
Lab Number : 08

Due Date : Nov 04, 2020

Student Details :

- Name : AB Satyaprakash
 - Roll Number : 180123062
 - Department : Mathematics and Computing
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Formulae used:

Apart from the ones needed for estimation of μ and σ , we have used the following formulae/algorithms in the code

1. $N(\mu, \sigma^2) = \mu + \sigma N(0, 1)$
2. Box-Muller algorithm to generate $N(0, 1)$
3. $R_{j+1} = -\log(U)/\lambda$
4. $X(0) = \log(S(0))$
5. $X(\tau_{j+1}) = X(\tau_j) + (\mu - 1/2\sigma^2)R_{j+1} + \sigma\sqrt{R_{j+1}} Z_{j+1} + \log Y_j$
6. $\tau_{j+1} = \tau_j + R_{j+1}$

Question :

Explanation:

-----Previous Assignment Info -----

First of all we used **pandas** (a python library) to read the csv file, i.e. the file having the daily adjusted closing stock prices for SBI for **July 1, 2020 to Sept 30, 2020**.

Then we moved on to the specific column of the data and stored it as a list. This list is then used to generate the **U**s given by natural logarithm of ratio of the current and previous day stock prices (more like previous entry, since days were missing in the csv accounting for non-working days).

Using the formulae given in the question pdf, corresponding to the gBm model, we obtained the **estimated** values of μ and σ .

After obtaining the values of μ and σ , we calculate values for 3 parameters (lists, each with 1000 values) namely,

- Z using box muller algorithm
- Y using the formula 1 and then taking exponential value
- R using formula 3

Now having the values for all these parameters, we can proceed, and obtain the value of X recursively using formula 5 (with X(0) being calculated as per formula 4), while we keep updating time as per formula 6. Also note that, since we have used the jump-point method, we need to stop our loop when we have actually reached 1000 time points. Now for each case, we can correspondingly find the S (stock prices), using the fact that $X=\log(S)$, or $S=\exp(X)$.

Finally we plot the S list obtained vs the time-point list obtained and get our required graphs!

Output:

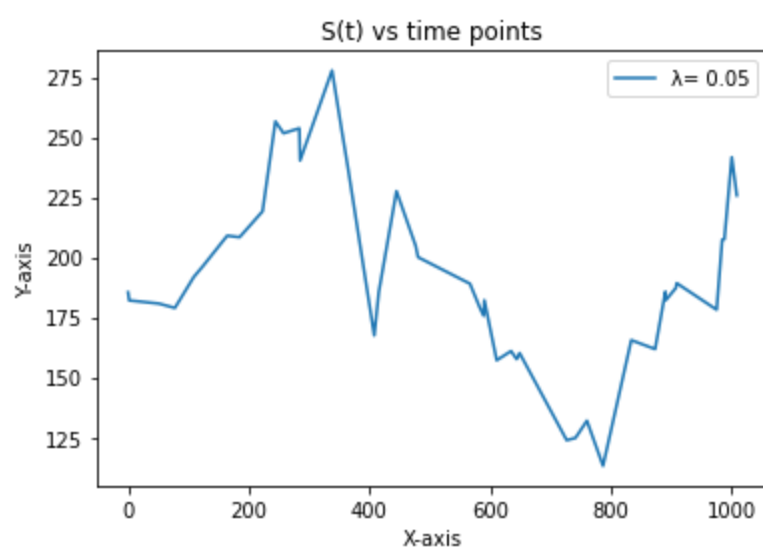
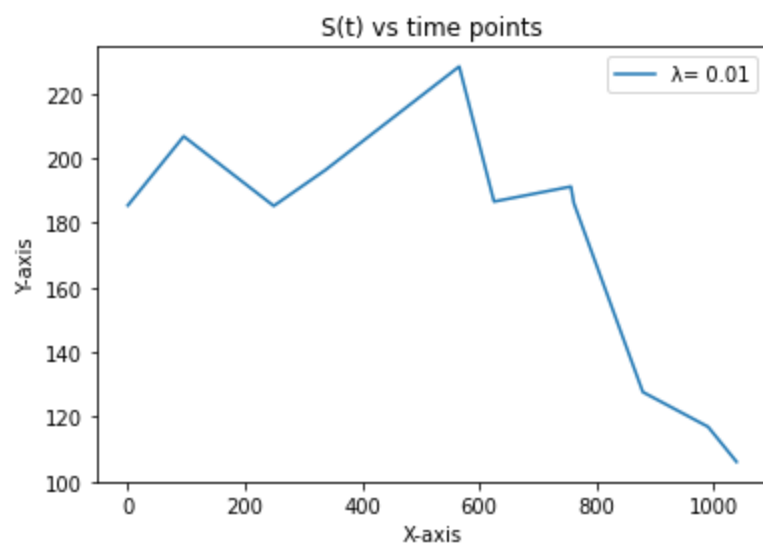
Please make sure that the file '**SBIN.NS.csv**' is in the same directory as well for pandas to do its work.

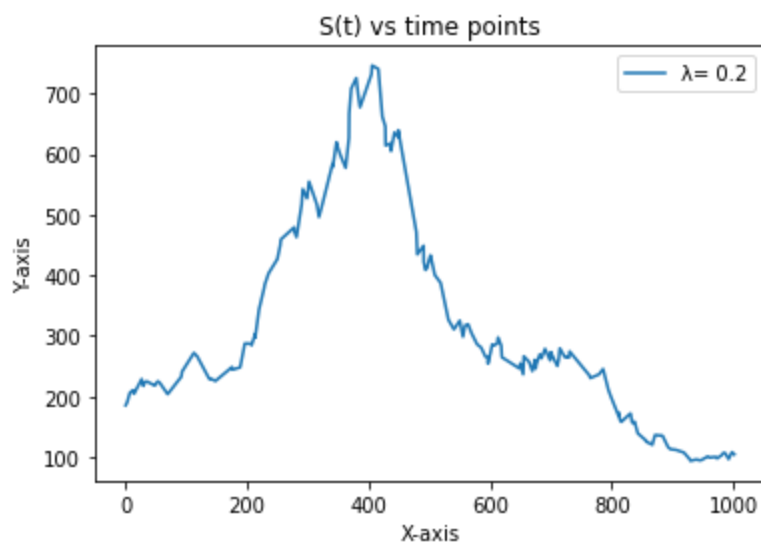
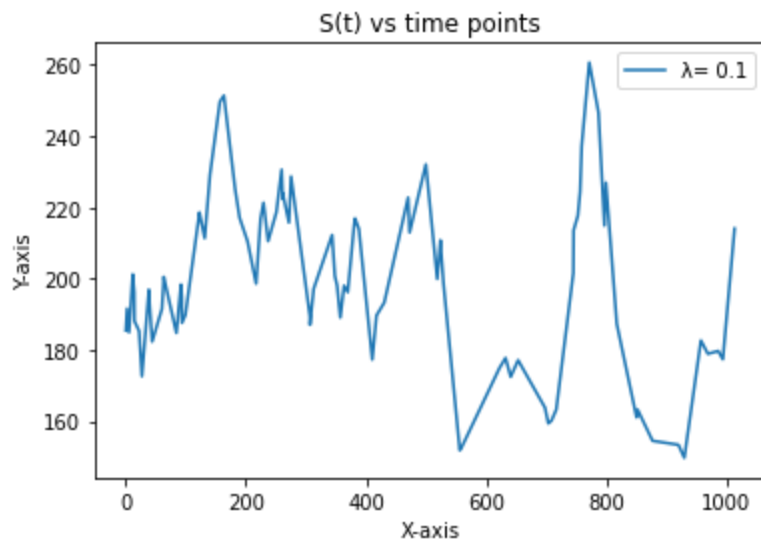
Also, the following command will install **pandas** on the linux system. One can use pip if one doesn't use python3.

```
pip3 install pandas
```

The following output is obtained in the terminal after running the program **180123062_AB.py**. (also find the 4 attached plots)

```
lord:Lab 7 imperial_lord$ python3 180123062_ABSatyaprakash.py
Estimated value of  $\mu$  (mean) = 0.0002981060700200034
Estimated value of  $\sigma$  (standard deviation) = 0.02228172705870555
```





Also note that the graphs won't be exactly the same in each case we run the program, since the value of $S(t)$ is actually governed by randomly generated values!