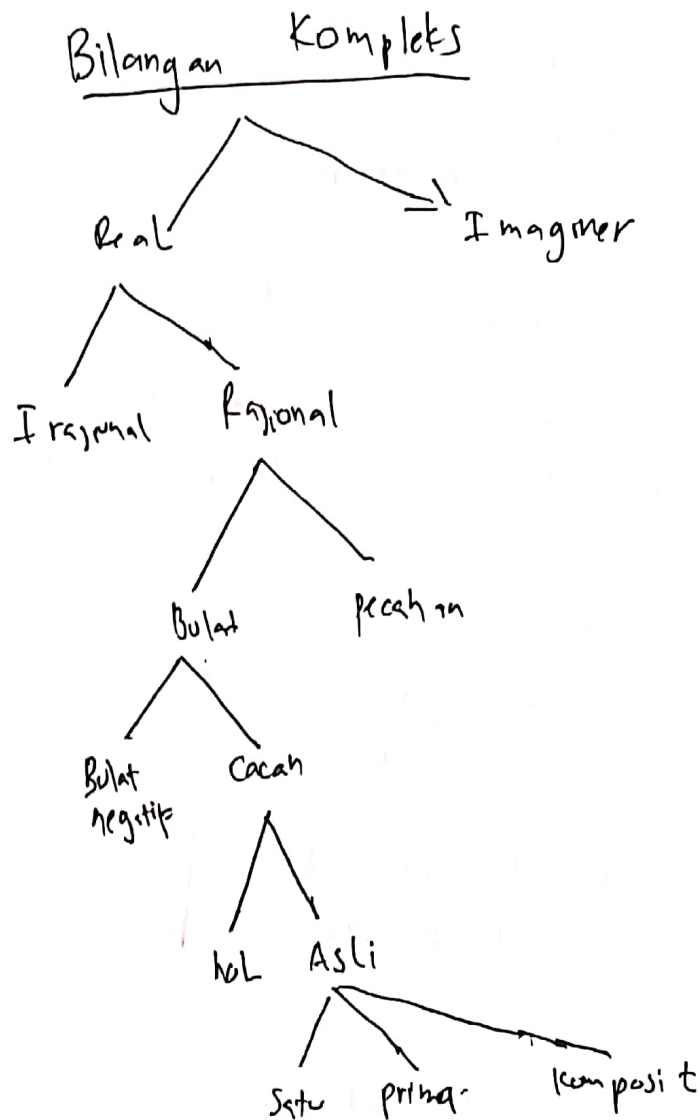


# Complex Variables and Applications



Bilangan kompleks

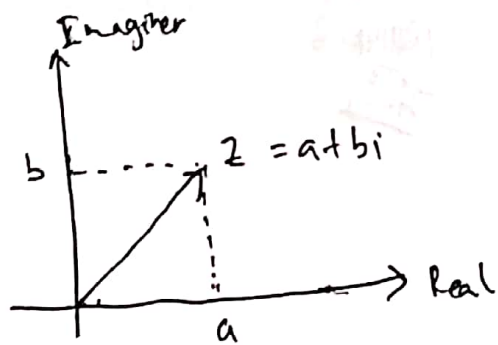
$$\mathbb{C} = \{a + bi \mid a, b \in \mathbb{R}\}$$

dan didefinisikan  $\sqrt{-1} = i$ ,  $i^2 = -1$

$$3 \in \mathbb{C} \rightarrow 3 = 3 + 0i$$

$$0 \in \mathbb{C} \rightarrow 0 = 0 + 0i$$

$$z = a + bi \in \mathbb{C} \begin{cases} \text{Re}(z) = a \\ \text{Im}(z) = b \end{cases}$$

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$$z = a + bi$$

$$\hookrightarrow z = (a, b)$$

$\nwarrow$  komp. real  
 $\nearrow$  komp. imaginer

### Operasi Bilangan kompleks

Misal  $z_1 = a + bi \in \mathbb{C} \xrightarrow{\text{dapat ditulis}} z_1 = (a, b)$

$z_2 = c + di \in \mathbb{C} \xrightarrow{\text{dapat ditulis}} z_2 = (c, d)$

$\rightarrow$  disebut pasangan terurut

$\rightarrow$  disebut pasangan terurut

#### (1) Penjumlahan / pengurangan

$$\begin{aligned} z_1 + z_2 &= (a + bi) + (c + di) \\ &= (a + c) + (b + d)i \end{aligned}$$

$$\begin{aligned} z_1 - z_2 &= (a + bi) - (c + di) \\ &= (a - c) + (b - d)i \end{aligned}$$

saat dipandang  
sebagai  
pasangan terurut

$$\begin{aligned} z_1 + z_2 &= (a, b) + (c, d) \\ &= (a + c, b + d) \end{aligned}$$

$$\begin{aligned} z_1 - z_2 &= (a, b) - (c, d) \\ &= (a - c, b - d) \end{aligned}$$

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$$z_1 = 3 + 2i \quad \left. \begin{array}{l} z_1 + z_2 = 8 + 9i \\ z_2 = 5 + 7i \end{array} \right\} z_1 - z_2 = -2 - 5i$$

$$z_2 = 5 + 7i$$

#### (2) Perkalian

$$\begin{aligned} z_1 z_2 &= (a + bi) \cdot (c + di) \\ &= ac + (ad)i + (bc)i - bd \\ &= (ac - bd) + (ad + bc)i \end{aligned}$$

$$\begin{aligned} z_1 z_2 &= (a, b) (c, d) \\ &= (ac - bd, ad + bc) \end{aligned}$$

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Makassar, 11 Februari 2020

~~Manu~~

3. Pembagian

$$z_1 = a + bi$$

$$z_2 = c + di \neq 0$$

$$\frac{z_1}{z_2} = \frac{a+bi}{c+di} \times \frac{c-di}{c-di}$$

$$= \frac{ac - (ad)i + (bc)i + bd}{c^2 + d^2}$$

$$= \frac{(ac+bd)}{c^2+d^2} + \frac{(bc-ad)i}{c^2+d^2}$$

$$= \left( \frac{ac+bd}{c^2+d^2} \right) + \left( \frac{bc-ad}{c^2+d^2} \right) i$$

Konjugat / Sekawan

konjugat bilangan kompleks  $z = a + bi$  ditulis  $\overline{z} = a - bi$

$$z = a + bi$$

$$\overline{z} = a - bi$$

