LAB 3 CODE

December 13, 2020

- 0.1 Antony Sikorski PHYS 164 Fall 2020
- 0.1.1 Lab 3 Code
- 0.2 Loading in FITS files

```
[1]: import numpy as np
import matplotlib.pyplot as plt
from astropy.io import fits
import os
from numpy.linalg import inv
```

```
[2]: data_dir = './data_folder/'
data_files = np.array(sorted(os.listdir(data_dir)))
```

```
[3]: def load_headers_all_files(headers):
    #Reads and returns multiple FITS headers from all files.

output = np.full([len(headers), len(data_files)], "", dtype = object)

# Reads the headers from all files

i = 0
j = 0

for i, data_file in enumerate(data_files):
    h = fits.open(data_dir + data_file)
    for j, header_name in enumerate(headers):
        output[j, i] = h[0].header[header_name]
    h.close()

return output
```

```
fits_dataframe1=pandas.DataFrame(headers_lists, columns=headers)
fits_dataframe1
```

```
[4]:
      OBSTYPE
                             OBJECT EXPTIME FILTNAM COVER
    O OBJECT
                               bias
                                           0
                                                         32
                          flatfield
    1 OBJECT
                                           3
                                                   R
                                                         32
                                                         32
    2 OBJECT Parthenope - Group A
                                          30
                                                   R.
    3 OBJECT
                     flatfield_dark
                                           3
                                                   R
                                                         32
    4 OBJECT
                                          30
                                                         32
                         Parthenope
                                                   R.
```

0.3 Data Reduction

```
[5]: first_flat = data_files[objects == 'flatfield'][0]

def load_frame_overscan_remove_bias_subtract(filename):

    # simply modified reduction function from the last lab
    flat = fits.getdata(data_dir+filename)
    bias = fits.getdata(data_dir+data_files[0])*1.000000001
    flat=flat-bias
    image = flat[:,:1024]

    return image
```

```
[6]: def plot_fits_im(ax, data, xlabel='x (px)', ylabel='y (px)', title='', 

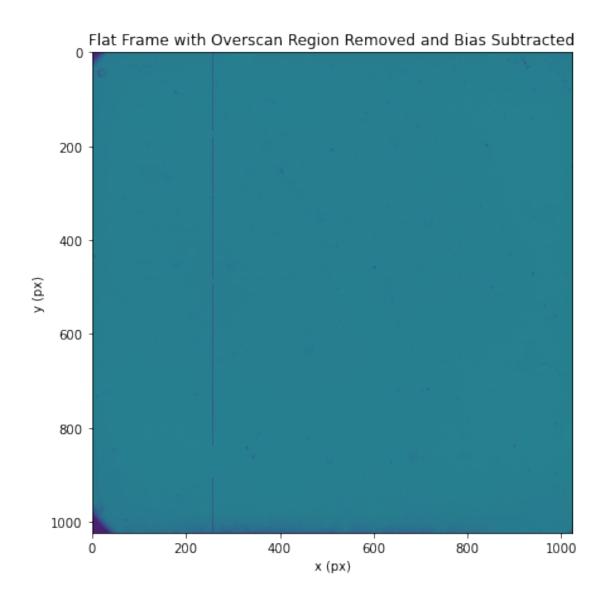
→**imshow_kwargs):

ax.imshow(data, **imshow_kwargs)

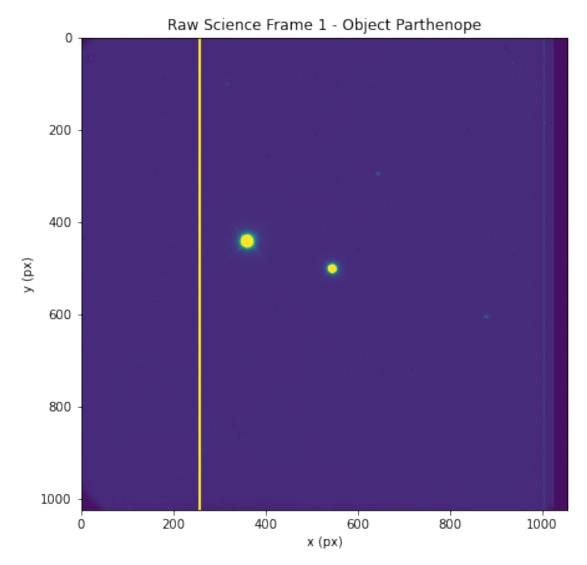
ax.set_xlabel(xlabel)

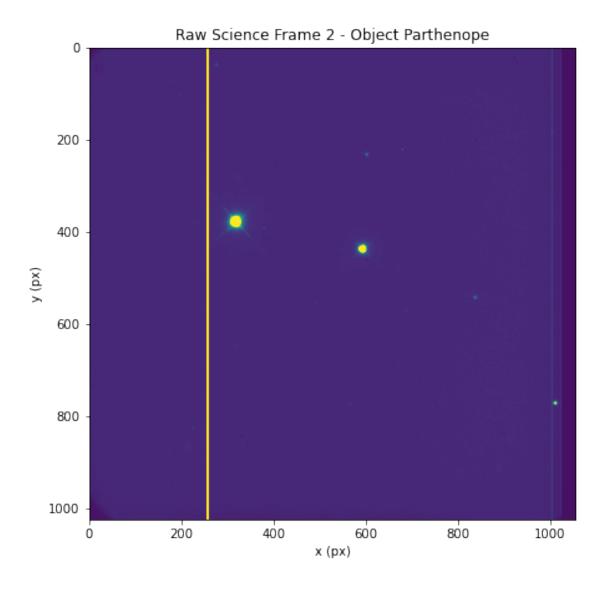
ax.set_ylabel(ylabel)

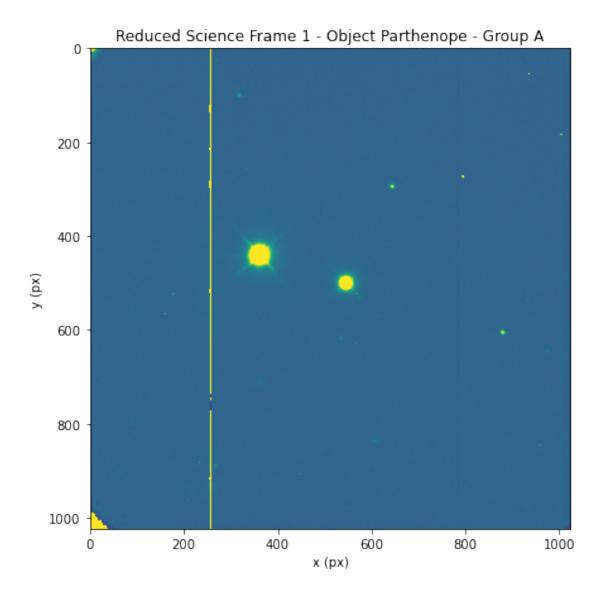
ax.set_title(title)
```

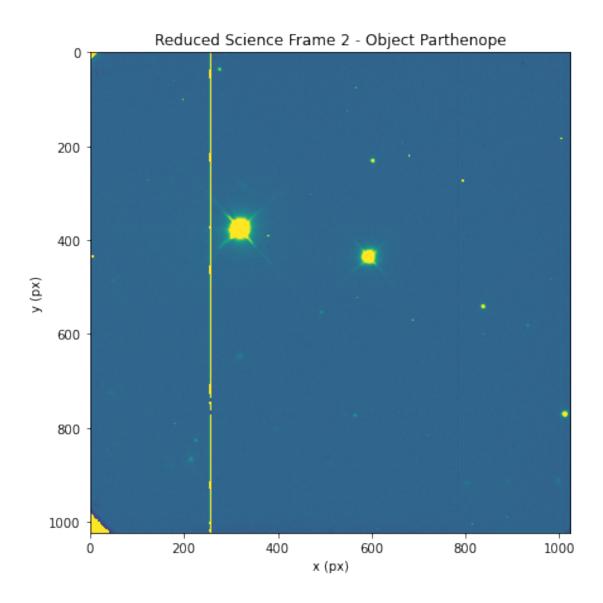


```
return data
      def load_reduced_science_frame2(filename):
          #Was having an issue with duplicate images, so two reduction functions was u
       \rightarrowmy frustrated solution
          science = fits.getdata(data_dir+data_files[4])[:,:1024]-fits.
       →getdata(data_dir+data_files[0])[:,:1024]+1.000000001
          flat = fits.getdata(data_dir+data_files[1])[:,:1024]-fits.
       →getdata(data_dir+data_files[0])[:,:1024]+1.000000001
          normflat = flat/(np.mean(flat))
          data = science/normflat
          return data
 [9]: #First and second science frames of Parthenope
      sci1 = 'd40.fits'
      sci2 = 'd90.fits'
[32]: #Plotting the science frames before and after they are reduced
      #Before:
      data3 = fits.getdata(data_dir+data_files[2])
      fig2, ax2 = plt.subplots(figsize = [7, 7])
      plot_fits_im(ax2, data3,
                   title='Raw Science Frame 1 - Object {}'.format(objects[data_files_
       \Rightarrow== sci2][0]),
                   vmax = np.median(data3) * 3, cmap = "viridis")
      data4 = fits.getdata(data_dir+data_files[4])
      fig2, ax2 = plt.subplots(figsize = [7, 7])
      plot_fits_im(ax2, data4,
                   title='Raw Science Frame 2 - Object {}'.format(objects[data_files_
      \Rightarrow== sci2][0]),
                   vmax = np.median(data4) * 3, cmap = "viridis")
      #After:
      data1 = load_reduced_science_frame1(sci1)
```









0.4 Identifying Stars

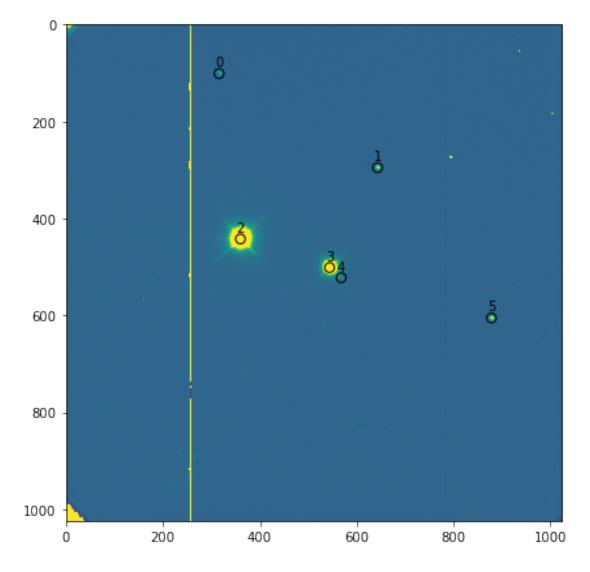
```
[11]: #Finds star locations
def find_star_locs(im_data, n_size = 10, bright_count_thresh=30):
    #set bright threshhold and neighbourhood size
    bright_thresh = np.median(im_data) * 1.5
    bright_pixels = np.array(np.where(im_data > bright_thresh)).T
    list_pos = []
    n_size = 10

for bright_pixel in bright_pixels:
```

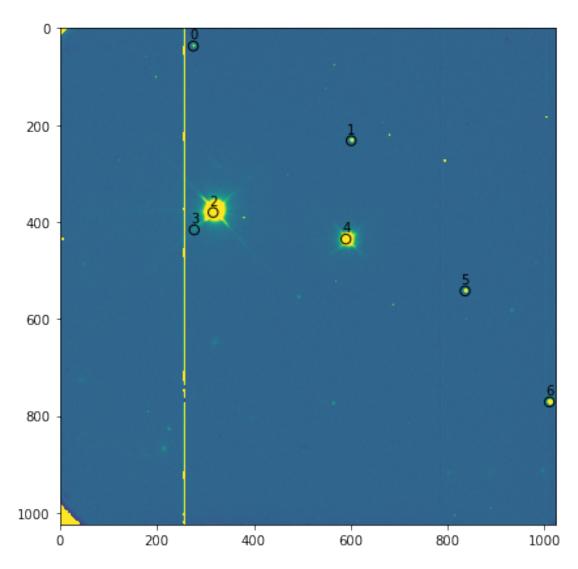
```
neighbourhood = im_data[bright_pixel[0] - n_size:bright_pixel[0] + u
→n_size, bright_pixel[1] - n_size:bright_pixel[1] + n_size]
  #If too close to the edge, we assume it isn't a star
       if np.size(neighbourhood) == 0:
           continue
           #Must exceed a certain number of bright pixels to be a star
      bright_count = len(neighbourhood[neighbourhood > bright_thresh])
       if bright_count < bright_count_thresh:</pre>
           continue
           #Computes width and height of a star
      n_bright_pixels = np.where(neighbourhood > bright_thresh)
      width = max(n_bright_pixels[0]) - min(n_bright_pixels[0])
      height = max(n_bright_pixels[1]) - min(n_bright_pixels[1])
      #If the shape of the object is too weird, it's probably not a star
      star_shape = min(width, height) / float(max(height, width))
      if star shape < (1.0 / 2.0):
           continue
       if (im_data[bright_pixel[0], bright_pixel[1]] >= np.max(neighbourhood)):
           list_pos += [[bright_pixel[0], bright_pixel[1]]]
  return list_pos
```

/opt/conda/lib/python3.7/site-packages/ipykernel_launcher.py:9:
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

if __name__ == '__main__':



/opt/conda/lib/python3.7/site-packages/ipykernel_launcher.py:21:
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.



0.5 Calculating the Star Centroids

[13]: #Function that calculates the centroids of the stars and returns their x and y_{\sqcup} \rightarrow coordinates def opentroidf(arr,locs):

```
i = 0
median = np.median(arr)
cx = []
cy = []
cxy = []
cxe = []
cye = []
cents = []
while i < len(locs):
    j = 0
    while arr[locs[i][0]+j][locs[i][1]] > median:
        j+=1
    if j > 30:
        j = 30
    x = locs[i][0]
    y = locs[i][1]
    s_{intensity} = np.sum(arr[x-j:x+j,y-j:y+j])
    k = 0
    xs = 0
    ys = 0
    while k<2*j:
        ys+=np.sum(np.multiply(np.arange(x-j,x+j),arr[x-j:x+j,y-j+k]))
        xs+=np.sum(np.multiply(np.arange(y-j,y+j),arr[x-j+k,y-j:y+j]))
        k+=1
    cy = (ys/s_intensity)
    cx = (xs/s_intensity)
    cents.append([cy,cx])
    i += 1
return cents
```

```
[14]: #Returns both the centroid coordinates and the star locations for comparison
    cents1=opcentroidf(data1,ident_star_locs1)
    print("Centroids:\n",cents1,"\n")
    print("Star Locations:\n",ident_star_locs1,"\n")
    print("Difference:\n",np.abs(np.subtract(cents1,ident_star_locs1)),"\n")
    cents2=opcentroidf(data2,ident_star_locs2)
    print("Centroids:\n",cents2,"\n")
```

```
print("Star Locations:\n",ident_star_locs2,"\n")
      print("Difference:\n",np.abs(np.subtract(cents2,ident_star_locs2)),"\n")
     Centroids:
      [[100.45701623819133, 315.6210525556931], [294.496987372875,
     642.5271416913764], [440.6843999831248, 358.88320431916577],
     [500.13565163060946, 543.4016225491586], [520.738361955559, 566.6831255824168],
     [604.529780706604, 877.516019596701]]
     Star Locations:
      [[101, 316], [295, 643], [442, 360], [501, 544], [522, 568], [605, 878]]
     Difference:
      [[0.54298376 0.37894744]
      [0.50301263 0.47285831]
      [1.31560002 1.11679568]
      [0.86434837 0.59837745]
      [1.26163804 1.31687442]
      [0.47021929 0.4839804 ]]
     Centroids:
      [[36.481087235435076, 274.6336046013176], [231.32051968589883,
     600.6721994831756], [377.058633944083, 316.93854514579044], [415.35247097184777,
     276.5331089353196], [435.8751467244046, 591.4180544889977], [541.3827074642261,
     835.6550434605468], [770.3345641542171, 1009.5787726161514]]
     Star Locations:
      [[37, 275], [232, 601], [380, 316], [416, 277], [435, 590], [542, 836], [771,
     1010]]
     Difference:
      [[0.51891276 0.3663954]
      [0.67948031 0.32780052]
      [2.94136606 0.93854515]
      [0.64752903 0.46689106]
      [0.87514672 1.41805449]
      [0.61729254 0.34495654]
      [0.66543585 0.42122738]]
[15]: #Finds the error on each centroid for both of the data sets, and then
      →calculates the average percent error for both.
      def ecent(arr,cents):
          i=0
          median = np.median(arr)
          e = []
          while i <len(cents):
```

```
Percent error on each centroid for data1: [0.0004873769648777923, 0.0009737514038465543, 0.0021300450205492135, 0.003583052956702228, 0.0007822933055267341, 0.0010522355164532178]

Average Percent Error: 0.15014591946592898

Percent error on each centroid for data2: [0.00089742391483719, 0.0017084749481659238, 0.00265602127645748, 0.0004439431380934641, 0.004286014209127055, 0.001822532812820504, 0.0035414405490488757]

Average Percent Error: 0.21936929783643563
```

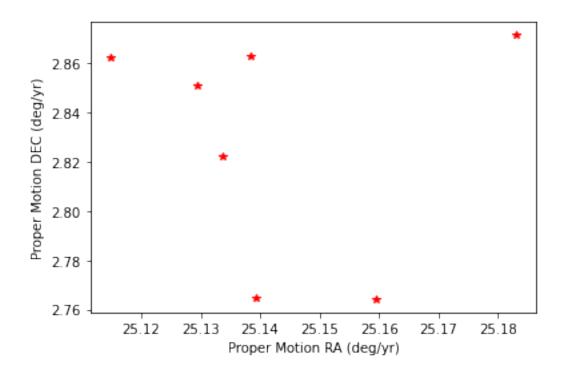
0.6 Retrieving Star Positions from USNO-B1 Catalog for field

```
h = fits.open(data_dir+data_files[4])
      science_ra_center = h[0].header["RA"]
      science_dec_center= h[0].header["DEC"]
      h.close()
      print("Parthenope (data file 2)")
      print("RA of science frame {}: {} radians".format(data_files[4],__
      →science_ra_center ))
      print("Dec of science frame {}:{} radians". format(data_files[4],__

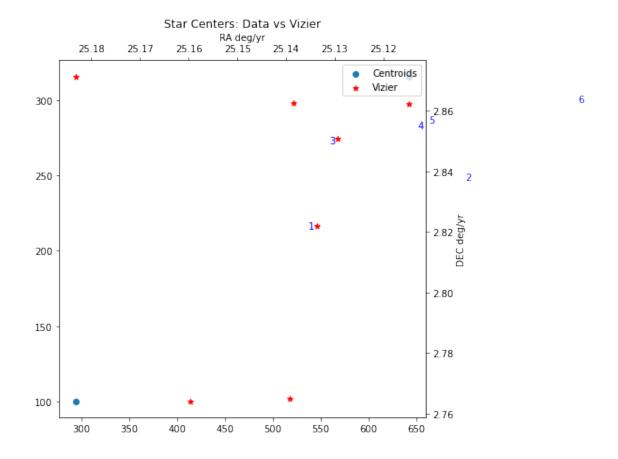
¬science_dec_center))
     Parthenope Group A (data_file 1)
     RA of science frame d40.fits: 01:40:43.09 radians
     Dec of science frame d40.fits:02:42:57.6 radians
     Parthenope (data file 2)
     RA of science frame d90.fits: 01:40:42.99 radians
     Dec of science frame d90.fits:02:41:58.0 radians
[17]: ra_center = '01:40:35.00'
      dec_center = '02:49:00.00'
      center_coord = SkyCoord(ra = ra_center, dec = dec_center, unit = (u.hour, u.
       →deg), frame='icrs')
[18]: #Setting a limit for star brightness
      magnitude_limit = 16.2
      # Create a VizieR object.
      vizier = Vizier(column_filters = {"R2mag" : "<{}}".format(magnitude_limit)})</pre>
      # By default, VizieR will limit the result to 50 stars. We change the limit tou
      → "-1" meaning "show everything you have"
      # This is a dangerous setting, since some queries may return enormous amounts_{\sqcup}
      →of data. In our case, however, only a small
      # part of the sky is being queried, heavily limited by magnitude. We should be
      ⇔safe.
      vizier.ROW_LIMIT = -1
      # Run the query. We are requesting the part of the sky defined by the
      → previously created coordinates object (center).
      # width, height specify the size of the region we need (in arc minutes).
      # Adjust this value to match your science frame
      # "catalog = "USNO-B1" tells VizieR which catalogue we want. This could be a_
      \rightarrow list of multiple catalogues.
```

```
fov_width = '7.0m'
     fov_height = '7.0m'
     result_table = vizier.query_region(center_coord, width = fov_width, height = u
      print ("Total number of objects retrieved:", len(result_table[0]))
     print ("Column names:", result_table[0].keys())
     Total number of objects retrieved: 7
     Column names: ['USNO-B1.0', 'RAJ2000', 'DEJ2000', 'e_RAJ2000', 'e_DEJ2000',
     'Epoch', 'pmRA', 'pmDE', 'Ndet', 'B1mag', 'R1mag', 'B2mag', 'R2mag', 'Imag']
[19]: ra_cat
                = np.array(result_table[0]["RAJ2000"])
     dec_cat = np.array(result_table[0]["DEJ2000"])
     pm_ra
              = np.array(result_table[0]["pmRA"])
              = np.array(result_table[0]["pmDE"])
     pm_dec
     mag
                = np.array(result_table[0]["R2mag"])
     epoch = 2020.0 # Image taken in 2020
     # Convert the units of pmDec from mas/yr to deg/yr
     pm_dec = pm_dec / 1000.0 / 3600.0
     # Same for RA, but with the cos(dec) correction. Note, np.cos() expects radians!
     pm_ra = pm_ra / 1000.0 / 3600.0 / np.cos(dec_cat * np.pi / 180.0)
     # Move the stars
     ra_cat += (epoch - 2000.0) * pm_ra
     dec_cat += (epoch - 2000.0) * pm_dec
     plt.xlabel("Proper Motion RA (deg/yr)")
     plt.ylabel("Proper Motion DEC (deg/yr)")
     plt.plot(ra_cat, dec_cat, 'r*')
```

[19]: [<matplotlib.lines.Line2D at 0x7fd3322ccd10>]



```
[20]: #Science frame 1
      fig4 = plt.figure(figsize = [7, 7])
      axs = fig4.add_subplot(111, label='science', frame_on=True)
      axq = fig4.add_subplot(111, label='Query' , frame_on=False)
      science_points = axs.scatter(np.squeeze(cents1[1]), np.squeeze(cents1[0]))
      queried_points = axq.scatter(ra_cat, dec_cat, color='red', marker='*')
      # Not flipping axis, worked much better without it
      for i, (loc_y, loc_x) in enumerate(cents1):
          axs.text((loc_x)/2 + 380, (loc_y)/6 + 198, str(i+1), color = 'blue')
      axq.xaxis.tick_top()
      axq.xaxis.set_label_position('top')
      axq.yaxis.tick_right()
      axq.yaxis.set_label_position('right')
      axq.set_xlim(axq.get_xlim()[::-1])
      plt.title("Star Centers: Data vs Vizier")
      plt.legend([science_points,queried_points],["Centroids","Vizier"])
      plt.xlabel("RA deg/yr")
      plt.ylabel("DEC deg/yr")
      fig4.show()
```



```
fig4 = plt.figure(figsize = [7, 7])
axs = fig4.add_subplot(111, label='science', frame_on=True)
axq = fig4.add_subplot(111, label='Query' , frame_on=False)

science_points = axs.scatter(np.squeeze(cents2[1]), np.squeeze(cents2[0]))
queried_points = axq.scatter(ra_cat, dec_cat, color='red', marker='*')

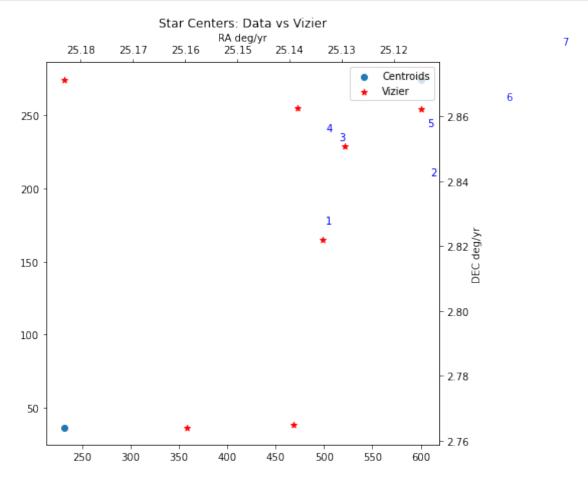
# Not flipping axis, worked much better without it

for i, (loc_y, loc_x) in enumerate(cents2):
    axs.text((loc_x)/3 + 410, (loc_y)/6 +170, str(i+1), color = 'blue')

axq.xaxis.tick_top()
axq.xaxis.set_label_position('top')
axq.yaxis.set_label_position('right')
axq.yaxis.set_label_position('right')
axq.set_xlim(axq.get_xlim()[::-1])

plt.title("Star Centers: Data vs Vizier")
```

```
plt.legend([science_points,queried_points],["Centroids","Vizier"])
plt.xlabel("RA deg/yr")
plt.ylabel("DEC deg/yr")
fig4.show()
```



0.7 Solving for Plate Constants

```
[22]: def sin(angle):
    """ Converts to degrees then does the sin """
    return np.sin(angle * np.pi / 180.0)

def cos(angle):
    """ Converts to degrees then does cos """
    return sin(angle + 90)

bottom = cos(center_coord.dec.deg) * cos(dec_cat) * cos(ra_cat - center_coord.
    →ra.deg) + sin(center_coord.dec.deg) * sin(dec_cat)
```

```
X = - cos(dec_cat) * sin(ra_cat - center_coord.ra.deg) / bottom
Y = - (sin(center_coord.dec.deg) * cos(dec_cat) * cos(ra_cat - center_coord.ra.

deg) - cos(center_coord.dec.deg) * sin(dec_cat)) / bottom

f = 16480
p = 0.015

fp = f/p
#The following would be done if we had an ideal camera. Unfortunately, we have
shear and distortion.

#x = f * (X/p) +np.shape(data1)[1] / 2.0
#y = f * (Y/p) +np.shape(data1)[0] / 2.0
```

```
[23]: #Matrix math for solving for plate constants
      B = np.array([
          [fp *X[0], fp * Y[0], 1],
          [fp *X[1], fp * Y[1], 1],
          [fp *X[2], fp * Y[2], 1],
          [fp *X[3], fp * Y[3], 1],
          [fp *X[4], fp * Y[4], 1],
          [fp *X[5], fp * Y[5], 1],
      ])
      a1 = np.array([
          cents1[0][0],
          cents1[1][0],
          cents1[2][0],
          cents1[3][0],
          cents1[4][0],
          cents1[5][0],
      ])
      a2 = np.array([
          cents1[0][1],
          cents1[1][1],
          cents1[2][1],
          cents1[3][1],
          cents1[4][1],
          cents1[5][1],
      ])
      c1 = np.matmul(inp.matmul(inv(np.matmul(np.transpose(B),B)),np.transpose(B)),a1)
      c2 = np.matmul(np.matmul(inv(np.matmul(np.transpose(B),B)),np.transpose(B)),a2)
      print(c1)
      print(c2)
```

[-3.07405165e-01 -1.45738058e-01 5.08229830e+02]

[-1.86117545e-01 -1.80003190e-01 6.49459623e+02]

```
[24]: #Final steps
a = [fp * c1[0], fp * c1[1], c1[2]]
b = [fp * c2[0], fp * c2[1], c2[2]]
T = np.array([a,b,[0,0,1]])
x_coords = [cents1[3][0], cents2[3][0]]
y_coords = [cents1[4][1], cents2[4][1]]
X1 = np.matmul(inv(T),np.transpose([x_coords[0],y_coords[0],1.0]))
X2 = np.matmul(inv(T),np.transpose([x_coords[1],y_coords[1],1.0]))
print(X1)
print(X2)
print(center_coord)
```

```
[-3.42230940e-04 7.72418909e-04 1.00000000e+00]

[2.66492385e-04 1.79451762e-05 1.00000000e+00]

<SkyCoord (ICRS): (ra, dec) in deg

(25.14583333, 2.81666667)>
```

0.8 Calculating Proper Motion of Parthenope

```
[25]: #Calculating proper motion via distance formula
      ra0 = center_coord.dec.deg
      dec0 = center_coord.ra.deg
      ra_i = np.arctan(-X1[0]/(cos(dec0)-X1[1]*sin(dec0))) + (ra0*np.pi/180)
      dec_i = np.arcsin((sin(dec0)+X1[1]*cos(dec0))/np.sqrt(1+X1[0]**2 + X1[1]**2))
      ra f = np.arctan(-X2[0]/(cos(dec0)-X2[1]*sin(dec0))) + (ra0*np.pi/180)
      dec_f = np.arcsin((sin(dec0)+X2[1]*cos(dec0))/np.sqrt(1+X2[0]**2 + X2[1]**2))
      print(ra_i,dec_i)
      print(ra f,dec f)
      dt = 2.15 \# hrs
      vra = (ra_f - ra_i)/dt * 180/np.pi
      vdec = (dec_f - dec_i)/dt * 180/np.pi
      error_p = (np.mean(ecents1) + np.mean(ecents2))/2
      print(" ")
      print("RA Velocity (arcsec/hr):", vra * 60)
      print("RA Velocity error: ", abs(vra * 60 * error_p))
      print(" ")
      print("DEC Velocity (arcsec/hr): ", vdec * 60)
      print("DEC Velocity error: ", abs(vdec * 60 * error_p))
```

- 0.04953830437152004 0.43964997603573414
- $0.04886571261874219 \ 0.43889551333151267$

RA Velocity (arcsec/hr): -1.0754419191482096 RA Velocity error: 0.0019869607722506136

DEC Velocity (arcsec/hr): -1.206349639588387 DEC Velocity error: 0.00222882274607566

This has been by far the most frustrating and difficult lab to complete. I spent hours trying to piece it all together, along with my lab partner, Lucas. Despite this, I've had a great time and learned an immense amount from these labs and this class. Thank you