

B

(1)

1. It is same as set A.

2. $(P \rightarrow Q \wedge R); Q; (\sim R \rightarrow \sim S)$

Q is true, and R ~~must~~ be true.
~~One R is~~ In $Q \wedge R$ to be true.

P can be both true or false.

- In $P \rightarrow (Q \wedge R)$ to be true.

When $(Q \wedge R)$ is true.

If R is true then $\sim R$ is false
then $\sim R \rightarrow \sim S$ is always

true. So.

When Q, R are true and

P and S can be true or

false. The statements

are consistent.

$$3. \quad \{x, y, z, u\}.$$

$$R: \left\{ (x, y), (y, z), (z, x), (x, u), (y, u), (z, u), (u, y) \right\}$$

$$4. \quad \{x, y, z, u\}.$$

$$xPy, yPz, xIz, uIx, zIu, yIu.$$

$$x \in \text{choice}_{\neq} \pi.$$

5.

Individual 1: $t \succeq y \succeq x$

Individual 2: $z \succeq x \succeq t \succeq y$

Individual 3: $t \succeq y \succeq z \succeq x$

Pareto optimal state

$$\{t, z\}.$$

$\{x, y, z, u, v, t\}$.

$x y z u v t : 1.$

$y z x u v t : 1$

$z x u y v t : 1.$

$N(x P_2 y) = 3 > N(y P_2 x) = 1 \rightarrow x P y.$

$N(y P_2 z) = 3 > N(z P_2 y) = 1 \rightarrow y P z.$

$N(x P_2 z) = 1 < N(z P_2 x) = 3 \rightarrow z P x.$

-

~~$x P y$~~
cycle over $x, y, z.$
=

7.

$\{x, y, z\}$

Individual 1: $x y z$

" 2: $y z x.$

" 3: $z y x.$

Individual 4: $x y z.$

Plurality method

Scores

x: 2

y: 1

z: 1

$\begin{pmatrix} x \\ y \\ z \end{pmatrix}$
↓
Social ranking

Borda Count.

Scores

x: $2 + 2 = 4$

y: $2 + 3 = 5$

z: $2 + 1 = 3$.

social ranking is

$\begin{pmatrix} y \\ x \\ z \end{pmatrix}$
=

8). Individual 1: x z y t

Individual 2: z t x y.

Individual 3: z x t y.

Individual 2 ^{can be} almost decisive
over ~~t~~ against x.

Assume that Individual 2 is
almost decisive over t against x .

Using Pareto principle

$$z P t, z P y.$$

$$\cancel{z P t}, \cancel{z P y}. x P y.$$

we have.

$$z P t, t P x, z P y, x P y.$$

From transitivity we have.

$$z P x, \text{ and } t P y.$$

$$\text{So } \underline{z P x y}.$$

Individual 2 is ~~also~~ decisive
over all ordered pairs.

So it is dictator.

9.
2

$$\{x, y, u, v, t\}.$$

$$x P_1 y \rightarrow x P y.$$

$$u P_2 v \rightarrow u P v$$

1

$x y v u t$

2

$y x v t$

3

$x v y u t$

$x p y, u p v, x p v, x p u.$
 $x p t.$

$x \in$ serial choice $x t.$

6.

$\{x, y, z, u, v, t\}.$

$x y z u v t : 1$

$y z u x v t : 2$

$z u x y v t : 3$

$u x y z v t : 4.$

$N(x, y) = 3 > N(y, x) = 2 \Rightarrow x p y$

$N(y, z) = 3 > N(z, y) = 2 \Rightarrow y p z$

$N(z, u) = 3 > N(u, z) = 2 \Rightarrow z p u.$

$N(u, x) = 3 > N(x, u) = 2 \Rightarrow u p x.$

\rightarrow creates
a
cycle.