## 1 layers.py

```
1 from builtins import range
  import numpy as np
  def affine forward(x, w, b):
      Computes the forward pass for an affine (fully-connected) layer
8
      The input x has shape (N, d 1, ..., d k) and contains a minibatch of N
      examples, where each example x[i] has shape (d 1, \ldots, d k). We will
10
      reshape each input into a vector of dimension D = d_1 * ... * d_k, and
11
12
      then transform it to an output vector of dimension M.
13
14
      - x: A numpy array containing input data, of shape (N, d_1, ..., d_k)
15
      - w: A numpy array of weights, of shape (D, M) - b: A numpy array of biases, of shape (M, M)
16
17
18
      Returns a tuple of:
19
      – out: output, of shape (N, M)
20
       cache: (x, w, b)
21
22
      out = None
23
      # TODO: Implement the affine forward pass. Store the result in out. You
25
26
      # will need to reshape the input into rows.
      27
      # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
28
29
      N = \times . shape [0]
30
      x \text{ row} = \text{np.reshape}(x, (N, -1)) \# \text{Reshape} \times \text{into}(N, D) \text{ matrix}
31
      out = x_row.dot(w) + b
32
33
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
34
      35
                                  END OF YOUR CODE
36
      37
      cache = (x, w, b)
38
39
      return out, cache
40
41
  def affine backward (dout, cache):
42
43
      Computes the backward pass for an affine layer.
44
45
      Inputs:
46

    dout: Upstream derivative, of shape (N, M)

47
      — cache: Tuple of:
48
       - x: Input data, of shape (N, d_1, ... d_k) - w: Weights, of shape (D, M)
49
50
       - b: Biases, of shape (M,)
51
52
      Returns a tuple of:
53
      - dx: Gradient with respect to x, of shape (N, d1, ..., d_k) - dw: Gradient with respect to w, of shape (D, M) - db: Gradient with respect to b, of shape (M,)
54
55
56
57
      x. w. b = cache
58
      dx, dw, db = None, None, None
59
      60
      # TODO: Implement the affine backward pass
61
      62
      # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
63
64
      N = x.shape[0]
65
66
      x row = np.reshape(x, (N, -1))
67
68
      # Based on the shape of of dx, dw and db, can get the calculation formula
69
      dx = dout.dot(w.T).reshape(x.shape)
70
      dw = x row.T.dot(dout)
71
72
      db = np.sum(dout, axis = 0)
73
```

```
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
74
     75
                           END OF YOUR CODE
76
     77
     return dx, dw, db
78
79
80
  def relu_forward(x):
81
82
     Computes the forward pass for a layer of rectified linear units (ReLUs).
83
84
85
     - x: Inputs, of any shape
86
87
     Returns a tuple of:
     - out: Output, of the same shape as \times
89
90
      cache: x
91
     out = None
92
     93
     # TODO: Implement the ReLU forward pass.
94
     95
     # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
96
97
     # Must truly copy the variables into new variables
98
     out = x.copy()
99
     out[out < 0] = 0
100
101
102
     # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
103
     104
                           END OF YOUR CODE
105
     106
     cache = x
107
108
     return out, cache
109
110
     relu backward(dout, cache):
111
112
     Computes the backward pass for a layer of rectified linear units (ReLUs).
113
114
115

    dout: Upstream derivatives, of any shape

116
     - cache: Input \times, of same shape as dout
117
118
     Returns:
119
     - dx: Gradient with respect to x
120
121
122
     dx, x = None, cache
     123
     # TODO: Implement the ReLU backward pass
124
     125
     # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
126
127
     dx = x
128
     dx[dx < 0] = 0
129
     dx[dx > 0] = 1
130
     dx = np. multiply(dx, dout)
131
132
133
     # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
134
     135
136
                           END OF YOUR CODE
     137
     return dx
138
139
140
     batchnorm forward(x, gamma, beta, bn param):
141
142
143
     Forward pass for batch normalization
144
     During training the sample mean and (uncorrected) sample variance are
145
     computed from minibatch statistics and used to normalize the incoming data
146
     During training we also keep an exponentially decaying running mean of the
147
     mean and variance of each feature, and these averages are used to normalize
148
     data at test-time.
149
```

```
At each timestep we update the running averages for mean and variance using
151
       an exponential decay based on the momentum parameter:
152
153
      running mean = momentum * running mean + (1 - momentum) * sample mean
154
155
       running var = momentum * running var + (1 - momentum) * sample var
156
       Note that the batch normalization paper suggests a different test-time
157
       behavior: they compute sample mean and variance for each feature using a
158
       large number of training images rather than using a running average. For
159
       this implementation we have chosen to use running averages instead since
160
       they do not require an additional estimation step; the torch7
161
162
       implementation of batch normalization also uses running averages
163
      Input:
       - x: Data of shape (N, D)
165
        gamma: Scale parameter of shape (D,)
166
        beta: Shift paremeter of shape (D,)
167
        bn param: Dictionary with the following keys:
168
169
        - mode: 'train' or 'test'; required

    eps: Constant for numeric stability

170
171
          momentum: Constant for running mean / variance
          running mean: Array of shape (D,) giving running mean of features
172
173
        — running var Array of shape (D,) giving running variance of features
174
       Returns a tuple of:
175
       – out: of shape (N, D)
176
        cache: A tuple of values needed in the backward pass
177
178
      mode = bn_param['mode']
179
       eps = bn param.get('eps'
                              1e-5
180
      momentum = bn param.get('momentum', 0.9)
181
182
      N, D = x.shape
183
      running\_mean = bn\_param.get('running\_mean', np.zeros(D, dtype=x.dtype))
184
       running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
185
186
      out, cache = None, None
187
       if mode == 'train':
188
          189
          # TODO: Implement the training—time forward pass for batch norm.
190
          \# Use minibatch statistics to compute the mean and variance , use
191
                                                                              #
          # these statistics to normalize the incoming data, and scale and
192
          # shift the normalized data using gamma and beta.
194
          # You should store the output in the variable out. Any intermediates
195
          # that you need for the backward pass should be stored in the cache
196
          # variable.
197
198
          # You should also use your computed sample mean and variance together
                                                                              #
199
          # with the momentum variable to update the running mean and running
200
          # variance, storing your result in the running_mean and running_var
                                                                              #
201
          # variables.
202
203
          # Note that though you should be keeping track of the running
204
          # variance, you should normalize the data based on the standard
                                                                              #
          # deviation (square root of variance) instead!
206
          # Referencing the original paper (https://arxiv.org/abs/1502.03167)
207
          # might prove to be helpful
208
          209
          # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
210
211
212
          sample mean = np.mean(x, axis = 0)
213
          sample\_var = np.var(x, axis = 0)
          running_mean = momentum * running_mean + (1 - momentum) * sample_mean
214
          running\_var = momentum * running\_var + (1 - momentum) * sample\_var
215
          sample normalized = (x - sample mean) / np.sqrt(sample var + eps)
216
          out = gamma * sample normalized + beta
217
          {\sf cache} = ({\sf sample\_normalized} \ , \ {\sf gamma}, \ {\sf beta} \ , \ {\sf sample\_mean} \ , \ {\sf sample\_var} \ , \ {\sf x}, \ {\sf eps})
218
219
          # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
220
          221
                                     END OF YOUR CODE
          223
       elif mode == 'test':
          225
```

```
# TODO: Implement the test-time forward pass for batch normalization.
226
         # Use the running mean and variance to normalize the incoming data,
227
         # then scale and shift the normalized data using gamma and beta.
228
         # Store the result in the out variable.
229
         230
         # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
231
232
         sample_normalized = (x - running_mean) / np.sqrt(running_var + eps)
233
         out = gamma * sample normalized + beta
234
235
         # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
236
         237
                                END OF YOUR CODE
238
         239
      else:
         raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
241
242
243
      # Store the updated running means back into bn param
      bn_param['running_mean'] = running mean
244
245
      bn_param['running_var'] = running_var
246
247
      return out, cache
248
249
      batchnorm backward (dout, cache):
250
251
      Backward pass for batch normalization.
252
253
      For this implementation, you should write out a computation graph for
254
      batch normalization on paper and propagate gradients backward through
255
      intermediate nodes.
256
257
      Inputs:
258

    dout: Upstream derivatives, of shape (N, D)

259
260

    cache: Variable of intermediates from batchnorm forward.

261
262
      Returns a tuple of:

    dx: Gradient with respect to inputs x, of shape (N, D)

263

    dgamma: Gradient with respect to scale parameter gamma, of shape (D,)

       dbeta: Gradient with respect to shift parameter beta, of shape (D,)
265
266
      dx, dgamma, dbeta = None, None, None
267
      268
      # TODO: Implement the backward pass for batch normalization. Store the
269
      # results in the dx, dgamma, and dbeta variables
270
      # Referencing the original paper (https://arxiv.org/abs/1502.03167)
271
      # might prove to be helpful.
272
      273
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
274
275
      sample normalized, gamma, beta, sample mean, sample var, x, eps = cache
276
     N = x.shape[0]
277
      dx hat = dout * gamma
278
      dvar = np.sum(dx_hat * (x - sample_mean) * (-1 / 2) * (sample_var + eps) **(-3 / 2), axis = 0)
279
      dmean = np.sum(np.divide(-dx_hat, np.sqrt(sample_var + eps)), axis = 0) + dvar * np.sum(-2 * (x - eps))
280
      sample mean), a \times is = 0 / N
      281
      dgamma = np.sum(dout * sample normalized, axis = 0)
282
      dbeta = np.sum(dout, axis = 0)
283
284
285
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
286
      287
                               END OF YOUR CODE
288
      289
290
      return dx, dgamma, dbeta
291
292
293
     batchnorm backward alt(dout, cache):
294
295
      Alternative backward pass for batch normalization.
296
297
      For this implementation you should work out the derivatives for the batch
298
      normalizaton backward pass on paper and simplify as much as possible. You
      should be able to derive a simple expression for the backward pass.
300
```

```
See the jupyter notebook for more hints.
301
302
           Note: This implementation should expect to receive the same cache variable
303
           as batchnorm backward, but might not use all of the values in the cache.
304
305
306
           Inputs / outputs: Same as batchnorm backward
307
           dx, dgamma, dbeta = None, None, None
308
                     309
           # TODO: Implement the backward pass for batch normalization. Store the
310
          \# results in the dx, dgamma, and dbeta variables.
311
312
313
          \# After computing the gradient with respect to the centered inputs,
                                                                                                                               #
          # should be able to compute gradients with respect to the inputs in a
314
           \# single statement; our implementation fits on a single 80—character line.\#
315
                                                                      316
          # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
317
318
           sample normalized, gamma, beta, sample mean, sample var, x, eps = cache
319
320
          N = x.shape[0]
           sigma = np.sqrt(sample var + eps)
321
322
323
          dgamma = np.sum(dout * sample normalized, axis = 0)
324
325
           dbeta = np.sum(dout, axis = 0)
326
           dx = (1 / N) * gamma * 1/sigma * ((N * dout) - np.sum(dout, axis=0) -
327
                                                               (x - sample\_mean) * np.square(1/sigma) * np.sum(dout * (x - sample\_mean)) * np.square(1/sigma) * np.square(1/sig
328
          sample mean), a \times is = 0)
320
330
          # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
331
          332
                                                          END OF YOUR CODE
333
          334
335
336
           return dx, dgamma, dbeta
337
338
          layernorm\_forward (x, gamma, beta, ln\_param):
339
340
           Forward pass for layer normalization
341
342
           During both training and test-time, the incoming data is normalized per data-point,
343
           before being scaled by gamma and beta parameters identical to that of batch normalization
344
345
           Note that in contrast to batch normalization, the behavior during train and test-time for
346
           layer normalization are identical, and we do not need to keep track of running averages
347
348
           of any sort.
349
350
            - x: Data of shape (N, D)
351
             gamma: Scale parameter of shape (D,)
352
353
             beta: Shift paremeter of shape (D,)
           – In param: Dictionary with the following keys:
354
355
                   eps: Constant for numeric stability
356
           Returns a tuple of:
357
           – out: of shape (N, D)
358
             cache: A tuple of values needed in the backward pass
359
360
           out. cache = None. None
361
362
           eps = In param.get('eps', 1e-5)
                        363
          # TODO: Implement the training—time forward pass for layer norm
364
           \# Normalize the incoming data , and scale and \, shift the normalized data
365
              using gamma and beta
366
          # HINT: this can be done by slightly modifying your training—time
367
          \# implementation of \, batch normalization , and inserting a line or two of
368
             well-placed code. In particular, can you think of any matrix
369
          \# transformations you could perform , that would enable you to copy over
370
                                                                                                                               #
          # the batch norm code and leave it almost unchanged?
371
          372
          # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
373
374
          \# Transpose x so that the dimension of x becomes (D, N), following calculation can be the same as
375
```

```
batch forward
      x = x T
376
377
      sample mean = np.mean(x, axis = 0)
378
      sample var = np.var(x, axis = 0)
379
      sample normalized = (x - sample mean) / np. sqrt(sample var + eps)
380
381
      \# Transpose sample normalized so that the result can has the correct dimension (N, D)
382
      sample normalized = sample normalized.T
383
      out = gamma * sample normalized + beta
384
385
      \# Transpose \times again so that \times is restored
386
387
      x = x.T
388
      cache = (sample normalized, gamma, beta, sample mean, sample var, x, eps)
390
391
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
392
      393
                                   END OF YOUR CODE
394
      395
       return out, cache
396
397
398
      layernorm_backward(dout, cache):
399
400
       Backward pass for layer normalization.
401
402
       For this implementation, you can heavily rely on the work you've done already
403
       for batch normalization.
404
405
406

    dout: Upstream derivatives, of shape (N, D)

407

    cache: Variable of intermediates from layernorm forward.

408
409
       Returns a tuple of:
410
       - dx: Gradient with respect to inputs x, of shape (N, D)
411

    dgamma: Gradient with respect to scale parameter gamma, of shape (D,)

412
413
        dbeta: Gradient with respect to shift parameter beta, of shape (D,)
414
415
      dx, dgamma, dbeta = None, None, None
      416
      # TODO: Implement the backward pass for layer norm.
                                                                              #
417
                                                                               #
418
      # HINT: this can be done by slightly modifying your training—time
419
      \# implementation of batch normalization . The hints to the forward pass
420
      # still apply!
421
      422
      # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
423
424
      sample normalized, gamma, beta, sample mean, sample var, x, eps = cache
425
426
      # The calculation of dgamma and dbeta remain the same
427
      dgamma = np.sum(dout * sample_normalized, axis = 0)
428
      dbeta = np.sum(dout, axis = 0)
429
      dx hat = dout * gamma
431
432
      \# At first transpose sample_normalized, 	imes and dx_hat so that their dimensions are all (D, N) now
433
      sample\_normalized = sample\_normalized.T
434
       \times = \times .T
435
      dx hat = dx hat.T
436
437
438
      # Actually x.shape[0] should be D now, but I still use N so that the code below don't have to be
439
      changed
      N = x.shape[0]
440
      \# The following calculation can be the same as they are in <code>batchnorm_backward</code>
442
       dvar = np.sum(dx hat * (x - sample mean) * (-1 / 2) * (sample var + eps) * (-3 / 2), axis = 0
443
      dmean = np.sum(np.divide(-dx hat, np.sqrt(sample var + eps)), axis = 0) + dvar * np.sum(-2 * (x - eps))
444
      sample mean), a \times is = 0)/ N
      dx = dx_hat / np.sqrt(sample_var + eps) + dvar * 2 * (x - sample_mean) / N + dmean / N
445
446
      \# Transpose dx so that dx can have the correct dimension (N, D) now
447
      dx = dx . T
448
```

```
450
451
     # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
452
     453
                              END OF YOUR CODE
454
     455
     return dx, dgamma, dbeta
456
457
458
     dropout forward(x, dropout param):
459
460
461
     Performs the forward pass for (inverted) dropout.
462
     Inputs:
463

    x: Input data, of any shape
    dropout_param: A dictionary with the following keys:

464
465

    p: Dropout parameter. We keep each neuron output with probability p

466
       mode: 'test' or 'train'. If the mode is train, then perform dropout;
467
468
         if the mode is test, then just return the input.
        seed: Seed for the random number generator. Passing seed makes this
469
         function deterministic, which is needed for gradient checking but not
470
        in real networks
471
472
473
     Outputs:
     - out: Array of the same shape as \times.
474
       cache: tuple (dropout param, mask). In training mode, mask is the dropout
475
       mask that was used to multiply the input; in test mode, mask is None.
476
477
     NOTE: Please implement **inverted** dropout, not the vanilla version of dropout
478
     See http://cs231n.github.io/neural-networks-2/#reg for more details.
479
480
     NOTE 2: Keep in mind that p is the probability of **keep** a neuron
481
     output; this might be contrary to some sources, where it is referred to
482
483
     as the probability of dropping a neuron output.
484
     p, mode = dropout param['p'], dropout param['mode']
485
        'seed' in dropout_param:
486
487
        np.random.seed(dropout param['seed'])
488
     mask = None
489
     out = None
490
491
      if mode == 'train':
492
        493
        # TODO: Implement training phase forward pass for inverted dropout
494
        # Store the dropout mask in the mask variable
495
        496
        # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
497
498
         mask = (np.random.rand(*x.shape) < p) / p
499
        out = x * mask
500
501
        # *****FND OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
502
        503
        505
      elif mode == 'test':
506
        507
        # TODO: Implement the test phase forward pass for inverted dropout
508
        # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
510
511
512
         out = x
513
        # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
514
        515
                                END OF YOUR CODE
        517
518
     cache = (dropout_param, mask)
519
     out = out.astype(x.dtype, copy=False)
520
521
     return out, cache
522
523
524
```

```
def dropout backward(dout, cache):
525
526
      Perform the backward pass for (inverted) dropout.
527
528
529
530

    dout: Upstream derivatives, of any shape

       cache: (dropout param, mask) from dropout forward.
531
532
      dropout param, mask = cache
533
      mode = dropout param['mode']
534
535
      dx = None
536
      if mode == 'train':
537
         538
         # TODO: Implement training phase backward pass for inverted dropout
                                   540
         # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
541
542
         dx = dout * mask
543
544
         # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
545
         546
                                  END OF YOUR CODE
547
548
         elif mode == 'test':
549
         dx = dout
550
      return dx
551
552
553
  def conv_forward_naive(x, w, b, conv_param):
554
555
      A naive implementation of the forward pass for a convolutional layer
556
557
      The input consists of N data points, each with C channels, height H and
558
      width W. We convolve each input with F different filters, where each filter
559
      spans all C channels and has height HH and width WW.
560
561
562
563
      x: Input data of shape (N, C, H, W)
      w: Filter weights of shape (F, C, HH, WW)
564
565
       b: Biases, of shape (F,)

    conv param: A dictionary with the following keys:

566
         'stride': The number of pixels between adjacent receptive fields in the
567
         horizontal and vertical directions
         'pad': The number of pixels that will be used to zero-pad the input.
569
570
571
      During padding, 'pad' zeros should be placed symmetrically (i.e equally on both sides)
572
573
      along the height and width axes of the input. Be careful not to modfiy the original
      input x directly
574
575
      Returns a tuple of:
576
       out: Output data, of shape (N, F, H', W') where H' and W' are given by
577
        H' = 1 + (H + 2 * pad - HH) / stride
578
       W' = 1 + (W + 2 * pad - WW) / stride
579
580
       cache: (x, w, b, conv param)
581
582
      583
      # TODO: Implement the convolutional forward pass.
584
             you can use the function np.pad for padding
585
      586
587
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
588
      stride = conv param['stride']
589
      pad = conv param['pad']
590
      x_{pad} = np.pad(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), 'constant')
591
      N, C, H, W = x.shape
      F, C, HH, WW = w.shape
593
594
      H \text{ out} = int (1 + (H + 2 * pad - HH) / stride)
595
      W out = int (1 + (W + 2 * pad - WW) / stride)
596
597
      out = np.zeros((N, F, H_out, W_out))
598
599
      for n in range (N):
600
```

```
for f in range(F):
601
             for i in range(H out):
602
                 for j in range(W out):
603
                    \operatorname{out}[n, f, i, j] = \operatorname{np.sum}(x_{pad}[n, :, i * stride: i * stride + HH, j * stride: j *
604
      stride + WW] * w[f]) + b[f]
605
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
606
      607
                                 END OF YOUR CODE
608
      609
      cache = (x, w, b, conv param)
610
      return out, cache
611
612
613
     conv backward naive(dout, cache):
614
615
      A naive implementation of the backward pass for a convolutional layer.
616
617
      Inputs:
618
619

    dout: Upstream derivatives

      - cache: A tuple of (x, w, b, conv param) as in conv forward naive
620
621
      Returns a tuple of:
622
      — dx: Gradient with respect to x
623
624

    dw: Gradient with respect to w

       db: Gradient with respect to b
625
626
      dx, dw, db = None, None, None
627
      628
      # TODO: Implement the convolutional backward pass.
629
      630
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
631
632
      x, w, b, conv_param = cache
633
634
      pad = conv param['pad']
      stride = conv_param['stride']
635
      F, C, HH, WW = w.shape
636
      N, C, H, W = x.shape
637
638
      H 	ext{ out} = int (1 + (H + 2 * pad - HH) / stride)
      W_{out} = int (1 + (W + 2 * pad - WW) / stride)
639
      x_{pad} = np.pad(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), 'constant')
640
641
      dx pad = np.zeros like(x pad)
642
      dw = np.zeros_like(w)
643
      db = np.zeros like(b)
644
645
      \# To calculte db, just sum up all the upstream gradients for each filters bias.
646
      for f in range(F):
647
         db[f] = np.sum(dout[:, f, :, :])
648
649
      for n in range(N):
650
          for f in range(F):
651
             for i in range(H out):
652
653
                 for j in range(W_out):
                    \# According to chain rule, dw = dout * x, dx = dout * w. Be careful about the
654
                    dw[f] += dout[n, f, i, j] * x pad[n, :, i * stride: i * stride + HH, j * stride: j *
655
      stride + WW
                    dx_pad[n, :, i * stride: i * stride + HH, j * stride: j * stride + WW] += dout[n, f, i]
656
      , j] * w[f]
657
      # Get rid of the pad around dx
658
659
      dx = dx pad[:, :, pad: pad+H, pad: pad+W]
660
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
661
      662
                                 END OF YOUR CODE
663
      664
      return dx, dw, db
665
666
667
      max pool forward naive(x, pool param):
668
669
      A naive implementation of the forward pass for a max-pooling layer.
670
671
      Inputs:
672
```

```
- x: Input data, of shape (N, C, H, W)
673
       pool param: dictionary with the following keys:
674
          'pool_height': The height of each pooling region 'pool width': The width of each pooling region
675
676

    'stride': The distance between adjacent pooling regions

677
678
      No padding is necessary here. Output size is given by
679
680
      Returns a tuple of:
681
       out: Output data, of shape (N, C, H', W') where H' and W' are given by
682
        H' = 1 + (H - pool\_height) / stride

W' = 1 + (W - pool\_width) / stride
683
684
685
        cache: (x, pool param)
686
      out = None
      688
      # TODO: Implement the max-pooling forward pass
689
      690
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
691
692
      pool_height = pool_param['pool_height']
693
      pool width = pool param['pool width']
694
      stride = pool_param['stride']
695
      N, C, H, W = x.shape
696
697
      H_{out} = int (1 + (H - pool_height) / stride)
698
      W out = int (1 + (W - pool width) / stride)
699
700
      out = np.zeros((N, C, H out, W out))
701
702
      for n in range(N):
703
          for c in range(C):
704
              for i in range(H out):
705
                  for j in range(W out):
706
707
                      \operatorname{out}[n, c, i, j] = \operatorname{np.max}(x[n, c, i * stride: i * stride + pool height, j * stride: j *
       stride + pool_width])
708
709
710
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
      711
                                   END OF YOUR CODE
712
      713
      cache = (x, pool_param)
714
      return out, cache
715
716
717
   def max_pool_backward_naive(dout, cache):
718
719
      A naive implementation of the backward pass for a max-pooling layer.
720
721
722
       dout: Upstream derivatives
723
      - cache: A tuple of (x, pool param) as in the forward pass.
724
725
      Returns:
726
727

    dx: Gradient with respect to x

728
729
      730
      # TODO: Implement the max-pooling backward pass
731
      732
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
733
734
735
      x, pool param = cache
      pool_height = pool_param['pool_height']
736
      pool_width = pool_param['pool_width']
737
      stride = pool param['stride']
738
      N, C, H, W = x.shape
739
740
      \begin{array}{lll} H\_out = int & (1 + (H - pool\_height) / stride) \\ W\_out = int & (1 + (W - pool\_width) / stride) \end{array}
741
742
743
      dx = np.zeros_like(x)
744
745
      for n in range(N):
746
          for c in range(C):
747
```

```
for i in range(H out):
748
                 for j in range(W out):
749
                     block = x[n, c, i * stride: i * stride + pool height, j * stride: j * stride +
      pool_width]
                     maximum = np.max(block)
751
                     dx[n, c, i * stride: i * stride + pool height, j * stride: j * stride + pool width] =
752
                                                                            (block == maximum) * dout[
      n, c, i, j]
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
755
      756
                                 END OF YOUR CODE
757
      758
      return dx
760
761
     spatial batchnorm forward(x, gamma, beta, bn param):
762
763
764
      Computes the forward pass for spatial batch normalization.
765
      Inputs:
766
      - \times: Input data of shape (N, C, H, W)
767
       gamma: Scale parameter, of shape (C,)
768
       beta: Shift parameter, of shape (C,)
769
      - bn_param: Dictionary with the following keys:
- mode: 'train' or 'test'; required
770
771
         eps: Constant for numeric stability
772
        - momentum: Constant for running mean / variance. momentum=0 means that
773
         old information is discarded completely at every time step, while
774
         momentum=1 means that new information is never incorporated. The
775
          default of momentum=0.9 should work well in most situations
776
        - running mean: Array of shape (D,) giving running mean of features
777
        - running var Array of shape (D,) giving running variance of features
778
779
      Returns a tuple of:
780
      out: Output data, of shape (N, C, H, W)
781
       cache: Values needed for the backward pass
782
783
      out, cache = None, None
784
785
      786
      # TODO: Implement the forward pass for spatial batch normalization.
787
                                                                          #
788
      # HINT: You can implement spatial batch normalization by calling the
789
      # vanilla version of batch normalization you implemented above
790
      # Your implementation should be very short; ours is less than five lines.
791
      792
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
793
794
      N, C, H, W = x.shape
795
796
      # Transpose x so that the shape is (N, H, W, C), then reshape x into (N * H * W, C)
797
      x_new = np.reshape(x.transpose(0, 2, 3, 1), (N * H * W, C))
798
      out, cache = batchnorm forward (x \text{ new}, \text{ gamma}, \text{ beta}, \text{ bn param})
799
      # Modify the final output
801
      out = np.transpose(out.reshape(N, H, W, C), (0, 3, 1, 2))
802
803
804
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
805
      806
807
                                 END OF YOUR CODE
      808
809
      return out, cache
810
811
812
      spatial batchnorm backward(dout, cache):
813
814
      Computes the backward pass for spatial batch normalization.
815
816
817
      Inputs:

    dout: Upstream derivatives, of shape (N, C, H, W)

818
        cache: Values from the forward pass
819
820
```

```
Returns a tuple of:
821

    dx: Gradient with respect to inputs, of shape (N, C, H, W)

822

    dgamma: Gradient with respect to scale parameter, of shape (C,)

823
       dbeta: Gradient with respect to shift parameter, of shape (C,)
824
825
      dx, dgamma, dbeta = None, None, None
826
827
      828
      # TODO: Implement the backward pass for spatial batch normalization.
829
830
      # HINT: You can implement spatial batch normalization by calling the
831
        vanilla version of batch normalization you implemented above.
832
833
      \# Your implementation should be very short; ours is less than five lines. \#
      834
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
835
836
837
      N, C, H, W = dout.shape
838
      dout new = np.reshape(dout.transpose(0, 2, 3, 1), (N * H * W, C))
839
840
      dx, dgamma, dbeta = batchnorm_backward(dout_new, cache)
      dx = np.transpose(dx.reshape(\overline{N}, H, W, C), (\overline{0}, 3, 1, 2))
841
842
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
843
      844
                                  END OF YOUR CODE
845
      846
      return dx, dgamma, dbeta
848
849
850
      spatial groupnorm forward(x, gamma, beta, G, gn param):
851
852
      Computes the forward pass for spatial group normalization
853
      In contrast to layer normalization, group normalization splits each entry
854
855
      in the data into G contiguous pieces, which it then normalizes independently
      Per feature shifting and scaling are then applied to the data, in a manner identical to that of batch
856
      normalization and layer normalization.
857
858
      - \times: Input data of shape (N, C, H, W)
859
       gamma: Scale parameter, of shape (C,)
860
        beta: Shift parameter, of shape (C,)
861
      - G: Integer mumber of groups to split into, should be a divisor of C
862
      — gn_param: Dictionary with the following keys:
863
        - eps: Constant for numeric stability
864
865
      Returns a tuple of:
866

    out: Output data, of shape (N, C, H, W)

867
868

    cache: Values needed for the backward pass

869
      out, cache = None, None
870
      eps = gn_param.get('eps',1e-5)
871
      872
873
      \# TODO: Implement the forward pass for spatial group normalization.
        This will be extremely similar to the layer norm implementation.
874
875
      \# In particular, think about how you could transform the matrix so that
      # the bulk of the code is similar to both train—time batch normalization
876
      # and layer normalization!
877
      878
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
879
880
881
882
      N, C, H, W = x.shape
883
      \# Just reshape 	imes so that the number of group is multiplied by {\sf G} while {\sf C} is divided by {\sf G}
884
      x = np.reshape(x, (N * G, C // G * H * W))
885
886
      # Other code are basically copied from layer norm implementation
887
888
      \times = \times .T
      sample mean = np.mean(x, axis = 0)
889
890
      sample var = np.var(x, axis = 0)
      sample normalized = (x - sample mean) / np.sqrt(sample var + eps)
891
892
      sample\_normalized = np.reshape(sample\_normalized.T, (N, C, H, W))
893
      out = gamma * sample_normalized + beta
      x = np.reshape(x.T, (N, C, H, W))
895
```

```
cache = (sample normalized, gamma, beta, sample mean, sample var, x, eps, G)
897
898
899
900
                # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
901
                902
                                                                                    END OF YOUR CODE
903
                904
                return out, cache
906
907
               spatial groupnorm backward(dout, cache):
908
909
                Computes the backward pass for spatial group normalization.
910
911
912
                Inputs:

    dout: Upstream derivatives, of shape (N, C, H, W)

913
                 - cache: Values from the forward pass
914
915
                Returns a tuple of:
916
917
                   dx: Gradient with respect to inputs, of shape (N, C, H, W)
                - dgamma: Gradient with respect to scale parameter, of shape (C,)
918
919
                   dbeta: Gradient with respect to shift parameter, of shape (C,)
920
                dx, dgamma, dbeta = None, None, None
921
922
                923
                # TODO: Implement the backward pass for spatial group normalization.
924
                \overset{\prime\prime}\# This will be extremely similar to the layer norm implementation.
925
                926
                # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
927
928
                sample normalized, gamma, beta, sample mean, sample var, x, eps, G = cache
930
               N, C, H, W = x.shape
931
                # Remember to keep dimensions of dgamma and dbeta unchanged
932
               dgamma = np.sum(dout * sample normalized, axis = (0, 2, 3), keepdims=True)
933
                dbeta = np.sum(dout, axis = (0, 2, 3), keepdims=True)
                dx_hat = dout * gamma
935
936
                # Reshape those matrices at first, then transpose them
937
                sample normalized = np.reshape(sample normalized, (N * G, C // G * H * W))
938
                x = np.reshape(x, (N * G, C // G * H * W))
939
                dx\_hat = np.reshape(dx\_hat, (N * G, C // G * H * W))
940
941
                sample_normalized = sample_normalized.T
942
                x = x.\overline{T}
943
                dx hat = dx hat.T
944
945
                 # The following calculation is quite similar to layer norm backward
946
               N new = \times.shape [0]
947
948
                dvar = np.sum(dx_hat * (x - sample_mean) * (-1 / 2) * (sample_var + eps)**(-3 / 2), axis = 0)
949
                dmean = np.sum(np.divide(-dx_hat, np.sqrt(sample_var + eps)), axis = 0) + (available of the context of the co
950
                                   dvar * np.sum(-2 * (x - sample mean), axis = 0) / N new
                dx = dx_hat / np.sqrt(sample_var + eps) + dvar * 2 * (x - sample_mean) / N_new + dmean / N_n
952
953
                dx = np.reshape(dx.T, (N, C, H, W))
954
955
                # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
956
               957
958
                                                                                     END OF YOUR CODE
                959
                return dx, dgamma, dbeta
960
961
962
       def svm loss(x, y):
963
964
                Computes the loss and gradient using for multiclass SVM classification.
965
966
                Inputs:
967
                - x: Input data, of shape (N, C) where 	imes [\, i\,\, ,\,\, j\,\,] is the score for the jth
968
                    class for the ith input
969
                    y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
                    0 \le y[i] < C
971
```

```
972
        Returns a tuple of:
973
        – loss: Scalar giving the loss
974
         dx: Gradient of the loss with respect to x
975
976
977
        N = x.shape[0]
        correct class\_scores = x[np.arange(N), y]
978
        margins = np.maximum(0, x - correct\_class\_scores[:, np.newaxis] + 1.0)
979
        margins[np.arange(N), y] = 0
980
        loss = np.sum(margins) / N
981
        num pos = np.sum(margins > 0, axis=1)
982
        dx = np.zeros like(x)
983
        dx[margins > \overline{0}] = \hat{1}
984
        dx[np.arange(N), y] = num_pos
985
986
        dx /= N
        return\ loss\ ,\ dx
987
988
989
    def softmax_loss(x, y):
990
991
        Computes the loss and gradient for softmax classification.
992
993
994
995
        - x: Input data, of shape (N, C) where x[i,j] is the score for the jth
          class for the ith input
996
        - y: Vector of labels , of shape (N,) where y[i] is the label for x[i] and
997
          0 \le y[i] < C
999
        Returns a tuple of:
1000

    loss: Scalar giving the loss

1001
          dx: Gradient of the loss with respect to x
1002
1003
        shifted_logits = x - np.max(x, axis=1, keepdims=True)
1004
        Z = np.sum(np.exp(shifted logits), axis=1, keepdims=True)
1005
1006
        log probs = shifted logits - np.log(Z)
        probs = np.exp(log_probs)
1007
1008
        N = x.shape[0]
        loss = -np.sum(log\_probs[np.arange(N), y]) / N
1009
1010
        dx = probs.copy()
        dx[np.arange(N), y] = 1
1011
        dx /= N
1012
        return loss, dx
1013
```

## 2 fc net.py

```
1 from builtins import range
2 from builtins import object
  import numpy as np
  from cs231n.layers import *
  from cs231n.layer utils import *
  class TwoLayerNet(object):
9
10
     A two-layer fully-connected neural network with ReLU nonlinearity and
11
      softmax loss that uses a modular layer design. We assume an input dimension
      of D, a hidden dimension of H, and perform classification over C classes.
13
14
      The architecure should be affine - relu - affine - softmax.
15
16
17
      Note that this class does not implement gradient descent; instead, it
      will interact with a separate Solver object that is responsible for running
18
      optimization.
19
20
      The learnable parameters of the model are stored in the dictionary
21
      self.params that maps parameter names to numpy arrays.
22
23
24
      \label{lem:def_init} $$ def_{init_i}(self, input_dim=3*32*32, hidden_dim=100, num_classes=10, 
25
                 weight scale=1e-3, reg=0.0):
26
27
         Initialize a new network
28
29
30
         Inputs:
         - input dim: An integer giving the size of the input
31
32
         hidden_dim: An integer giving the size of the hidden layer
          num_classes: An integer giving the number of classes to classify
33
          weight scale: Scalar giving the standard deviation for random
34
           initialization of the weights.
35
          reg: Scalar giving L2 regularization strength.
37
         self.params = \{\}
38
         self.reg = reg
39
40
         41
         # TODO: Initialize the weights and biases of the two-layer net. Weights
42
         # should be initialized from a Gaussian centered at 0.0 with
43
                                                                             #
         # standard deviation equal to weight_scale, and biases should be
44
         # initialized to zero. All weights and biases should be stored in the
45
         # dictionary self.params, with first layer weights
         # and biases using the keys 'W1' and 'b1' and second layer
47
         # weights and biases using the keys 'W2' and 'b2
48
         49
         # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
50
51
         # Weights is initialized from a Gaussian centered at 0.0 with standard deviation equal to
52
         # Use np.random.normal function
53
         self.params [W1'] = np.random.normal(0.0, weight scale, (input dim, hidden dim))
54
         self.params['b1'] = np.zeros((1, hidden_dim))
55
         56
57
58
         # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
59
         60
                                    END OF YOUR CODE
61
         62
63
      def loss(self, X, y=None):
65
66
         Compute loss and gradient for a minibatch of data.
67
68
         Inputs:
         - X: Array of input data of shape (N, d_1, \ldots, d_k)
70
71
          y: Array of labels, of shape (N,). y[i] gives the label for X[i].
72
```

```
If y is None, then run a test-time forward pass of the model and return:
     scores: Array of shape (N, C) giving classification scores,
    scores [i, c] is the classification score for X[i] and class c.
   If y is not None, then run a training—time forward and backward pass and
   return a tuple of
    loss: Scalar value giving the loss
    grads: Dictionary with the same keys as self.params, mapping parameter
    names to gradients of the loss with respect to those parameters.
   # TODO: Implement the forward pass for the two-layer net, computing the
   # class scores for X and storing them in the scores variable
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
   W1, b1 = self.params['W1'], self.params['b1']
   W2, b2 = self.params['W2'], self.params['b2']
   # Firstly, do the affine relu forward pass to get the hidden layer
   hidden1, cache1 = affine_relu_forward(X, W1, b1)
   # Secondly, do the affine forward pass
   out, cache2 = affine_forward(hidden1, W2, b2)
   scores = out
   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
   END OF YOUR CODE
   # If y is None then we are in test mode so just return scores
   if y is None:
      return scores
   loss, grads = 0, \{\}
                  <del>.</del>
   # TODO: Implement the backward pass for the two-layer net. Store the loss #
   \# in the loss variable and gradients in the grads dictionary. Compute data \#
   # loss using softmax, and make sure that grads[k] holds the gradients for
   # self.params[k]. Don't forget to add L2 regularization!
   # NOTE: To ensure that your implementation matches ours and you pass the
   # automated tests, make sure that your L2 regularization includes a factor #
   # of 0.5 to simplify the expression for the gradient.
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
   # Use softmax to calculate the loss and gradient dout.
   loss, dout = softmax loss(scores, y)
   \# Based on the upstream gradient dout, use affine_backward to get the first downstream gradient.
   dX2, dW2, db2 = affine backward(dout, cache2)
   # Based on the first downstream gradient dX2, use affine relu backward to get the second
downstream gradient
   dX1, dW1, db1 = affine relu backward(dX2, cache1)
   loss += 0.5 * self.reg * (np.sum(W1 * W1) + np.sum(W2 * W2))
   dW2 += self.reg * W2
   dW1 += self.reg * W1
   grads['W1'] = dW1
   grads['b1'] = db1
   grads['W2'] = dW2
   grads['b2'] = db2
   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
   END OF YOUR CODE
```

74

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131 132

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135

136 137

138

139

140

141 142 143

145

146

```
148
149
                  return loss, grads
151
152
153
     class FullyConnectedNet(object):
154
            A fully—connected neural network with an arbitrary number of hidden layers ,
155
           ReLU nonlinearities, and a softmax loss function. This will also implement
156
            dropout and batch/layer normalization as options. For a network with L layers,
157
158
            the architecture will be
159
            \{\mathsf{affine} - [\mathsf{batch/layer} \ \mathsf{norm}] - \mathsf{relu} - [\mathsf{dropout}]\} 	imes (\mathsf{L}-1) - \mathsf{affine} - \mathsf{softmax} \}
160
161
            where \mathsf{batch/layer} normalization and dropout are optional, and the \{\ldots\} block is
162
            repeated L-1 times.
163
164
            Similar to the TwoLayerNet above, learnable parameters are stored in the
165
            self.params dictionary and will be learned using the Solver class.
166
167
168
            \label{lem:def_init} $$ def __init__(self, hidden_dims, input_dim=3*32*32, num_classes=10, 
169
                                 dropout=1, normalization=None, reg=0.0,
170
                                 weight scale=1e-2, dtype=np.float32, seed=None):
171
172
                  Initialize a new FullyConnectedNet.
173
174
175
                  Inputs:
                   – hidden dims: A list of integers giving the size of each hidden layer.
176
177
                  input_dim: An integer giving the size of the input.
                     num_classes: An integer giving the number of classes to classify.
178
                     dropout: Scalar between 0 and 1 giving dropout strength. If dropout=1 then
179
                     the network should not use dropout at all
180
                     normalization: What type of normalization the network should use. Valid values
181
                     are "batchnorm", "layernorm", or None for no normalization (the default).
182
                     reg: Scalar giving L2 regularization strength.
183
                      weight_scale: Scalar giving the standard deviation for random
184
                     initialization of the weights.
185
                    dtype: A numpy datatype object; all computations will be performed using
186
                     this datatype. float32 is faster but less accurate, so you should use
187
                      float64 for numeric gradient checking
188
                     seed: If not None, then pass this random seed to the dropout layers. This
189
                     will make the dropout layers deteriminstic so we can gradient check the
190
                     model.
191
192
                  self.normalization = normalization
193
                  self.use_dropout = dropout != 1
194
                  self.reg = reg
195
196
                  self.num layers = 1 + len(hidden dims)
                  self.dtype = dtype
197
                  self.params = \{\}
198
199
                  200
201
                  # TODO: Initialize the parameters of the network, storing all values in
                  \# the <code>self.params</code> dictionary. Store weights and biases for the first layer \#
202
203
                  # in W1 and b1; for the second layer use W2 and b2, etc. Weights should be
                  # initialized from a normal distribution centered at 0 with standard
204
                  # deviation equal to weight scale. Biases should be initialized to zero
205
206
                  \# When using batch normalization, store scale and shift parameters for the \# first layer in gamma1 and beta1; for the second layer use gamma2 and
207
208
                  # beta2, etc. Scale parameters should be initialized to ones and shift
209
210
                  # parameters should be initialized to zeros
                  211
                  # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
212
213
                  all dims = [input dim] + hidden_dims + [num_classes]
214
                  for i in range (len (all dims) -1):
215
                         self.params[\ 'W' \ + \ str(i \ + \ 1)] = np.random.normal(0.0, \ weight\_scale, \ (all\_dims[i], \ all\_dims[i] \ + \ (all\_dims[i], \ all\_dims[i], \ all\_dim
216
             1]))
                         self.params['b' + str(i + 1)] = np.zeros((1, all dims[i + 1]))
217
218
                        \# If we haven't reached the final output layer, there may be a normalization layer
                         if i = self.num layers -1:
220
                                if self.normalization != None:
221
                                      self.params['gamma' + str(i + 1)] = np.ones((1, all_dims[i + 1]))
222
```

```
self.params['beta' + str(i + 1)] = np.zeros((1, all dims[i + 1]))
   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
   END OF YOUR CODE
   # When using dropout we need to pass a dropout param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout param to each dropout layer.
   self.dropout param = \{\}
   if self.use dropout:
       self.dropout_param = {'mode': 'train', 'p': dropout}
       if seed is not None:
          self.dropout_param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   \# variances, so we need to pass a special bn param object to each batch
   # normalization layer. You should pass self.bn params[0] to the forward pass
   # of the first batch normalization layer, self.bn params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn params = []
   if self.normalization=='batchnorm':
       self.bn\_params = [\{ \ 'mode' \colon \ 'train' \} \ for \ i \ in \ range(self.num \ layers - 1)]
   if self normalization="layernorm":
       self.bn\_params = [\{\} for i in range(self.num\_layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
       self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   \# Set train/test mode for batchnorm params and dropout param since they
   # behave differently during training and testing.
   if self.use dropout:
       self.dropout_param['mode'] = mode
      self.normalization=='batchnorm'
       for bn_param in self.bn_params:
          bn param['mode'] = mode
   scores = None
   # TODO: Implement the forward pass for the fully—connected net, computing
   # the class scores for X and storing them in the scores variable
   # When using dropout, you'll need to pass self.dropout_param to each
   # dropout forward pass.
   # When using batch normalization, you'll need to pass self.bn params[0] to
   # the forward pass for the first batch normalization layer, pass
   \# self.bn_params[1] to the forward pass for the second batch normalization \#
   # laver. etc
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
   affine cache = \{\}
   norm cache = \{\}
   relu cache = \{\}
   dropout cache = \{\}
   input param = X
   for i in range (self.num layers -1):
      W, b = self.params['W' + str(i + 1)], self.params['b' + str(i + 1)]
       if self.normalization == 'batchnorm':
          # the first part is affine — batchnorm — relu
```

225

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281

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284 285 286

287

288

289

291 292

293

294

296

297

```
affine outcome, affine cache [i + 1] = affine forward (input param, W, b)
299
                                  norm\_outcome, norm\_cache[i+1] = batchnorm\_forward(affine\_outcome, gamma, beta, self.
300
            bn params[i])
                                  relu_outcome, relu_cache[i + 1] = relu_forward(norm_outcome)
301
302
303
                           elif self.normalization == 'layernorm':
                                 # the first part is affine
                                                                                  layernorm — relu
304
                                  gamma, beta = self.params['gamma' + str(i + 1)], self.params['beta' + str(i + 1)]
305
                                  affine outcome, affine cache[i + 1] = affine forward(input_param, W, b)
306
                                  norm outcome, norm cache [i + 1] = layernorm forward (affine outcome, gamma, beta, self.
307
            bn params[i])
                                  relu_outcome, relu_cache[i + 1] = relu_forward(norm_outcome)
308
309
                           else:
310
                                 # the first part is affine — relu
311
                                  {\sf relu\_outcome} \;,\; ({\sf affine\_cache} [\; i \; + \; 1] \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf relu\_cache} [\; i \; + \; 1]) \; = \; {\sf affine\_relu\_forward} ({\sf input\_param} \;,\; {\sf input\_param} \;,\; 
312
            W, b)
313
                           if self.use dropout:
314
315
                                 dropout outcome, dropout cache [i + 1] = dropout forward (relu outcome, self.dropout param)
316
                           # Update input
317
                          input_param = dropout_outcome if self.use_dropout else relu_outcome
318
319
                   # Get the last layer
320
                   scores, last cache = affine_forward(input_param,
321
                                                                                      self.params['W'+str(self.num layers)],
322
                                                                                      self.params['b'+str(self.num_layers)])
323
324
                   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
325
                   326
                                                                         END OF YOUR CODE
327
                   328
329
330
                   # If test mode return early
                    if mode == 'test':
331
332
                           return scores
333
334
                   loss, grads = 0.0, \{\}
                                                       <del>.</del>
335
                   \# TODO: Implement the backward pass for the fully—connected net. Store the \#
336
337
                   \# loss in the loss variable and gradients in the grads dictionary. Compute \#
                   # data loss using softmax, and make sure that grads[k] holds the gradients #
338
                   # for self.params[k]. Don't forget to add L2 regularization!
340
                   # When using batch/layer normalization, you don't need to regularize the scale
341
                   # and shift parameters.
342
343
344
                   # NOTE: To ensure that your implementation matches ours and you pass the
                   # automated tests, make sure that your L2 regularization includes a factor
                                                                                                                                                        #
345
                   # of 0.5 to simplify the expression for the gradient
346
                   347
                   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
348
340
                   # Use softmax to calculate the loss and gradient dout.
350
351
                   loss, dout = softmax loss(scores, y)
352
353
                    reg loss = 0
                   for i in range(self.num_layers):
354
                          reg loss += 0.5 * self.reg * np.sum(np.square(self.params['W' + str(i+1)]))
355
                    loss += reg_loss
357
358
                   \# Based on the upstream gradient dout, use affine backward to get the first downstream gradient.
359
                   dX, dW, db = affine backward(dout, last cache)
360
                   dW += self.reg * self.params['W' + str(self.num layers)]
361
                   grads['W'+str(self.num layers)] = dW
362
                    grads['b'+str(self.num layers)] = db
363
364
                    for i in range (self.num layers -1, 0, -1):
365
366
                           if self.use_dropout:
                                     If there is a dropout at the end
367
                                  dX = dropout\_backward(dX, dropout\_cache[i])
369
                          dX = relu \ backward(dX, relu \ cache[i])
370
371
```

```
if self.normalization == 'batchnorm':
372
                # If there is a batchnorm in the middle
373
374
                dX, dgamma, dbeta = batchnorm backward(<math>dX, norm cache[i])
                grads['gamma'+str(i)] = dgamma
375
                grads['beta'+str(i)] = dbeta
376
             elif self.normalization == 'layernorm':
377
                # If there is a layernorm in the middle
378
                dX, dgamma, dbeta = layernorm_backward(dX, norm_cache[i])
379
                grads['gamma'+str(i)] = dgamma
380
                grads['beta'+str(i)] = dbeta
381
382
             dX, dW, db = affine_backward(dX, affine_cache[i])
383
384
             dW += self.reg * self.params['W' + str(i)]
385
             grads['W'+str(i)] = dW
387
             grads['b'+str(i)] = db
388
389
390
         # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
391
         392
393
                                    END OF YOUR CODE
         394
395
         return loss, grads
396
```

## 3 optim.py

```
1 import numpy as np
  0.00
  This file implements various first-order update rules that are commonly used
5 for training neural networks. Each update rule accepts current weights and the
6 gradient of the loss with respect to those weights and produces the next set of
  weights. Each update rule has the same interface:
  def update(w, dw, config=None):
10
11 Inputs:
12
    - w: A numpy array giving the current weights
    - dw: A numpy array of the same shape as w giving the gradient of the
13
      loss with respect to w.
14
      config: A dictionary containing hyperparameter values such as learning
15
      rate, momentum, etc. If the update rule requires caching values over many
16
      iterations, then config will also hold these cached values.
17
18
19
20

    next w: The next point after the update.

      config: The config dictionary to be passed to the next iteration of the
21
22
      update rule
23
24 NOTE: For most update rules, the default learning rate will probably not
25 perform well; however the default values of the other hyperparameters should
26
  work well for a variety of different problems.
28 For efficiency, update rules may perform in-place updates, mutating w and
  setting next w equal to w.
30
31
32
  def sgd(w, dw, config=None):
33
34
      Performs vanilla stochastic gradient descent.
35
36
      config format:
37
       learning_rate: Scalar learning rate.
38
39
      if config is None: config = \{\} config.setdefault('learning_rate', 1e-2)
40
41
42
      w -= config['learning rate'] * dw
43
44
      return w, config
45
46
      sgd momentum(w, dw, config=None):
47
48
      Performs stochastic gradient descent with momentum.
49
50
51
      config format:

    learning rate: Scalar learning rate.

52
      — momentum: Scalar between 0 and 1 giving the momentum value
53
        Setting momentum = 0 reduces to sgd.
54
        velocity: A numpy array of the same shape as w and dw used to store a
55
        moving average of the gradients
56
57
      if config is None: config = \{\}
58
      config.setdefault ('learning_rate', 1e-2) config.setdefault ('momentum', 0.9)
59
60
      v = config.get('velocity', np.zeros_like(w))
61
62
      next w = None
63
      64
      \# TODO: Implement the momentum update formula. Store the updated value in \#
65
      # the next w variable. You should also use and update the velocity v.
66
      67
68
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
69
      v = config['momentum'] * v - config['learning rate'] * dw
70
      w += v
71
72
      next w = w
73
```

```
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
74
      75
                                  END OF YOUR CODE
76
      77
      config['velocity'] = v
78
79
      return next w, config
80
81
82
83
   def rmsprop(w, dw, config=None):
84
85
86
      Uses the RMSProp update rule, which uses a moving average of squared
      gradient values to set adaptive per-parameter learning rates.
87
89
      config format:
        learning rate: Scalar learning rate.
90
      - decay rate: Scalar between 0 and 1 giving the decay rate for the squared
91
        gradient cache
92
93
      {	extstyle -} epsilon: Small scalar used for smoothing to avoid dividing by zero.
        cache: Moving average of second moments of gradients.
94
95
      if config is None: config = \{\}
96
      config.setdefault('learning rate', 1e-2)
97
      config.setdefault('decay_rate', 0.99)
98
      config.setdefault('epsilon', 1e-8)
config.setdefault('cache', np.zeros_like(w))
99
100
101
      next w = None
102
      103
      # TODO: Implement the RMSprop update formula, storing the next value of w #
104
      # in the next w variable. Don't forget to update cache value stored in
105
      # config['cache']
106
      107
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
108
109
      config['cache'] = config['decay_rate'] * config['cache'] + (1 - config['decay_rate']) * dw**2
110
      w += - config['learning_rate'] * dw / (np.sqrt(config['cache']) + config['epsilon'])
111
112
      next w = w
113
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
114
      115
                                  END OF YOUR CODE
116
      117
118
      return next w, config
119
120
121
      adam(w, dw, config=None):
122
123
      Uses the Adam update rule, which incorporates moving averages of both the
124
      gradient and its square and a bias correction term.
125
126
127
      config format:
        learning rate: Scalar learning rate.
128
129
        beta1: Decay rate for moving average of first moment of gradient

    beta2: Decay rate for moving average of second moment of gradient

130
       - epsilon: Small scalar used for smoothing to avoid dividing by zero.
131

    m: Moving average of gradient.

132
       v: Moving average of squared gradient.
133
        t: Iteration number
134
135
136
      if config is None: config = \{\}
      config.setdefault ('learning_rate', 1e-3) config.setdefault ('beta1', 0.9) config.setdefault ('beta2', 0.999)
137
138
139
      config.setdefault('epsilon', 1e-8)
140
      config.setdefault('m', np.zeros_like(w))
141
      config.setdefault('v', np.zeros_like(w))
config.setdefault('t', 0)
142
143
144
      next w = None
145
      146
      # TODO: Implement the Adam update formula, storing the next value of w in #
147
      \# the next w variable. Don't forget to update the m, v, and t variables
148
      # stored in config.
149
```

```
# NOTE: In order to match the reference output, please modify t before
151
152
      # using it in any calculations
      153
      # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
154
155
      \begin{array}{ll} m = \; config\left[\,{}^{\prime}m^{\prime}\,\right] \\ v = \; config\left[\,{}^{\prime}v^{\,\prime}\,\right] \end{array}
156
157
       beta1 = config['beta1']
158
       beta2 = config['beta2']
159
       learning_rate = config['learning_rate']
160
       epsilon = config['epsilon']
161
       t = config['t'] + 1
162
163
164
      m = beta1*m + (1-beta1)*dw
      mt = m / (1-beta1**t)
165
      v = beta2*v + (1-beta2)*(dw**2)
166
      vt = v / (1-beta2**t)
167
      w += - learning_rate * mt / (np.sqrt(vt) + epsilon)
168
169
      next_w = w
170
      config['m'] = m
config['v'] = v
config['t'] = t
171
172
173
174
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
175
      176
                                    END OF YOUR CODE
177
      178
179
       return next w, config
180
```

## 4 cnn.py

```
1 from builtins import object
  import numpy as np
4 from cs231n.layers import *
5 from cs231n.fast layers import *
6 from cs231n.layer utils import *
  class ThreeLayerConvNet(object):
10
      A three-layer convolutional network with the following architecture:
11
12
      conv - relu - 2x2 max pool - affine - relu - affine - softmax
13
14
      The network operates on minibatches of data that have shape (N, C, H, W)
15
      consisting of N images, each with height H and width W and with C input
16
      channels.
17
18
      def __init__(self, input_dim=(3, 32, 32), num_filters=32, filter size=7,
20
                  hidden dim=100, num classes=10, weight scale=1e-3, reg=0.0,
21
22
                  dtype=np.float32):
23
24
          Initialize a new network
25
26
         Inputs
          - input dim: Tuple (C, H, W) giving size of input data
27
          - num \overline{} filters: Number of filters to use in the convolutional layer
28
          filter_size: Width/height of filters to use in the convolutional layer
           hidden dim: Number of units to use in the fully-connected hidden layer
30
           num classes: Number of scores to produce from the final affine layer
31
         - weight scale: Scalar giving standard deviation for random initialization
32
           of weights.
33

    reg: Scalar giving L2 regularization strength

34
           dtype: numpy datatype to use for computation.
35
          self.params = \{\}
37
          self.reg = reg
38
          self.dtype = dtype
30
40
         41
         # TODO: Initialize weights and biases for the three-layer convolutional
42
         # network. Weights should be initialized from a Gaussian centered at 0.0
43
         # with standard deviation equal to weight_scale; biases should be
44
         # initialized to zero. All weights and biases should be stored in the
45
            dictionary self.params. Store weights and biases for the convolutional
46
         # layer using the keys 'W1' and 'b1'; use keys 'W2' and 'b2' for the
47
         # weights and biases of the hidden affine layer, and keys 'W3' and 'b3
48
         # for the weights and biases of the output affine layer.
                                                                                  #
49
50
         # IMPORTANT: For this assignment, you can assume that the padding
51
         # and stride of the first convolutional layer are chosen so that
52
         \# **the width and height of the input are preserved **. Take a look at
53
         # the start of the loss() function to see how that happens.
54
         55
         # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
56
57
         C, H, W = input dim
58
          self.params [ 'Wl' ] = weight\_scale * np.random.random(num\_filters, C, filter\_size, filter\_size) \\ self.params [ 'bl' ] = np.zeros((1, num\_filters))
59
60
61
         # 2x2 max pool reduces the width and height by half
          self.params['W2'] = weight scale * np.random.randn(num filters * H * W // (2 * 2), hidden dim)
63
          self.params['b2'] = np.zeros((1, hidden_dim))
64
65
          self.params['W3'] = weight scale * np.random.randn(hidden dim, num classes)
66
          self.params['b3'] = np.zeros((1, num classes))
67
68
         # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
69
         70
                                      END OF YOUR CODE
71
72
         73
```

```
for k, v in self.params.items():
 74
                        self.params[k] = v.astype(dtype)
 75
 77
           def loss(self , X , y=None):
 78
 79
                 Evaluate loss and gradient for the three-layer convolutional network
 80
 81
                 Input / output: Same API as TwoLayerNet in fc net.py.
 82
 83
                 W1, b1 = self.params['W1'], self.params['b1']
W2, b2 = self.params['W2'], self.params['b2']
 84
                                                         ], self.params[
 85
                 W3, b3 = self.params['W3'], self.params['b3']
 86
 87
                 # pass conv param to the forward pass for the convolutional layer
                 # Padding and stride chosen to preserve the input spatial size
 89
                 filter size = W1.shape[2]
 90
                 conv param = \{'stride': 1, 'pad': (filter size - 1) // 2\}
 91
 92
 93
                 # pass pool param to the forward pass for the max-pooling layer
                 pool param = {'pool height': 2, 'pool width': 2, 'stride': 2}
 94
 95
 96
                 scores = None
                 97
                 # TODO: Implement the forward pass for the three—layer convolutional net,
 98
                 # computing the class scores for X and storing them in the scores
99
100
101
                 # Remember you can use the functions defined in cs231n/fast layers.py and
102
                 # cs231n/layer_utils.py in your implementation (already imported).
103
                 104
                 # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
105
106
                 {\tt conv} \ \ {\tt relu} \ \ {\tt pool} \ \ {\tt outcome} \ , \ \ {\tt conv} \ \ {\tt relu} \ \ {\tt pool} \ \ {\tt forward} \ ({\tt X}, \ {\tt W1}, \ {\tt b1} \ , \ {\tt conv} \ \ {\tt param} \ ,
107
           pool param)
                 affine_relu_outcome, affine_relu_cache = affine_relu_forward(conv_relu_pool_outcome, W2, b2)
108
                 scores, last_cache = affine_forward(affine_relu_outcome, W3, b3)
109
110
111
                 # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
112
                 113
                                                                END OF YOUR CODE
114
                 115
                 if y is None:
117
                        return scores
118
119
                 loss, grads = 0, \{\}
120
                 121
                 # TODO: Implement the backward pass for the three-layer convolutional net, #
122
                 \# storing the loss and gradients in the loss and grads variables. Compute
123
                 \# data loss using softmax, and make sure that grads[k] holds the gradients \#
124
                 # for self.params[k]. Don't forget to add L2 regularization!
125
126
                 # NOTE: To ensure that your implementation matches ours and you pass the
127
128
                 # automated tests, make sure that your L2 regularization includes a factor
                 \# of 0.5 to simplify the expression for the gradient.
129
                 130
                 # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
131
132
                 loss, dout = softmax loss(scores, y)
133
                 reg\_loss = 0.5 * sel\overline{f}.reg * (np.sum(np.square(self.params['W1'])) + np.sum(np.square(self.params['w1'])) + np.sum(np.square(self.p
134
          W2'])) +
                                                                              np.sum(np.square(self.params['W3'])))
135
                 loss += reg loss
136
                 dX3, dW3, db3 = affine backward(dout, last cache)
137
                 dX2, dW2, db2 = affine relu backward(dX3, affine relu cache)
138
                 dX1, dW1, db1 = conv relu pool backward (dX2, conv relu pool cache)
139
140
                 dW1 += self.reg * self.params['W1'
141
                 dW2 += self.reg * self.params['W2']
142
                 dW3 += self.reg * self.params['W3']
143
                 grads['W1'] = dW1
grads['b1'] = db1
145
146
                 grads['W2'] = dW2
147
```

```
\begin{array}{l} \texttt{grads} \left[ \begin{tabular}{l} \mathsf{b2} \end{tabular} \right] &=& \mathsf{db2} \\ \texttt{grads} \left[ \begin{tabular}{l} \mathsf{W3} \end{tabular} \right] &=& \mathsf{dW3} \\ \texttt{grads} \left[ \begin{tabular}{l} \mathsf{b3} \end{tabular} \right] &=& \mathsf{db3} \end{array}
148
149
150
151
152
153
                 154
155
                                                                  END OF YOUR CODE
156
                  157
158
159
                 return loss, grads
```