

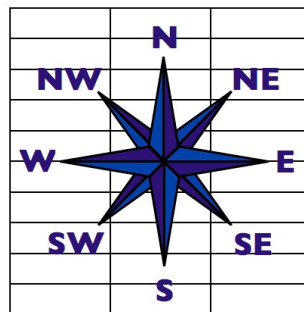
Interactive Spreadsheets for Celestial Navigation



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Introduction

In our world of ever expanding technology, many people have reached to the past to rediscover the traditions of navigation on the high seas by using the sun, the moon, the planets, and the stars. Even today in the age of the Internet, telecommunication satellites, and the Global Positional System (GPS), there still are people who have reconnected with the earth and the sun through the art and science of celestial navigation. Just as sailors did in the days of tall ships and billowing sails, we also are able to determine our position on the earth by looking at the sky armed with just a sextant, a chronometer, and some tables.

The spreadsheets available through this website are designed to increase the accuracy, reliability, and the speed with which you can derive your position from observations of the heavens. First, you take a sight with a sextant, make the appropriate corrections to the measured altitude, and retrieve the necessary astronomical data from an almanac spreadsheet. Then you enter the data into the appropriate sight reduction spreadsheet - *and you're done!* The use of these spreadsheets finds a middle ground between manually doing all the steps needed to plot your line of position on a chart and simply pushing a button to read your location on a GPS receiver.

Our spreadsheets are programmed to provide and process several types of sight data commonly acquired in celestial navigation:

- Intersections of lines of position
- Running fix
- Noon sight, noon curve, and meridian transits
- Dead reckoning (DR) position and a DR fix along a line of position
- Sextant altitude corrections
- Solutions of the navigation triangle (the intercept method and sailings calculations)
- Almanac data (calculation of Geographical Positions of main celestial bodies)
- Lunar distance (UT recovery)

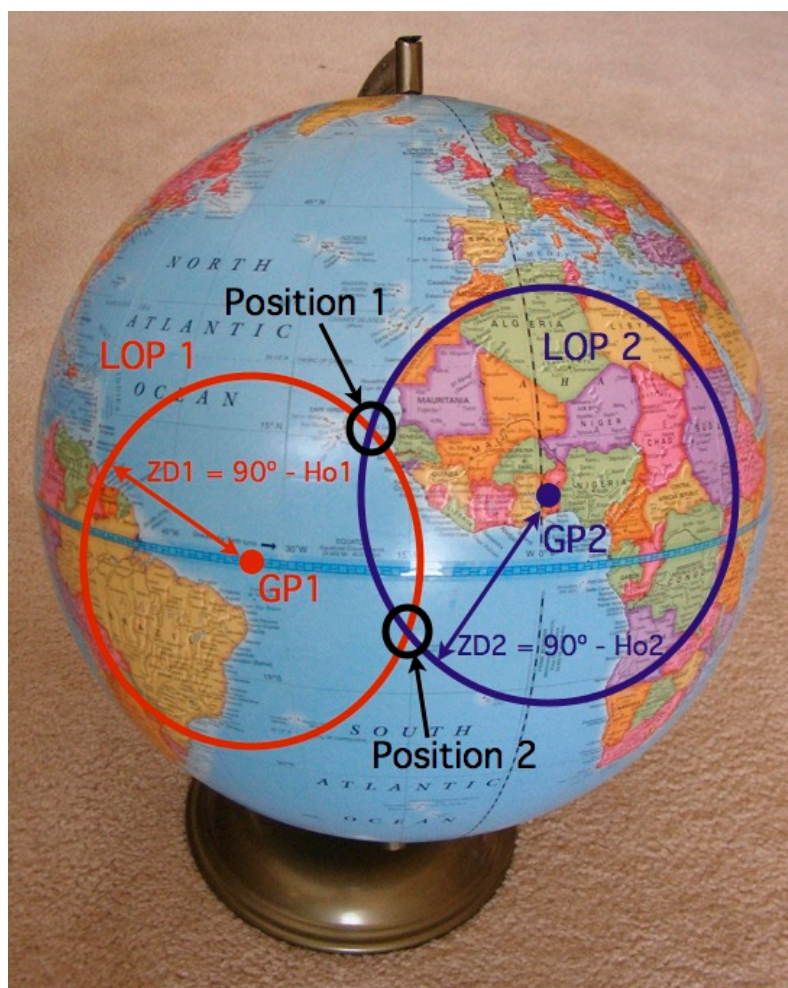
In all spreadsheets the cells expecting the user's input data are formatted in *italics* on green background and the results are displayed with the normal font in cyan cells, all next to labels in **bold**. Cells marked yellow are used for both input and output (i.e. intermediate results). Except in the spreadsheet *aries_stars.xls*, the cells containing angular input data are formatted as compound fractions with three-digit denominators; thus the angle of $27^{\circ} 31.1'$ is to be entered as 27 311/600. These angular input data are accompanied by grey cells displaying the fractional portion of the data value in minutes of arc. This way you can verify that the input value was entered correctly. You may also use the **minispreadsheet** *minutes.xls* for the same purpose. Enter the fractional value in cell B1, or the decimal value in cell B5, and inspect the equivalent angular value in arcminutes. Cells containing time data (with the exception of cell B6 in *running_fix.xls*, *dr.xls*, and *dr_fix_lop.xls*) are formatted using the 24-hour clock as HH:MM:SS. (For times between 12 and 1 o'clock make sure that the cell ends up with the correct AM/PM value.) All other cell contents represent partial results of the computations and can be ignored, unless you want to get into the nitty-gritty details. Our adopted sign convention marks north latitudes and east longitudes as positive; south latitudes and west longitudes are considered negative. On output, fractions of degrees (minutes of arc) are displayed without their sign. We also provide a simple worksheet in which you may record intermediate results, such as output of almanac spreadsheets that need to be transferred into the input of the sight reduction spreadsheets. OpenOffice seems to have a problem here; you may need to reformat these cells using only two-digit fractions and therefore round angles to whole minutes. Another alternative is to enter these values using the formula bar as: =27+311/600. If the value is negative (e.g. declination S $27^{\circ} 31.1'$), then in the formula you must use minus signs for both the whole degree component and its fraction: =-27-311/600. The formatting of some results does not explicitly separate the sign on output from the integer degree value. Therefore, for results between -1° and $+1^{\circ}$ be sure to pick up the correct sign from the decimal value of the result in a neighboring cell, because zeroes are usually displayed unsigned. The spreadsheets are protected against accidental changes of data and formulae by locking all but the input cells. You do have the option of unlocking everything, since there is no password, although this is not recommended.

Lines of position (two-body) fix

If, for instance, both the sun and the moon are simultaneously visible in the sky it is possible to obtain your position by finding the intersection of the two lines of position (LOP) obtained from each sight. Typically there are two distinct possible positions and it should be very easy to decide which one is the correct one.

The measured sextant altitude is corrected for index error, refraction, parallax, and semidiameter which results in the observed altitude (H_o). The Universal Time (UT) of the sight is used to determine the Geographical Position (GP) with the help of an

almanac. The declination and Greenwich Hour Angle (GHA) of the GP plus the H_o for the two sights are entered in row 3 of the spreadsheet. The solutions are displayed in rows 8 and 10.



The following image shows the spreadsheet *lops.xls*.

A B C D E F					
Intersections of two LOPs (lines of position)					
Enter Geographical Positions and observed altitudes (Ho)					
Declination 1	GHA 1	Altitude 1	Declination 2	GHA 2	Altitude 2
16 43/75	112 253/300	27 511/600	-14 241/300	8 3/40	30 31/200
34.4	50.6	51.1	48.2	04.5	09.3
Retrieve the solutions					
Latitude 1	Degrees	Minutes	Longitude 1	Degrees	Minutes
33.09	33	05.5	-45.66	-45	39.9
Latitude 2	Degrees	Minutes	Longitude 2	Degrees	Minutes
-31.25	-31	15.0	-71.50	-71	29.9
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *lops.xls*:

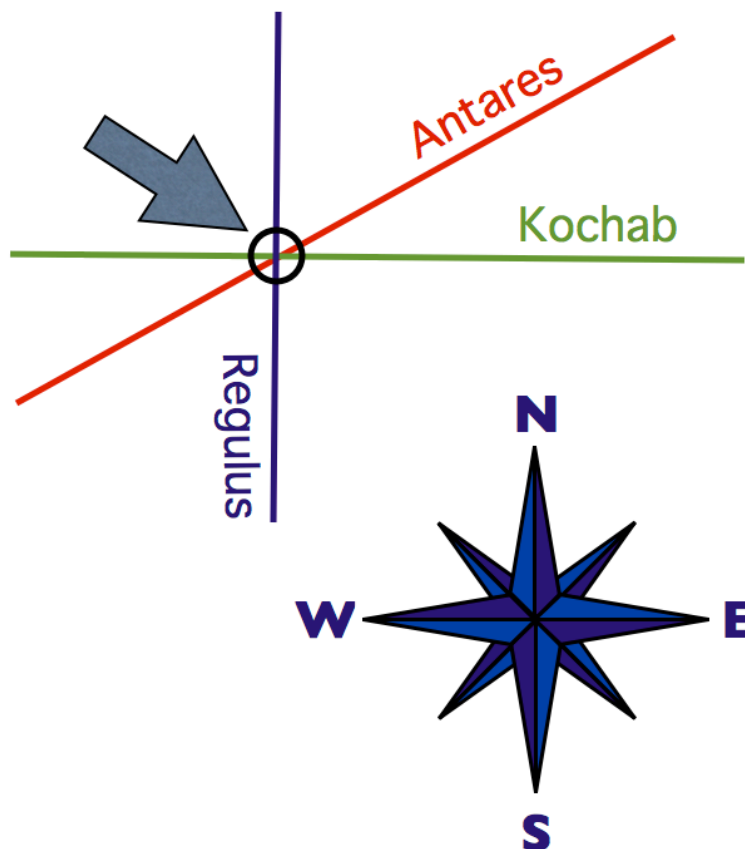
Input cells: A3, B3, C3, D3, E3, F3

Output cells: A8, B8, C8, D8, E8, F8, A10, B10, C10, D10, E10, F10

The problem preset in this spreadsheet is treated in *The Celestial Navigation Mystery Solved* by David Owen Bell on p. 79.

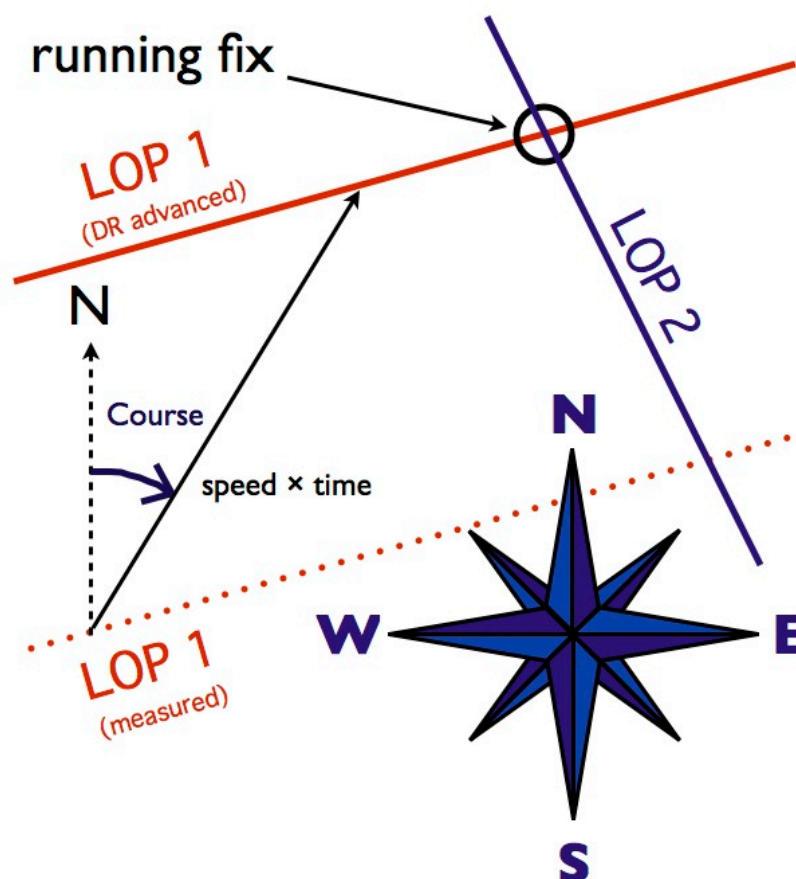
The spreadsheet *two_body_fix.xls* has the same interface as *lops.xls* and solves the same problem using a different method. Whereas *lops.xls* employs the techniques of spatial geometry (Van Allen paper), *two_body_fix.xls* applies the equations of spherical trigonometry (John Karl, *Celestial Navigation in the GPS Age*, pp. 78-79). The latter reference also discusses the applicability of this approach to finding the latitude without a meridian sight or knowledge of UT (the double-altitude method).

Lines of position (many-body) fix



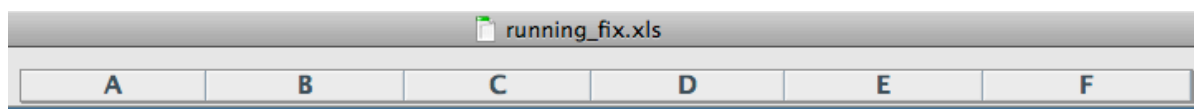
Spreadsheet *many_body_fix.xls* implements a procedure for computing a location from multiple lines of position obtained on a moving vessel. This navigation problem typically arises from a round of observations acquired during twilight. Enter the desired UT of the fix in cell A2, vessel speed in knots in cell B2, and course (track) in cell C2. The initial best guess for the position goes into cells E2 and F2. The observational and GP data start in line 9 and are entered into columns A (name), B (UT of observation), C (observed altitude H_o), E (GHA), and G (declination). The computed coordinates are displayed in row 6. The spreadsheet performs a block of four iterations of this procedure. On output, the value d in cell D4 should be less than 20 nautical miles; if that is not the case, copy cells A6 and D6 into cells E2 and F2 and repeat this procedure until convergence is reached.

Running fix



If two different celestial bodies are not available for simultaneous measurements, it is possible to obtain the two lines of position by observing the same body twice within a few hours. The first observed LOP then has to be displaced by the distance and direction traveled during the time interval between observations. The spreadsheet *running_fix.xls* is an extended version of *two_body_fix.xls* and is used the same way. Additional input information consists of the average speed in knots (cell A7), time interval in hours (cell B7, formatted as a regular floating-point number), and course (cell C7 - track, measured from true north clockwise). The solutions are displayed in rows 10 and 12. The distance traveled (in nautical miles) is in cell D7.

The following image shows the spreadsheet *running_fix.xls*.



Running fix: Intersections of two LOPs (LOP1 advanced in time)

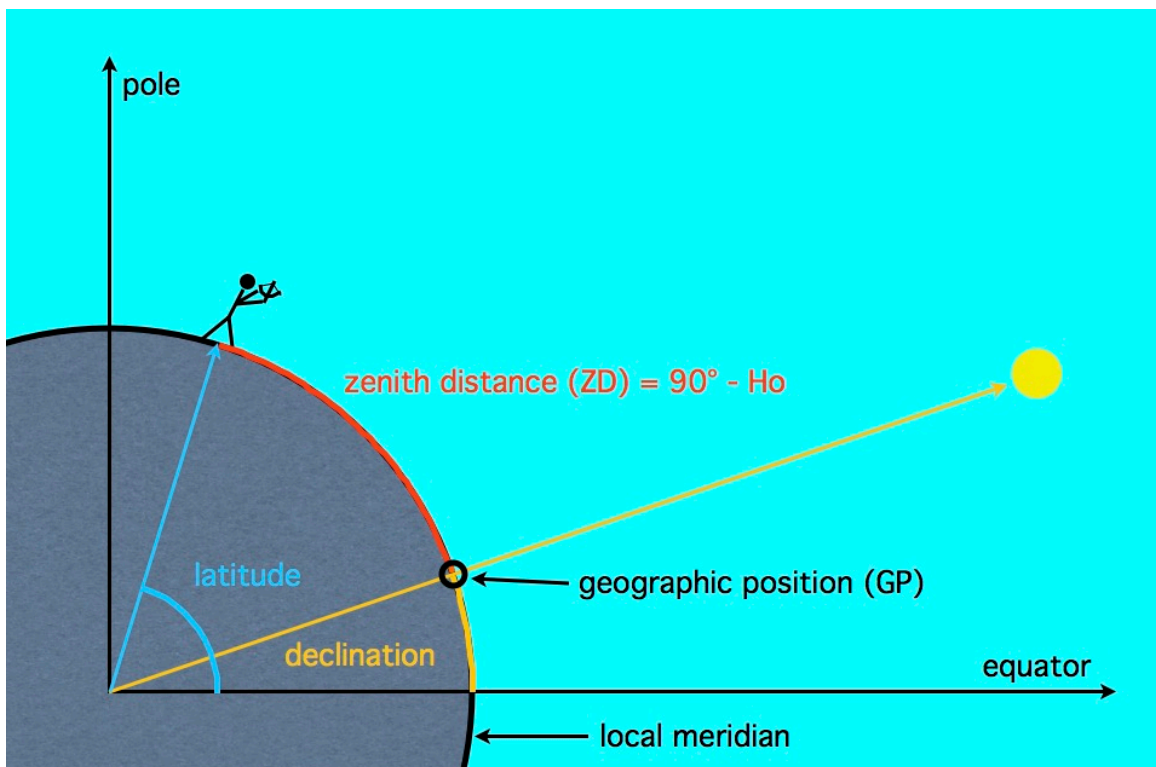
Enter Geographical Positions and observed altitudes (Ho)					
Declination 1	GHA 1	Altitude 1	Declination 2	GHA 2	Altitude 2
3 109/200	92 61/75	79 77/100	3 16/25	182 229/600	5 47/60
32.7	48.8	46.2	38.4	22.9	47.0
Speed (kn)	Time (hours)	Course	Distance (nm)		
4.5	6	340	27		
Latitude 1	Degrees	Minutes	Longitude 1	Degrees	Minutes
13.18	13	10.8	-97.48	-97	28.6
Latitude 2	Degrees	Minutes	Longitude 2	Degrees	Minutes
-4.65	-4	38.9	-98.49	-98	29.6
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *running_fix.xls*:

Input cells: A3, B3, C3, D3, E3, F3, A7, B7, C7

Output cells: D7, A10, B10, C10, D10, E10, F10, A12, B12, C12, D12, E12, F12

Noon sight



Observing the sun at LAN (local apparent noon) allows you to determine the position from a single sight. The need for a second line of position is eliminated by the additional piece of information implicitly contained in a noon sight: i.e. that the sun and the observer are on the same meridian. Thus the geometric arrangement is reduced to a 1-dimensional problem along this meridian, with the sun bearing either directly north or south from the observer. In the spreadsheet *noon_sight.xls* the H_o at LAN is entered in cell D1 and the UT in cell D13. From an almanac you find the sun's declination (D3) and the correction for equation of time; the latter is entered in D14 if positive, or in D15 if negative (without its sign). This correction is always less than one hour, therefore it is to be entered as *00:MM:SS*. It can be (optionally) copied from cell B16 that interpolates between cells B14, B15; therein you may enter the equation of time values (without their signs) for the 00^h and 12^h instants that straddle your noon UT in cell D13. (This interpolator works in the vast majority of cases when the two equation of time values are of the same sign.) The final two entries identify the observer's hemisphere (D4) and the sun's bearing

(D5); enter *N* for north and *S* for south. In the special case of the sun in zenith ($H_o = F1 = 90^\circ$) your position is the sun's GP and the sun's bearing (D5) is as unimportant as it is undefined. The latitude of the position is displayed in cells D9, D10, D11 and cells D16, D17, D18 contain the longitude.

The following image shows the spreadsheet *noon_sight.xls*.

noon_sight.xls					
A	B	C	D	E	F
<p style="text-align: center;">Noon sight</p> <p style="text-align: center;">Enter Altitude (H_o) in cell D1, UT in cell D13, EoT in cells B14, B15, D14, D15</p>					
		Noon Altitude =	70 37/200	11.1	
		Zenith Dist =	19.82	48.9	
		Declination =	-13 41/100	24.6	
		Hemisphere =	N		
		Sun bearing =	S		
		SAME =	FALSE		
		D =	13 41/100	24.6	
		L =	6 81/200	24.3	
		Latitude =	6.41		
		Degrees =	6		
		Minutes =	24.3		
	0.393681	Noon UT =	16:43:27		
EoT past =	0:00:05	Eq. of time +			
EoT next =	0:00:11	Eq. of time -	0:00:07		
EoT int =	0:00:07	Longitude =	-70.83		
		Degrees =	-70		
		Minutes =	50.0		

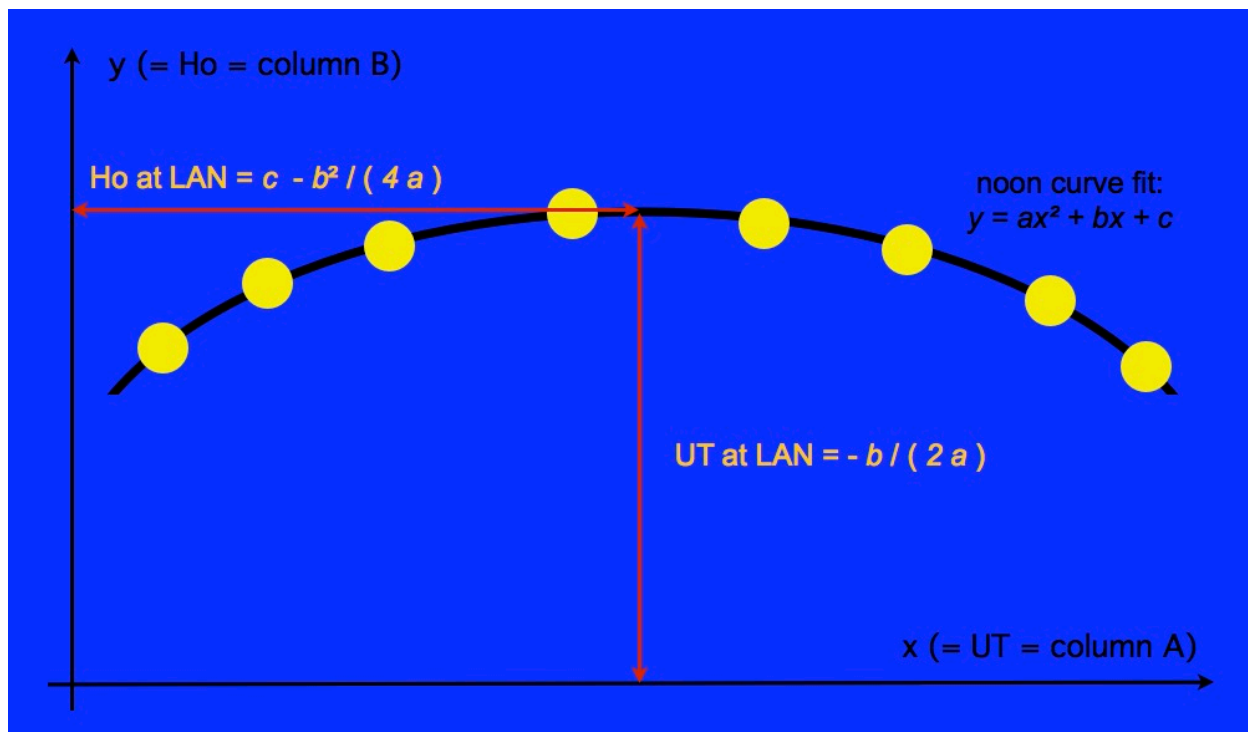
Summary for spreadsheet *noon_sight.xls*:

Input cells: D1, D3, D4, D5, D13, D14, D15, (B14, B15 optional)

Output cells: D9, D10, D11, D16, D17, D18

Intermediate cell: B16

Noon curve



The noon sight in principle allows you to determine the position and indeed the latitude can be measured to a good accuracy. However, in practice the inferred longitude is often inaccurate due to the difficulty of marking the precise moment of LAN. The sun hangs at its maximum altitude for a couple of minutes and every four seconds of uncertainty in the time of LAN introduce an error of 1 arc minute of longitude.

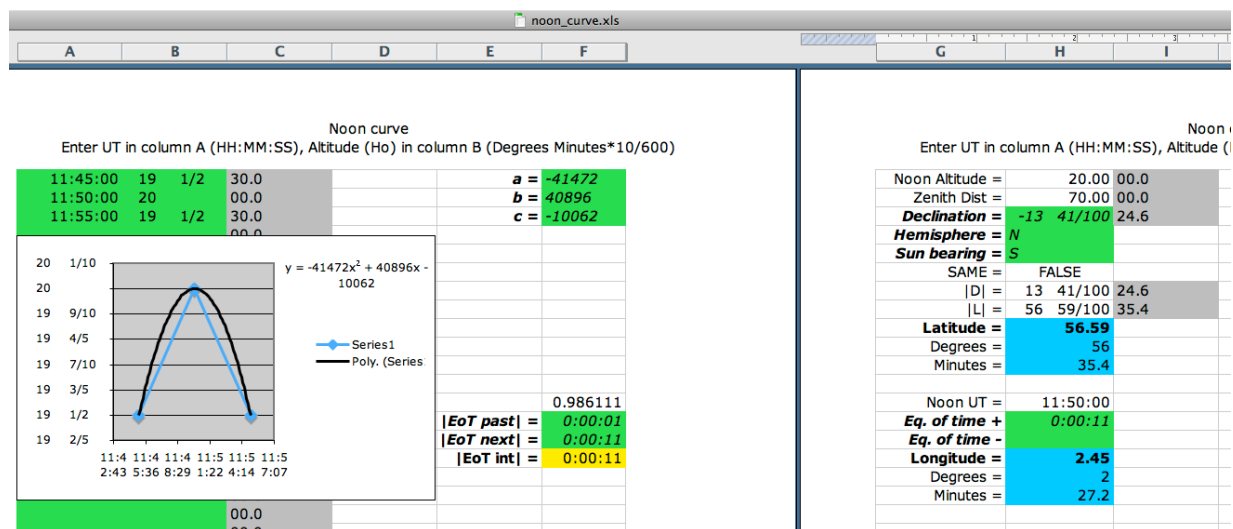
In order to mitigate this problem with the noon sight it is recommended to make several observations around the time of LAN, fit the measurements with a “noon curve” and infer the Ho and UT from this fit. The spreadsheet *noon_curve.xls* does precisely that. It is an extended version of the *noon_sight.xls* spreadsheet with the difference that the Ho (H1) and UT (H13) at LAN are computed from the noon curve instead of being entered by the user.

The noon curve is constructed via the following steps:

- Enter the UT's of your sights in column A and the corresponding Ho's in column B. You will need at least three observations for the noon curve (which is a quadratic fit) to be defined.
- Insert a Chart (XY scatter type) with column B as the Y axis ("Data range" tab) and column A for X-values ("Series" tab).
- Right-click on the plotted curve and select "Add Trendline" from the context menu. In the "Type" tab select "polynomial" of order 2; in the "Options" tab check "Display equation on chart."
- Find the noon curve fitting equation of the type $y = ax^2 + bx + c$ on the plot, retrieve the a , b , c coefficients (complete with signs) and enter them into cells F1, F2, and F3.
- The entries for Hemisphere (H4), Sun bearing (H5), and Equation of time (H14 or H15, plus the optional interpolation data in cells F14, F15) are entered as in the *noon_sight.xls* spreadsheet.
- The position is displayed in cells H9, H10, H11 (latitude) and in cells H16, H17, H18 (longitude).

Alternatively, you may also use the spreadsheet *noon_motion.xls* (see below), which produces the same results without the need for plotting a chart. That spreadsheet computes the coefficients a , b , and c of the quadratic fit automatically. Extra pieces of information on input include the number of observations in cell F4. Also, in this context set F1 cell value to zero and enter a solstice day (June or December 21) in cells F6 and F7.

The following image shows the spreadsheet *noon_curve.xls*.



Summary for spreadsheet *noon_curve.xls*:

Input cells: column A, column B, F1, F2, F3, H3, H4, H5, H14, H15, (F14, F15 optional)

Output cells: H9, H10, H11, H16, H17, H18

Intermediate cell: F16

Meridian transit on a moving vessel

The spreadsheet *transit.xls* is a generalization of *noon_motion.xls* that can process meridian transit data (both upper and lower) for any celestial body. The rate of change of declination (in arc minutes per hour) is entered in cell F7. In cell H15 enter “U” for upper and “L” for lower meridian transit.

The following image shows the spreadsheet *transit.xls*.

transit.xls

A	B	C	D	E	F	G	H	I
---	---	---	---	---	---	---	---	---

Meridian transit curve (no chart required) on a moving vessel

Enter UT in column A (HH:MM:SS), Altitude (Ho) in column B (Degrees Minutes*10/600)

12:10:00	10 197/250	47.3	Speed (kn) = 10
12:15:00	10 413/500	49.6	Course = 225
12:20:00	10 113/125	54.2	
12:25:00	10 469/500	56.3	N = 13
12:30:00	10 239/250	57.4	
12:35:00	10 413/421	58.9	Dec change
12:40:00	10 217/243	53.6	per hour = 0.0
12:45:00	10 223/250	53.5	
12:50:00	10 106/125	50.9	
12:55:00	10 161/200	48.3	
13:00:00	10 143/200	42.9	
13:05:00	10 272/427	38.2	
13:10:00	10 271/500	32.5	
		00.0	
		00.0	
		00.0	
		00.0	
		00.0	
		00.0	

Meridian transit curve (no chart required) on a moving vessel

Enter UT in column A (HH:MM:SS), Altitude (Ho) in column B (Degrees Minutes*10/600)

Transit Altitude =	11.02	01.3
Zenith Dist =	78.98	58.7
Dec at end =	-23 11/25	26.4
Hemisphere =	N	
Body bearing =	S	
SAME =	FALSE	
D =	23 11/25	26.4
L =	55 445/826	32.3
Latitude =	55.54	
Degrees =	55	
Minutes =	32.3	
Transit UT =	12:29:37	
GHA at UT =	7 173/200	51.9
Upper/Lower =	U	
Longitude =	-8.01	
Degrees =	-8	
Minutes =	00.3	

Ex-meridian latitude calculation

The *ex-meridian.xls* spreadsheet has the same general format of input and output cells as the other meridian-transit-category spreadsheets. The one extra input data point is in cell B11 marking the time away from the actual meridian transit in the hours:minutes:seconds (HH:MM:SS) format. Cell B12 displays the intermediate results: (altitude factor) from Bowditch Table 24, and cell B13 shows the absolute value of the resulting change in altitude/latitude from Bowditch Table 25.

The following image shows the spreadsheet *ex-meridian.xls*.

ex_meridian.xls					
A	B	C	D	E	F
Ex-meridian latitude calculation					
Enter time away from meridian transit in B11 as HH:MM:SS					
Altitude =	40	00.0		ZD upper =	50
Zenith Dist =	50.00	00.0		ZD lower =	170
Declination =	-20	00.0		ZD assumed =	50
Hemisphere =	N				
Body bearing =	S				
SAME =	FALSE				
D =	20	00.0			
L =	30	00.0			
AP Latitude =	30	00.0			
Lat MT =	30.00				Body bearing
t (HH:MM:SS) =	0:10:00				1
a ("/min^2) =	02.1				
d Lat (') =	03.5				
U/L =	1				
Upper/Lower =	U				
Latitude =	29.94			CoDec =	70
Degrees =	29			Lat =	110
Minutes =	56.5			Lat (L) =	110

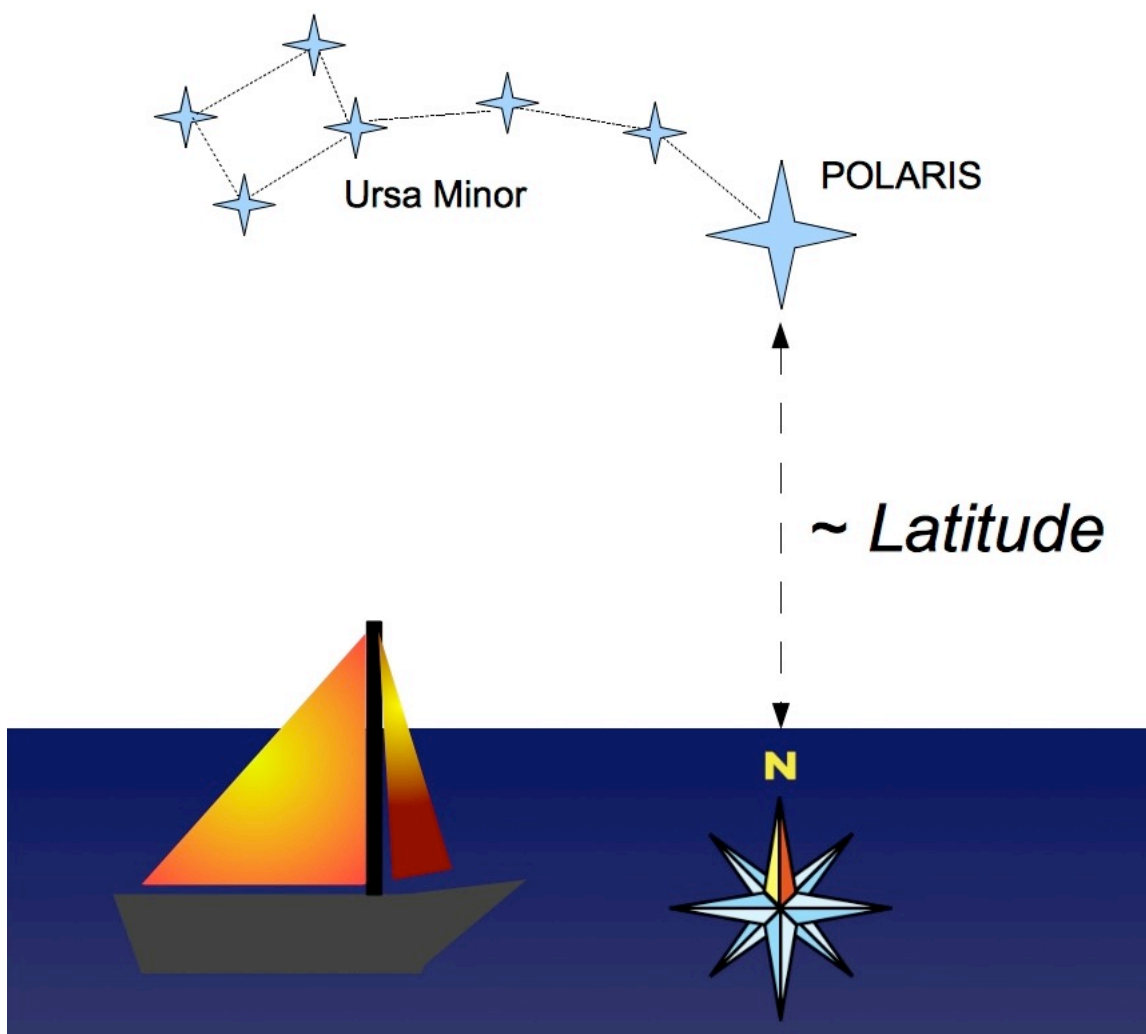
Summary for spreadsheet *ex-meridian.xls*:

Input cells: B1, B3, B4, B5, B9, B11, B15

Output cells: B16, B17, B18

Intermediate cells: B12, B13

Latitude from Polaris



In the northern hemisphere, the observed altitude of Polaris indicates your latitude. This value is only approximate because Polaris does not sit exactly above the North Pole. If you know your longitude, you may use the *polaris.xls* spreadsheet to improve your latitude determination by accounting for the small distance of Polaris from the Pole. Enter Universal Time (UT) of your observation in row 2, longitude in cell A5, and observed altitude (Ho) of Polaris in cell B5. Your latitude is displayed in cells D5 and E5. Cell F5 contains the azimuth of Polaris. In row 10 you may see the Geographical Position of Polaris, which is computed from the UT. The SHA may differ a little from published almanacs but this does not affect the spreadsheet's latitude result.

The following image shows the spreadsheet *polaris.xls*.

polaris.xls					
A	B	C	D	E	F
Latitude from Polaris Enter UT, Ho, and longitude					
Year	Month	Day	Hours	Minutes	Seconds
2009	04	21	23	18	56
Longitude	Altitude (Ho)	Latitude	Degrees	Minutes	Azimuth
-37 7/30	49 79/150		49	54.1	359.1
14.0	31.6				
Polaris					
SHA	Degrees	Minutes	Declination	Degrees	Minutes
	319	45.0	N 89		18.4
#####	#####	#####	#####	#####	#####

Summary for spreadsheets *polaris.xls*:

Input cells: A2, B2, C2, D2, E2, F2, A5, B5

Output cells: D5, E5, F5

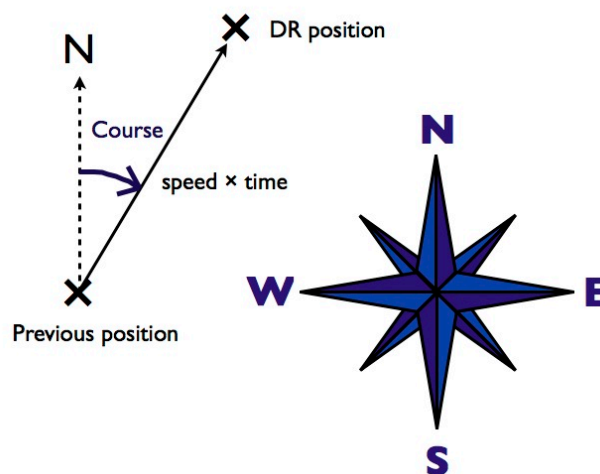
Intermediate cells: B10, C10, E10, F10

The example preset in this spreadsheet is taken from p. 275 of the Nautical Almanac, 2009 Commercial Edition.

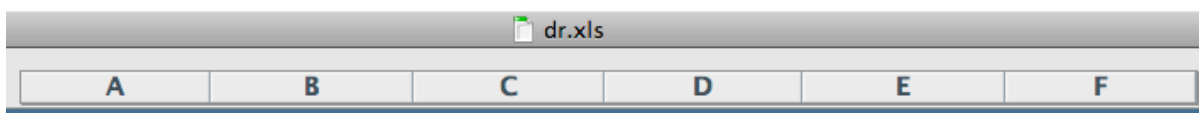
If your longitude is unknown, you may instead use the *polaris_lha.xls* spreadsheet with the LHA of Polaris as input in cell A5. This LHA can be estimated by inspecting the relative orientation of nearby star patterns (most likely the Ursa Minor constellation) with respect to the horizon. All other data are placed in the same cells as in the *polaris.xls* spreadsheet.

Dead reckoning position

Spreadsheet *dr.xls* computes the dead reckoning (DR) position (row 11) from the previous known position (cells A3 and B3), average speed in knots (cell A7), time interval in hours (cell B7, formatted as a regular floating point number), and course (cell C7).



The following image shows the spreadsheet *dr.xls*.



Advancing a position by dead reckoning

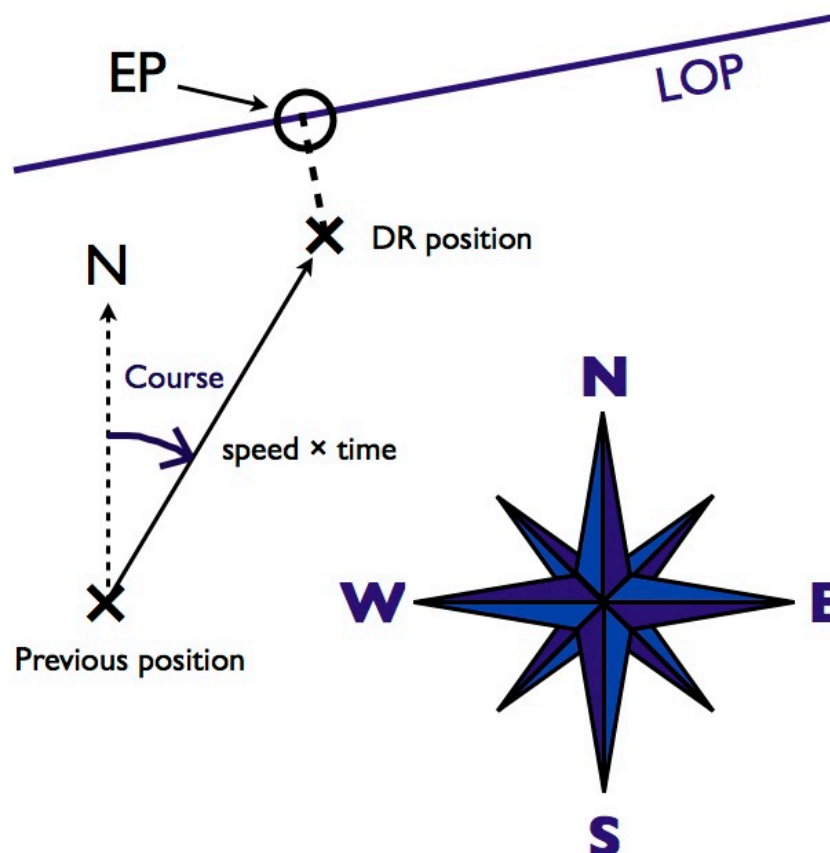
Enter previous position					
Latitude	Longitude				
3 109/200	92 61/75				
32.7	48.8				
Speed (kn)	Time (hours)	Course			
4.5	6	340			
Find new position					
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes
3.97	3	58.1	92.66	92	39.5

Summary for spreadsheet *dr.xls*:

Input cells: A3, B3, A7, B7, C7

Output cells: A11, B11, C11, D11, E11, F11

Dead reckoning fix of Estimated Position along LOP



When only one line of position (LOP) is available, it is possible to find your estimated position (EP) by using the dead reckoning position (DRP) as a guide. Spreadsheet *dr_fix_lop.xls* finds the EP as the point along the LOP which is closest to the DRP. The previous known position is entered in cells A3 and B3, average speed in knots in cell A7, time interval in hours in cell B7 (formatted as a regular floating point number), and course in cell C7. The LOP is defined as usual by the GP and Ho (cells D3, E3, and F3). The EP is displayed in row 11. The distance (in nautical miles) and bearing from the DRP to the EP are shown in cells C13 and F13, respectively.

The following image shows the spreadsheet *dr_fix_lop.xls*.

dr_fix_lop.xls					
A	B	C	D	E	F
Dead reckoning fix of EP along LOP					
Enter previous position, Geographical Position, and observed altitude (Ho)					
Latitude	Longitude		Declination	GHA	Altitude
-11 29/200	89 73/600		-13 139/200	288 61/75	72 47/200
08.7	07.3		41.7	48.8	14.1
Speed (kn)	Time (hours)	Course		Lat_DRP	Lon_DRP
15	3	160		-11.85	89.38
Retrieve the solution					
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes
-11.86	-11	51.6	89.31	89	18.6
DRP to EP:	Distance =	4.3	nautical miles	Bearing =	262
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *dr_fix_lop.xls*:

Input cells: A3, B3, D3, E3, F3, A7, B7, C7

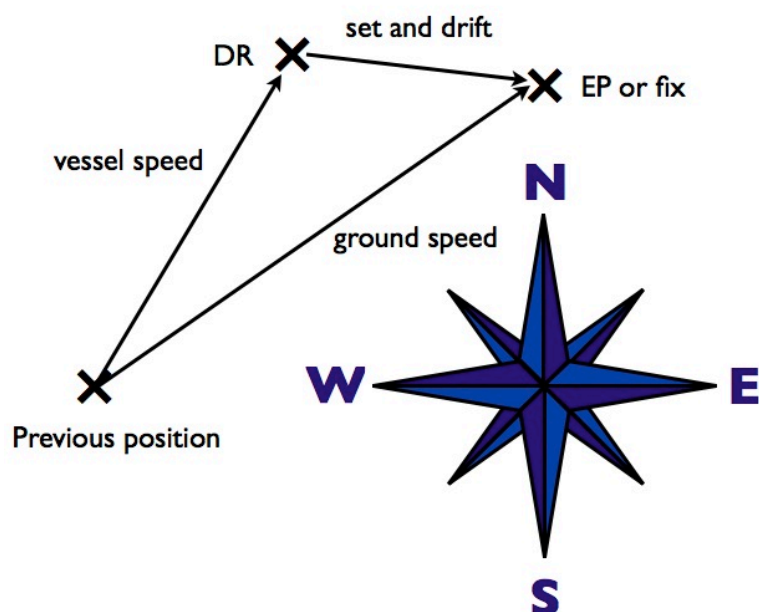
Output cells: A11, B11, C11, D11, E11, F11, C13, F13

The problem preset in this spreadsheet is a variation on the one treated in *The Celestial Navigation Mystery Solved* by David Owen Bell on p. xliii (Problem 1).

The auxiliary **minispreadsheet** *time.xls* can be used to add and subtract time data and also to perform conversions between the HH:MM:SS and hours-decimal formats.

Set and drift

The following four spreadsheets solve a number of variations of the set and drift problem. The preset values are taken from the end of the "Dead Reckoning" chapter in Bowditch.



set_and_drift.xls:

Calculation of set and drift from the difference between dead-reckoning and estimated positions.

set_and_drift.xls				
A	B	C	D	E

Set and drift from difference between DR and EP

DR Latitude	DR Longitude	EP Latitude	EP Longitude	Time (hours)
30	-40	30 1/5	-40 1/5	6.0
00.0	00.0	12.0	12.0	
Set	Drift (knots)			
319.1	2.6			
#####	#####	#####	#####	#####

ground_speed.xls:

Calculation of the ground speed from the current's speed and direction (i.e. set and drift) and the vessel speed relative to the water.

ground_speed.xls					
A	B	C	D	E	F

Track and speed made good

Vessel		Current		Ground	
Course	Speed	Set	Drift	Track	Speed
80.0	10.0	140.0	2.0	88.9	11.1
#####	#####	#####	#####	#####	#####

course_to_steel.xls:

Given the set and drift, the vessel's speed and the intended direction relative to ground, this spreadsheet calculates the required vessel course and the resulting ground speed. If the vessel's speed is too small to counteract the current, an error message is displayed in row 4.

course_to_steel.xls					
A	B	C	D	E	F

Course to steer, resulting ground speed

Vessel		Current		Ground	
Course	Speed	Set	Drift	Track	Speed
83.4	12.0	170.0	2.5	95.0	12.4
#####	#####	#####	#####	#####	#####

course_and_speed.xls:

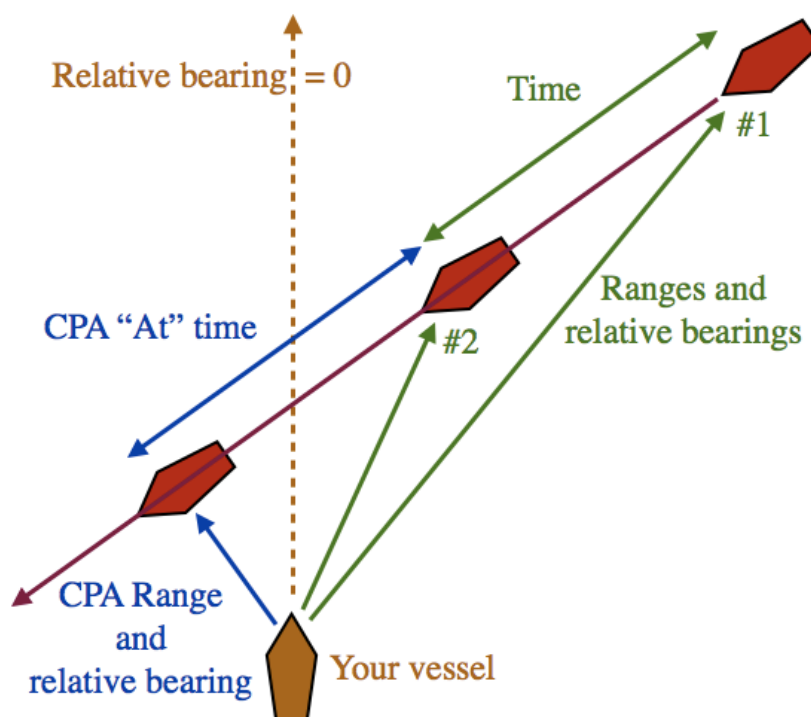
Calculation of the required vessel speed and course from the set and drift and the desired ground speed and track.

course_and_speed.xls					
A	B	C	D	E	F

Vessel speed and course to steer

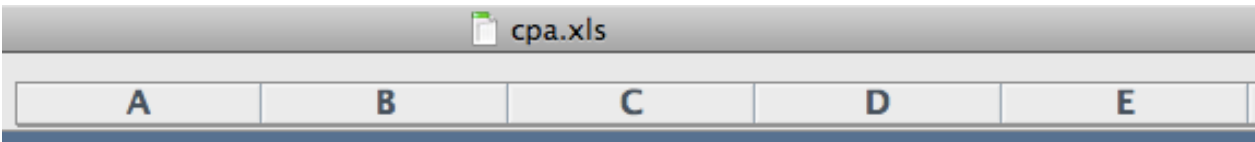
Vessel		Current		Ground	
Course	Speed	Set	Drift	Track	Speed
276.5	14.8	185.0	3.0	265.0	15.0
#####	#####	#####	#####	#####	#####

Closest point of approach



The spreadsheet *cpa.xls* computes the closest point of approach (CPA) of another vessel. This type of computation is useful for collision avoidance. All bearings and ranges (in nautical miles) are relative to your vessel's heading. The calculation encoded into this spreadsheet works with a locally flat Earth's surface (i.e. it is only valid for small distances) and assumes that both vessels in question move with constant speeds and tracks during the relevant time interval. The vessel is observed at two different ranges (cells A2 and C2) and relative bearings (cells B2 and D2) separated by time interval entered into cell E2 in the HH:MM:SS format. From this information the spreadsheet calculates the relative speed of the other vessel in knots (cell A5), range (cell B5) and relative bearing (cell C5) at the CPA, and the time interval between the second observation and the moment of the CPA (cell D5, in the HH:MM:SS format). If the range at CPA (cell A5) is close to zero, and if the "at" time (cell D5) is positive, the two vessels are headed for collision.

The following image shows the spreadsheet *cpa.xls*.



The screenshot shows a spreadsheet window titled 'cpa.xls'. The visible data is as follows:

Range 1	Bearing 1	Range 2	Bearing 2	Time (H:M:S)
5.0	50	2.0	40	0:10:00
Rel. speed	CPA range	Bearing	At (H:M:S)	since 2nd observation
18.3	0.6	326.5	0:06:17	
#####	#####	#####	#####	#####

Summary for spreadsheet *cpa.xls*:

Input cells: A2, B2, C2, D2, E2

Output cells: A5, B5, C5, D5

Sextant altitude corrections



The spreadsheet *alt_corr.xls* performs the corrections to the sextant altitude H_s (cell B1) that are needed to produce the apparent altitude H_a (cells B6, B7, B8) and the observed altitude H_o (cells B12, B13, B14). The index correction goes to cell B2. Cell B4 contains a yes/no (Y/N) answer to the question whether a reflecting artificial horizon was used. The semidiameter correction is entered in cell B9; this is positive for lower limb and negative for upper limb observations. The height of eye in cell E1 (enter “ft” for feet or “m” for meters in cell F1) determines the dip correction. Cells E2 and E3 control the refraction correction; the standard values are Temperature = 10 °C and Pressure = 1010 mb. Cell E6 contains the value of the horizontal parallax (HP) in arc minutes. The Moon parallax can also be corrected for the oblateness of the Earth by entering the latitude (E8) and azimuth (E9). The semidiameter value from either cell E11 (Sun - typical preset value, or from the almanac) or E12 (Moon - computed from the HP) is to be copied (with the appropriate sign characterizing the limb) into cell B11.

The following image shows the spreadsheet *alt_corr.xls*.

alt_corr.xls					
A	B	C	D	E	F
Corrections to sextant altitude					
Hs =	26 21/188	06.7	H. of eye =	5.4 m	
Index Corr =	0	00.0	Pressure =	982 mb	
Hs + IC =	26 21/188	06.7	Temp =	-3 C	
AH? (Y/N) =	N		Refraction =	-0.0336409	-0.0347807
Dip =	-0.0681645				-3
Ha =	26.044		HP (') =	60.7	1.01166667
Degrees =	26		Latitude =		0
Minutes =	02.6		Z =		0
Refraction =	-0.0336409	-02.0	OB =	0	
Parallax =	0.909	54.5	Sun SD (°) =	163/600	
SD =	-167/606	-16.5	Moon SD (°) =	0.275578	
Ho =	26.643				
Degrees =	26				
Minutes =	38.6				

Summary for spreadsheet *alt_corr.xls*:

Input cells: B1, B2, B4, B11, E1, F1, E2, E3, (E6, E8, E9 optional)

Output cells: B6, B7, B8, B12, B13, B14

Input/Output cells: E11, E12

The preset example contained in the spreadsheet is the upper limb Moon sight from p. 281 of the Nautical Almanac, 2009 Commercial Edition.

Precomputed sextant altitude

The spreadsheet *alt_prec.xls* is a reversed version of *alt_corr.xls*. It provides the altitude H_s to which the sextant may be preset before an observation. The observed altitude H_o (computed with *intercept.xls*) is now input in cell B12 and the sextant altitude is displayed in cells B1 and C1. The remaining cells have the same meaning as in *alt_corr.xls*.

The following image shows the spreadsheet *alt_prec.xls*.

alt_prec.xls					
A	B	C	D	E	F
Precomputing the sextant altitude					
Hs =	26 83/718	06.9	H. of eye =	5.4 m	
Index Corr =	0	00.0	Pressure =	982 mb	
Hs + IC =	26 83/718	06.9	Temp =	-3 C	
AH? (Y/N) =	N		Refraction =	-0.0327668	-0.0339968
Dip =	-0.0681645				-3
Ha =	26.047		HP (') =	60.7	1.01166667
Degrees =	26		Latitude =		0
Minutes =	02.8		Z =		0
Refraction =	-0.0327668	-02.0	OB =	0	
Parallax =	0.904	54.3	Sun SD (°) =	163/600	
SD =	- 167/606	-16.5	Moon SD (°) =	0.275578	
Ho =	26 193/300	38.6			

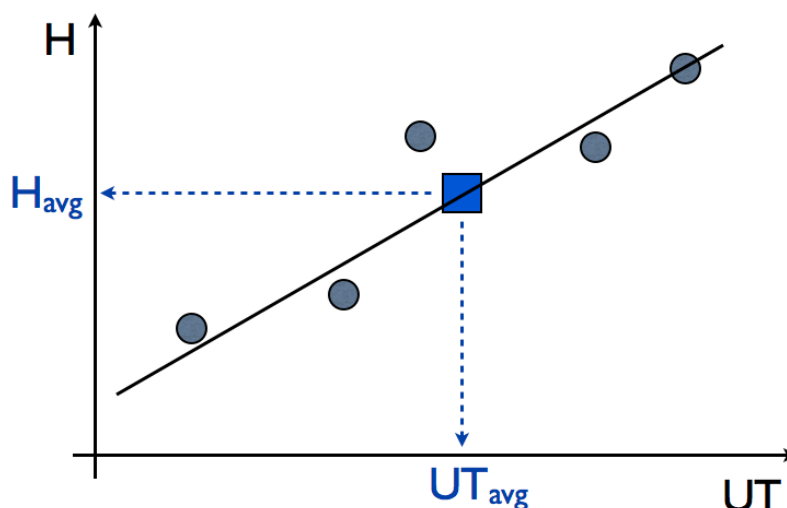
Summary for spreadsheet *alt_prec.xls*:

Input cells: B2, B4, B11, B12, E1, F1, E2, E3, (E6, E8, E9 optional)

Output cells: B1, C1, B6, B7, B8

Input/Output cells: E11, E12

Averaging of sights: 1) precomputed slope



Random errors can affect every individual sight. This problem can be mitigated by taking a set of measurements and averaging them. The spreadsheet *average1.xls* can perform this function for sextant altitude data (Hs). Enter the UT set in column A and the corresponding Hs set (in degrees) in column B. In cells F1 and F2 enter the expected sextant altitudes based on your position (*dr.xls*, *almanac*, *intercept.xls*, and *alt_prec.xls* spreadsheets are relevant here). This spreadsheet then calculates a weighted least-squares straight-line fit to the data, whose slope is derived from values in cells F2 and F3. From this fit it then extracts the average UT (cell G5) and Hs (cells G6, G7, G8). You also have the option of evaluating the average Hs (cells F6, F7, F8) at the UT of your choice (cell F5). Column D contains the weights (maximum=1.000) with which each particular data point is influencing the final result. The “Scatter” parameter (cell F13, in arcminutes) should be adjusted so that cell F14 is as close to 1 as possible and the weights in column D end up neither all 1.000, nor all (but one) much smaller than 1.000. Cells F10, F11, F12 should be small as they indicate the convergence of the encoded iterative procedure and the closeness of the fit to the original data. (Further details about the technique and the meaning of these cells are available upon request.) The time interval over which the average is computed should be short (about 5 minutes maximum), so that the assumed straight-line approximation remains justified. The resulting average altitude is a sextant altitude Hs and therefore should be processed with *alt_corr.xls* to yield the observed altitude Ho.

The following image shows the spreadsheet *average1.xls*.

average1.xls						
A	B	C	D	E	F	G
Averaging of sights (precomputed slope)						
Enter UT in column A (HH:MM:SS), Altitude (Hs) in column B (Degrees Minutes*10/600)						
12:00:00	10	00.0	0.096	Hs comp init =	10	00.1
12:02:00	10 1/6	10.0	1.000	Hs comp final =	10 2/3	40.0
12:05:00	10 1/2	30.0	0.338	Hs change =	0.665	39.9
		00.0	0.000			
		00.0	0.000	Time of sight =	12:02:00	12:02:34
		00.0	0.000	Altitude =	10.158	10.234
		00.0	0.000	Degrees =	10	10
		00.0	0.000	Minutes =	09.5	14.0
		00.0	0.000			
		00.0	0.000	Last diff =	0.001	00.0
		00.0	0.000	 Hfit - Hinit =	0.020	01.2
		00.0	0.000	 Max diff =	0.108	06.5
		00.0	0.000	Scatter (') =	02.0	
		00.0	0.000	Norm. Q2 =	1.031	
		00.0	0.000			

Summary for spreadsheet *average1.xls*:

Input cells: column A, column B, F1, F2, F5, F13

Output cells: column D, F6, F7, F8, F10, F11, F12, F14, G5, G6, G7, G8

Averaging of sights: 2) fitted slope

The spreadsheet *average2.xls* performs the same function as *average1.xls*, but for ***observed*** altitude data (Ho) in column B, while allowing the procedure to also choose the slope of the fit. Additional input data include the speed (cell F1) and course (cell F2) of the vessel, the hourly declination change rate (cell F5, in arcminutes), and azimuth (cell F7, in degrees) of the observed body. The remaining cells serve the same function as in *average1.xls*. The weights in column D should come out neither all 1.000, nor all (but two) very small.

The following image shows the spreadsheet *average2.xls*.

average2.xls						
A	B	C	D	E	F	G
Averaging of sights (fitted slope)						
Enter UT in column A (HH:MM:SS), Altitude (Ho) in column B (Degrees Minutes*10/600)						
12:00:00	9 59/60	59.0	1.000	Speed (kn) = 0		
12:00:30	10 1/10	06.0	0.751	Course = 0		
12:01:00	10 1/10	06.0	1.000			
		00.0	0.000	Dec change		
		00.0	0.000	(') per hour = 0.0		
		00.0	0.000			
		00.0	0.000	Azimuth = 0		
		00.0	0.000			
		00.0	0.000	Time of sight = 12:00:30		
		00.0	0.000	Altitude = 10.058		
		00.0	0.000	Degrees = 10		
		00.0	0.000	Minutes = 03.5		
		00.0	0.000			
		00.0	0.000	Last diff = 0.000		
		00.0	0.000	Hfit - Hinit = 0.004		
		00.0	0.000	Max diff = 0.042		
		00.0	0.000	Scatter (') = 02.2		
		00.0	0.000	Norm. Q2 = 1.381		
		00.0	0.000			

Summary for spreadsheet *average2.xls*:

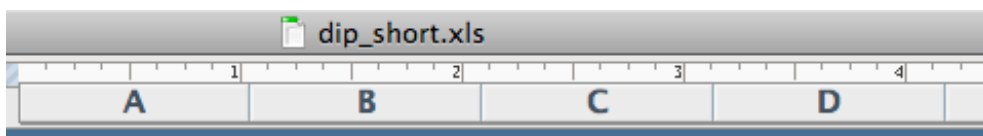
Input cells: column A, column B, F1, F2, F5, F7, F9, F17

Output cells: column D, F10, F11, F12, F14, F15, F16, F18, G9, G10, G11, G12

Dip short of the horizon

The spreadsheet *dip_short.xls* implements the formula behind Table 14 in Bowditch. The height of eye can be entered in meters or feet (enter "m" or "ft" in cell C1). The distance to the waterline in cell B2 is in nautical miles. The resulting dip is output in cell B3 in nautical miles.

The following image shows the spreadsheet *dip_short.xls*.



Dip short of the horizon

H. of eye =	30.0 ft		
Distance =	2.5 nm		
Dip =	7.8 arc minutes		

Summary for spreadsheet *dip_short.xls*:

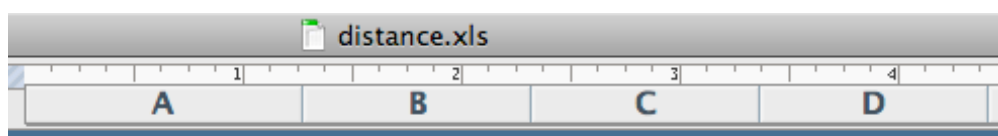
Input cells: B1, C1, B2

Output cells: B3

Distance by vertical angle

The spreadsheet *distance.xls* implements the formula from Bowditch to calculate the distance by vertical angle between the waterline and the top of an object. Select "ft" or "m" in cells C1 and C2, and enter the corrected vertical angle in cell B3. The distance in nautical miles is displayed in cell B4.

The following image shows the spreadsheet *distance.xls*.



Distance to an object

H. of eye =	30.0 ft	
H. of object =	100.0 ft	
Vertical angle =	7/600 00.7	
Distance =	9.0 nm	

Summary for spreadsheet *distance.xls*:

Input cells: B1, C1, B2, C2, B3

Output cells: B4

Altitude correction for motion of the vessel

The spreadsheet *alt_move.xls* calculates the effective observed altitude associated with a line of position that is advanced or retarded by dead reckoning. In this technique of compensating for the vessel motion the assumed position is unchanged and only the final adjusted LOP needs to be plotted. Enter the original observed altitude and azimuth from spreadsheet *intercept.xls* in cells A2 and B2. Enter ground speed and course made good in cells C2 and D2. The time interval in cell E2 is positive to advance the LOP and negative to retard the LOP. The (signed) distance traveled in nautical miles is displayed in cell F2. Reenter the adjusted observed altitude from row 6 in cell E2 of *intercept.xls* to obtain the new intercept.

The following image shows the spreadsheet *alt_move.xls*.

A	B	C	D	E	F
---	---	---	---	---	---

Adjustment of observed altitude for motion of the vessel

Ho original	Azimuth	Speed (kts)	Course	Time (hours)	DR (nm)
30	160.0	10.0	100.0	0.1000	1.0
00.0					
Ho adjusted	Degrees	Minutes			
30.008	30	00.5			

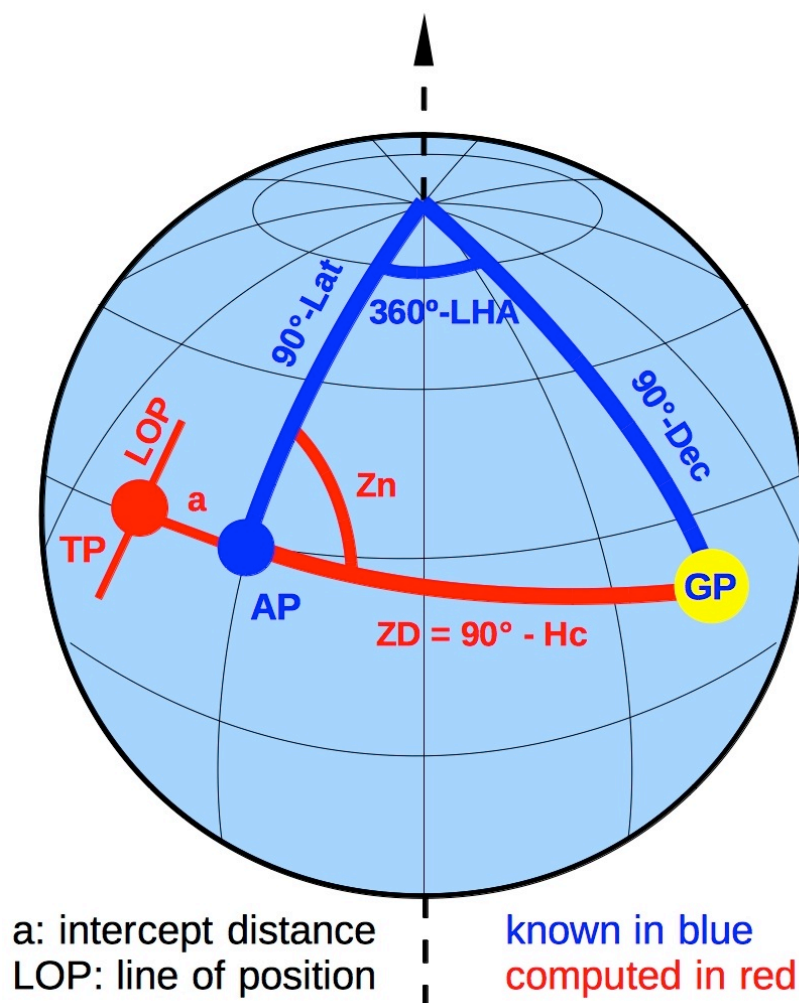
Summary for spreadsheet *alt_move.xls*:

Input cells: A2, B2, C2, D2, E2

Output cells: A6, B6, C6

Intermediate cell: F2

Sight reduction using the intercept method



The spreadsheet *intercept.xls* solves the navigation triangle in accordance with the intercept method of Marcq Saint-Hilaire. Enter the latitude and longitude of the assumed position (AP) in cells A2, B2, the GHA and Declination (GP) in cells C2, D2, and the observed altitude (Ho) in cell E2. Cell F2 computes and displays the Local Hour Angle (LHA). If you have already determined LHA and want to use it as input, enter it in place of GHA (cell C2) and set the AP Longitude (in cell B2) to zero. The calculated altitude (Hc) at the AP is in cells A6, B6, C6 and the intercept distance (in nautical miles) is displayed in cells D6 and E6. The azimuth Zn toward the GP from the assumed position is in cell F6. This allows you to plot the line of position (LOP), along which the “true” position (TP) is located. Rows 7, 9, 12, and 15 contain additional

information about LOP properties that allow the plotting of the LOP without the azimuth line using the T-Plotter™. This reduces the clutter on the chart when multiple LOP's are plotted.

The following image shows the spreadsheet *intercept.xls*.

intercept.xls					
A	B	C	D	E	F
LOP properties from the assumed position and Ho based on the intercept method of Marcq St. Hilaire					
AP Latitude	AP Longitude	GHA	Declination	Ho	LHA
13	0	334	3 179/200	62 3/5	334
00.0	00.0	00.0	53.7	36.0	00.0
Hc	Degrees	Minutes	Intercept		Azimuth
62.75	62	45.0	9.0 AWAY		107.2
			9.0 TOWARD		287.2
LOP properties		Directions =	197.2	17.2	
LOP intersects	AP latitude:	Longitude	Degrees	Minutes	nm from AP
		-0.16	0	09.7	-9.4
LOP intersects	AP longitude:	Latitude	Degrees	Minutes	nm from AP
		13.51	13	30.4	30.4
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *intercept.xls*:

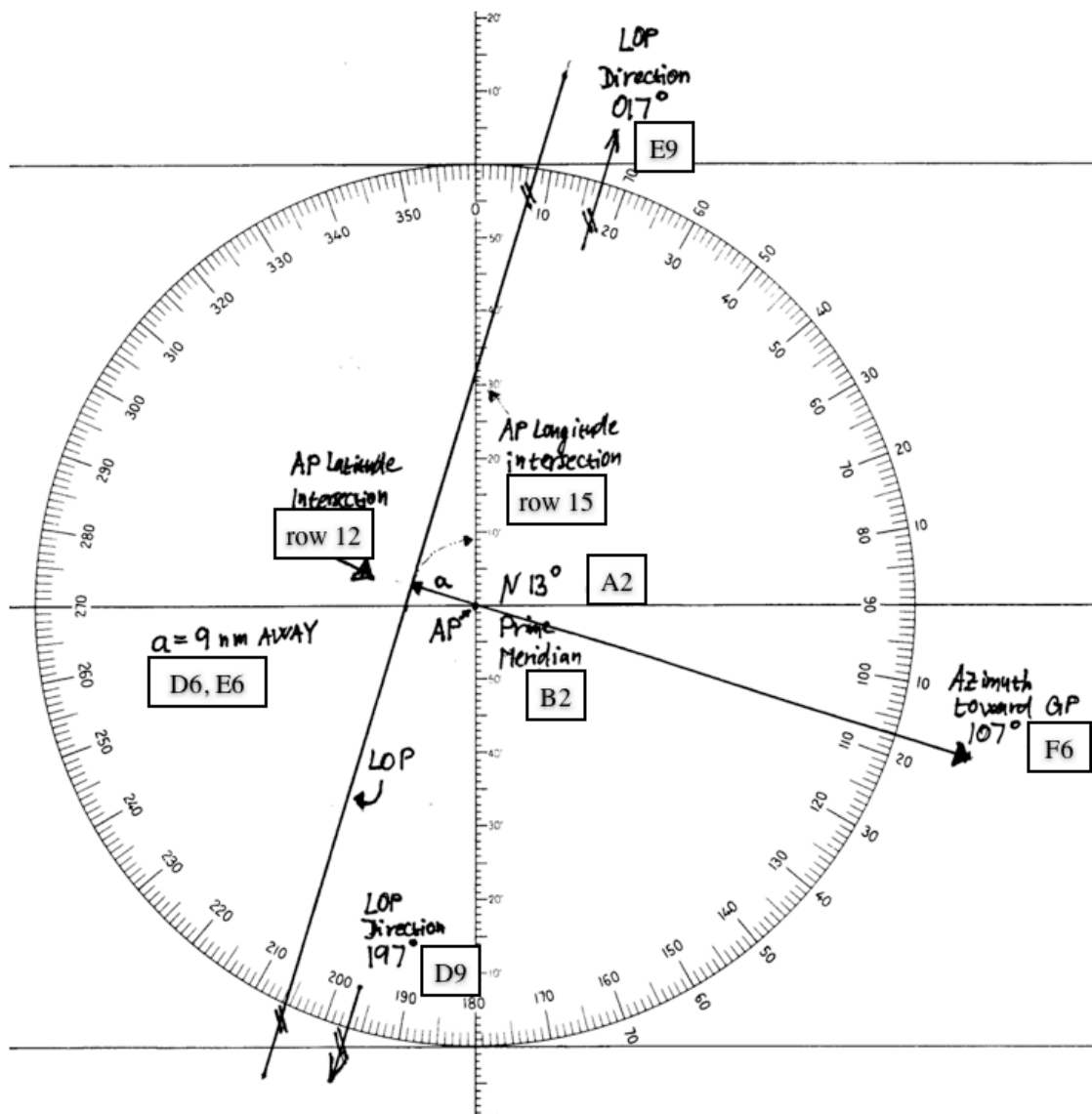
Input cells: A2, B2, C2, D2

Output cells: A6-F6, D7-F7, D9, E9, C12-F12, C15-F15

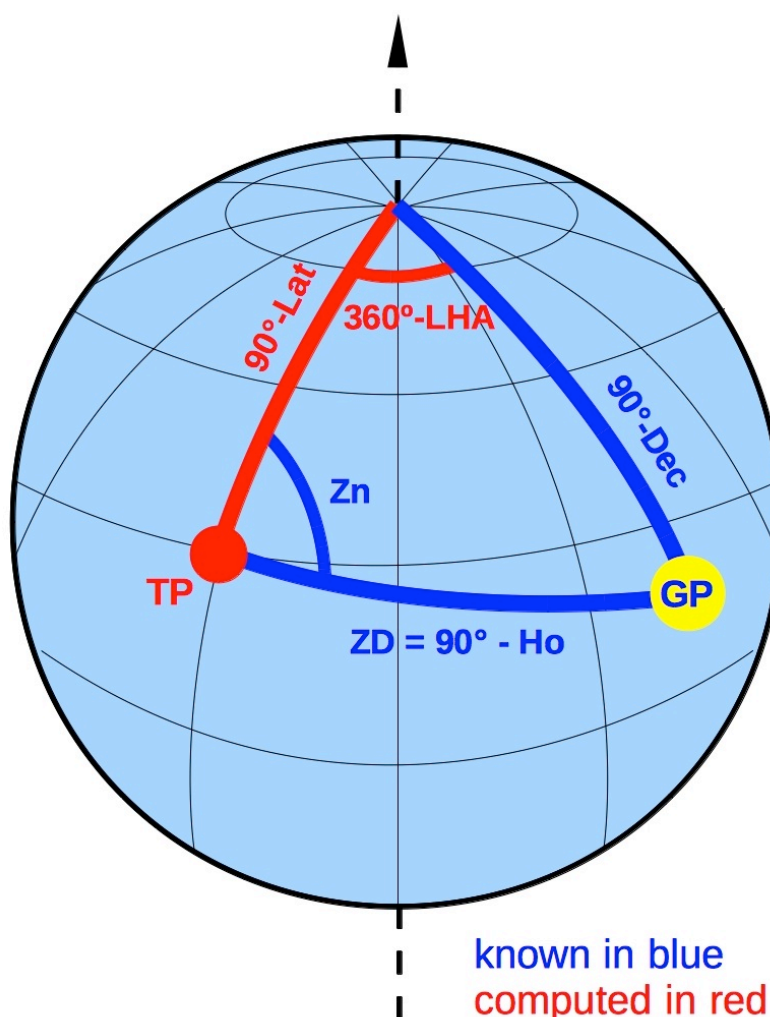
Intermediate cell: F2

It is also possible to use this spreadsheet to precompute altitudes before an observation. For that purpose the computed altitude Hc displayed in cell A6 can be further matched to the actual observation conditions with spreadsheet *alt_prec.xls* (enter Hc in cell B12), which corrects for refraction, semidiameter, parallax, and index error.

The calculated LOP on a plotting sheet:

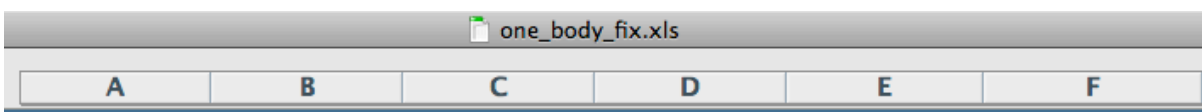


The one-body fix



If both the azimuth (Z_n) and the altitude (H_o) of a celestial body is known, then it is possible to obtain a fix for the “true” position (TP) from observing that one body alone. The spreadsheet *one_body_fix.xls* solves the navigation triangle in this scenario. The GP is characterized by its declination (cell A2) and Greenwich Hour Angle (B2). The azimuth (Z_n) is entered in cell C2, and the observed altitude (H_o) goes into cell D2. The TP coordinates are displayed in row 6.

The following image shows the spreadsheet *one_body_fix.xls*.



One-body fix from the Ho and the GP (declination, GHA, azimuth)

Declination	GHA	GP Azimuth	Altitude		
3 179/200	0	107.22	62 3/4		
53.7	00.0		45.0		
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes
13.00	13	00.1	-26.00	-25	60.0
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *one_body_fix.xls*:

Input cells: A2, B2, C2, D2

Output cells: A6, B6, C6, D6, E6, F6

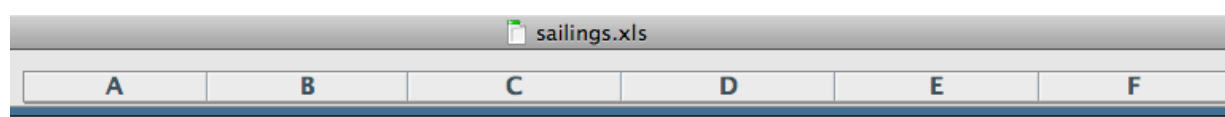
The preset data in this spreadsheet define an inverse problem to the one preset in *intercept.xls*.

Great-circle and rhumb-line sailings

This group of spreadsheets (*sailings.xls*, *waypoints.xls*, *composite.xls*) can assist you in planning your trip from the point of Departure to Destination. The example preset in these spreadsheets pertains to a trip from San Francisco (USA) to Yokohama (Japan). This choice is inspired by Figure 2404 in Bowditch (p. 347).

In spreadsheet *sailings.xls* you enter the coordinates of the Departure and Destination points in row 2. The spreadsheet calculates the distances and courses from Departure to Destination along the resulting great circle (columns B, C) and rhumb line (columns E, F). The results are displayed both assuming a perfectly spherical (row 6) as well as a flattened (row 7) Earth model. The initial great-circle course in the yellow cell C6 is displayed with (otherwise unrealistic) three decimal places in order to minimize numerical round-off errors when that value is subsequently copied into the D2 input cell of the spreadsheet *waypoints.xls*. Finally, row 11 displays the coordinates of the great-circle vertex on the path from Departure toward Destination..

The following image shows the spreadsheet *sailings.xls*.



The screenshot shows a spreadsheet window titled 'sailings.xls' with columns A through F. Below the spreadsheet, the title 'Great-circle and rhumb-line sailings' is centered. The data is as follows:

Departure	Latitude	Longitude	Destination	Latitude	Longitude
	37 4/5	-122 11/20		34 7/10	140 1/10
	48.0	33.0		42.0	06.0
Great circle	Distance (nm)	Initial Course	Rhumb line	Distance (nm)	Course
spherical =	4475.1	302.240	spherical =	4712.9	267.7
ellipsoidal =	4481.0	302.3	ellipsoidal =	4733.9	267.7
Great circle vertex					
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes
48.062	48	03.7	-168.371	-168	22.2
#####	#####	#####	#####	#####	#####

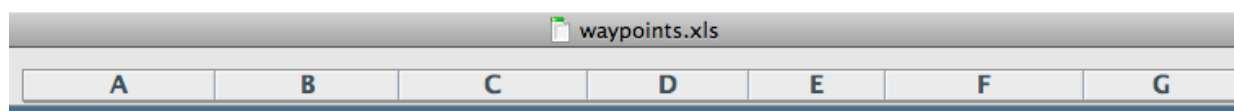
Summary for spreadsheet *sailings.xls*:

Input cells: B2, C2, E2, F2

Output cells: B6, C6, E6, F6, B7, C7, E7, F7, row 11

The spreadsheet *waypoints.xls* takes the coordinates of the Departure point (cells B2, C2) and (in cell D2) the initial course (e.g. from cell C6 in *sailings.xls*). Row 7 displays the great-circle vertex. Starting in row 11 you can use column A to specify the longitude of each waypoint along the great circle. The spreadsheet then calculates the corresponding latitude (columns C, D, E) and the (flattened Earth model) rhumb-line distance (column F) and the constant course (column G) from the previous waypoint. The total length of this path is shown in cell F2.

The following image shows the spreadsheet *waypoints.xls*.



Great-circle vertex and waypoints
Rhumb lines between waypoints

Departure	Latitude	Longitude	I. Course		Total (nm)	
	37 4/5	-122 11/20	302.240		4489.5	
	48.0	33.0				
Great circle vertex						
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes	
48.062	48	03.7	-168.370	-168	22.2	
Waypoints						
Longitude		Latitude	Degrees	Minutes	Distance (nm)	Course
-125	00.0	38.976	38	58.6	135.5	301.4
-130	00.0	41.109	41	06.5	263.7	299.0
-135	00.0	42.908	42	54.5	248.4	295.8
-140	00.0	44.402	44	24.1	235.5	292.4

Summary for spreadsheet *waypoints.xls*:

Input cells: B2, C2, D2, column A starting in row 11

Output cells: F2, row 7, columns C, D, E, F, G starting in row 11

For more information on the preset example please visit the **SAILINGS** entry on our [blog](#).

Composite sailing

The spreadsheet *composite.xls* takes the initial great-circle course from *sailings.xls* (cell C6) and modifies this calculated great-circle route from the point of Departure (cells B2, C2) to Destination (cells E2, F2) so as not to go beyond the chosen limiting parallel of latitude (cell B9). The resulting two waypoints along this limiting parallel (plus the third waypoint, which is the Destination) are displayed in rows 12, 13, and 14. The courses shown in cells F12 and F14 are the initial great-circle (spherical Earth) courses to the first waypoint and to the Destination, respectively. The constant course in cell F13 reflects the east or west direction of the latitude sailing along the limiting parallel from the first to the second waypoint. If needed, waypoints along the two great-circle legs of this trip can be calculated with *waypoints.xls*.

Yellow cells in rows 5 and 9 display text messages about the result and status of the composite sailing calculation. These messages are:

cell D9: INVALID: the limiting parallel was chosen between the equator and either the Departure or the Destination point. Composite sailing path cannot be computed in this case. Rows 12, 13, and 14 are zeroed out.

cell F9: Composite OK: Non-trivial composite sailing path is successfully calculated.

cell E9: Unconstrained gc (great circle): The limiting parallel is between the vertex and its Pole and therefore does not affect the originally computed great-circle sailing path. The first and second waypoints are identical as they coincide with the vertex.

cell C5: Vertex beyond destination: This happens for relatively close Departure and Destination points, which are not separated by the vertex. The choice of limiting parallel is voided in this case and rows 13 and 14 are zeroed out. A great-circle sailing calculation is displayed in row 12. The Unconstrained gc message is also displayed in cell E9 in this case.

The following image shows the spreadsheet *composite.xls*.

composite.xls					
A	B	C	D	E	F
Composite sailing between two locations Enter latitude of the limiting parallel in B9					
Departure	Latitude	Longitude	Destination	Latitude	Longitude
	37 4/5	-122 11/20		34 7/10	140 1/10
	48.0	33.0		42.0	06.0
Great circle	vertex				
Latitude	Degrees	Minutes	Longitude	Degrees	Minutes
48.062	48	03.7	-168.371	-168	22.2
Limiting parallel	40	00.0	Composite OK		
Waypoints	Longitude	Degrees	Minutes	Distance (nm)	Initial Course
From departure	-144.969	-144	58.1	1052.3	284.190
Along parallel	174.490	174	29.4	1863.4	270
To destination	140.100	140	06.0	1660.2	270
			Total (nm) =	4575.8	
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *composite.xls*:

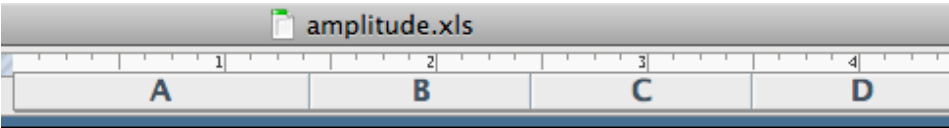
Input cells: B2, C2, E2, F2, B9

Output cells: row 7, block B12 through F14, E15

Amplitude

Rising and setting celestial bodies can be used to check for compass errors. In spreadsheet *amplitude.xls* enter whether the body is rising or setting in cell B1, the ship's latitude goes into cell B2, and cell B3 takes the declination of the body observed on the celestial horizon. The calculated amplitude in cell B4 inherits its sign from the declination input in B3. The calculated azimuth from cell B5 can be compared with the one observed and thus used to determine the error of that compass.

The following image shows the spreadsheet *amplitude.xls*.



Amplitude and Azimuth
of a rising or setting body

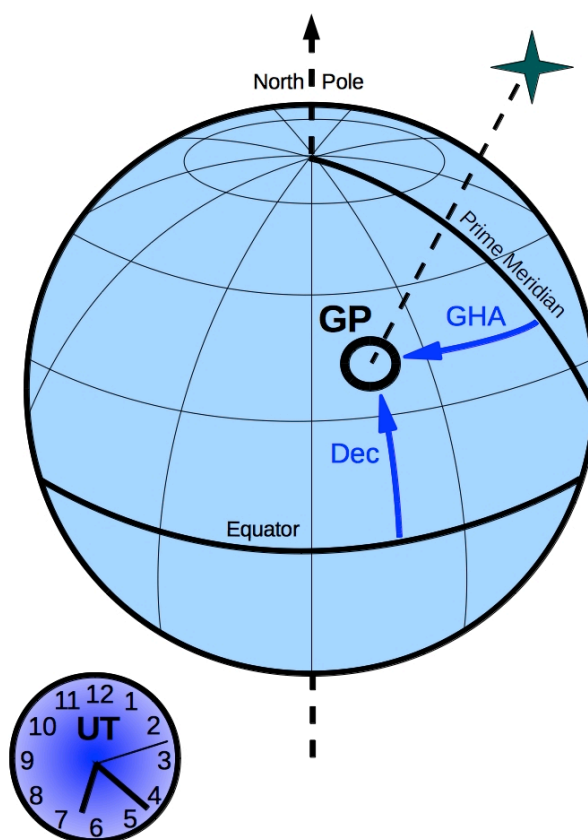
Rise/Set (R/S)?	S		
Latitude	51 41/100	24.6	
Declination	19 101/150	40.4	
Amplitude	32.7		
Azimuth	302.7		

Summary for spreadsheet *amplitude.xls*:

Input cells: B1, B2, B3

Output cells: B4, B5

Almanac data



The Geographical Position (GP) of a celestial body is the location on the surface of the Earth from which this body appears directly overhead (at a given point in time). The measurement of the body's altitude above the horizon (H_o) with a sextant tells us how far we are from the GP (Zenith distance = $ZD = 90^\circ - H_o$). Therefore, in order to derive our position we need to know the observed body's GP at the moment its altitude was measured. The GP's and other data are published in almanacs as a function of Universal Time (UT). The spreadsheets *sun.xls*, *moon.xls*, *mercury.xls*, *venus.xls*, *mars.xls*, *jupiter.xls*, *saturn.xls*, *uranus.xls*, *neptune.xls*, and *aries_stars.xls* calculate the GP's of these bodies from the year, month, day, hour, minute, and second of UT. Thus there is no need for interpolation (increments and corrections). Data calculated by the solar system spreadsheets also include the semidiameter (SD) and horizontal parallax (HP) data. The equation of time is provided by the *sun.xls* spreadsheet.

The following image shows the spreadsheet *moon.xls*.

moon.xls					
A	B	C	D	E	F
GP of Moon Enter Universal Time					
Year	Month	Day	Hours	Minutes	Seconds
2011	01	01	12	00	00
GHA	Degrees	Minutes	Declination	Degrees	Minutes
	37	09.9	S 23		39.1
SD (')		HP (')		Age (d)	Phase (%)
15.7		57.6		27	9
#####					

Summary for the Sun, Moon, and planetary spreadsheets:

Input cells: A2, B2, C2, D2, E2, F2 (Universal Time)

Output cells: B5, C5, E5, F5 (GP); A8 (SD), C8 (HP, both in arcminutes); E8, F8

The spreadsheet *aries_stars.xls* provides the GHA of Aries from which the GHA of any star can be determined by adding it to its SHA (sidereal hour angle). The UT is entered in row 2. The GHA of Aries is displayed in cells B5 and C5. You may enter the SHA of the observed star in cells E10, F10 (compound fractions are not used here) and retrieve its GHA from cells B11, C11. If the observed star is one of the 57 main navigation stars you may also scroll down the spreadsheet and find its GP there. The SHA's and declinations of these main stars are in columns E, F. The spreadsheet calculates these quantities from the UT taking into account the effects of light aberration, Earth's precession and nutation, and the star's proper motion. The SHA for each star is then added to the GHA of Aries resulting in the star's GHA in columns B, C. The numbers next to the star's name are its almanac ID (column B) and magnitude (column C).

The following image shows the spreadsheet *aries_stars.xls*. Data in rows 10, 11 are for Markab.

aries_stars.xls					
A	B	C	D	E	F
GHA of Aries, GP of main navigation stars					
Enter Universal Time					
Year	Month	Day	Hours	Minutes	Seconds
2011	01	01	12	00	00
GHA Aries	Degrees	Minutes			
280.80	280	47.8			
#####	#####	#####	#####	#####	#####
Star	Number	Magnitude	SHA =	Degrees	Minutes
GHA	Degrees	Minutes		13	40.2
294.47	294	28.0			
#####	#####	#####	#####	#####	#####
Acamar	7	3.2	SHA =	315	19.4
GHA	Degrees	Minutes	Declination	Degrees	Minutes
236.12	236	07.1	S 40		15.8
#####	#####	#####	#####	#####	#####
Achernar	5	0.5	SHA =	335	27.8
GHA	Degrees	Minutes	Declination	Degrees	Minutes
256.26	256	15.6	S 57		11.1
#####	#####	#####	#####	#####	#####
Acrux	30	1.3	SHA =	173	11.4
GHA	Degrees	Minutes	Declination	Degrees	Minutes

Summary for spreadsheet *aries_stars.xls*:

Input cells (in green): A2, B2, C2, D2, E2, F2 (Universal Time), E10, F10 (SHA)

Output cells (in cyan): columns B and C (GHA), columns E and F (declination)

Intermediate cells (in yellow): columns E and F (SHA) - from row 15 down

The Sun and planetary data are computed using the VSOP87 theory by Bretagnon and Francou.

The Moon data are calculated from the improved Chapront ELP-2000/82 lunar theory.

What star is this?

The spreadsheet *what_star.xls* is the combination of the *aries_stars.xls* and *intercept.xls* spreadsheets. It allows the identification of the observed star based on UT (row 2), your known location (cells A5, B5), observed altitude (cell C5), and azimuth (D5) of the star. Working with the catalog of the 57 main navigation stars, in cell E5 the spreadsheet displays the star that is the closest match to the input data.

The following image shows the spreadsheet *what_star.xls*.

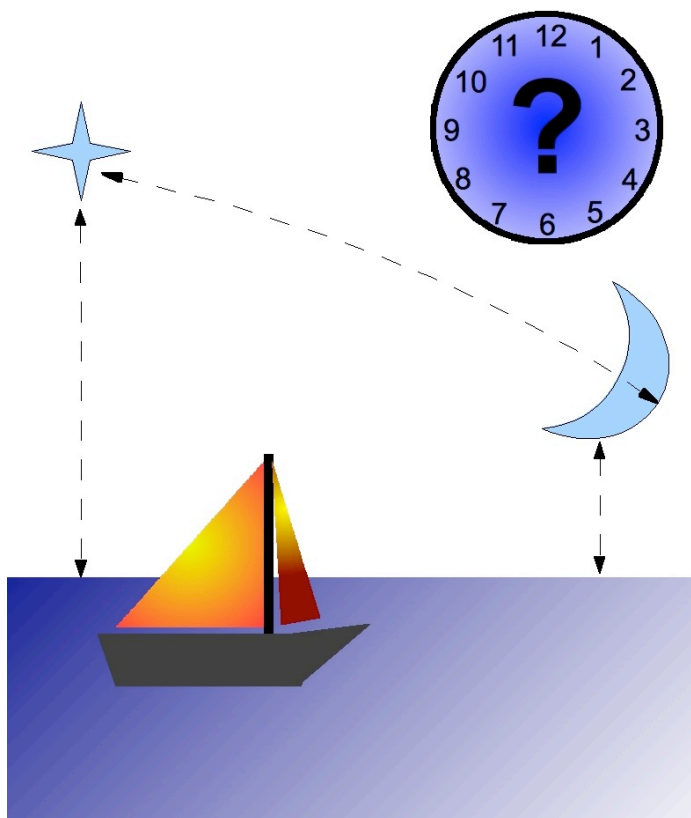
what_star.xls					
A	B	C	D	E	F
Star identification based on UT, Ho, and azimuth from a known location					
Year	Month	Day	Hours	Minutes	Seconds
2011	01	01	12	00	00
Latitude	Longitude	Altitude	Azimuth	Star	
-30	-120	66 257/300	227.9	Suhail	
00.0	00.0	51.4			
#####	#####	#####	#####	#####	#####

Summary for spreadsheet *what_star.xls*:

Input cells: A2, B2, C2, D2, E2, F2 (Universal Time), A5, B5, C5, D5

Output cell: E5

Lunar distance clearing and UT recovery



The lunar distance technique allows you to determine Universal Time (UT) in case you cannot rely on a chronometer. This method is not all that accurate by modern standards but it is rigorous and can serve as a viable backup option. The spreadsheet *lunar_distance.xls* clears the lunar distance and then performs the interpolation that yields an improved UT. Start by entering your best estimate of UT in row 3. Select Time1 and Time2 instants on opposite sides of this estimate and enter the corresponding GPs of the Moon and the other body in rows 7 and 12. The apparent and observed altitudes go to row 17. Enter the observed lunar distance (corrected for index error only) into cell B22. The objects' semidiameters are placed in cells C22 and E22 (enter near-limb values as positive, and far-limb values as negative). The computed UT is displayed in cell C30, which is $\text{Time1} + T_{\text{add}}$ (i.e. the sum of cells A7 and B30). Verify that the interpolation factor IntF (cell A30) lies between 0 and 1. If that is not the case then the two instants Time1 and Time2 do not “bracket” the “true” UT and need to be changed accordingly.

The following image shows the spreadsheet *lunar_distance.xls*.

lunar_distance.xls					
A	B	C	D	E	F
UT from lunar distance Enter estimated UT in row 3					
Estimated UT					
Year	Month	Day	Hours	Minutes	Seconds
2005	05	12	21	18	16
Bracketing UTs	from almanac				
Time1	Moon GHA	Moon Dec	Body GHA	Body Dec	LD1
21:00:00	79 59/60	27 497/600	135 23/25	18 13/40	51.9036333
	59.0	49.7	55.2	19.5	54.2
	1.39597251	0.48569604	2.372251519	0.31983159	0.90588929
Time2	Moon GHA	Moon Dec	Body GHA	Body Dec	LD2
22:00:00	94 139/300	27 467/600	150 23/25	18 67/200	52.3615952
	27.8	46.7	55.2	20.1	21.7
	1.64869619	0.48482338	2.634050907	0.32000612	0.91388224
Altitudes (Ha)	Moon	Body	Altitudes (Ho)	Moon	Body
apparent	30 121/200	38 199/300	observed	31 107/300	38 129/200
	36.3	39.8		21.4	38.7
	0.53415802	0.67480247		0.54727708	0.67448249
Lunar distance	Obs. LD (°)	SD Moon (')	SD Moon aug	SD Body (')	Cent. LD (°)
	51 523/600	14.9	15.0323703	15.9	52.3872062
	52.3				23.2
					0.91432923
cos RBA	cos LD0	LD0 rad	LD0 deg	Cleared LD	
0.434865249	0.61499997	0.9084104	52.04808187	52	02.9
0 < IntF < 1 ?	T add	UT			
0.32	0:18:55	21:18:55			

Summary for spreadsheet *lunar_distance.xls*:

Input cells: row 3, A7-E7, A12-E12, B17, C17, E17, F17, B22, C22, E22

Output cells: A30, B30, C30

Intermediate lunar distance cells: F7, F12 (computed), F22 (centered), E27, F27 (cleared)

The method and example preset in this spreadsheet can be found in *Celestial Navigation in the GPS Age* by John Karl, pp. 93-95.

Precomputed lunar distance

The spreadsheet *ld_comp.xls* allows the calculation of the center-to-center (i.e. no semidiameter) geocentric lunar distance (cells A10, B10, C10) from almanac data (row 2). The topocentric result in cells D10, E10, F10 includes the effect of Moon's parallax on the lunar distance, when observed from an assumed position (cells E6, F6). While these results do not include the effects of refraction, they are close enough for your sextant to be preset to an angle that is sufficiently close to the actual observed value. The values are preset for a Sun lunar on January 8, 2011, UT = 22:00:00.

The following image shows the spreadsheet *ld_prec.xls*.

Lunar distance calculation from almanac data					
Moon GHA	Moon Dec	Moon HP (')		Body GHA	Body Dec
98 511/600	-3 31/60	54.3		148 187/600	-22 19/100
51.1	31.0			18.7	11.4
				AP Latitude	AP Longitude
				37 4/5	-122 11/20
Lunar distance:				48.0	33.0
Geocentric	Degrees	Minutes	Topocentric	Degrees	Minutes
51.401	51	24.0	51.404	51	24.2
#####					

Summary for spreadsheet *ld_prec.xls*:

Input cells: A2, B2, C2, E2, F2, E6, F6

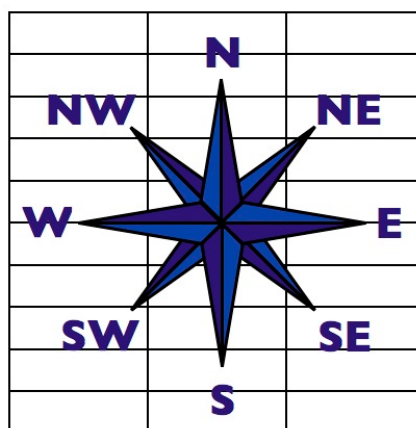
Output cells: A10, B10, C10, D10, E10, F10

Alphabetical list of spreadsheets

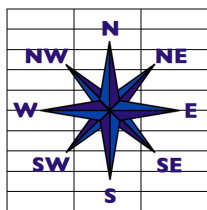
1. **alt_corr**: sextant altitude corrections
2. **alt_move**: correction of observed altitude for motion of the vessel
3. **alt_prec**: precomputed sextant altitude
4. **amplitude**: amplitude and azimuth of a rising or a setting body
5. **aries_stars**: GHA of Aries and GPs of 57 main navigation stars
6. **average1**: averaging of sights (precomputed slope)
7. **average2**: averaging of sights (fitted slope)
8. **composite**: composite sailing calculation
9. **course_and_speed**: ground speed from the vessel speed and speed of current
10. **course_to_steer**: vessel course from set and drift and desired ground track
11. **cpa.xls**: closest point of approach from two ranges and relative bearings
12. **dip_short**: dip short of the horizon
13. **distance**: distance by vertical angle
14. **dr**: dead reckoning position (DRP)
15. **dr_fix_lop**: estimated position (EP) from a DRP and a celestial LOP
16. **ex_meridian**: ex-meridian latitude calculation
17. **ground_speed**: ground speed from vessel speed and set and drift
18. **intercept**: intercept and azimuth for the St. Hilaire method
19. **jupiter**: almanac data for Jupiter
20. **ld_prec**: geocentric and topocentric lunar distance from almanac data
21. **lops**: two-body fix (using spatial geometry)
22. **lunar_distance**: LD clearing and chronometer resetting
23. **many_body_fix**: multiple LOP fix calculation
24. **mars**: almanac data for Mars
25. **mercury**: almanac data for Mercury
26. **minutes**: conversion of fractional angles into minutes of arc
27. **moon**: almanac data for Moon
28. **neptune**: almanac data for Neptune
29. **noon_curve**: Sun LAN curve fix
30. **noon_motion**: Sun LAN curve fix with motion of the vessel
31. **noon_sight**: Sun LAN fix
32. **one_body_fix**: fix from a zenith distance and azimuth
33. **polaris**: latitude from Polaris (UT input)
34. **polaris_lha**: latitude from Polaris (LHA input)
35. **running_fix**: running fix (LOP1 advanced in time)
36. **sailings**: great-circle and rhumb-line sailings
37. **saturn**: almanac data for Saturn
38. **set_and_drift**: set and drift from the difference between DRP and EP
39. **sun**: almanac data for Sun
40. **time**: conversion of time data between formats
41. **transit**: fix from a meridian transit on a moving vessel
42. **two_body_fix**: two-body fix (using spherical trigonometry)
43. **uranus**: almanac data for Uranus
44. **venus**: almanac data for Venus
45. **waypoints**: rhumb-line sailing between great-circle waypoints
46. **what_star**: star identification based on altitude and azimuth

Literature

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- <http://eclipse.gsfc.nasa.gov/SEhelp/deltatpoly2004.html>
- <http://simbad.u-strasbg.fr/>
- <http://www.absoluteastronomy.com/stars/>



<http://www.navigation-spreadsheets.com>



Worksheet for _____

<http://www.navigation-spreadsheets.com>



Universal Time (UT)

Year	Month	Day	Hours	Minutes	Seconds

Geographical Position (GP), semidiameter (SD), horizontal parallax (HP), Eq. of Time

GHA	Declination	SD	HP	Eq. of Time

Sextant altitude corrections

Hs	IC	AH? (Y/N)	Ha	Ho

Notes: