CS 61A Fall 2014

Structure and Interpretation of Computer Programs

FINAL EXAM

INSTRUCTIONS

- You have 3 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written $8.5" \times 11"$ crib sheet of your own creation and the 3 official 61A midterm study guides attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

Last name	
First name	
SID	
Login	
TA & section time	
Name of the person to your left	
Name of the person to your right	
All the work on this exam is my own. (please sign)	

For staff use only

Q. 1	Q. 2	Q. 3	Q. 4	Q. 5	Q. 6	Total	
/14	/16	/12	/12	/18	/8	/80	

1. (14 points) Representing Scheme Lists

For each row below, write the output displayed by the interactive Python interpreter when the expression is evaluated. Expressions are evaluated in order, and expressions may affect later expressions.

Whenever the interpreter would report an error, write ERROR. You *should* include any lines displayed before an error. *Reminder*: The interactive interpreter displays the **repr** string of the value of a successfully evaluated expression, unless it is **None**.

The Pair class from Project 4 is described on your final study guide. Recall that its <code>__str__</code> method returns a Scheme expression, and its <code>__repr__</code> method returns a Python expression. The full implementation of Pair and nil appear at the end of the exam as an appendix. Assume that you have started Python 3, loaded Pair and nil from <code>scheme_reader.py</code>, then executed the following:

```
blue = Pair(3, Pair(4, nil))
gold = Pair(Pair(6, 7), Pair(8, 9))

def process(s):
    cal = s
    while isinstance(cal, Pair):
        cal.bear = s
        cal = cal.second
    if cal is s:
        return cal
    else:
        return Pair(cal, Pair(s.first, process(s.second)))

def display(f, s):
    if isinstance(s, Pair):
        print(s.first, f(f, s.second))

y = lambda f: lambda x: f(f, x)
```

Expression	Output	Expression	Output
Pair(1, nil)	Pair(1, nil)	process(blue.second)	
<pre>print(Pair(1, nil))</pre>	(1)		
1/0	Error		
<pre>print(print(3), 1/0)</pre>		<pre>print(process(gold))</pre>	
<pre>print(Pair(2, blue))</pre>		gold.second.bear.first	
print(gold)		y(display)(gold)	

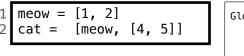
2. (16 points) Environments

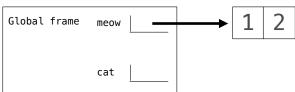
- (a) (8 pt) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You may not need to use all of the spaces or frames. A complete answer will:
 - Add all missing names and parent annotations to all local frames.
 - Add all missing values created during execution.
 - Show the return value for each local frame.

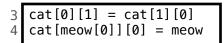
<pre>def tattoo(heart): def mom(): nonlocal mom</pre>	Global frame	tattoo	→ func	tattoo(heart)	[parent=Global]
<pre>mom = lambda: heart(2) + 1 return 3 return mom() + mom() + 4</pre>	f1:	_ [parent=]			
tattoo(lambda ink: ink + 0.5)					
		Return Value			
	f2:	_ [parent=]			
		Return Value			
		neturn vatae			
	f3:	_ [parent=]			
		Return Value			
	f4.	_ [parent=]			
	17.				
		Poturn Volue			
		Return Value			

(b) (6 pt) For the six-line program below, fill in the three environment diagrams that would result after executing each pair of lines in order. You must use box-and-pointer diagrams to represent list values. You do not need to write the word "list" or write index numbers.

Important: All six lines of code are executed in order! Line 3 is executed after line 2 and line 5 after line 4.

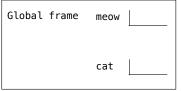








```
5 meow[0] = [cat.pop(0)]
6 cat.extend(cat[0][1:])
```



(c) (2 pt) Circle the value, True or False, of each expression below when evaluated in the environment created by executing all six lines above. If you leave this question blank, you will receive 1 point.

Circle True or False: meow is cat[0]

Circle True or False: meow[0][0] is cat[0][0]

3. (12 points) Expression Trees

Your partner has created an interpreter for a language that can add or multiply positive integers. Expressions are represented as instances of the Tree class and must have one of the following three forms:

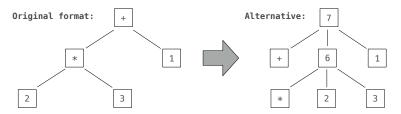
- (Primitive) A positive integer entry and no branches, representing an integer
- (Combination) The entry '+', representing the sum of the values of its branches
- (Combination) The entry '*', representing the product of the values of its branches

The Tree class is on the Midterm 2 Study Guide. The sum of no values is 0. The product of no values is 1.

(a) (6 pt) Unfortunately, multiplication in Python is broken on your computer. Implement eval_with_add, which evaluates an expression without using multiplication. You may fill the blanks with names or call expressions, but the only way you are allowed to combine two numbers is using addition.

```
def eval_with_add(t):
   """Evaluate an expression tree of st and + using only addition.
  >>> plus = Tree('+', [Tree(2), Tree(3)])
  >>> eval_with_add(plus)
  >>> times = Tree('*', [Tree(2), Tree(3)])
  >>> eval_with_add(times)
  >>> deep = Tree('*', [Tree(2), plus, times])
  >>> eval_with_add(deep)
  60
  >>> eval_with_add(Tree('*'))
  1
  if t.entry == '+':
     return sum(_____)
  elif t.entry == '*':
     total = _____
     for b in t.branches:
        total, term = 0, ______
        for _____:
           total = total + term
     return total
  else:
     return t.entry
```

(b) (6 pt) A TA suggests an alternative representation of an expression, in which the entry is the value of the expression. For combinations, the operator appears in the left-most (index 0) branch as a leaf.



Implement transform, which takes an expression and mutates all combinations so that their entries are values and their first branches are operators. In addition, transform should return the value of its argument. You may use the calc_apply function defined below.

```
def calc_apply(operator, args):
   if operator == '+':
      return sum(args)
   elif operator == '*':
      return product(args)
def product(vals):
   total = 1
   for v in vals:
      total *= v
   return total
def transform(t):
   """Transform expression tree t to have value entries and operator leaves.
   >>> seven = Tree('+', [Tree('*', [Tree(2), Tree(3)]), Tree(1)])
   >>> transform(seven)
   7
   >>> seven
   Tree(7, [Tree(+), Tree(6, [Tree(*), Tree(2), Tree(3)]), Tree(1)])
   if t.branches:
      args = []
      for b in t.branches:
         args.append(_____)
      t.branches = _______
      t.entry = _____
```

return _____

4. (12 points) Lazy Sunday

(a) (4 pt) A flat-map operation maps a function over a sequence and flattens the result. Implement the flat_map method of the FlatMapper class. You may use at most 3 lines of code, indented however you choose.

class FlatMapper:

"""A FlatMapper takes a function fn that returns an iterable value. The flat_map method takes an iterable s and returns a generator over all values in the iterables returned by calling fn on each element of s.

```
>>> stutter = lambda x: [x, x]
>>> m = FlatMapper(stutter)
>>> g = m.flat_map((2, 3, 4, 5))
>>> type(g)
<class 'generator'>
>>> list(g)
[2, 2, 3, 3, 4, 4, 5, 5]
"""

def __init__(self, fn):
    self.fn = fn

def flat_map(self, s):
```

(b) (2 pt) Define cycle that returns a Stream repeating the digits 1, 3, 0, 2, and 4. Hint: (3+2)%5 equals 0. def cycle(start=1):

"""Return a stream repeating 1, 3, 0, 2, 4 forever.

```
>>> first_k(cycle(), 12)  # Return the first 12 elements as a list [1, 3, 0, 2, 4, 1, 3, 0, 2, 4, 1, 3]
```

def compute_rest():

return _____

return Stream(______)

(c) (4 pt) Implement the Scheme procedure directions, which takes a number n and a symbol sym that is bound to a nested list of numbers. It returns a Scheme expression that evaluates to n by repeatedly applying car and cdr to the nested list. Assume that n appears exactly once in the nested list bound to sym.

Hint: The implementation searches for the number n in the nested list s that is bound to sym. The returned expression is built during the search. See the tests at the bottom of the page for usage examples.

```
(define (directions n sym)
   (define (search s exp)
      ; Search an expression s for n and return an expression based on exp.
      (cond ((number? s) _____)
           ((null? s) nil)
           (else (search-list s exp))))
   (define (search-list s exp)
      ; Search a nested list s for n and return an expression based on exp.
      (let ((first _____)
           (rest
                _____))
          (if (null? first) rest first)))
   (search (eval sym) sym))
(define a '(1 (2 3) ((4))))
(directions 1 'a)
; expect (car a)
(directions 2 'a)
; expect (car (cdr a)))
(define b '((3 4) 5))
(directions 4 'b)
; expect (car (cdr (car b)))
```

(d) (2 pt) What expression will (directions 4 'a) evaluate to?

5. (18 points) Basis Loaded

Ben Bitdiddle notices that any positive integer can be expressed as a sum of powers of 2. Some examples:

```
11 = 8 + 2 + 1
23 = 16 + 4 + 2 + 1
24 = 16 + 8
45 = 32 + 8 + 4 + 1
2014 = 1024 + 512 + 256 + 128 + 64 + 16 + 8 + 4 + 2
```

A basis is a linked list of decreasing integers (such as powers of 2) with the property that any positive integer n can be expressed as the sum of elements in the basis, starting with the largest element that is less than or equal to n.

(a) (4 pt) Implement sum_to, which takes a positive integer n and a linked list of decreasing integers basis. It returns a linked list of elements of the basis that sum to n, starting with the largest element of basis that is less than or equal to n. If no such sum exists, raise an ArithmeticError. Each number in basis can only be used once (or not at all). The Link class is described on your Midterm 2 Study Guide.

```
only be used once (or not at all). The Link class is described on your Midterm 2 Study Guide.
def sum_to(n, basis):
    """Return elements of linked list basis that sum to n.
    >>> twos = Link(32, Link(16, Link(8, Link(4, Link(2, Link(1))))))
    >>> sum_to(11, twos)
   Link(8, Link(2, Link(1)))
    >>> sum_to(23, twos)
   Link(16, Link(4, Link(2, Link(1))))
    >>> sum_to(24, twos)
   Link(16, Link(8))
   >>> sum_to(45, twos)
   Link(32, Link(8, Link(4, Link(1))))
       return Link.empty
    elif _____:
       raise ArithmeticError
    elif basis.first > n:
       return sum_to(n, basis.rest)
    else:
```

(b) (6 pt) Cross out as many lines as possible in the implementation of the FibLink class so that all doctests pass. A FibLink is a subclass of Link that contains decreasing Fibonacci numbers. The up_to method returns a FibLink instance whose first element is the largest Fibonacci number that is less than or equal to positive integer n.

```
class FibLink(Link):
    """Linked list of Fibonacci numbers.
    >>> ten = FibLink(2, FibLink(1)).up_to(10)
    >>> ten
    Link(8, Link(5, Link(3, Link(2, Link(1))))
    >>> ten.up_to(1)
   Link(1)
    >>> six, thirteen = ten.up_to(6), ten.up_to(13)
    Link(5, Link(3, Link(2, Link(1))))
    >>> thirteen
    Link(13, Link(8, Link(5, Link(3, Link(2, Link(1))))))
    successor = self.first + self.rest
    @property
    def successor():
    def successor(self):
        return first + rest.first
        return self.first + self.rest.first
    def up_to(n):
    def up_to(self, n):
        while self.first > n:
            self = self.rest.first
            self = rest
            self.first = self.rest.first
        if self.first == n:
            return self
        elif self.first > n:
            return self.up_to(n)
            return self.rest.up_to(n)
        elif self.successor > n:
        elif self.first < n:</pre>
            return self
        else:
            return FibLink(self.successor(self), self).up_to(n)
            return FibLink(self.successor, self).up_to(n)
            return FibLink(self.successor(self), self.rest).up_to(n)
            return FibLink(self.successor, self.rest).up_to(n)
```

(c) (2 pt) Circle the Θ expression below that describes the number of calls made to FibLink.up_to when evaluating FibLink(2, FibLink(1)).up_to(n). The constant ϕ is $\frac{1+\sqrt{5}}{2}=1.618...$

 $\Theta(1)$ $\Theta(\log_{\phi} n)$ $\Theta(n)$ $\Theta(n^2)$ $\Theta(\phi^n)$

(d) (2 pt) Alyssa P. Hacker remarks that Fibonacci numbers also form a basis. How many total calls to FibLink.up_to will be made while evaluating all the doctests of the fib_basis function below? Assume that sum_to and FibLink are implemented correctly. Write your answer in the box.

```
def fib_basis():
    """Fibonacci basis with caching.
    >>> r = fib_basis()
    >>> r(11)
    Link(8, Link(3))
    >>> r(23)
    Link(21, Link(2))
    >>> r(24)
    Link(21, Link(3))
    >>> r(45)
    Link(34, Link(8, Link(3)))
    fibs = FibLink(2, FibLink(1))
    def represent(n):
        nonlocal fibs
        fibs = fibs.up_to(n)
        return sum_to(n, fibs)
    return represent
```

(e) (4 pt) Implement fib_sums, a function that takes positive integer n and returns the number of ways that n can be expressed as a sum of unique Fibonacci numbers. Assume that FibLink is implemented correctly.

6. (8 points) Sequels

Assume that the following table of movie ratings has been created.

```
create table ratings as
                                                                Correct output
  select "The Matrix" as title,
                                      9 as rating union
                                                                 Judgment Day
  select "The Matrix Reloaded",
                                      7
                                                   union
                                                                  Terminator
  select "The Matrix Revolutions", 5
                                                   union
                                                                  The Matrix
  select "Toy Story",
                                                   union
                                                                  Toy Story
  select "Toy Story 2"
                                      8
                                                   union
                                                                  Toy Story 2
  select "Toy Story 3",
                                      9
                                                   union
                                                                  Toy Story 3
                                      8
  select "Terminator",
                                                   union
  select "Judgment Day",
                                      9
                                                   union
  select "Rise of the Machines",
                                      5;
```

The correct output table for both questions below happens to be the same. It appears above to the right for your reference. **Do not hard code your solution to work only with this table!** Your implementations should work correctly even if the contents of the ratings table were to change.

(a) (2 pt) Select the titles of all movies that have a rating greater than 7 in alphabetical order.

(b) (6 pt) Select the titles of all movies for which at least 2 other movies have the same rating. The results should appear in alphabetical order. Repeated results are acceptable. You may only use the SQL features introduced in this course.

with

```
groups(name, score, n) as (

select ______, ______ from ratings union

select _____, from groups, ratings

where ______
)

select title from ______

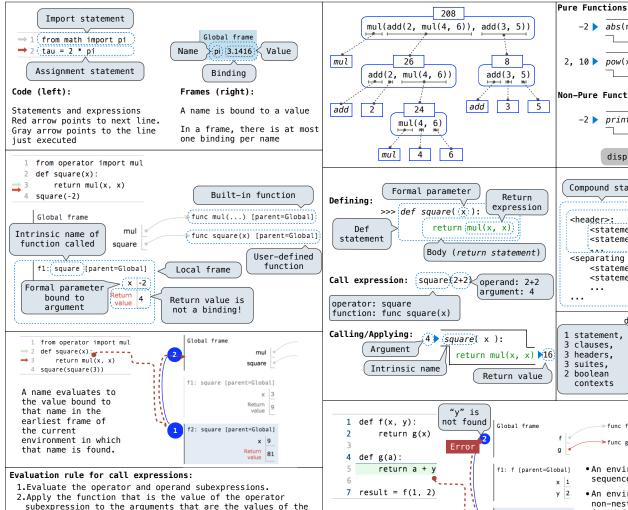
where ______

order by ______;
```

Appendix: Pair and nil Implementations

This page does not contain a question. These classes were originally defined in scheme_reader.py.

```
class Pair:
    """A pair has two instance attributes: first and second. For a Pair to be
    a well-formed list, second is either a well-formed list or nil. Some
    methods only apply to well-formed lists.
    >>> s = Pair(1, Pair(2, nil))
    >>> s
    Pair(1, Pair(2, nil))
    >>> print(s)
    (1 \ 2)
    def __init__(self, first, second):
        self.first = first
        self.second = second
    def __repr__(self):
        return "Pair({0}, {1})".format(repr(self.first), repr(self.second))
    def __str__(self):
        s = "(" + str(self.first)
        second = self.second
        while isinstance(second, Pair):
            s += " " + str(second.first)
            second = second.second
        if second is not nil:
            s += " . " + str(second)
        return s + ")"
class nil:
    """The empty list"""
    def __repr__(self):
        return "nil"
    def __str__(self):
        return "()"
    def __len__(self):
        return 0
    def __getitem__(self, k):
        if k < 0:
            raise IndexError("negative index into list")
        raise IndexError("list index out of bounds")
    def map(self, fn):
        return self
nil = nil() # Assignment hides the nil class; there is only one instance
```



2.Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

Applying user-defined functions:

- 1.Create a new local frame with the same parent as the function that was applied.
- 2. Bind the arguments to the function's formal parameter names in that frame.
- 3.Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

- 1.Create a new function value with the specified name, formal parameters, and function body.
 2.Its parent is the first frame of the current environment.
- 3.Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

1.Evaluate the expression(s) on the right of the equal sign. 2.Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

1.Evaluate the header's expression.

2.If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- 1.Evaluate the subexpression <left>
- 2.If the result is a true value v, then the expression evaluates to v.
- 3.Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

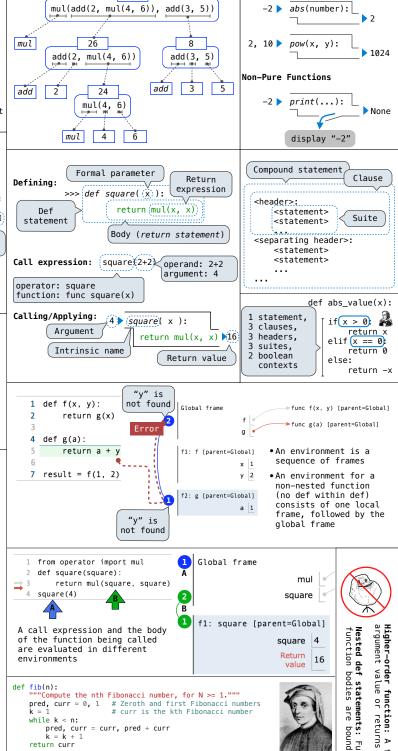
- 1.Evaluate the subexpression <left>.
- 2.If the result is a false value v, then the expression evaluates to v.
- 3.0 therwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

1.Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- 1. Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.



ef statements: Functions
bodies are bound to name function s a functi es in the takes a function a return value within e local other frame as an

Function of a single

argument (not called term)

A formal parameter that

The cube function is passed

as an argument value

The function bound to term

gets called here

def cube(k):

225

return pow(k, 3)

total, k = 0, 1

while k <= n:</pre>

return total

 $0 + 1^3 + 2^3 + 3^3 + 4^3 + 5^5$

>>> summation(5, cube)

def summation(n, term) will be bound to a function

"""Sum the first n terms of a sequence.

total, k = total + (term(k)), k + 1

```
square = lambda x: x * x
 square = \left| \frac{x,y}{x} \right| = \left| \frac{x+y}{x} \right| Evaluates to a function.
                                      No "return" keyword!
                                                                                   • Both create a function with the same domain, range, and behavior.
           A function
                with formal parameters x and y
                                                                                   • Both functions have as their parent the environment in which they
                      that returns the value of "\times \times y,"
                   Must be a single expression
def make_adder(n): A function that returns a function
        'Return a function that takes one argument k and returns k + n.
     >>> add_three = make_adder(3) 
                                            The name add three is
                                             bound to a function
     7
                               A local
    def adder(k):
                            def statement
         return k +(n)
     return adder
                            Can refer to names in
                            the enclosing function
• Every user-defined function has
  a parent frame
 • The parent of a function is the
  frame in which it was defined
                                                 A function's signature
 • Every local frame has a parent
                                                 has all the information
  frame
                                                 to create a local frame
 • The parent of a frame is the
  parent of the function called
                                  3
                                      Global frame
                                                                   func make adder(n) [parent=Global]
                                                make_adder
   1 def make_adder(n):
                                                                  func adder(k) [parent=f1]
                                                  add_three
     def adder(k):
return k + n
 Nested
                                      f1: make_adder [parent=G]
         return adder
  def
   6 add_three = make_adder(3)
                                                     adder
   7 add_three(4)
                                                     Return
                                       f2: adder [parent=f1]
 def curry2(f):
       ""Returns a function g such that g(x)(y) returns f(x, y)."""
     def g(x):
         def h(y):
                                Currying: Transforming a multi-argument
function into a single-argument,
             return f(x, y)
         return h
                                 higher-order function.
     return q
 Anatomy of a recursive function:
 • The def statement header is similar to other functions
• Conditional statements check for base cases

    Base cases are evaluated without recursive calls

 • Recursive cases are evaluated with recursive calls
 def sum_digits(n):
  """Return the sum of the digits of positive integer n.""" if \frac{n}{l} < 10 \colon
       return n
   else:
       all_but_last, last = n // 10, n % 10
       return sum_digits(all_but_last) + last
                           Global frame
    def cascade(n):
                                                      >> func cascade(n) [parent=Global]
       if n < 10:
                                         cascade e
          print(n)
        else:
                           f1: cascade [parent=Global] \circ Each cascade frame is from a different call
           print(n)
                                          n 123
           cascade(n//10)
                                                    to cascade.
           print(n)
                           f2: cascade [parent=Global]
                                                  • Until the Return value
                                         n 12
                                                   appears, that call has not completed.
  9 cascade(123)
                                       Return
value None
Program output:
Any statement can
                                                    appear before or after
1 12
                                                    the recursive call.
                                       Return
value None
                                               n: 0, 1, 2, 3, 4, 5, 6, 7, 8,
           def inverse_cascade(n):
1
                                          fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21,
                grow(n)
12
                print(n)
                                         def fib(n):
    if n == 0:
                shrink(n)
123
                                             if n == 0:
return 0
elif n == 1:
           def f_then_g(f, g, n):
1234
                if n:
                                                  return 1
123
                     f(n)
                                             else:
return fib(n-2) + fib(n-1)
                     q(n)
12
           grow = lambda n: f_then_g(grow, print, n//10)
1
           shrink = lambda n: f_then_g(print, shrink, n//10)
```

```
· Both bind that function to the name square.
• Only the def statement gives the function an intrinsic name.
When a function is defined:

    Create a function value: func <name>(<formal parameters>)

2. Its parent is the current frame.
         f1: make_adder
                               func adder(k) [parent=f1]
3. Bind <name> to the function value in the current frame
   (which is the first frame of the current environment).
When a function is called:
1. Add a local frame, titled with the <name> of the function being
    called.
    Copy the parent of the function to the local frame: [parent=<label>]

    Bind the <formal parameters> to the arguments in the local frame.
    Execute the body of the function in the environment that starts with

    the local frame.
                    def fact(n):
                         if n == 0:
                             return 1
                  4
                         else:
                             return n * fact(n-1)
                  7 fact(3)
                                                → func fact(n) [parent=Global]
                Global frame
                                  fact
                f1: fact [parent=Global]
                                   n 3
                f2: fact [parent=Global]
                                   n 2
                f3: fact [parent=Global]
                                   n 1
                f4: fact [parent=Global]
                                   n 0
                                Return 1
            Is fact implemented correctly?
                  Verify the base case.
                  Treat fact as a functional abstraction!
            2.
            3.
                  Assume that fact(n-1) is correct.
                  Verify that fact(n) is correct.
                  assuming that fact(n-1) correct.

    Recursive decomposition:

                                 def count_partitions(n, m):
 finding simpler instances of
                                     if n == 0:
 a problem.
                                         return 1
E.g., count_partitions(6, 4)
                                      elif n < 0:
Explore two possibilities:Use at least one 4
                                          return 0
                                     elif m == 0:
  Don't use any 4
                                         return 0
Solve two simpler problems:count_partitions(2, 4)
                                     else:
                                     with_m = count_partitions(n-m, m)
  count_partitions(6, 3)
                                         without_m = count_partitions(n, m-1)
• Tree recursion often involves
                                          return with_m + without_m
 exploring different choices.
from operator import floordiv, mod
def divide_exact(n, d):
     """Return the quotient and remainder of dividing N by D.
    \Rightarrow \neq (q, r = divide\_exact(2012, 10)) \leq Multiple assignment
    >>> 'q
                                                to two names
    201
    >>> r
    000
                                            Multiple return values,
                                              separated by commas
    return floordiv(n, d), mod(n, d) <
```

def square(x):

return x * x

VS

```
Numeric types in Python:
                                                                          List comprehensions:
                                                                                                                                                                                        List & dictionary mutation:
                                                                              [<map exp> for <name> in <iter exp> if <filter exp>]
                                                                                                                                                                                        >>> a = [10]
                                                                                                                                                                                                                        >>> a = [10]
  >>> type(2)
                                   Represents
                                                                                                                                                                                        >>> b = a
  <class 'int'>-
                                                                                                                                                                                                                        >>> b = [10]
                                     integers
                                                                               Short version: [<map exp> for <name> in <iter exp>]
                                                                                                                                                                                        >>> a == b
                                                                                                                                                                                                                        >>> a == b
                                      exactly
 >>> type(1.5)
                                                                          A combined expression that evaluates to a list using this
                                                                                                                                                                                        True
                                                                                                                                                                                                                        True
                                                                                                                                                                                        >>> a.append(20)
  <class 'float'> <
                                                                                                                                                                                                                        >>> b.append(20)
                                                                          evaluation procedure:
                               Represents real
                                                                                                                                                                                                                        >>> a
                                                                                                                                                                                        >>> a == b
                                                                          1. Add a new frame with the current frame as its parent
                                      numbers
  >>> type(1+1j)
                                                                                                                                                                                        True
                                                                                                                                                                                                                        [10]
                                                                          2. Create an empty result list that is the value of the
                                 approximately
  <class 'complex'>
                                                                                                                                                                                        >>> a
                                                                                                                                                                                                                        >>> b
                                                                              expression
                                                                                                                                                                                        [10, 20]
                                                                                                                                                                                                                        [10, 20]
                                                                          3. For each element in the iterable value of <iter exp>:
 Functional pair implementation:
                                                                                                                                                                                        >>> h
                                                                                                                                                                                                                        >>> a == b
                                                                              A. Bind <name> to that element in the new frame from step 1
                                                                                                                                                                                        [10, 20]
                                                                                                                                                                                                                        False
                                                                              B. If <filter exp> evaluates to a true value, then add
                                                                                                                                                                                        >>> nums = { 'I': 1.0, 'V': 5, 'X': 10}
  def pair(x, y):
                                                                                   the value of <map exp> to the result list
         """Return a functional pair."""
                                                                                                                                                                                        >>> nums['X']
                                                                           def apply_to_all(map_fn, s):
        def get(index):
              if index == 0:
                                                                                     "Apply map_fn to each element of s.
                                                                                                                                                       0, 1, 2, 3, 4
                                                                                                                                                                                        >>> nums['I'] = 1
                                             This function
                     return x
                                                                                                                                                                                        >>> nums['L'] = 50
                                             represents a
                                                                                 >>> apply_to_all(lambda x: x*3, range(5))
               elif index == 1:
                                                     pair
                                                                                                                                                           λx: x*3
                                                                                                                                                                                        >>> nums
                     return y
                                                                                 [0, 3, 6, 9, 12]
                                                                                                                                                                                        {'X': 10, 'L': 50, 'V': 5, 'I': 1}
        return get
                                                                                                                                                                                        >>> sum(nums.values())
                                                                                                                                                       0, 3, 6, 9, 12
                                                                                  return [map_fn(x) for x in s]
                                      Constructor is a
                                                                                                                                                                                        >>> dict([(3, 9), (4, 16), (5, 25)])
{3: 9, 4: 16, 5: 25}
 def select(p, i): higher-order function
                                                                           def keep_if(filter_fn, s):
                                                                                    "List elements x of s for which
                                                                                                                                                       0, 1, 2, 3, 4, 5, 6, 7, 8, 9
                                                                                                                                                                                        >>> nums.get('A', 0)
        """Return element i of pair p."""
                                                                                 filter_fn(x) is true.
        return p(i) _
                                                                                                                                                                                        0
                                                                                                                                                                                        >>> nums.get('V'. 0)
                                    Selector defers to
                                                                                  >>> keep_if(lambda x: x>5, range(10))
                                                                                                                                                           \lambda x: x>5
                                     the object itself
  >>> p = pair(1, 2)
                                                                                  [6, 7, 8, 9]
                                                                                                                                                                                        >>> {x: x*x for x in range(3,6)}
 >>> select(p, 0)
                                                                                                                                                                                        {3: 9, 4: 16, 5: 25}
                                                                                                                                                         6, 7, 8, 9
                                                                                 return [x for x in s if filter_fn(x)]
                                                                                                                                                                                        >>> suits = ['coin', 'string', 'myriad']
  >>> select(p, 1)
                                                                                                                                                                                        >>> original_suits = suits
                                                                          def reduce(reduce_fn, s, initial):
                                                                                                                                                                                        >>> suits.pop()
                                                                                  ""Combine elements of s pairwise using reduce_fn,
Lists:
                                                                                  starting with initial.
                                                                                                                                                                                         'mvriad'
                                                                                                                                       16,777,216
                                                                                                                                                                                        >>> suits.remove('string')
>>> digits = [1, 8, 2, 8]
                                                                                                                                                                                        >>> suits.append('cup')
                                                                                 r = initial
>>> len(digits)
                                                                                                                                                                                        >>> suits.extend(['sword', 'club'])
                                             list
                                                                                                                                              64
                                                                                                                                                                       4
                                                                                                                            pow
                                                                                 for x in s:
                         digits ___
                                             0 1 2 3
                                                                                      r = reduce_fn(r, x)
                                                                                                                                                                                        >>> suits[2] = 'spade'
>>> digits[3]
                                                                                                                                                                                        >>> suits
['coin', 'cup', 'spade', 'club']
>>> suits[0:2] = ['heart', 'diamond']
                                                     8
                                                         2 8
                                                                                                                                               4
                                                                                                                                                                  3
                                                                                                                               pow
>>> [2, 7] + digits * 2
                                                                                                                                              2
                                                                                                                                                            2
                                                                           reduce(pow, [1, 2, 3, 4], 2)
                                                                                                                                 pow
 [2, 7, 1, 8, 2, 8, 1, 8, 2, 8]
                                                                                                                                                                                        >>> suits
['heart', 'diamond', 'spade', 'club']
>>> pairs = [[10, 20], [30, 40]]
                                                                                                                                             2
                                                                                                                                   pow
                                                                                                                                                                                        >>> original_suits
 >>> pairs[1]
                                                       list
                                                                                                                                                                                         ['heart, 'diamond', 'spade', 'club']
                         pairs 0 1
 [30, 40]
                                                                         Type dispatching: Look up a cross-type implementation of an
 >>> pairs[1][0]
                                                               20
                                                         10
                                                                                                                                                                                         Identity:
                                                                         operation based on the types of its arguments

Type coercion: Look up a function for converting one type to
30
                                                                                                                                                                                         <exp0> is <exp1>
                                                                                                                                                                                         evaluates to True if both <exp0> and
                                                       list
Executing a for statement:
                                                                         another, then apply a type-specific implementation.
                                                                                                                                                                                         <exp1> evaluate to the same object
for <name> in <expression>:
                                                                                                \Theta(b^n) Exponential growth. Recursive fib takes
                                                                                                                                                                                         Equality:
                                                                              e are positive |\mathbf{k_2} such that |\leq k_2 \cdot f(n) than some \mathbf{m}
       <suite>
                                                                                                             \Theta(\phi^n) steps, where \phi=\frac{1+\sqrt{5}}{2}\approx 1.61828 Incrementing the problem scales R(n)
                                                                                                                                                                                         <exp0> == <exp1>
 1. Evaluate the header <expression>,
                                                                                                                                                                                         evaluates to True if both <exp0> and
     which must yield an iterable value
                                                                                                                                                                                         <exp1> evaluate to equal values
     (a sequence)
                                                                                                                                                                                        Identical objects are always equal values
                                                                                                             by a factor
 2. For each element in that sequence.
                                                                                                \Theta(n^2)
                                                                                                                                                                                         You can copy a list by calling the list
                                                                                                             Quadratic growth. E.g., overlap
     in order:
                                                                             at there is \mathbf{k_1} and \mathbf{k} \leq R(n) \leq
                                                                                                                                                                                         constructor or slicing the list from the
                                                                                                             Incrementing n increases R(n) by the
    A. Bind <name> to that element in
                                                                                                                                                                                         beginning to the end.
         the current frame
                                                                                                             problem size n
                                                                                                                                                                                       Constants: Constant terms do not affect
    B. Execute the <suite>
                                                                                                 \Theta(n)
                                                                                                                                                                                       the order of growth of a process
                                                                                                             Linear growth. E.g., factors or exp
                                                                         R(n) = \Theta(f)
means that constants k constants k k_1 \cdot f(n) \land k_1 \cdot f(n) \land k_1 \land k_2 \land k_3 \land k_4 \land k
                                                                                                                                                                                       \Theta(n) \qquad \Theta(500 \cdot n) \qquad \Theta(\frac{1}{500} \cdot n) 
 Logarithms: The base of a logarithm does
 Unpacking in a
                                                                                                             Logarithmic growth. E.g., exp_fast
                                      A sequence of
  for statement:
                             fixed-length sequences
                                                                                                             Doubling the problem only increments R(n)
                                                                                                                                                                                       not affect the order of growth of a process
                                                                                                  \Theta(1)
                                                                                                             Constant. The problem size doesn't matter
>>> pairs=[[1, 2], [2, 2], [3, 2], [4, 4]]
                                                                                                                                                                                         \Theta(\log_2 n) ~~ \Theta(\log_{10} n)
                                                                                                                                                                                                                                \Theta(\ln n)
>>> same_count = 0
                                                                                                                                                                                      Nesting: When an inner process is repeated
                                                                                                                             → func make withdraw(balance) [parent=Global
                                                                          Global frame
         A name for each element in a
                                                                                                                                                                                       for each step in an outer process, multiply
               fixed-length sequence
                                                                                               make_withdraw
                                                                                                                                                                                       the steps in the outer and inner processes
                                                                                                                              func withdraw(amount) [parent=f1]
                                                                                                      withdraw
                                                                                                                                                                                       to find the total number of steps
>>> for (x, y) in pairs:
... if x == y:
                                                                                                                             >>> withdraw = make_withdraw(100)
                                                                                                                                                                                       def overlap(a, b):
                                                                                                                             >>> withdraw(25)
                                                                          f1: make withdraw [parent=Global]
                                                                                                                                                                                             count = 0
                    same_count = same_count + 1
                                                                                                                             75
                                                                                                                                                                                                                           Outer: length of a
                                                                                                                                                                                              for item in a: —
                                                                                                      balance 50
                                                                                                                             >>> withdraw(25)
                                                                               The parent
                                                                                                                                                                                                   if item in b:
count += 1 Inner: length of b
                                                                                                     withdraw
                                                                                                                             50
>>> same_count
                                                                            frame contains
                                                                                                                            def make_withdraw(balance):
                                                                                                       Return
                                                                            the balance of
                                                                                                                                                                                             return count
                                                                                                         value
                                                                                                                                 def withdraw(amount):
                                                                                                                                                                                      If a and b are both length n,
       \dots, -3, -2, -1, 0, 1, 2, 3, 4, \dots
                                                                                                                                         nonlocal balance
                                                                          f2: withdraw [parent=f1]
                                                                                                                                                                                       then overlap takes \Theta(n^2) steps
                                                                                                                                          if amount > balance:
    return 'No funds
                                                                                                                                                                                      Lower-order terms: The fastest-growing part
                                                                                                      amount 25
                                                                               Every call
                                                                                                                                                                                      of the computation dominates the total
                                                                                                                                         balance = balance - amount
                                                                                                       Return
value 75
                                                                            decreases the
                                                                                                                                          return balance
                     range(-2, 2)
                                                                                                                                                                                       \Theta(n^2) \quad \Theta(n^2 + n) \quad \Theta(n^2 + 500 \cdot n + \log_2 n + 1000)
                                                                             same balance
                                                                                                                                   return withdraw
 Length: ending value - starting value
                                                                          f3: withdraw [parent=f1]
                                                                                                                                 Status
                                                                                                                                                                                Effect
                                                                                                                                                             x = 2
 Element selection: starting value + index
                                                                                                     amount 25
                                                                                                                               •No nonlocal statement
                                                                                                                                                                            Create a new binding from name "x" to number 2
                                                                                                                               •"x" is not bound locally
                                                                                                                                                                            in the first frame of the current environment
                                                                                                       Return
value 50
  >>> list(range(-2, 2)) \ List constructor
                                                                                                                                                                            Re-bind name "x" to object 2 in the first frame
  [-2, -1, 0, 1]
                                                                                                                              •No nonlocal statement
                                                                           Strings as sequences:
                                                                                                                               •"x" is bound locally
                                                                                                                                                                            of the current environment
  >>> list(range(4)) {
[0. 1. 2. 3]
                                    Range with a 0
                                                                          >>> city = 'Berkeley'
                                                                                                                               •nonlocal x
                                    starting value
                                                                                                                                                                            Re-bind "x" to 2 in the first non-local frame of
                                                                           >>> len(city)
  [0, 1, 2, 3]
                                                                                                                               •"x" is bound in a
                                                                                                                                                                            the current environment in which "x" is bound
                                                                          8
                                                                                                                               non-local frame
Membership:
                                          Slicing:
                                                                           >>> city[3]
                                          >>> digits[0:2]
>>> digits = [1, 8, 2, 8]
                                                                                                                               •nonlocal x
                                                                                                                                                                            SyntaxError: no binding for nonlocal 'x' found
>>> 2 in digits
                                           [1.8]
                                                                                                                               •"x" is not bound in
                                                                          >>> 'here' in "Where's Waldo?"
                                           >>> digits[1:]
True
                                                                                                                                a non-local frame
                                                                          True
                                           [8, 2, 8]
>>> 1828 not in digits
                                                                                                                               •nonlocal x
                                                                          >>> 234 in [1, 2, 3, 4, 5]
                                                                                                                               •"x" is bound in a
                                            Slicing creates
                                                                          False
                                                                                                                                                                            SyntaxError: name 'x' is parameter and nonlocal
```

non-local frame

•"x" also bound locally

>>> [2, 3, 4] in [1, 2, 3, 4]

False

a new object

```
Linked list data abstraction:
                             def partitions(n, m):
 empty = 'empty'
                                   "Return a linked list of partitions
                                 of n using parts of up to m.
 def link(first, rest):
                                 Each partition is a linked list.
     return [first, rest]
 def first(s):
                                 if n == 0:
     return s[0]
                                      return link(empty, empty)
                                 elif n < 0:
 def rest(s):
                                      return empty
     return s[1]
                                 elif m == 0:
                                     return empty
 def len_link(s):
                                 else:
     x = 0
                                      # Do I use at least one m?
     while s != empty:
                                      yes = partitions(n-m, m)
         s, x = rest(s), x+1
                                      no = partitions(n, m-1)
                                     add_m = lambda s: link(m, s)
yes = apply_to_all_link(add_m, yes)
     return x
 def getitem_link(s, i):
                                      return extend(yes, no)
     while i > 0:
         s, i = rest(s), i - 1
     return first(s)
                                                     def extend(s, t):
    assert is_link(s) and is_link(t)
     if s == empty:
         return t
     else:
         return link(first(s), extend(rest(s), t))
def apply_to_all_link(f, s):
    if s == empty:
         return s
     else:
         return link(f(first(s)), apply_to_all_link(f, rest(s)))
                            link(1, link(2, link(3, link(4, empty)
          A linked list
                                    represents the sequence
             is a pair
                                         1 2 3
                                                                  "empty"
                                                      4
                                                                 represents
                                                                 the empty
          list
                         list
                                        list
                                                      list
                                                                    list
           0
                          0
                                                       0
                                        0
                           2
                                         3
             1
                                                        4
                                                              "empty"
      The 0-indexed element of the
                                          The 1-indexed element
      pair is the first element of
                                         of the pair is the rest
             the linked list
                                           of the linked list
The result of calling repr on a value is
                                                 Memoization:
what Python prints in an interactive session
                                                def memo(f):
The result of calling str on a value is
                                                     cache = \{\}
what Python prints using the print function
                                                     def memoized(n):
                                                         if n not in cache:
 >>> 12e12
                            >>> print(today)
                                                              cache[n] = f(n)
 120000000000000.0
                            2014-10-13
                                                         return cache[n]
 >>> print(repr(12e12))
                                                     return memoized
 120000000000000.0
str and repr are both polymorphic; they apply to any object
repr invokes a zero-argument method __repr__ on its argument
>>> today._
                                   >>> today.__str__()
>>> today.__repr__()
'datetime.date(2014, 10, 13)'
                   Some zero
class Link:
    empty = () < length sequence</pre>
          _init__(self, first, rest=empty):
        self.first = first
        self.rest = rest
                                     Sequence abstraction special names:
          _getitem__(self, i):
                                        _getitem__ Element selection []
        if i == 0:
            return self.first
                                                    Built-in len function
                                        len-
        else:
            return self.rest[i-1]
          <u>len__(self):</u>
                                        Yes, this call is recursive
        return 1 + len(self.rest)
class Tree:
                                                     Built-in isinstance
    def
          __init__(self, entry, branches=()):
                                                  function: returns True if
         self.entry = entry
         for branch in branches:
                                                  branch has a class that
             assert (isinstance(branch, Tree))
                                                  is or inherits from Tree
         self.branches = list(branches)
class BinaryTree(Tree):
                                              E: An empty tree
     empty = Tree(None)
     empty.is_empty = True
         __init__(self, entry, left=empty, right=empty):
Tree.__init__(self, entry, (left, right))
                                                             1
         self.is\_empty = False
     @property
     def left(self):
                                   Bin = BinaryTree
         return self.branches[0] | t = Bin(3, Bin(1),
                                               Bin(7, Bin(5),
     @property
                                                                          11
     def right(self):
                                                      Bin(9, Bin.empty, / Bin(11)))) E
         return self.branches[1]
```

```
Python object system:
Idea: All bank accounts have a balance and an account holder;
the Account class should add those attributes to each of its instances
                         >>> a = Account('Jim')
  A new instance is
                         >>> a.holder
 created by calling a
                         'Jim'
        class
                         >>> a.balance
                                                 An account instance
When a class is called:
                                                          holder: 'Jim'
                                            balance: 0
1.A new instance of that class is created:
2. The __init__ method of the class is called with the new object as its first
 argument (named self), along with any additional arguments provided in the
  call expression.
                     class Account:
                             __init__(self, account_holder):
                        ⊳def
   init is called a
                             self.balance = 0
     constructor
                             self.holder = account_holder
                         def deposit(self, amount):
                             self.balance = self.balance + amount
                             return self.balance
 self should always be
                             withdraw(self, amount):
if amount > self.balance:
    return 'Insufficient funds'
                         def
bound to an instance of
 the Account class or a
  subclass of Account
                             self.balance = self.balance - amount
                             return self.balance
                      >>> type(Account.deposit)
 Function call: all
                      <class 'function'
                      >>> type(a.deposit)
  arguments within
    parentheses
                      <class 'method'>
                      >>> Account.deposit(a, 5)
 Method invokation:
  One object before
  the dot and other
                          a.deposit(2)
                                                  Call expression
  arguments within
     parentheses
                           Dot expression
                          <expression> . <name>
 The <expression> can be any valid Python expression.
The <name> must be a simple name.
Evaluates to the value of the attribute looked up by <name> in the object
that is the value of the <expression>.
To evaluate a dot expression:
   Evaluate the <expression> to the left of the dot, which yields
     the object of the dot expression
     <name> is matched against the instance attributes of that object;
     if an attribute with that name exists, its value is returned
    If not, <name> is looked up in the class, which yields a class
     attribute value
     That value is returned unless it is a function, in which case a
     bound method is returned instead
 Assignment statements with a dot expression on their left-hand side affect
 attributes for the object of that dot expression
 • If the object is an instance, then assignment sets an instance attribute
 • If the object is a class, then assignment sets a class attribute
          Account class
                             interest: 0.02 0.04 0.05
            attributes
                             (withdraw, deposit, _
                                                   init
     Instance
                    balance:
                              0
                                         Instance
                                                        balance:
                              'Jim'
                                                                   'Tom'
                    holder:
                                                        holder:
  attributes of
                                       attributes of
   jim_account
                    interest: 0.08
                                        tom account
                                         >>> jim_account.interest = 0.08
 >>> jim_account = Account('Jim')
     tom_account = Account('Tom')
                                         >>> jim_account.interest
                                         0.08
 >>> tom_account.interest
0.02
                                         >>> tom account.interest
                                         0.04
>>> jim_account.interest
                                         >>> Account.interest = 0.05
0.02
                                         >>> tom_account.interest
>>> Account.interest = 0.04
                                         0.05
 >>> tom_account.interest
                                         >>> jim_account.interest
 0.04
                                         0.08
 >>> jim_account.interest
0.04
class CheckingAccount(Account):
       "A bank account that charges for withdrawals."""
    withdraw fee = 1
     interest = 0.01
    return (super().withdraw(
                                       amount + self.withdraw_fee)
 To look up a name in a class:
 1. If it names an attribute in the class, return the attribute value.
 2. Otherwise, look up the name in the base class, if there is one.
 >>> ch = CheckingAccount('Tom') # Calls Account.__init_
                     # Found in CheckingAccount
 >>> ch.interest
 0.01
 >>> ch.deposit(20) # Found in Account
 20
 >>> ch.withdraw(5) # Found in CheckingAccount
```

```
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```

Exceptions are raised with a raise statement.

raise <expression>

<expression> must evaluate to a subclass of BaseException or an instance of one.

Exceptions are constructed like any other object. E.g., TypeError('Bad argument!')

```
try:
                                             >>> try:
     <try suite>
except <exception class> as <name>:
                                                      x = 1/0
     <except suite>
                                                  except ZeroDivisionError as e:
                                                      print('handling a', type(e))
The <trv suite> is executed first.
If, during the course of executing the
                                                      x = 0
<try suite>, an exception is raised that is not handled otherwise, and
If the class of the exception inherits
                                             handling a <class 'ZeroDivisionError'>
from <exception class>, then
The <except suite> is executed, with
<name> bound to the exception.
```

for <name> in <expression>:
 <suite>

- 1. Evaluate the header <expression>, which yields an iterable object.
- 2. For each element in that sequence, in order:
- A. Bind <name> to that element in the first frame of the current environment.
- B. Execute the <suite>.

```
An iterable object has a method __iter__ that returns an iterator.
                                                 >>> items = counts.__iter__()
       >>> counts = [1, 2, 3]
>>> for item in counts:
                                                 >>> trv:
                                                           while True:
   item = items.__next__()
   print(item)
                print(item)
                                                      except StopIteration:
                                                          pass
                                            >>> fibs = FibIter()
class FibIter:
```

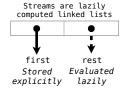
```
def __init__(self):
    self(_next = 0)
                                        >>> [next(fibs) for _ in range(10)]
[0, 1, 1, 2, 3, 5, 8, 13, 21, 34]
     self._addend = 1
                "Please don't reference these directly. They may change."
     __next__(self):
result = self._next
     self._addend, self._next = self._next, self._addend + self._next
     return result
```

A stream is a linked list, but the rest of the list is computed on demand.

Once created. Streams and Rlists can be used interchangeably using first and rest.

```
'A lazily computed linked list."""
class empty:

def __repr__(self):
    return 'Stream.empty'
empty = empty()
```



```
__init__(self, first, compute_rest=lambda: Stream.empty):
assert callable(compute_rest), 'compute_rest must be callable.'
self.first = first
         self._compute_rest = compute_rest
@property
def rest(self):
       icst():
""Return the rest of the stream, computing it if necessary."""
if self._compute_rest is not None:
    self._rest = self._compute_rest()
    self._compute_rest = None
return self._rest
```

def integer_stream(first=1): def compute_rest():
 return integer stream(first+1) return Stream(first, compute_rest)

def filter_stream(fn, s): def map_stream(fn, s): if s is Stream.empty: if s is Stream.empty: return s def compute_rest(): return s
compute_rest(): return map_stream(fn, s.rest)
return Stream(fn(s.first), return filter_stream(fn, s.rest) if fn(s.first): return Stream(s.first, compute_rest) compute_rest) else: return compute_rest()

def primes(positives): def not_divisible(x): return x % positives.first != 0

def compute_rest():
 return primes(filter_stream(not_divisible, positives.rest))
return Stream(positives.first, compute_rest)

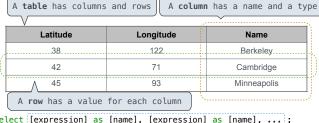
The way in which names are looked up in Scheme and Python is called lexical scope (or static scope).

Lexical scope: The parent of a frame is the environment in which a procedure was defined. (lambda ...)

Dynamic scope: The parent of a frame is the environment in which a procedure was called. (mu ...)

```
> (define f (mu (x) (+ x y)))
> (define g (lambda (x y) (f (+ x x))))
> (g 3 7)
```

```
>>> a_to_c = LetterIter('a', 'c')
class LetterIter:
    def __init__(self, start='a', end='e'):
                                                         >>> next(a_to_c)
         self.next_letter = start
self.end = end
                                                         >>> next(a_to_c)
         __next__(self):
if self.next letter >= self.end:
                                                         >>> next(a_to_c)
Traceback (most recent call last):
             raise StopIteration
         result = self.next_letter
                                                         StopIteration
          self.next letter = chr(ord(result)+1)
         return result
                                                         >>> b to k = Letters('b', 'k')
                                                         >>> first_iterator =
                                                        b_to_k.__iter__()
>>> next(first_iterator)
class Letters:
    def __init__(self, start='a', end='e'):
    self.start = start
    self.end = end
                                                         >>> next(first_iterator)
                                                         >>> second_iterator = iter(b_to_k)
          __iter__(self):
return LetterIter(self.start, self.end)
                                                         >>> second_iterator.__next__()
def letters_generator(next_letter, end):
                                                         >>> first iterator. next ()
    while next_letter < end:
    yield next_letter</pre>
         next letter = chr(ord(next letter)+1)
                                                         >>> for letter in
                                                         letters_generator('a', 'e'):
                                                                  print(letter)
 • A generator is an iterator backed
   by a generator function.
 • Each time a generator function is
   called, it returns a generator.
```



select [expression] as [name], [expression] as [name], ...; select [columns] from [table] where [condition] order by [order]: create table parents as



select a.child as first, b.child as second from parents as a, parents as b where a.parent = b.parent and a.child < b.child; ancestors(ancestor, descendent) as (
 select parent, child from parents union

select ancestor, child

First Second barack clinton abraham delano abraham grover delano grover ancestor

н

D ¦ G

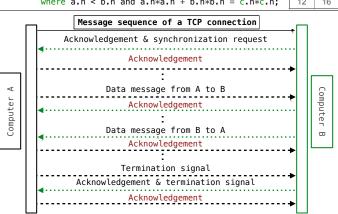
delano

fillmore

eisenhower

from ancestors, parents where parent = descendent select ancestor from ancestors where descendent="herbert";

а b С 3 4 5 create table pythagorean_triples as with 5 12 13 i(n) as (6 8 10 select 1 union select n+1 from i where n < 208 15 17 select a.n as a. b.n as b. c.n as c 9 12 15 from i as a, i as b, i as c where a.n < b.n and a.n*a.n + b.n*b.n = c.n*c.n; 12 16 20



CS 61A Final Exam Study Guide - Page 2 Scheme programs consist of expressions, which can be: Primitive expressions: 2, 3.3, true, +, quotient,...
Combinations: (quotient 10 2), (not true),... Numbers are self-evaluating; symbols are bound to values. Call expressions have an operator and 0 or more operands. A combination that is not a call expression is a special form:

• If expression: (if <predicate> <consequent> <alternative>)
• Binding names: (define <name> <expression>) New procedures: (define (<name> <formal parameters>) <body>) > (define pi 3.14) > (define (abs x) (if (< x 0) (- x)> (* pi 2) x)) (abs -3) Lambda expressions evaluate to anonymous procedures. (lambda (<formal-parameters>) <body>) Two equivalent expressions: (define (plus4 x) (+ x 4))(define plus4 (lambda (x) (+ x 4)))An operator can be a combination too: ((lambda (x y z) (+ x y (square z))) 1 2 3) In the late 1950s, computer scientists used confusing names.

cons: Two-argument procedure that creates a pair

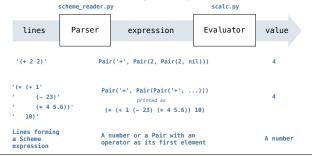
car: Procedure that returns the first element of a pair

cdr: Procedure that returns the second element of a pair nil: The empty list They also used a non-obvious notation for linked lists. (linked) Scheme list is a pair in which the second element is nil or a Scheme list.
Scheme lists are written as space-separated combinations. A dotted list has an arbitrary value for the second element of the last pair. Dotted lists may not be well-formed lists. > (define x (cons 1 2)) (1) 2) < Not a well-formed list! > (car x) (cdr x) (cons 1 (cons 2 (cons 3 (cons 4 nil)))) (1234)Symbols normally refer to values; how do we refer to symbols? > (define a 1) (define b 2) No sign of "a" and "b" in > (list a b) the resulting value $(1\ 2)$ -Ouotation is used to refer to symbols directly in Lisp. > (list 'a 'b) (a b) — Symbols are now values > (list 'a b) (a 2) Quotation can also be applied to combinations to form lists. > (car '(a b c)) а > (cdr '(a b c)) (b c) Dots can be used in a quoted list to specify the second element of the final pair. > (cdr (cdr '(1 2 . 3))) 3 However, dots appear in the output only of ill-formed lists. '(1 2 . 3) 1 • 2 3 (1 2 . 3) > '(1 2 . (3 4)) (1 2 3 4) \rightarrow 2 \bullet 3 \bullet 4 \bullet nil '(1 2 3 . nil) 1 • 2 • 3 • nil $(1\ 2\ 3)$ > (cdr '((1 2) . (3 4 . (5)))) (3 4 5) The Calculator language "A Pair has first and second attributes. For a Pair to be a well-formed list, second is either a well-formed list or nil. Calculator Expression init (self, first, second): self.first = first self.second = second (* 6 7 8)) >>> s = Pair(1, Pair(2, Pair(3, nil))) Expression Tree >>> print(s)

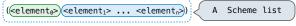
has primitive expressions and call expressions >>> len(s) >>> print(Pair(1, 2)) >>> print(Pair(1, Pair(2, 3))) Representation as Pairs 3 7 8 nil

5

A basic interpreter has two parts: a parser and an evaluator.



A Scheme list is written as elements in parentheses:

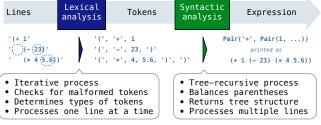


Each <element> can be a combination or atom (primitive). (+ (* 3 (+ (* 2 4) (+ 3 5))) (+ (- 10 7) 6))

The task of parsing a language involves coercing a string representation of an expression to the expression itself.

Parsers must validate that expressions are well-formed.

A Parser takes a sequence of lines and returns an expression.

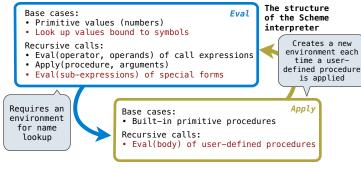


Syntactic analysis identifies the hierarchical structure of an expression, which may be nested.

Each call to scheme_read consumes the input tokens for exactly one expression.

Base case: symbols and numbers

Recursive call: scheme_read sub-expressions and combine them



To apply a user-defined procedure, create a new frame in which formal parameters are bound to argument values, whose parent is the $\mbox{\it env}$ of the procedure, then evaluate the body of the procedure in the environment that starts with this new frame.

(define (f s) (if (null? s) '(3) (cons (car s) (f (cdr s))))) (f (list 1 2)) g: Global frame LambdaProcedure instance [parent=g] 2 1 [parent=q] s [parent=g] S

A procedure call that has not yet returned is active. Some procedure calls are tail calls. A Scheme interpreter should support an unbounded number of active tail calls.

A tail call is a call expression in a tail context, which are:

- The last body expression in a lambda expression
 Expressions 2 & 3 (consequent & alternative) in a tail context

[parent=g]

if expression

