

## 1. Union Find Disjoint Set & Kruskal

```
struct DisJointSet{
    vector<int> par, rnk, cnt; int numOfsets;

    DisJointSet(int n){
        par.assign(n, -1); rnk.assign(n, 0); cnt.assign(n, 1); //par==parent
        numOfsets=n; // if wanna count number of disjoint sets
    }

    int Find(int a){
        int i=a, j=a, tmp;
        while(par[i]!=-1){ i=par[i]; }
        while(par[j]!=-1){ tmp=par[j]; par[j]=i; j=tmp; } //path compression
        return i;
    }

    int Uni(int a, int b){
        int A=Find(a), B=Find(b);
        if(A!=B){
            if(rnk[A]<rnk[B]) swap(A, B); // union using rank
            if(rnk[A]==rnk[B]) rnk[A]++;
            par[B]=A;
            cnt[A]+=cnt[B]; // if we wanna count each set size
            numOfsets--; // if wanna count number of disjoint sets
        }
        return cnt[A]; // if we wanna count each set size
    }
};

struct edge{ int u, v, w;
    edge(int u=0, int v=0, int w=0):u(u), v(v), w(w){};
    bool operator<(const edge& b) const {
        if(w == b.w && v == b.w) return u < b.u;
        if(w == b.w) return v < b.v; return w < b.w;
    }
};

int n, m, bit; vector<edge> e; vi marked;

int Kruskal(){
    DisJointSet djst(n); marked.clear();
    sort(e.begin(), e.end()); int ans=0; int j=0;
    for(int i=0; i<e.size() && j<n-1; i++){
        if(djst.Find(e[i].u) != djst.Find(e[i].v)){
            djst.Uni(e[i].u, e[i].v); ans+=e[i].w; j++; marked.push_back(i);
        }
    }
}
```

```
return ans;
}
```

## 2. Segment Tree

```
class SegmentTree { // the segment tree is stored like a heap array
private: vi st, A; // recall that vi is: typedef vector<int> vi;
    int n;
    int left(int p) { return p << 1; } // same as binary heap operations
    int right(int p) { return (p << 1) + 1; }
    void build(int p, int L, int R) { // O(n)
        if (L == R) // as L == R, either one is fine
            st[p] = L; // store the index
        else { // recursively compute the values
            build(left(p), L, (L + R) / 2);
            build(right(p), (L + R) / 2 + 1, R);
            int p1 = st[left(p)], p2 = st[right(p)];
            st[p] = (A[p1] <= A[p2]) ? p1 : p2;
        }
    }
    int rmq(int p, int L, int R, int i, int j) { // O(log n)
        if (i > R || j < L) return -1; // current segment outside query
        range
        if (L >= i && R <= j) return st[p]; // inside query range
        // compute the min position in the left and right part
        of the interval
        int p1 = rmq(left(p), L, (L + R) / 2, i, j);
        int p2 = rmq(right(p), (L + R) / 2 + 1, R, i, j);
        if (p1 == -1) return p2; // if we try to access segment outside
        query
        if (p2 == -1) return p1; // same as above
        return (A[p1] <= A[p2]) ? p1 : p2; // as in build routine
    }
public:
    SegmentTree(const vi &_A) {
        A = _A; n = (int)A.size(); // copy content for local usage
        st.assign(4 * n, 0); // create large enough vector of zeroes
        build(1, 0, n - 1); // recursive build
    }
    int rmq(int i, int j) { return rmq(1, 0, n - 1, i, j); } // overloading
};

int main() {
    int arr[] = { 18, 17, 13, 19, 15, 11, 20 }; // the original array
    vi A(arr, arr + 7);
    SegmentTree st(A);
    printf("RMQ(1, 3) = %d\n", st.rmq(1, 3)); // answer = index 2
    printf("RMQ(4, 6) = %d\n", st.rmq(4, 6)); // answer = index 5
}
```

### 3. Counting inversions

```
vector<int> tree,a,b; int n;

int64 read(int idx){
    int64 sum=0;
    while(idx>0){
        sum+=tree[idx]; idx=(idx & -idx);
    }
    return sum;
}

void update(int idx, int val){
    int64 sum=0;
    while(idx<n){
        tree[idx]+=val; idx+=(idx & -idx);
    }
}

// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) { // ***Change Needed***
    int idx = 0, mask = TREE_SIZE; //(must be a power of 2)
    while(mask && idx < TREE_SIZE) {
        int t = idx + mask;
        if(x >= tree[t]) {idx = t; x -= tree[t]; }
        mask >>= 1;
    }
    return idx;
}

int main(){
    while(cin >> n){
        a.assign(n,0); b.assign(n,0); tree.assign(n,0);
        for(int i=0 ; i<n; i++){
            cin >> a[i]; b[i]=a[i];
        }
        sort(b.begin(),b.end());
        for(int i=0 ; i<n ; i++){
            int rank=(int)(lower_bound(b.begin(),b.end(),a[i])-b.begin());
            a[i]=rank+1;
        }
        int64 invs=0;//num of inversions
        for(int i=n-1 ; i>=0 ; i--){
            invs+=read(a[i]-1);
            update(a[i],1);
        }
        cout << invs << endl;
    }

    return 0;
}
```

### 4. FenwickTree

```
class FenwickTree {
private: vi ft; // recall that vi is: typedef vector<int> vi;
public: FenwickTree(int n) { ft.assign(n + 1, 0); } // init n + 1 zeroes

    int rsq(int b) { // returns RSQ(1, b)
        int sum = 0; for (; b; b -= LSOne(b)) sum += ft[b];
        return sum;
    } // note: LSOne(S) (S & (-S))
    int rsq(int a, int b) { // returns RSQ(a, b)
        return rsq(b) - (a == 1 ? 0 : rsq(a - 1));
    }
    // adjusts value of the k-th element by v (v can be +ve/inc or -ve/dec)
    void adjust(int k, int v) { // note: n = ft.size() - 1
        for (; k < (int)ft.size(); k += LSOne(k)) ft[k] += v;
    }
};

int main() {
    int f[] = { 2,4,5,5,6,6,6,7,7,8,9 }; // m = 11 scores
    FenwickTree ft(10); // declare a Fenwick Tree for range [1..10]
    // insert these scores manually one by one into an empty Fenwick Tree
    for (int i = 0; i < 11; i++) ft.adjust(f[i], 1); // this is O(k log n)

    printf("%d\n", ft.rsq(1, 1)); // 0 => ft[1] = 0
    printf("%d\n", ft.rsq(1, 2)); // 1 => ft[2] = 1
    printf("%d\n", ft.rsq(1, 6)); // 7 => ft[6] + ft[4] = 5 + 2 = 7
    printf("%d\n", ft.rsq(1, 10)); // 11 => ft[10] + ft[8] = 1 + 10 = 11
    printf("%d\n", ft.rsq(3, 6)); // 6 => rsq(1, 6) - rsq(1, 2) = 7 - 1
    ft.adjust(5, 2); // update demo
    printf("%d\n", ft.rsq(1, 10)); // now 13
} // return 0;
```

### 5. Programming Tips

Lower bound and upper bound for binary Search

- lower bound Returns an iterator pointing to the first element in the range[first, last) which does not compare less than val.
- upper bound Returns an iterator pointing to the first element in the range[first, last) which compares greater than val.

```
map<string, int> dict;
class cmp {
public:
    bool operator()(const string& a, const string& b) const {
        return dict[a] < dict[b];
    }
};
typedef set<string, cmp> sset;
```

## 6. Maximum Subrectangle Sum

```
for(int i=1 ; i<n ; i++)//preprocess
    for(int j=0 ; j<n ; j++)
        a[i][j]+=a[i-1][j];

int Max=0, ans=0;
for(int k=0 ; k<n ; k++){//calc
    for(int i=0 ; i<n-k ; i++){ Max=0;
        for(int j=0 ; j<n ; j++){
            if(Max<0) Max=a[i+k][j]-a[i][j];
            else Max+=a[i+k][j]-a[i][j];
            if(Max>ans) ans=Max;
        } } }

//sub array, finish and start point p=(val, startidx, finishidx)
p ans=p(-1,0,0); int sum=0,id=1;
for(int i=1 ; i<n ; i++){
    if(sum<0){sum=0; id=i;}
    sum+=a[i];
    p tmp=p(sum,id,i+1); ans=Max(ans,tmp);
}
```

## 7. Optimal Array Multiplication Sequence (Print Path)

```
int n,a[10+5],p[10+5][10+5],dp[10+5][10+5];

int solve(int L, int R){
    if(L==R){ return 0; }
    if(dp[L][R]!=-1) return dp[L][R];
    int Min=INF;
    for(int i=L ; i<R ; i++){
        int slv=solve(L,i)+solve(i+1,R)+a[(L-1)]*a[i]*a[R];
        if(Min>slv) Min=slv; p[L][R]=i;
    }
    return dp[L][R]=Min;
}

//prints like this => (A1 x (A2 x A3))
void print(int L, int R){
    if(L==R){ cout << "A" <<L; return; }
    cout << "("; print(L,p[L][R]);
    cout << " x ";
    print(p[L][R]+1,R); cout << ")";
}

int main(){ int t=1;
    while(cin >> n && n){
        for(int i=1 ; i<=n ; i++)cin >> a[i-1] >> a[i];
        memset(dp,-1,sizeof dp);
        solve(1,n);//cout << solve(1,n) << endl;
        printf("Case %d: ",t++); print(1,n); printf("\n");
    }
    return 0;
}
```

## 8. LIS

```
vector<int> v;
v.push_back(inf);
for (int i = 0; i<n; i++) {
    int x = dolls[i].w; // array element
    int id = lower_bound(v.begin(), v.end(), x + 1) - v.begin();

    if (id == v.size() - 1) v.push_back(inf); v[id] = x;
}
cout << v.size() - 1 << endl;
```

## 9. LCS

```
dp[MAX][MAX]={0};
for(int i=1 ; i<=n ; i++){
    for(int j=1 ; j<=n ; j++){
        if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
        else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
    }
}
cout << dp[n][n] << endl;
```

## 10.TSP

```
p a[15]; int n, dp[15][1<<15];

int solve(int pos, int bitset){
    int& dpp=dp[pos][bitset]; //dpp = dp pointer
    if(bitset==(1<<n)-1) return dist(a[pos],a[0]);
    if(dpp!=-1) return dpp;
    dpp=INF;
    for(int i=0 ; i<n ; i++){
        if(!(bitset&(1<<i))) dpp=min(dpp,solve(i,bitset|(1<<i))+dist(a[pos],a[i]));
    }
    return dpp;
}

int main(){
    int tc; cin >> tc;
    while(tc--){
        cin >> a[0].X >> a[0].Y; cin >> n; n++;
        for(int i=1 ; i<n ; i++) cin >> a[i].X >> a[i].Y;
        memset(dp, -1, sizeof dp);
        cout << solve(0,1) << endl;
    }
    return 0;
}
```

## 11. Articulation Points & Bridges

```
int n, lev, dfsRoot, rootChilds;
int dfsLow[MAX], dfsNum[MAX], parent[MAX];
vvi adj; set<pii> bridges; set<int> artPoints;

void dfs(int u) {
    dfsLow[u] = dfsNum[u] = lev++;
    for (int i = 0; i < adj[u].size(); i++) {
        int v = adj[u][i];
        if (dfsNum[v] == 0) {
            if (u == dfsRoot) rootChilds++;
            parent[v] = u; dfs(v);

            if (dfsLow[v] >= dfsNum[u] && u != dfsRoot) // u is articulation point
                artPoints.insert(u);

            if (dfsLow[v] > dfsNum[u]) {
                bridges.insert(pii(v, u));
                bridges.insert(pii(u, v));
            }

            dfsLow[u] = min(dfsLow[u], dfsLow[v]);
        }
        else if (parent[u] != v)
            dfsLow[u] = min(dfsLow[u], dfsNum[v]);
    }
}

int main() {
    while (cin >> n) {
        adj.assign(n, vi()); // initialization
        memset(dfsLow, 0, sizeof dfsLow);
        memset(dfsNum, 0, sizeof dfsNum);
        memset(parent, 0, sizeof parent);
        bridges.clear(); artPoints.clear();
        lev = 1; int tmp, u, m;
        for (int i = 0; i < n; i++) { // construct the graph
            scanf("%d %d", &u, &m); cin.ignore();
            for (int i = 0; i < m; i++) {
                cin >> tmp; adj[u].push_back(tmp);
            }
        }
        for (int i = 0; i < n; i++) {
            if (dfsNum[i] == 0) {
                dfsRoot = i; rootChilds = 0; dfs(i);
                if (rootChilds >= 2) artPoints.insert(dfsRoot);
            }
        }
        printf("%d critical links\n", bridges.size());
        set<pii>::iterator itr; // print answer
        for (itr = bridges.begin(); itr != bridges.end(); itr++)
            printf("%d - %d\n", itr->first, itr->second);
        cout << endl;
    }
    return 0;
}
```

## 12. Finding Strongly Connected Components

```
#define MAX 100000

using namespace std;

int dfsNum[MAX+10], dfsLow[MAX+10], vis[MAX+10], in[MAX+10], n, m, lev, ans;
vector<int> SCC, adj[MAX+10];

void dfs(int u) {
    dfsLow[u] = dfsNum[u] = lev++; vis[u] = 1; SCC.push_back(u);
    for (int i = 0; i < adj[u].size(); i++) {
        int v = adj[u][i];
        if (dfsNum[v] == 0) dfs(v);
        if (vis[v]) dfsLow[u] = min(dfsLow[u], dfsLow[v]), in[v]--;
    }
    if (dfsLow[u] == dfsNum[u]) {
        // this prints all vertices v blong to SCC with dfsLow[v] == dfsLow[u]
        bool flag = true;
        for (int i = 0, v; !SCC.empty(); i++) {
            v = SCC.back(); SCC.pop_back(); vis[v] = 0;
            printf("%d ", v);
            if (in[v]) flag = false;
            if (v == u) break;
        }
        printf("\n");
        if (flag) ans++;
    }
    // counts number of SCCs without indegree outside of other SCCs
}

int main() {
    int tc; scanf("%d", &tc); int x, y;
    while (tc--) {
        scanf("%d %d", &n, &m);
        memset(dfsNum, 0, sizeof dfsNum); // memset(adj, 0, sizeof adj);
        memset(dfsLow, 0, sizeof dfsLow); memset(vis, 0, sizeof vis);
        memset(in, 0, sizeof in); lev = 1; ans = 0;

        for (int i = 0, j = 0; i < m; i++) {
            scanf("%d %d", &x, &y); x--; y--;
            adj[x].push_back(y); in[y]++;
        }
        for (int i = 0; i < n; i++) {
            if (dfsNum[i] == 0) dfs(i);
        }
        cout << ans << endl;
    }
    return 0;
}
```

### 13.Graphic Sequence

// given a sequence of integers see if it's a sequence of degrees of graph or not.

```
int a[10010]; long long sum,Min;;

int main(){
    int n;
    while(cin >> n && n){
        for(int i=0 ; i<n ; i++) scanf("%d",&a[i]);
        sort(a,a+n, ::greater<int>() );
        bool possible=true; sum=0;
        for(int i=0 ; i<n ; i++){
            sum+=a[i]; Min=0;
            for(int j=i+1 ; j<n; j++) Min+=min(a[j],i+1);
            if(sum>i*(i+1)+Min){
                possible=false;
                break;
            }
        }
        if(!possible || sum%2) cout << "Not possible" << endl;
        else cout << "Possible" << endl;
    }
    return 0;}
```

### 14. BFS Topological Sort

```
//store indegree of vertice u in indegree[u]
fr(i,n) if(!indegree[i]) q.push(i);
while(!q.empty()){
    int v = q.front(); q.pop();
    cout << v + 1 << " ";
    int s = adjlist[v].size();
    fr(i,s){
        if(!(--indegree[ adjlist[v][i] ])) q.push(adjlist[v][i]);
    }
}
```

### 15.Floyd Warshal (Print Path)

```
#define MAX (100+10)
```

```
int adj[MAX][MAX],path[MAX][MAX]; int n;
```

```
void print(int i,int j){
    if(i!=j){
        printf(" %d",i );
        print(path[i][j],j);
    }
}
```

```
int main(){
    int tc; cin >> tc;
    while(tc--){
        cin >> n;
        for(int i=0 ; i<n ; i++){
            for(int j=0 ; j<n ; j++){
                adj[i][j]=1e9; if(i==j) adj[i][j]=0;
                path[i][j]=j;//initial parent
            }
        }
    }
```

```
for(int k=0 ; k<n ; k++){
    for(int i=0 ; i<n ; i++){
        for(int j=0 ; j<n ; j++){
            if(adj[i][j]>adj[i][k]+adj[k][j]){
                adj[i][j]=adj[i][k]+adj[k][j];
                path[i][j]=path[i][k];//set parent
            }
        }
    }
}
```

```
int s,d;
cin >> s >> d;
printf("%d euros\n",adj[s][d]);
```

```
//this prints the path even if source and distinaion are same
printf("%d",s); print(path[s][d],d); printf(" %d\n",d);
```

```

}
return 0;
}
```

## 16. Edmonds Karp's

```
//UVA 820 - Internet Bandwidth
#define INF (int)1e9
#define MAX 100+10

using namespace std;

int res[MAX][MAX],mf,f,s,t,n,m,par[MAX]; vector<int> dist,adj[MAX];

void agument(int v, int minEdge){
    if(v==s) f=minEdge;
    else if(par[v]!=-1){
        agument(par[v],min(minEdge,res[par[v]][v]));
        res[par[v]][v]-=f; res[v][par[v]]+=f;
    }
}

int main(){
    int tc=1;
    while(cin >> n && n){
        mf=0; memset(res,0,sizeof res); for(int i=0 ; i<n ; i++)
        adj[i].clear();
        cin >> s >> t >> m; s--; t--;
        int u,v,c;
        while(m--){
            cin >> u >> v >> c; u--; v--;
            res[u][v]+=c; res[v][u]+=c;
            adj[u].push_back(v); adj[v].push_back(u);
        }
        while(1){
            f=0; memset(par,-1,sizeof par); dist.assign(n,INF);
            dist[s]=0; queue<int> q; q.push(s);
            while(!q.empty()){
                int u=q.front(); q.pop();
                if(u==t) break;
                for(int i=0 ; i<adj[u].size(); i++){
                    int v=adj[u][i];
                    if(res[u][v]>0 && dist[v]==INF){
                        dist[v]=dist[u]+1; q.push(v); par[v]=u;
                    }
                }
            }
            agument(t,INF);
            if(f==0) break;
            mf+=f;
        }
        printf("Network %d\n", tc++);
        printf("The bandwidth is %d.\n\n", mf);
    }
    return 0;}
```

## 17. Dinic

```
// Adjacency list implementation of Dinic's blocking flow algorithm.
// This is very fast in practice, and only loses to push-relabel flow.
// Running time:  $O(|V|^2 |E|)$ 
// INPUT:
// - graph, constructed using AddEdge() - source - sink
// OUTPUT:
// - maximum flow value
// - To obtain the actual flow values, look at all edges with
//   capacity > 0 (zero capacity edges are residual edges).
using namespace std;
const int INF = 2000000000;
struct Edge {
    int from, to, cap, flow, index;
    Edge(int from, int to, int cap, int flow, int index) :
        from(from), to(to), cap(cap), flow(flow), index(index) {}
};
struct Dinic {
    int N; vector<vector<Edge>> G;
    vector<Edge*> dad; vector<int> Q;
    Dinic(int N) : N(N), G(N), dad(N), Q(N) {}
    void AddEdge(int from, int to, int cap) {
        G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
        if (from == to) G[from].back().index++;
        G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
    }
    long long BlockingFlow(int s, int t) {
        fill(dad.begin(), dad.end(), (Edge*)NULL);
        dad[s] = &G[s][0] - 1;
        int head = 0, tail = 0;
        Q[tail++] = s;
        while (head < tail) {
            int x = Q[head++];
            for (int i = 0; i < G[x].size(); i++) {
                Edge &e = G[x][i];
                if (!dad[e.to] && e.cap - e.flow > 0) {
                    dad[e.to] = &G[x][i];
                    Q[tail++] = e.to;
                }
            }
            if (!dad[t]) return 0;
            long long totflow = 0;
            for (int i = 0; i < G[t].size(); i++) {
                Edge *start = &G[G[t][i].to][G[t][i].index];
                int amt = INF;
                for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
                    if (!e) { amt = 0; break; }
                    amt = min(amt, e->cap - e->flow);
                }
                if (amt == 0) continue;
                for (Edge *e = start; amt && e != dad[s]; e = dad[e->from]) {
                    e->flow += amt;
                    G[e->to][e->index].flow -= amt;
                }
                totflow += amt;
            }
            return totflow;
        }
    }
    long long GetMaxFlow(int s, int t) {
        long long totflow = 0;
        while (long long flow = BlockingFlow(s, t))
            totflow += flow;
        return totflow;
    }
};
```

## 18. Min Cut

```
// Adjacency matrix implementation of Stoer-Wagner min cut algorithm.
// Running time:  $O(|V|^3)$ 
// INPUT:
// graph, constructed using AddEdge()
// OUTPUT:
// (min cut value, nodes in half of min cut)
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;

typedef vector<int> VI;
typedef vector<VI> VVI;

const int INF = 1000000000;

pair<int, VI> GetMinCut(VVI &weights) {
    int N = weights.size();
    VI used(N), cut, best_cut;
    int best_weight = -1;

    for (int phase = N - 1; phase >= 0; phase--) {
        VI w = weights[0];
        VI added = used;
        int prev, last = 0;
        for (int i = 0; i < phase; i++) {
            prev = last;
            last = -1;
            for (int j = 1; j < N; j++)
                if (!added[j] && (last == -1 || w[j] > w[last])) last = j;
            if (i == phase - 1) {
                for (int j = 0; j < N; j++) weights[prev][j] += weights[last][j];
                for (int j = 0; j < N; j++) weights[j][prev] = weights[j][last];
                used[last] = true;
                cut.push_back(last);
                if (best_weight == -1 || w[last] < best_weight) {
                    best_cut = cut;
                    best_weight = w[last];
                }
            }
            else {
                for (int j = 0; j < N; j++)
                    w[j] += weights[last][j];
                added[last] = true;
            }
        }
    }
    return make_pair(best_weight, best_cut);
}
```

## 19. Alternating Path Algorithm for Max Bipartite Matching

```
//UVA 11138 - Nuts and Bolts //  $O(V^2 + VE)$ 
#define vi vector<int>

using namespace std;

vector< vi > adj; vector<int> owner, vis; int n,b;

int altpath(int u){
    if(vis[u]) return 0; vis[u]=1;
    for(int i=0 ; i<adj[u].size() ; i++){
        int v=adj[u][i];
        if(owner[v]==-1 || altpath(owner[v])){
            owner[v]=u; return 1;
        }
    }
    return 0;
}

int main(){
    int tmp,tc,t=1; cin >> tc;
    while(tc--){
        cin >> n >> b; adj.assign(n+b,vi());
        for(int i=0 ; i<n ; i++){
            for(int j=0 ; j<b ; j++){
                cin >> tmp; if(tmp==1) adj[i].push_back(j+n);
            }
        }
        int ans=0; owner.assign(n+b,-1);
        for(int u=0 ; u<n ; u++){
            vis.assign(n,0); ans+=altpath(u);
        }
        printf("Case %d: a maximum of %d matched\n", t++, ans);
    }
    return 0;
}
```

## 20.Bitmask

```
bit&(1<<i) // bit i is 0 or 1
(bit>>j)&1// bit i is 0 or 1 // use this & multiplication to avoid TLE
bit|(1<<i) // set bit i to 1
bit^(1<<i) // toggle bit i
x & ( x - 1) // check if x is a power of 2
string stmp; bitset<12> tmp; //Debuging
tmp=bit; stmp=tmp.to_string();
```

## 21.MinCost Max Flow

```
// forward and reverse edges separately (so you can set cap[i][j] !=
// cap[j][i]). For a regular max flow, set all edge costs to 0.
// Running time,  $O(|V|^2)$  cost per augmentation
//     max flow:  $O(|V|^3)$  augmentations
//     min cost max flow:  $O(|V|^4 * \text{MAX\_EDGE\_COST})$  augmentations
// INPUT:
//     - graph, constructed using AddEdge() - source - sink
// OUTPUT:
//     - (maximum flow value, minimum cost value)
//     - To obtain the actual flow, look at positive values only.
```

```
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
```

```
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef long long L;
typedef vector<L> VL;
typedef vector<VL> VVL;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
```

```
const L INF = numeric_limits<L>::max() / 4;
```

```
struct MinCostMaxFlow {
    int N; VPII dad;
    VVL cap, flow, cost;
    VI found; VL dist, pi, width;
```

```
MinCostMaxFlow(int N) :
    N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N, VL(N)),
    found(N), dist(N), pi(N), width(N), dad(N) {}
```

```
void AddEdge(int from, int to, L cap, L cost) {
    this->cap[from][to] = cap;
    this->cost[from][to] = cost;
}
```

```
void Relax(int s, int k, L cap, L cost, int dir) {
    L val = dist[s] + pi[s] - pi[k] + cost;
    if (cap && val < dist[k]) {
        dist[k] = val;
```

```
        dad[k] = make_pair(s, dir);
        width[k] = min(cap, width[s]);
    }
}
```

```
L Dijkstra(int s, int t) {
    fill(found.begin(), found.end(), false);
    fill(dist.begin(), dist.end(), INF);
    fill(width.begin(), width.end(), 0);
    dist[s] = 0;
    width[s] = INF;

    while (s != -1) {
        int best = -1;
        found[s] = true;
        for (int k = 0; k < N; k++) {
            if (found[k]) continue;
            Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
            Relax(s, k, flow[k][s], -cost[k][s], -1);
            if (best == -1 || dist[k] < dist[best]) best = k;
        }
        s = best;
    }
}
```

```
for (int k = 0; k < N; k++)
    pi[k] = min(pi[k] + dist[k], INF);
return width[t];
}
```

```
pair<L, L> GetMaxFlow(int s, int t) {
    L totflow = 0, totcost = 0;
    while (L amt = Dijkstra(s, t)) {
        totflow += amt;
        for (int x = t; x != s; x = dad[x].first) {
            if (dad[x].second == 1) {
                flow[dad[x].first][x] += amt;
                totcost += amt * cost[dad[x].first][x];
            }
            else {
                flow[x][dad[x].first] -= amt;
                totcost -= amt * cost[x][dad[x].first];
            }
        }
    }
    return make_pair(totflow, totcost);
};
```



## 22.Dijkstra

```
struct ToNode {
    int v, w;
    ToNode(int v, int w)
        :v(v), w(w) {}
};

struct QEntry {
    int node, cost;
    QEntry(int node, int cost):node(node), cost(cost) {}
    bool operator<(const QEntry& op) const {
        return cost < op.cost;
    }
};

int n, m; vvt<int> adj;

int dijkstra(int s, int t, vi& dist) {
    dist.assign(n, INF);
    priority_queue<QEntry> q;
    q.push(QEntry(s, 0)); dist[s] = 0;

    while (!q.empty()) {
        QEntry u = q.top(); q.pop();
        if (u.node == t) return u.cost;
        if (u.cost > dist[u.node]) continue;
        for (int i = 0; i < adj[u.node].size(); i++) {
            QEntry v(adj[u.node][i].v, u.cost + adj[u.node][i].w);
            if (dist[v.node] > v.cost) {
                dist[v.node] = v.cost; q.push(v);
            }
        }
    }
    return INF;
}
```

## 23.Catalan

$Catalan(n+1) = (catalan(n) * (2n+2) * (2n+1)) / ((n+1) * (n+2))$   
/\*n!\*/Catalan(n)=2n!/(n!\*n!\*(n+1)), Catalan(1)=1;

```
000 001 002 003 004 005 006
001 001 002 005 014 042 132
```

## 24. Strongly Connected Component - Kosaraju

```
// Doesn't run properly
vvi adjOrg, adjRev; vi vis, ord, col;
void dfsOrg(int u) {
    if (vis[u]) return; vis[u] = true;
    for (int i = 0; i < adjOrg[u].size(); i++) {
        dfsOrg(adjOrg[u][i]);
    }
    ord.push_back(u);
}

int dfsRev(int u, int color) {
    if (col[u]) return 0; col[u] = color;
    int ret = 1;
    for (int i = 0; i < adjRev[u].size(); i++) {
        ret += dfsRev(adjRev[u][i], color);
    }
    return ret;
}

int main() {
    while (cin >> n && n) {
        int u, v; string line;
        adjOrg.assign(n, vi()); adjRev.assign(n, vi());
        for (int i = 0; i < n; i++) {
            stringstream sstr(line); sstr >> u;
            while (sstr >> v) {
                adjOrg[u].push_back(v); adjRev[v].push_back(u);
            }
        }
        ord.clear();
        vis.assign(n, 0);
        for (int u = 0; u < n; u++) {
            if (!vis[u]) dfsOrg(u);
        }
        int color = 1;
        col.assign(n, 0);
        while (!ord.empty()) {
            int u = ord.back();
            if (!col[u]) {
                int size = dfsRev(u, color); // SCC Size
                if (size > 1) {
                    for (int v = 0; v < n; v++) {
                        if (col[v] == color); //inSame SCC;
                    }
                }
                color++;
            }
            ord.pop_back();
        }
    }
}
```

## 25. Primes

```
const int64 MAX = 1e6 + 100;

bitset<MAX> isp; // isprime
vector<int64> primes, pfs, pws; // pfs = prime factors, pws = prime powers

void genprime() {
    isp.set(); isp[0] = isp[1] = 0;
    for (int64 i = 2; i < MAX; i++) {
        if (isp[i]) {
            primes.push_back(i);
            for (int64 j = i*i; j < MAX; j += i) isp[j] = 0;
        }
    }
}

bool isprime(int n) {
    if (n < MAX) return isp[n];
    for (int i = 0; i < primes.size() && primes[i] * primes[i] <= n; i++) {
        if (n % primes[i] == 0) return 0;
    }
    return 1;
}

// generation prime factors of a number
int main() {
    int64 n; genprime();
    while (cin >> n) {
        int64 tmp = n, cnt = 0, cop = n, div = 1;
        // cop = euler Phi funcion
        // cop = coprimes = all m (m < n && gcd(m,n)==1)
        // div = divisors = all m (m < n && gcd(m,n)==m)
        for (int i = 0, pf = 2; pf*pf <= n; i++, pf = primes[i]) {
            int pow = 0;
            while (tmp % pf == 0) {
                tmp /= pf; pow++;
            }
            if (pow) {
                pfs.push_back(pf), pws.push_back(pow);
                cop -= cop / pf; div *= (pow + 1);
            }
        }
        if (tmp > 1) cop -= cop / tmp, div *= (1 + 1); // Keep Attention to this
        cout << cop + div + 1 << endl;
    }
}
```

## 26. Extended Euclid

```
ax + by = c, d = GCD(a, b), d | c == 0:
int x, y, d;
void extendedEuclid(int a, int b) {
    if (b == 0) { x = 1; y = 0; d = a; return; }
    extendedEuclid(b, a % b);
    int x1 = y; int y1 = x - (a / b) * y;
    x = x1; y = y1;
}
```

## 27. Geometry 1

```
const double eps = 1e-8;
const double PI = acos(-1.0);

struct Point
{
    double x, y;
    Point(double x = 0, double y = 0) : x(x), y(y) {}
    bool operator < (const Point& a) const
    {
        if (a.x != x) return x < a.x;
        return y < a.y;
    }
};

typedef Point Vector;

struct Line
{
    Point P;
    Vector v;
    double ang;
    Line() {}
    Line(Point P, Vector v) : P(P), v(v) { ang = atan2(v.y, v.x); }
    bool operator < (const Line& L) const
    {
        return ang < L.ang;
    }
};

Vector operator + (Vector A, Vector B) { return Vector(A.x + B.x, A.y + B.y); }

Vector operator - (Point A, Point B) { return Vector(A.x - B.x, A.y - B.y); }

Vector operator * (Vector A, double p) { return Vector(A.x * p, A.y * p); }

Vector operator / (Vector A, double p) { return Vector(A.x / p, A.y / p); }

int dcmp(double x)
{
    if (fabs(x) < eps) return 0; else return x < 0 ? -1 : 1;
}

bool operator == (const Point& a, const Point &b)
```

```

{
    return dcmp(a.x - b.x) == 0 && dcmp(a.y - b.y) == 0;
}

double Dot(Vector A, Vector B) { return A.x*B.x + A.y*B.y; }

double Length(Vector A) { return sqrt(Dot(A, A)); }

double Angle(Vector A, Vector B) { return acos(Dot(A, B) / Length(A) / Length(B)); }

double Cross(Vector A, Vector B) { return A.x*B.y - A.y*B.x; }
double Area2(Point A, Point B, Point C) { return fabs(Cross(B - A, C - A)) / 2; }

Vector Rotate(Vector A, double rad)
{
    return Vector(A.x*cos(rad) - A.y*sin(rad), A.x*sin(rad) + A.y*cos(rad));
}

Point GetLineIntersection(Point P, Vector v, Point Q, Vector w)
{
    Vector u = P - Q;
    double t = Cross(w, u) / Cross(v, w);
    return P + v*t;
}

bool SegmentProperIntersection(Point a1, Point a2, Point b1, Point b2)
{
    double c1 = Cross(a2 - a1, b1 - a1), c2 = Cross(a2 - a1, b2 - a1);
    double c3 = Cross(b2 - b1, a1 - b1), c4 = Cross(b2 - b1, a2 - b1);
    return dcmp(c1) * dcmp(c2) < 0 && dcmp(c3) * dcmp(c4) < 0;
}

bool OnSegment(Point p, Point a1, Point a2)
{
    return dcmp(Cross(a1 - p, a2 - p)) == 0 && dcmp(Dot(a1 - p, a2 - p)) < 0;
}

double PolygonArea(Point* p, int n)
{
    double area = 0;
    for (int i = 1; i < n - 1; i++)
        area += Cross(p[i] - p[0], p[i + 1] - p[0]);
    return area / 2;
}

double PointDistanceToLine(Point P, Point A, Point B)
{
    Vector v1 = B - A, v2 = P - A;
    return fabs(Cross(v1, v2)) / Length(v1);
}

double PointDistanceToSegment(Point P, Point A, Point B)
{
    if (A == B) return Length(P - A);
    Vector v1 = B - A, v2 = P - A, v3 = P - B;
    if (dcmp(Dot(v1, v2) < 0)) return Length(v2);
    else if (dcmp(Dot(v1, v3) > 0)) return Length(v3);
    else return fabs(Cross(v1, v2)) / Length(v1);
}

int isPointInPolygon(Point p, Point *poly, int n)
{
    int wn = 0;
    for (int i = 0; i < n; i++)
    {
        const Point& p1 = poly[i], p2 = poly[(i + 1) % n];
        if (p == p1 || p == p2 || OnSegment(p, p1, p2)) return -1;
        int k = dcmp(Cross(p2 - p1, p - p1));
        int d1 = dcmp(p1.y - p.y);
        int d2 = dcmp(p2.y - p.y);
        if (k > 0 && d1 <= 0 && d2 > 0) wn++;
        if (k < 0 && d2 <= 0 && d1 > 0) wn--;
    }
    if (wn != 0) return 1;
    return 0;
}

Vector Normal(Vector A)
{
    double L = Length(A);
    return Vector(-A.y / L, A.x / L);
}

double Dist2(Point p1, Point p2)
{
    return (p1.x - p2.x)*(p1.x - p2.x) + (p1.y - p2.y)*(p1.y - p2.y);
}

double RotatingCalipers(Point *P, int n)
{
    if (n == 1) return 0;
    if (n == 2) return Dist2(P[0], P[1]);
    P[n] = P[0];
    double ans = 0;
    for (int u = 0, v = 1; u < n; u++)
    {
        for (;;)
        {
            double diff = Cross(P[u + 1] - P[u], P[v + 1] - P[v]);
            if (diff <= 0)
            {
                ans = max(ans, Dist2(P[u], P[v]));
                if (diff == 0) ans = max(ans, Dist2(P[u], P[v + 1]));
                break;
            }
            v = (v + 1) % n;
        }
    }
    return ans;
}

bool OnLeft(Line L, Point p)
{

```

```

    return Cross(L.v, p - L.P) > 0;
}

Point GetLineIntersection2(const Line &a, const Line &b)
{
    Vector u = a.P - b.P;
    double t = Cross(b.v, u) / Cross(a.v, b.v);
    return a.P + a.v*t;
}

int HalfPlaneIntersection(Line* L, int n, Point* poly)
{
    sort(L, L + n);
    int first, last;
    Point *p = new Point[n];
    Line* q = new Line[n];
    q[first = last = 0] = L[0];
    for (int i = 1; i < n; i++)
    {
        while (first < last && !OnLeft(L[i], p[last - 1])) last--;
        while (first < last && !OnLeft(L[i], p[first])) first++;
        q[++last] = L[i];
        if (fabs(Cross(q[last].v, q[last - 1].v)) < eps)
        {
            last--;
            if (OnLeft(q[last], L[i].P)) q[last] = L[i];
        }
        if (first < last) p[last - 1] = GetLineIntersection2(q[last - 1], q[last]);
    }
    while (first < last && !OnLeft(q[first], p[last - 1])) last--;
    if (last - first <= 1) return 0;
    p[last] = GetLineIntersection2(q[last], q[first]);

    int m = 0;
    for (int i = first; i <= last; i++) poly[m++] = p[i];
    return m;
}

vector<Point> CutPolygon(const vector<Point> &poly, Point A, Point B)
{
    vector<Point> newpoly;
    int n = poly.size();
    for (int i = 0; i < n; i++)
    {
        Point C = poly[i], D = poly[(i + 1) % n];
        if (dcmp(Cross(B - A, C - A)) >= 0) newpoly.push_back(C);
        if (dcmp(Cross(B - A, C - D)) != 0)
        {
            Point ip = GetLineIntersection(A, B - A, C, D - C);
            if (OnSegment(ip, C, D)) newpoly.push_back(ip);
        }
    }
    return newpoly;
}

```

## 28. Geometry 2

```

#include <iostream>
#include <vector>
#include <cmath>
#include <cassert>

using namespace std;

double INF = 1e100;
double EPS = 1e-12;

#define M_PI acos(-1)

struct PT {
    double x, y;
    PT() {}
    PT(double x, double y) : x(x), y(y) {}
    PT(const PT &p) : x(p.x), y(p.y) {}
    PT operator + (const PT &p) const { return PT(x + p.x, y + p.y); }
    PT operator - (const PT &p) const { return PT(x - p.x, y - p.y); }
    bool operator < (const PT &p) const { return (x != p.x ? x < p.x : y < p.y); }
    PT operator * (double c) const { return PT(x*c, y*c); }
    PT operator / (double c) const { return PT(x / c, y / c); }
};

double dot(PT p, PT q) { return p.x*q.x + p.y*q.y; }
double dist2(PT p, PT q) { return dot(p - q, p - q); }
double cross(PT p, PT q) { return p.x*q.y - p.y*q.x; }

// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y, p.x); }
PT RotateCW90(PT p) { return PT(p.y, -p.x); }
PT RotateCCW(PT p, double t) {
    return PT(p.x*cos(t) - p.y*sin(t), p.x*sin(t) + p.y*cos(t));
}

// project point c onto line through a and b
// assuming a != b
PT ProjectPointLine(PT a, PT b, PT c) {
    return a + (b - a)*dot(c - a, b - a) / dot(b - a, b - a);
}

// project point c onto line segment through a and b
PT ProjectPointSegment(PT a, PT b, PT c) {
    double r = dot(b - a, b - a);
    if (fabs(r) < EPS) return a;
    r = dot(c - a, b - a) / r;
    if (r < 0) return a;
    if (r > 1) return b;
    return a + (b - a)*r;
}

// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
    return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
}

```

```

// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane(double x, double y, double z,
    double a, double b, double c, double d)
{
    return fabs(a*x + b*y + c*z - d) / sqrt(a*a + b*b + c*c);
}

// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
    return fabs(cross(b - a, c - d)) < EPS;
}

bool LinesCollinear(PT a, PT b, PT c, PT d) {
    return LinesParallel(a, b, c, d)
        && fabs(cross(a - b, a - c)) < EPS
        && fabs(cross(c - d, c - a)) < EPS;
}

// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
    if (LinesCollinear(a, b, c, d)) {
        if (dist2(a, c) < EPS || dist2(a, d) < EPS ||
            dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
        if (dot(c - a, c - b) > 0 && dot(d - a, d - b) > 0 && dot(c - b, d - b) > 0)
            return false;
        return true;
    }
    if (cross(d - a, b - a) * cross(c - a, b - a) > 0) return false;
    if (cross(a - c, d - c) * cross(b - c, d - c) > 0) return false;
    return true;
}

// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
    b = b - a; d = c - d; c = c - a;
    assert(dot(b, b) > EPS && dot(d, d) > EPS);
    return a + b*cross(c, d) / cross(b, d);
}

// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
    b = (a + b) / 2;
    c = (a + c) / 2;
    return ComputeLineIntersection(b, b + RotateCW90(a - b), c, c + RotateCW90(a -
c));
}

// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.

```

```

// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
    bool c = 0;
    for (int i = 0; i < p.size(); i++) {
        int j = (i + 1) % p.size();
        if ((p[i].y <= q.y && q.y < p[j].y ||
            p[j].y <= q.y && q.y < p[i].y) &&
            q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
            c = !c;
    }
    return c;
}

// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
    for (int i = 0; i < p.size(); i++)
        if (dist2(ProjectPointSegment(p[i], p[(i + 1) % p.size()], q), q) < EPS)
            return true;
    return false;
}

// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
    vector<PT> ret;
    b = b - a;
    a = a - c;
    double A = dot(b, b);
    double B = dot(a, b);
    double C = dot(a, a) - r*r;
    double D = B*B - A*C;
    if (D < -EPS) return ret;
    ret.push_back(c + a + b*(-B + sqrt(D + EPS)) / A);
    if (D > EPS)
        ret.push_back(c + a + b*(-B - sqrt(D)) / A);
    return ret;
}

// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
    vector<PT> ret;
    double d = sqrt(dist2(a, b));
    if (d > r + R || d + min(r, R) < max(r, R)) return ret;
    double x = (d*d - R*R + r*r) / (2 * d);
    double y = sqrt(r*r - x*x);
    PT v = (b - a) / d;
    ret.push_back(a + v*x + RotateCCW90(v)*y);
    if (y > 0)
        ret.push_back(a + v*x - RotateCCW90(v)*y);
    return ret;
}

double ComputeSignedArea(const vector<PT> &p) {

```

```

double area = 0;
for (int i = 0; i < p.size(); i++) {
    int j = (i + 1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
}
return area / 2.0;
}

double ComputeArea(const vector<PT> &p) {
    return fabs(ComputeSignedArea(p));
}

PT ComputeCentroid(const vector<PT> &p) {
    PT c(0, 0);
    double scale = 6.0 * ComputeSignedArea(p);
    for (int i = 0; i < p.size(); i++) {
        int j = (i + 1) % p.size();
        c = c + (p[i] + p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
    }
    return c / scale;
}

// tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p) {
    for (int i = 0; i < p.size(); i++) {
        for (int k = i + 1; k < p.size(); k++) {
            int j = (i + 1) % p.size();
            int l = (k + 1) % p.size();
            if (i == 1 || j == k) continue;
            if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
                return false;
        }
    }
    return true;
}

```

## 29. Great Circle Distance

```

struct PT {
    double lat, lon; PT() {}
    PT(double lat, double lon) : lat(lat), lon(lon) {}
    PT operator * (double c) const { return PT(lat*c, lon*c); }
}pts[1000 + 10];

const double eps = 1e-9;
const double PI = 3.141592653589793;
const double R = 6378.00; // radius of earth

double GCDist(PT p1, PT p2) {
    p1 = p1*(PI / 180.); p2 = p2*(PI / 180.);
    double dlon = p2.lon - p1.lon;
    double dlat = p2.lat - p1.lat;
    double a = pow((sin(dlat / 2)), 2)
        + cos(p1.lat) * cos(p2.lat) * pow(sin(dlon / 2), 2);
    double c = 2 * atan2(sqrt(a), sqrt(1 - a));
    double d = R * c;
    return d + eps;
}

```

## 30. Convex Hull

```

#include <algorithm>
#include <vector>
using namespace std;
typedef int coord_t; // coordinate type
typedef long long coord2_t; // must be big enough to hold 2*max(|coordinate|)^2
struct Point {
    coord_t x, y;

    bool operator <(const Point &p) const {
        return x < p.x || (x == p.x && y < p.y);
    }
};

coord2_t cross(const Point &O, const Point &A, const Point &B)
{
    return (A.x - O.x) * (B.y - O.y) - (A.y - O.y) * (B.x - O.x);
}

// Returns a list of points on the convex hull in counter-clockwise order.
// Note: the last point in the returned list is the same as the first one.
vector<Point> convex_hull(vector<Point> P)
{
    int n = P.size(), k = 0;
    vector<Point> H(2 * n);
    // Sort points lexicographically
    sort(P.begin(), P.end());
    // Build lower hull
    for (int i = 0; i < n; i++) {
        while (k >= 2 && cross(H[k - 2], H[k - 1], P[i]) <= 0) k--;
        H[k++] = P[i];
    }
    // Build upper hull
    for (int i = n - 2, t = k + 1; i >= 0; i--) {
        while (k >= t && cross(H[k - 2], H[k - 1], P[i]) <= 0) k--;
        H[k++] = P[i];
    }
    H.resize(k);
    return H;
}

int main()
{
    vector<Point> h, p(1000000); //,p(6);
    srand(time(nullptr));
    for (int i = 0; i < 100000; ++i) {
        p[i] = Point(rand(), rand());
        if (!(i % 1000)) srand(time(nullptr));
    }
    clock_t start = clock();
    h = convex_hull(p);
    for (int i = 0; i < h.size(); ++i) {
        cout << "(" << h[i].x << "," << h[i].y << ")" << endl;
    }
}

```

## 31. Number Theory

```
#include <iostream>
#include <vector>
#include <algorithm>

using namespace std;

typedef vector<int> VI;
typedef pair<int, int> PII;

// return a % b (positive value)
int mod(int a, int b) {
    return ((a%b) + b) % b;
}

// computes gcd(a,b)
int gcd(int a, int b) {
    int tmp;
    while (b) { a %= b; tmp = a; a = b; b = tmp; }
    return a;
}

// computes lcm(a,b)
int lcm(int a, int b) {
    return a / gcd(a, b)*b;
}

// returns d = gcd(a,b); finds x,y such that d = ax + by
int extended_euclid(int a, int b, int &x, int &y) {
    int xx = y = 0;
    int yy = x = 1;
    while (b) {
        int q = a / b;
        int t = b; b = a%b; a = t;
        t = xx; xx = x - q*xx; x = t;
        t = yy; yy = y - q*yy; y = t;
    }
    return a;
}

// finds all solutions to ax = b (mod n)
VI modular_linear_equation_solver(int a, int b, int n) {
    int x, y;
    VI solutions;
    int d = extended_euclid(a, n, x, y);
    if (!(b%d)) {
        x = mod(x*(b / d), n);
        for (int i = 0; i < d; i++)
            solutions.push_back(mod(x + i*(n / d), n));
    }
    return solutions;
}

// computes b such that ab = 1 (mod n), returns -1 on failure
int mod_inverse(int a, int n) {
    int x, y;
```

```
int d = extended_euclid(a, n, x, y);
if (d > 1) return -1;
return mod(x, n);
}

// Chinese remainder theorem (special case): find z such that
// z % x = a, z % y = b. Here, z is unique modulo M = lcm(x,y).
// Return (z,M). On failure, M = -1.
PII chinese_remainder_theorem(int x, int a, int y, int b) {
    int s, t;
    int d = extended_euclid(x, y, s, t);
    if (a%d != b%d) return make_pair(0, -1);
    return make_pair(mod(s*b*x + t*a*y, x*y) / d, x*y / d);
}

// Chinese remainder theorem: find z such that
// z % x[i] = a[i] for all i. Note that the solution is
// unique modulo M = lcm_i (x[i]). Return (z,M). On
// failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese_remainder_theorem(const VI &x, const VI &a) {
    PII ret = make_pair(a[0], x[0]);
    for (int i = 1; i < x.size(); i++) {
        ret = chinese_remainder_theorem(ret.second, ret.first, x[i], a[i]);
        if (ret.second == -1) break;
    }
    return ret;
}

// computes x and y such that ax + by = c; on failure, x = y = -1
void linear_diophantine(int a, int b, int c, int &x, int &y) {
    int d = gcd(a, b);
    if (c%d) {
        x = y = -1;
    }
    else {
        x = c / d * mod_inverse(a / d, b / d);
        y = (c - a*x) / b;
    }
}

long conquer_fibonacci_lgN(long n) {
    long i, h, j, k, t;
    i = h = 1;
    j = k = 0;
    while (n > 0) {
        if (n % 2 == 1) {
            t = j * h;
            j = i * h + j * k + t;
            i = i * k + t;
        }
        t = h * h;
        h = 2 * k * h + t;
        k = k * k + t;
        n = (long)n / 2;
    }
    return j;}
```

## 32. Gauss - Jordan elimination

```
// Uses:
// (1) solving systems of linear equations (AX=B)
// (2) inverting matrices (AX=I)
// (3) computing determinants of square matrices
// Running time: O(n^3)
// INPUT:  a[][] = an nxn matrix
//          b[][] = an nxm matrix
// OUTPUT: X      = an nxm matrix (stored in b[][])
//          A^{-1} = an nxn matrix (stored in a[][])
//          returns determinant of a[][]

using namespace std;
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan(VVT &a, VVT &b) {
    const int n = a.size();
    const int m = b[0].size();
    VI irow(n), icol(n), ipiv(n);
    T det = 1;
    for (int i = 0; i < n; i++) {
        int pj = -1, pk = -1;
        for (int j = 0; j < n; j++) if (!ipiv[j])
            for (int k = 0; k < n; k++) if (!ipiv[k])
                if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
        if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl; exit(0); }
        ipiv[pj]++;
        swap(a[pj], a[pk]);
        swap(b[pj], b[pk]);
        if (pj != pk) det *= -1;
        irow[i] = pj;
        icol[i] = pk;
        T c = 1.0 / a[pk][pk];
        det *= a[pk][pk];
        a[pk][pk] = 1.0;
        for (int p = 0; p < n; p++) a[pk][p] *= c;
        for (int p = 0; p < m; p++) b[pk][p] *= c;
        for (int p = 0; p < n; p++) if (p != pk) {
            c = a[p][pk]; a[p][pk] = 0;
            for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
            for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
        }
    }
    for (int p = n - 1; p >= 0; p--) if (irow[p] != icol[p]) {
        for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
    }
    return det;
}

int main() {
    const int n = 4;
    const int m = 2;
    double A[n][n] = { { 1,2,3,4 }, { 1,0,1,0 }, { 5,3,2,4 }, { 6,1,4,6 } };
    double B[n][m] = { { 1,2 }, { 4,3 }, { 5,6 }, { 8,7 } };
    VVT a(n), b(n);
```

```
    for (int i = 0; i < n; i++) {
        a[i] = VT(A[i], A[i] + n);
        b[i] = VT(B[i], B[i] + m);
    }
    double det = GaussJordan(a, b);
    // expected: 60
    cout << "Determinant: " << det << endl;
    // expected: -0.233333 0.166667 0.133333 0.0666667
    //              0.166667 0.166667 0.333333 -0.333333
    //              0.233333 0.833333 -0.133333 -0.0666667
    //              0.05 -0.75 -0.1 0.2
    cout << "Inverse: " << endl;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
            cout << a[i][j] << ' ';
        cout << endl;
    }
    // expected: 1.63333 1.3
    //              -0.166667 0.5
    //              2.36667 1.7
    //              -1.85 -1.35
    cout << "Solution: " << endl;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < m; j++)
            cout << b[i][j] << ' ';
        cout << endl;
    }
}
```

## 33. Big Integer Square

```
import java.math.BigInteger;
import java.util.Scanner;
//import java.util.
public class Main {
    // https://en.wikipedia.org/wiki/Integer_square_root
    public static BigInteger sqrt(BigInteger n) {
        BigInteger cur = null; // X(k)
        BigInteger nxt = n; // X(k+1)
        while (true) {
            cur = nxt;
            nxt = cur.add(n.divide(cur)).divide(BigInteger.valueOf(2));
            if (nxt.equals(cur)) break;
        }
        if (cur.multiply(cur).equals(n)) return cur;
        else return null;
    }

    public static void main(String[] args) {
        Scanner sc = new Scanner(System.in);
        int tc = Integer.parseInt(sc.nextLine());
        while (tc-- > 0) {
            sc.nextLine();
            BigInteger y = new BigInteger(sc.nextLine());
            if (y.equals(BigInteger.ZERO)) System.out.println(0);
            else System.out.println(sqrt(y));
            if (tc > 0) System.out.println();
        }
    }
}
```



## 34.Convex Hull Diameter

```
typedef pair<double, double> point;

bool cw(const point &a, const point &b, const point &c) {
    return (b.first - a.first) * (c.second - a.second) - (b.second - a.second) * (c.first - a.first) < 0;
}

vector<point> convexHull(vector<point> p) {
    int n = p.size();
    if (n <= 1)
        return p;
    int k = 0;
    sort(p.begin(), p.end());
    vector<point> q(n * 2);
    for (int i = 0; i < n; q[k++] = p[i++])
        for (; k >= 2 && !cw(q[k - 2], q[k - 1], p[i]); --k)
            ;
    for (int i = n - 2, t = k; i >= 0; q[k++] = p[i--])
        for (; k > t && !cw(q[k - 2], q[k - 1], p[i]); --k)
            ;
    q.resize(k - 1 - (q[0] == q[1]));
    return q;
}

double area(const point &a, const point &b, const point &c) {
    return abs((b.first - a.first) * (c.second - a.second) - (b.second - a.second) * (c.first - a.first));
}

double dist(const point &a, const point &b) {
    return hypot(a.first - b.first, a.second - b.second);
}

double diameter(const vector<point> &p) {
    vector<point> h = convexHull(p);
    int m = h.size();
    if (m == 1)
        return 0;
    if (m == 2)
        return dist(h[0], h[1]);
    int k = 1;
    while (area(h[m - 1], h[0], h[(k + 1) % m]) > area(h[m - 1], h[0], h[k]))
        ++k;
    double res = 0;
    for (int i = 0, j = k; i <= k && j < m; i++) {
        res = max(res, dist(h[i], h[j]));
        while (j < m && area(h[i], h[(i + 1) % m], h[(j + 1) % m]) > area(h[i], h[(i + 1) % m], h[j])) {
            res = max(res, dist(h[i], h[(j + 1) % m]));
            ++j;
        }
    }
    return res;
}

int main() {
    vector<point> points(4);
    points[0] = point(0, 0);
    points[1] = point(3, 0);
    points[2] = point(0, 3);
    points[3] = point(1, 1);
    double d = diameter(points);
    cout << d << endl;
}
```

## 35.2D Fenwick

```
public class FenwickTree2D {

    public static void add(int[][] t, int r, int c, int value) {
        for (int i = r; i < t.length; i |= i + 1)
            for (int j = c; j < t[0].length; j |= j + 1)
                t[i][j] += value;
    }

    // sum[(0, 0), (r, c)]
    public static int sum(int[][] t, int r, int c) {
        int res = 0;
        for (int i = r; i >= 0; i = (i & (i + 1)) - 1)
            for (int j = c; j >= 0; j = (j & (j + 1)) - 1)
                res += t[i][j];
        return res;
    }

    // sum[(r1, c1), (r2, c2)]
    public static int sum(int[][] t, int r1, int c1, int r2, int c2) {
        return sum(t, r2, c2) - sum(t, r1 - 1, c2) - sum(t, r2, c1 - 1) + sum(t, r1 - 1, c1 - 1);
    }

    public static int get(int[][] t, int r, int c) {
        return sum(t, r, c, r, c);
    }

    public static void set(int[][] t, int r, int c, int value) {
        add(t, r, c, -get(t, r, c) + value);
    }

    // Usage example
    public static void main(String[] args) {
        int[][] t = new int[10][20];
        add(t, 0, 0, 1);
        add(t, 9, 19, -2);
        System.out.println(-1 == sum(t, 0, 0, 9, 19));
    }
}
```

## 36.Data Structure Ideas

- Hash Table + Lookup
- Sparse Table
- SQRT Decomposition
- Bucketing
- Integer Arrays as matrices
- Recursive Tree Building
- Shortest Cycles
- Problem DAG

## 37.Extended Fenwick

```
public class FenwickTreeExtended {

    // T[i] += value
    public static void add(int[] t, int i, int value) {
        for (; i < t.length; i |= i + 1)
            t[i] += value;
    }

    // sum[0..i]
    public static int sum(int[] t, int i) {
        int res = 0;
        for (; i >= 0; i = (i & (i + 1)) - 1)
            res += t[i];
        return res;
    }

    public static int[] createTreeFromArray(int[] a) {
        int[] res = new int[a.length];
        for (int i = 0; i < a.length; i++) {
            res[i] += a[i];
            int j = i | (i + 1);
            if (j < a.length)
                res[j] += res[i];
        }
        return res;
    }

    // sum[a..b]
    public static int sum(int[] t, int a, int b) {
        return sum(t, b) - sum(t, a - 1);
    }

    public static int get(int[] t, int i) {
        int res = t[i];
        if (i > 0) {
            int lca = (i & (i + 1)) - 1;
            for (--i; i != lca; i = (i & (i + 1)) - 1)
                res -= t[i];
        }
        return res;
    }

    public static void set(int[] t, int i, int value) {
        add(t, i, -get(t, i) + value);
    }

    // interval add
    public static void add(int[] t, int a, int b, int value) {
        add(t, a, value);
        add(t, b + 1, -value);
    }

    // point query
    public static int get1(int[] t, int i) {
        return sum(t, i);
    }

    // interval query
    public static int sum(int[] t1, int[] t2, int i) {
        return sum(t1, i) * i + sum(t2, i);
    }

    // Returns min(p|sum[0,p]>=sum)
    public static int lower_bound(int[] t, int sum) {
        --sum;
        int pos = -1;
        for (int blockSize = Integer.highestOneBit(t.length); blockSize != 0; blockSize >>= 1) {
            int nextPos = pos + blockSize;
            if (nextPos < t.length && sum >= t[nextPos]) {
                sum -= t[nextPos];
                pos = nextPos;
            }
        }
        return pos + 1;
    }

    // Usage example
    public static void main(String[] args) {
        int[] t = new int[10];
        set(t, 0, 1);
        add(t, 9, -2);
        System.out.println(-1 == sum(t, 0, 9));

        t = createTreeFromArray(new int[] {1, 2, 3, 4, 5, 6});
        for (int i = 0; i < t.length; i++)
            System.out.print(get(t, i) + " ");
        System.out.println();
        t = createTreeFromArray(new int[] {0, 0, 1, 0, 0, 1, 0, 0});
        System.out.println(5 == lower_bound(t, 2));

        int[] t1 = new int[10];
        int[] t2 = new int[10];
        add(t1, t2, 0, 9, 1);
        add(t1, t2, 0, 0, -2);
        System.out.println(sum(t1, t2, 9));
    }
}
```

## 38.KD Tree

```
import java.util.*;

public class KdTreePointQuery {

    public static class Point {
        int x, y;

        public Point(int x, int y) {
            this.x = x;
            this.y = y;
        }
    }

    int[] tx;
    int[] ty;

    public KdTreePointQuery(Point[] points) {
        int n = points.length;
        tx = new int[n];
        ty = new int[n];
        build(0, n, true, points);
    }

    void build(int low, int high, boolean divX, Point[] points) {
        if (low >= high)
            return;
        int mid = (low + high) >> 1;
        nth_element(points, low, high, mid, divX);

        tx[mid] = points[mid].x;
        ty[mid] = points[mid].y;

        build(low, mid, !divX, points);
        build(mid + 1, high, !divX, points);
    }

    static void nth_element(Point[] a, int low, int high, int n, boolean divX) {
        while (true) {
            int k = randomizedPartition(a, low, high, divX);
            if (n < k)
                high = k;
            else if (n > k)
                low = k + 1;
            else
                return;
        }
    }

    static final Random rnd = new Random();

    static int randomizedPartition(Point[] a, int low, int high, boolean divX) {
        swap(a, low + rnd.nextInt(high - low), high - 1);
        int v = divX ? a[high - 1].x : a[high - 1].y;
        int i = low - 1;
        for (int j = low; j < high; j++)

            if (divX ? a[j].x <= v : a[j].y <= v)
                swap(a, ++i, j);
        return i;
    }

    static void swap(Point[] a, int i, int j) {
        Point t = a[i];
        a[i] = a[j];
        a[j] = t;
    }

    long bestDist;
    int bestNode;

    public int findNearestNeighbour(int x, int y) {
        bestDist = Long.MAX_VALUE;
        findNearestNeighbour(0, tx.length, x, y, true);
        return bestNode;
    }

    void findNearestNeighbour(int low, int high, int x, int y, boolean divX) {
        if (low >= high)
            return;
        int mid = (low + high) >> 1;
        long dx = x - tx[mid];
        long dy = y - ty[mid];
        long dist = dx * dx + dy * dy;
        if (bestDist > dist) {
            bestDist = dist;
            bestNode = mid;
        }
        long delta = divX ? dx : dy;
        long delta2 = delta * delta;

        if (delta <= 0) {
            findNearestNeighbour(low, mid, x, y, !divX);
            if (delta2 < bestDist)
                findNearestNeighbour(mid + 1, high, x, y, !divX);
        }
        else {
            findNearestNeighbour(mid + 1, high, x, y, !divX);
            if (delta2 < bestDist)
                findNearestNeighbour(low, mid, x, y, !divX);
        }
    }

    public static void main(String[] args) {
        Point[] points = new Point[n];
        //fill points
        //build tree
        KdTreePointQuery kdTree = new KdTreePointQuery(points);

        int index = kdTree.findNearestNeighbour(qx, qy);
        Point p = points[index];
    }
}
```

## 39. Lazy Segment Tree

```
int64_t arr[100006];
int64_t t[262200];
int64_t lazy[262200];

void build(int64_t node, int64_t a, int64_t b)
{
    if (a>b) return;
    if (a == b)
    {
        t[node] = arr[a];
        return;
    }

    build(node * 2, a, (a + b) / 2);
    build(node * 2 + 1, (a + b) / 2 + 1, b);

    t[node] = t[node * 2] + t[node * 2 + 1];

int64_t query(int64_t node, int64_t a, int64_t b, int64_t i, int64_t j)
{
    if (a>b || a>j || b<i) return 0;
    if (lazy[node] != 0)
    {
        t[node] += lazy[node] * (b - a + 1);
        if (a != b)
        {
            lazy[node * 2] += lazy[node];
            lazy[node * 2 + 1] += lazy[node];
        }
        lazy[node] = 0;
    }

    if (a >= i && b <= j) return t[node];

    int64_t q1 = query(node * 2, a, (a + b) / 2, i, j);
    int64_t q2 = query(node * 2 + 1, (a + b) / 2 + 1, b, i, j);

    return q1 + q2;
}

void update(int64_t node, int64_t a, int64_t b, int64_t i, int64_t j, int64_t inc)
{
    if (a>b) return;
    if (lazy[node] != 0)
    {
        t[node] += lazy[node] * (b - a + 1);
        if (a != b)
        {
            lazy[node * 2] += lazy[node];
            lazy[node * 2 + 1] += lazy[node];
        }
        lazy[node] = 0;
    }
    if (a>b || a>j || b<i) return;
    if (a >= i && b <= j)
    {
        t[node] += inc*(b - a + 1);
        if (a != b)
        {
            lazy[node * 2] += inc;
            lazy[node * 2 + 1] += inc;
        }
    }
}
```

```
return;
}

update(node * 2, a, (a + b) / 2, i, j, inc);
update(node * 2 + 1, (a + b) / 2 + 1, b, i, j, inc);
t[node] = t[node * 2] + t[node * 2 + 1];
}

int main(int argc, char const *argv[])
{
    int64_t t, n, qu, q, p, a; cin >> t;
    int64_t inc;
    while (t-->0)
    {
        cin >> n >> qu;
        build(1, 0, n - 1);
        for (int i = 0; i < 262200; ++i) lazy[i] = 0; //CAREFUL
        while (qu-->0)
        {
            cin >> a;
            if (a == 0)
            {
                cin >> p >> q >> inc;
                update(1, 0, n - 1, p - 1, q - 1, inc);
            }
            else
            {
                cin >> p >> q;
                cout << query(1, 0, n - 1, p - 1, q - 1) << endl;
            }
        }
    }
    return 0;
}
```

## 40. LCA Tree Dist

```
const int max_nodes, log_max_nodes;
int num_nodes, log_num_nodes, root;

vector<int> children[max_nodes]; // children[i] contains the children of node i
int A[max_nodes][log_max_nodes + 1]; // A[i][j] is the 2^j-th ancestor of node i, or -1 if
that ancestor does not exist
int L[max_nodes]; // L[i] is the distance between node i and the root

// floor of the binary logarithm of n
int lb(unsigned int n)
{
    if (n == 0)
        return -1;
    int p = 0;
    if (n >= 1 << 16) { n >>= 16; p += 16; }
    if (n >= 1 << 8) { n >>= 8; p += 8; }
    if (n >= 1 << 4) { n >>= 4; p += 4; }
    if (n >= 1 << 2) { n >>= 2; p += 2; }
    if (n >= 1 << 1) { p += 1; }
    return p;
}

void DFS(int i, int l)
{
    L[i] = l;
    for (int j = 0; j < children[i].size(); j++)
```

```

    DFS(children[i][j], l + 1);
}

int LCA(int p, int q)
{
    // ensure node p is at least as deep as node q
    if (L[p] < L[q])
        swap(p, q);

    // "binary search" for the ancestor of node p situated on the same level as q
    for (int i = log_num_nodes; i >= 0; i--)
        if (L[p] - (1 << i) >= L[q])
            p = A[p][i];

    if (p == q)
        return p;

    // "binary search" for the LCA
    for (int i = log_num_nodes; i >= 0; i--)
        if (A[p][i] != -1 && A[p][i] != A[q][i])
        {
            p = A[p][i];
            q = A[q][i];
        }

    return A[p][0];
}

int main(int argc, char* argv[])
{
    // read num_nodes, the total number of nodes
    log_num_nodes = lb(num_nodes);

    for (int i = 0; i < num_nodes; i++)
    {
        int p;
        // read p, the parent of node i or -1 if node i is the root

        A[i][0] = p;
        if (p != -1)
            children[p].push_back(i);
        else
            root = i;
    }

    // precompute A using dynamic programming
    for (int j = 1; j <= log_num_nodes; j++)
        for (int i = 0; i < num_nodes; i++)
            if (A[i][j - 1] != -1)
                A[i][j] = A[A[i][j - 1]][j - 1];
            else
                A[i][j] = -1;

    // precompute L
    DFS(root, 0);

    return 0;
}

```

## 41. SegmentTree2D

```

import java.util.*;

public class SegmentTree2D {
    public static int max(int[][] t, int x1, int y1, int x2, int y2) {
        int n = t.length >> 1;
        x1 += n;
        x2 += n;
        int m = t[0].length >> 1;
        y1 += m;
        y2 += m;
        int res = Integer.MIN_VALUE;
        for (int lx = x1, rx = x2; lx <= rx; lx = (lx + 1) >> 1, rx = (rx - 1) >> 1)
            for (int ly = y1, ry = y2; ly <= ry; ly = (ly + 1) >> 1, ry = (ry - 1) >> 1) {
                if ((lx & 1) != 0 && (ly & 1) != 0) res = Math.max(res, t[lx][ly]);
                if ((lx & 1) != 0 && (ry & 1) == 0) res = Math.max(res, t[lx][ry]);
                if ((rx & 1) == 0 && (ly & 1) != 0) res = Math.max(res, t[rx][ly]);
                if ((rx & 1) == 0 && (ry & 1) == 0) res = Math.max(res, t[rx][ry]);
            }
        return res;
    }

    public static void add(int[][] t, int x, int y, int value) {
        x += t.length >> 1;
        y += t[0].length >> 1;
        t[x][y] += value;
        for (int tx = x; tx > 0; tx >= 1)
            for (int ty = y; ty > 0; ty >= 1) {
                if (tx > 1) t[tx >> 1][ty] = Math.max(t[tx][ty], t[tx ^ 1][ty]);
                if (ty > 1) t[tx][ty >> 1] = Math.max(t[tx][ty], t[tx][ty ^ 1]);
            }
    }

    public static void main(String[] args) {

        int[][] t = new int[sx * 2][sy * 2];
        add(t, x, y, v); // tree-x-y-value
        int res1 = max(t, x1, y1, x2, y2); // t-[x1,y1]*[x2,y2]
    }
}

```

## 42. Static RMQ

```

// keep code simple.
int lookup[MAX][LOGMAX];

struct Query
{
    int L, R;
};

void preprocess(int arr[], int n)
{
    // Initialize M for the intervals with length 1
    for (int i = 0; i < n; i++)
        lookup[i][0] = i;
}

```

```

for (int j = 1; (1 << j) <= n; j++)
{
    for (int i = 0; (i + (1 << j) - 1) < n; i++)
    {
        if (arr[lookup[i][j - 1]] < arr[lookup[i + (1 << (j - 1))][j - 1]])
            lookup[i][j] = lookup[i][j - 1];
        else
            lookup[i][j] = lookup[i + (1 << (j - 1))][j - 1];
    }
}

// Returns minimum of arr[L..R]
int query(int arr[], int L, int R)
{
    int j = (int)log2(R - L + 1);

    if (arr[lookup[L][j]] <= arr[lookup[R - (int)pow(2, j) + 1][j]])
        return arr[lookup[L][j]];

    else return arr[lookup[R - (int)pow(2, j) + 1][j]];
}

void RMQ(int arr[], int n, Query q[], int m)
{
    // Fills table lookup[n][Log n]
    preprocess(arr, n);

    for (int i = 0; i < m; i++)
    {
        // Left and right boundaries of current range
        int L = q[i].L, R = q[i].R;
        // Print sum of current query range
        cout << "Minimum of [" << L << ", "
              << R << "] is " << query(arr, L, R) << endl;
    }
}

int main()
{
    int a[] = { 7, 2, 3, 0, 5, 10, 3, 12, 18 };
    int n = sizeof(a) / sizeof(a[0]);
    Query q[] = { { 0, 4 }, { 4, 7 }, { 7, 8 } };
    int m = sizeof(q) / sizeof(q[0]);
    RMQ(a, n, q, m);
    return 0;
}

```

## 43. Infix to postfix

import java.util.Stack;

```

public class ShuntingYard {

    public static void main(String[] args) {
        String infix = "3 + 4 * 2 / ( 1 - 5 ) ^ 2 ^ 3";
        System.out.printf("infix:  %s\n", infix);
        System.out.printf("postfix: %s\n", infixToPostfix(infix));
    }

    static String infixToPostfix(String infix) {
        final String ops = "-+/*^";
        StringBuilder sb = new StringBuilder();
        Stack<Integer> s = new Stack<>();

        for (String token : infix.split("\\s")) {
            if (token.isEmpty())
                continue;
            char c = token.charAt(0);
            int idx = ops.indexOf(c);

            // check for operator
            if (idx != -1) {
                if (s.isEmpty())
                    s.push(idx);

                else {
                    while (!s.isEmpty()) {
                        int prec2 = s.peek() / 2;
                        int prec1 = idx / 2;
                        if (prec2 > prec1 || (prec2 == prec1 && c != '^'))
                            sb.append(ops.charAt(s.pop())).append(' ');
                        else break;
                    }
                    s.push(idx);
                }
            }
            else if (c == '(') {
                s.push(-2); // -2 stands for '('
            }
            else if (c == ')') {
                // until '(' on stack, pop operators.
                while (s.peek() != -2)
                    sb.append(ops.charAt(s.pop())).append(' ');
                s.pop();
            }
            else {
                sb.append(token).append(' ');
            }
        }
        while (!s.isEmpty())
            sb.append(ops.charAt(s.pop())).append(' ');
        return sb.toString();
    }
}

```

## 44.KMP

```
public class Kmp {

    public static int[] prefixFunction(String s) {
        int[] p = new int[s.length()];
        int k = 0;
        for (int i = 1; i < s.length(); i++) {
            while (k > 0 && s.charAt(k) != s.charAt(i))
                k = p[k - 1];
            if (s.charAt(k) == s.charAt(i))
                ++k;
            p[i] = k;
        }
        return p;
    }

    public static int kmpMatcher(String s, String pattern) {
        int m = pattern.length();
        if (m == 0)
            return 0;
        int[] p = prefixFunction(pattern);
        for (int i = 0, k = 0; i < s.length(); i++)
            for (; k = p[k - 1];) {
                if (pattern.charAt(k) == s.charAt(i)) {
                    if (++k == m)
                        return i + 1 - m;
                    break;
                }
                if (k == 0)
                    break;
            }
        return -1;
    }
}
```

## 45.Longest Palindrome

```
using namespace std;
template <class RAI1, class RAI2>
void fastLongestPalindromes(RAI1 seq, RAI1 seqEnd, RAI2 out)
{
    int seqLen = seqEnd - seq;
    int i = 0, j, d, s, e, lLen, k = 0;
    int pallen = 0;
    while (i < seqLen)
    {
        if (i > pallen && seq[i - pallen - 1] == seq[i])
        {
            pallen += 2;
            i++;
            continue;
        }
        out[k++] = pallen;
    }
```

```
        s = k - 2;
        e = s - pallen;
        bool b = true;
        for (j = s; j > e; j--)
        {
            d = j - e - 1;
            if (out[j] == d){
                pallen = d;
                b = false;
                break;
            }
            out[k++] = min(d, out[j]);
        }
        if (b)
        {
            pallen = 1;
            i++;
        }
    }
    out[k++] = pallen;
    lLen = k;
    s = lLen - 2;
    e = s - (2 * seqLen + 1 - lLen);
    for (i = s; i > e; i--)
    {
        d = i - e - 1;
        out[k++] = min(d, out[i]);
    }
}
```

```
//Example
//opposes
//[0, 1, 0, 1, 4, 1, 0, 1, 0, 1, 0, 3, 0, 1, 0]
//Longest palindrome has length 4
```

```
int main()
{
    string s; cin >> s;
    vector<int> V(2 * s.length() + 1);
    fastLongestPalindromes(s.begin(), s.end(), V.begin());
    int best = 0;
    cout << "[";
    for (int i = 0; i < V.size(); i++)
    {
        if (i > 0) cout << ", ";
        cout << V[i];
        best = max(best, V[i]);
    }
    cout << "]" << endl << "Longest palindrome has length " << best << endl;
    return 0;
}
```

## 46.Simple Parser

```
const char * expressionToParse = "3*2+4*1+(4+9)*6";
char peek(){
    return *expressionToParse;
}
char get(){
    return *expressionToParse++;
}
int expression();
int number(){
    int result = get() - '0';
    while (peek() >= '0' && peek() <= '9'){
        result = 10 * result + get() - '0';
    }
    return result;
}

int factor(){
    if (peek() >= '0' && peek() <= '9')
        return number();
    else if (peek() == '('){
        get(); // '('
        int result = expression();
        get(); // ')'
        return result;
    }
    else if (peek() == '-'){
        get();
        return -factor();
    }
}
return 0; // error
}

int term(){
    int result = factor();
    while (peek() == '*' || peek() == '/'){
        if (get() == '*')
            result *= factor();
        else
            result /= factor();
    }
    return result;
}

int expression(){
    int result = term();
    while (peek() == '+' || peek() == '-'){
        if (get() == '+')
            result += term();
        else
            result -= term();
    }
    return result;
}

int _tmain(int argc, _TCHAR* argv[]){
    int result = expression();
    return 0;
}
```

## 47.Suffix array

```
/*
Suffix array O(n lg^2 n)
LCP table O(n)
*/
#include <cstdio>
#include <algorithm>
#include <cstring>

using namespace std;

#define REP(i, n) for (int i = 0; i < (int)(n); ++i)

const int MAXN = 1 << 21;
char * S;
int N, gap;
int sa[MAXN], pos[MAXN], tmp[MAXN], lcp[MAXN];

bool sufCmp(int i, int j)
{
    if (pos[i] != pos[j])
        return pos[i] < pos[j];
    i += gap;
    j += gap;
    return (i < N && j < N) ? pos[i] < pos[j] : i > j;
}

void buildSA()
{
    N = strlen(S);
    REP(i, N) sa[i] = i, pos[i] = S[i];
    for (gap = 1; gap * 2 < N; gap *= 2)
    {
        sort(sa, sa + N, sufCmp);
        REP(i, N - 1) tmp[i + 1] = tmp[i] + sufCmp(sa[i], sa[i + 1]);
        REP(i, N) pos[sa[i]] = tmp[i];
        if (tmp[N - 1] == N - 1) break;
    }
}

void buildLCP()
{
    for (int i = 0, k = 0; i < N; ++i) if (pos[i] != N - 1)
    {
        for (int j = sa[pos[i] + 1]; S[i + k] == S[j + k]; ++k);
        lcp[pos[i]] = k;
        if (k)--k;
    }
}
```



## 48. Prefix Function

```
std::vector<int> prefix_function(const std::string& str) {
    std::vector<int> prefs(str.size(), 0);
    for (int i = 1; i < str.size(); ++i) {
        int pref = prefs[i - 1];
        while (pref > 0 && str[i] != str[pref]) {
            pref = prefs[pref - 1];
        }
        if (str[i] == str[pref]) {
            ++pref;
        }
        prefs[i] = pref;
    }
    return prefs;
}

std::vector<int> z_function(const std::string& str) {
    std::vector<int> zfunc(str.size(), 0);
    zfunc[0] = str.size();
    for (int i = 1, left = 0, right = 0; i < str.size(); ++i) {
        if (i <= right) {
            zfunc[i] = std::min(right - i + 1, zfunc[i - left]);
        }
        while (i + zfunc[i] < str.size() && str[zfunc[i]] == str[i + zfunc[i]]) {
            ++zfunc[i];
        }
        if (i + zfunc[i] - 1 > right) {
            left = i;
            right = i + zfunc[i] - 1;
        }
    }
    return zfunc;
}

std::string from_prefix_function(const std::vector<int>& prefs) {
    std::string str(prefs.size(), '.');
    char current_symbol = 'a';
    for (int i = 0; i < prefs.size(); ++i) {
        if (prefs[i] > 0) {
            str[i] = str[prefs[i] - 1];
        }
        else {
            str[i] = current_symbol++;
        }
    }
    return str;
}

std::vector<int> prefix_to_z(const std::vector<int>& prefs) {
    return z_function(from_prefix_function(prefs));
}

std::vector<int> z_to_prefix(const std::vector<int>& z_func) {
    std::vector<int> prefs(z_func.size(), 0);
    for (int i = 1; i < z_func.size(); ++i) {
        prefs[i + z_func[i] - 1] = std::max(prefs[i + z_func[i] - 1], z_func[i]);
    }
    for (int i = z_func.size() - 2; i >= 0; --i) {
        prefs[i] = std::max(prefs[i + 1] - 1, prefs[i]);
    }
    return prefs;
}
```

## 49. KMP

```
void computeLPSArray(char *pat, int M, int *lps);

void KMPSearch(char *pat, char *txt){
    int M = strlen(pat);
    int N = strlen(txt);

    // create lps[] that will hold the longest prefix suffix
    // values for pattern
    int *lps = (int *)malloc(sizeof(int)*M);
    int j = 0; // index for pat[]

    // Preprocess the pattern (calculate lps[] array)
    computeLPSArray(pat, M, lps);

    int i = 0; // index for txt[]
    while (i < N)
    {
        if (pat[j] == txt[i]) {
            j++;
            i++;
        }
        if (j == M){
            printf("Found pattern at index %d \n", i - j);
            j = lps[j - 1];
        }

        // mismatch after j matches
        else if (i < N && pat[j] != txt[i]){
            // Do not match lps[0..lps[j-1]] characters,
            // they will match anyway
            if (j != 0)
                j = lps[j - 1];
            else
                i = i + 1;
        }
    }
    free(lps); // to avoid memory leak
}

void computeLPSArray(char *pat, int M, int *lps){
    int len = 0;
    int i;
    lps[0] = 0;
    i = 1;
    while (i < M){
        if (pat[i] == pat[len]){
            len++;
            lps[i] = len;
            i++;
        }
        else{
            if (len != 0){
                len = lps[len - 1];
            }
            else{
                lps[i] = 0;
                i++;
            }
        }
    }
}

// Driver program to test above function
int main(){
    char *txt = "ABABDABACDABABCABAB";
    char *pat = "ABABCABAB";
    KMPSearch(pat, txt);
    return 0; }
```