

LhARA linear optics documentation

N. Dover, K.R. Long, J. McGarrigle, M. Maxouti

Contents

| | 1 | Intro | oduction |
|---|---|-------------|---|
| | 2 | Cool | rdinate systems |
| | | 2.1 | Laboratory coordinate system |
| 5 | | 2.2 | Reference particle local coordinate system |
| | | 2.3 | Transforming to and from reference particle local coordinates to laboratory coordinates |
| | 3 | Phas | se space, trace space, beam parameters |
| | | 3.1 | Phase space |
| | | 3.2 | Trace space |
| 0 | | 3.3 | Beam parameters |
| | 4 | Tran | asfer matrices |
| | | 4.1 | Drift |
| | | 4.2 | Quadrupole |
| | | 4.3 | Solenoid |
| 5 | | 4.4 | Non-neutral (electron) plasma (Gabor) lens |
| | | 4.5 | Dipole |
| | 5 | Sour | rce |
| | | 5.1 | Energy distribution |
| | | 5.2 | Angular Distribution |
|) | | 5.3 | Spatial distribution |
| | | 5.4 | Simulated distributions |
| | 6 | Bear | m-line specification and scripts |
| | | 6.1 | Beam-line specification |
| | | 6.2 | Scripts |
| i | A | Mod | ule, class and data structures |
| | | A. 1 | BeamLine |
| | | A.2 | Particle and ReferenceParticle |
| | | A.3 | Beam and extrapolateBeam |
| | | A.4 | BeamLineElement |
| ı | | A.5 | UserFramework |
| | | A.6 | visualise |
| | | A.7 | BeamIO |
| | | A.8 | Simulation |
| | | A.9 | Physical constants |
| 5 | | A.10 | Report |
| | | Λ 11 | |

B Set-up and run 71

1 Introduction

The LhARA [1, 2] linear optics package was written to allow rapid calculations to initiate more detailed studies of the LhARA beam lines and for use as a tool to check issues as they arise. The package has been written in Python so that it is accessible and can readily be updated, modified and maintained. At present the code treats proton beams only.

This document presents the approximations and notation used and summarises the module, class and data structures that have been adopted.

2 Coordinate systems

2.1 Laboratory coordinate system

The origin of the LhARA coordinate system, the "laboratory coordinate system" or "laboratory reference frame", is at the position of the laser focus at the laser-target interaction point [3]. The z axis is horizontal and parallel to the nominal capture axis, pointing in the downstream direction. The y axis points vertically upwards and the x axis completes a right-handed orthogonal coordinate system.

Unit vectors along the x, y and z axes are i, j and k respectively. The position of the reference particle as well as its momentum and energy are described as functions of the distance it has travelled from the origin of coordinates. The distance the reference particle has travelled is s, making the position, r_0 , momentum, p_0 , and energy, E_0 , of the reference particle position, s:

$$r_0 = r_0(s);$$

 $p_0 = p_0(s);$ and $E_0 = E_0(s).$ (1)

The magnitude of the reference particle velocity is v_0 and the relativistic parameters that determine the reference particle energy and momentum are:

$$\beta_0 = \frac{v_0}{c}; \text{ and}$$

$$\gamma_0 = \frac{1}{\sqrt{1 - \beta_0^2}};$$

where c is the speed of light. The time, t, at which the reference particle is at s is also a function of s:

$$t = t(s) = \frac{s}{v_0} = \frac{s}{c} \frac{E_0}{cp_0};$$
 (2)

where $p_0 = |p_0|$.

2.2 Reference particle local coordinate system

A coordinate system defined relative to the position of the reference particle, the "reference particle local coordinate" (RPLC) system, may be defined using the direction in which the particle is travelling. The position of the particle defines the origin of the RPLC system, see figure 1. The tangent to the reference particle trajectory at s defines the z_r axis with unit vector k_r . In the laboratory frame, the presence of local electric or magnetic fields may cause the reference particle's trajectory to change. In the neighbourhood of the particle,

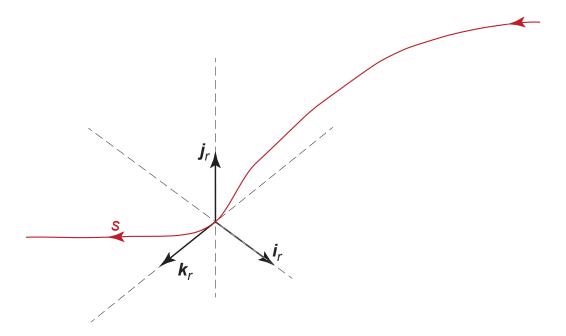


Figure 1: Reference particle local coordinate system. The trajectory of the reference particle is shown as the red line. The distance the reference particle has travelled, measured from the origin of coordinates in the laboratory frame, is labelled s. The origin of the "reference particle local coordinate (RPLC) system is coincident with the position of the reference particle. The directions of unit vectors along each of three righthanded, orthogonal coordinate axes are shown as black arrows labelled i_T , j_T , and j_T .

the curved trajectory may be described in terms of an arc of a circle. The x_r axis (with unit vector i_r) is then taken to be in the direction pointing away from the centre of the circle. The third coordinate axis, y_r , is defined to complete the right-handed orthogonal coordinate system; the unit vector along the y_r axis being given by $j_r = k_r \times i_r$.

The trajectory of the reference particle is a straight line as it traverses a drift space and a variety of beam-line elements. Examples of such beam-line elements include solenoids and quadrupoles. The reference trajectory is also undeviated by passage through an accelerating cavity placed such that the accelerating field is parallel to the reference-particle trajectory.

The RPLC coordinate system at s=0 is taken to coincide with the laboratory coordinate system. Beamline elements are placed sequentially along the trajectory of the reference particle. If necessary a coordinate transformation is performed to ensure that the RPLC system at the entrance to a particular beam-line element is consistent with the definition given above.

2.3 Transforming to and from reference particle local coordinates to laboratory coordinates

In the RPLC system, the trajectory of the reference particle, R_0 , is:

$$\mathbf{R}_0(s) = \mathbf{0} \,. \tag{3}$$

The position of a test particle in the RPLC frame, *R*, is described with reference to the position of the reference particle. In the laboratory frame, the position of the test particle is:

$$\mathbf{r}(s) = \mathbf{r}_0(s) + \boldsymbol{\delta}\mathbf{r}(s); \tag{4}$$

where:

100

$$\delta r(s) = \underline{R}(s)R(s)$$
; and (5)

 $\underline{\underline{R}}(s)$ is a rotation matrix that takes the RPLCs at s to the laboratory frame coordinates. In the laboratory frame, the unit vectors i_r , j_r and k_r are given by:

$$i_{r} = \begin{pmatrix} i_{rx} \\ i_{ry} \\ i_{rz} \end{pmatrix};$$

$$j_{r} = \begin{pmatrix} j_{rx} \\ j_{ry} \\ j_{rz} \end{pmatrix}; \text{ and }$$

$$k_{r} = \begin{pmatrix} k_{rx} \\ k_{ry} \\ k_{rz} \end{pmatrix}.$$
(6)

The rotation matrix, \underline{R} , may now be written:

$$\underline{\underline{R}}(s) = \begin{bmatrix} i_{rx} & j_{rx} & k_{rx} \\ i_{ry} & j_{ry} & k_{ry} \\ i_{rz} & j_{rz} & k_{rz} \end{bmatrix} . \tag{7}$$

3 Phase space, trace space, beam parameters

The motion of particles passing through an accelerator is most often described using classical Hamiltonian mechanics; quantum mechanics being required only in particular cases such as the description of spin polarisation in a storage ring. In classical Hamiltonian mechanics the equations of motion are solved to give the evolution of the position, momentum, and energy as functions of a single independent parameter. The independent parameter is often taken to be time.

Relativistic mechanics exploits four-vector position, $\underline{\mathcal{R}}=(r,ct)$, and four-vector momentum, $\underline{\mathcal{P}}=(cp,E)$. In the Hamiltonian description of particle dynamics, these four vectors become functions of the independent variable, i.e. $\underline{\mathcal{R}}=\underline{\mathcal{R}}(t)$ and $\underline{\mathcal{P}}=\underline{\mathcal{P}}(t)$. In the laboratory system, the position of the reference particle along its trajectory is directly related to the time coordinate by $t=c\beta_0 s$. This allows s to be taken as the independent variable and for the motion of particles in the beam to be derived as functions of s.

The 6D phase-space coordinates of a particle as a function of s are given by the position and momentum three vectors. The particle energy may be determined from the invariant mass and the time coordinate from the invariant interval between the origin and the position represented by s.

The "trace-space" coordinates of a particle are defined relative to the reference particle. Usually, a beam is understood to contain particles which follow trajectories that differ rather little from that of the reference particle. Trace space is defined such that the position, "momentum", and "energy" coordinates are small for particles which follow trajectories close to that of the reference particle. The utility of this approach is that trace-space coordinates may be used to perform Taylor expansions of the Hamiltonian which may readily be solved to yield a description of particle transport using functions that are linear in the trace-space coordinates.

The notation used for the 6D phase and trace spaces are defined in this section.

3.1 Phase space

The 6D phase-space vector is defined in terms of the three-vector position and three vector momentum as:

$$\begin{bmatrix} \boldsymbol{r} \\ \boldsymbol{p} \end{bmatrix} = \begin{bmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} \\ \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix} \end{bmatrix}$$
(8)

The trajectory of the particle may be evaluated as a function of time or s.

110 3.2 Trace space

Trace space is defined to simplify the calculation of the trajectory of particles through the accelerator lattice and is derived from the phase space expressed in the RPLC frame. Consider a particle with position $r_{\rm RPLC} = (x_{\rm RPLC}, y_{\rm RPLC}, z_{\rm RPLC})$ and momentum $p_{\rm RPLC} = (p_{\rm x\,RPLC}, p_{\rm y\,RPLC}, p_{\rm z\,RPLC})$. Taking the magnitude of the momentum of the reference particle in the laboratory frame to be p_0 , the trace-space coordinates are given by:

$$\underline{\phi} = \begin{pmatrix} x_{\text{RPLC}} \\ x'_{\text{RPLC}} \\ y_{\text{RPLC}} \\ y'_{\text{RPLC}} \\ z_{\text{RPLC}} \end{pmatrix};$$
(9)

115 where:

$$x'_{\text{RPLC}} = \frac{\partial x}{\partial s} = \frac{cp_{x \text{ RPLC}}}{cp_0};$$
 (10)

$$y'_{\text{RPLC}} = \frac{\partial y}{\partial s} = \frac{cp_{y \text{ RPLC}}}{cp_0};$$
 (11)

$$z_{\text{RPLC}} = \frac{s}{\beta_0} - ct = \frac{\Delta s}{\beta_0}$$
; and (12)

$$\delta_{\text{RPLC}} = \frac{E}{cp_0} - \frac{1}{\beta_0} = \frac{\Delta E}{cp_0}. \tag{13}$$

Here $\Delta s = s - s_0$ and $\Delta E = E - E_0$, where s_0 and E_0 are the reference particle position and energy respectively; E and s are the energy and position of a particular particle in the beam.

3.3 Beam parameters

The trace space vector, $\underline{\phi}_i$, of the i^{th} particle at a position along the beam line contains the varaince of the particle coordinates with respect to those of the reference particle. For a sample containing N particles, the covariance matrix, \underline{C}_6 , may therefore be obtained by evaluating:

$$\underline{\underline{C}}_{6} = \frac{1}{N} \sum_{i}^{N} \underline{\phi}_{i} \, \underline{\phi}_{i}^{T} = \langle \underline{\phi} \, \underline{\phi}^{T} \rangle ; \qquad (14)$$

where the notation $\langle \rangle$ is used to denote evaluating the expectation value. The RMS emittance of the beam in all 6 trace-space dimensions is then given by:

$$\varepsilon_6 = \sqrt[6]{\left|\underline{\underline{C}}_6\right|} \ . \tag{15}$$

In an analagous notation, the four-dimensional transverse trace space (x, x', y, y') may be used to define the four-dimensional covariance matrix $\underline{\underline{C}}_4$, which, in turn, can be used to evaluate the four-dimensional transverse emittance:

$$\varepsilon_4 = \sqrt[4]{\left|\underline{\underline{C}}_4\right|} \ . \tag{16}$$

The size of the beam in the two "transverse planes" (x, x') and (y, y') is contained in two, 2×2 submatrices of $\underline{\underline{C}}_6$, $\underline{\underline{C}}_x$ and $\underline{\underline{C}}_y$. If the x and y coordinates are to be taken as uncoupled, then the emittance of the (x, x') and (y, y') trace space my be obtained using:

$$\varepsilon_x = \sqrt{\left|\underline{\underline{C}}_x\right|} \text{ and }$$
 (17)

$$\varepsilon_y = \sqrt{\left|\underline{\underline{C}}_y\right|}$$
 (18)

With u = x or y, the area of the trace space ellipse is given by $\pi \varepsilon_u$ and the Twise parameters, α_u , β_u , and γ_u are given by:

$$\sigma_u^2 = \langle u^2 \rangle = \beta_u, \varepsilon_u; \tag{19}$$

$$\langle u'^2 \rangle = \gamma_u, \varepsilon_u : \text{and}$$
 (20)

$$\langle uu' \rangle = -\alpha_u \varepsilon_u; \tag{21}$$

where:

$$\beta_u \gamma_u - \alpha_u^2 = 1. (22)$$

4 Transfer matrices

A beam line may be described as a series of beam-line elements arranged one after the other. A particle may then be transported through the beam line by transporting it through each element in turn. Taking advantage of the trace-space defined above, the transport of a particle across a particular beam-line element may be performed using a linear transformation:

$$\underline{\phi}_{\text{end}} = \underline{\underline{T}} \, \underline{\phi}_{\text{start}} \,; \tag{23}$$

where $\phi_{\rm start}$ is the trace-space vector at the start of the beam-line element and $\phi_{\rm end}$ is the transformed trace-space vector at the end. The step across the beam-line element implies an increment, δs , to the s-coordinate given by:

$$s_{\rm end} = s_{\rm start} + \delta s;$$
 (24)

where $s_{\rm start}$ and $s_{\rm end}$ are the coordinate along the reference particle trajectory at the start and end of the beam-line element respectively. There are many excellent descriptions of the derivation of the transfer matrices, $\underline{\underline{T}}$, so only the results are quoted here. The notation used below is developed from that used in [4].

4.1 Drift

A "drift" space refers to a region in which the beam propagates in the absence of any electromagnetic fields. In a drift, particles propagate in straight lines, therefore:

$$\underline{\underline{T}}_{\text{drift}} = \begin{pmatrix} 1 & l & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & l & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}; \tag{25}$$

where l is the length of the drift. The increment in the reference particle position is:

$$\delta s = l. \tag{26}$$

4.2 Quadrupole

The passage of a beam particle through a quadrupole magnet may be described by specifying the field gradient, g, within the magnet and the length, l_q , of the quadrupole measured along its axis. The impact of a quadrupole on the trajectory of a particle in the xy plane is independent of the impact of the magnet on the particle's trajectory in the yz plane. In this sense quadrupole focusing in the xz and yz planes is said to be "uncoupled".

If the field gradient along the x and y axes is identical, then:

$$g_x = \frac{\partial B_{qx}}{\partial x} = g_y = \frac{\partial B_{qy}}{\partial y} = g;$$
 (27)

where the field in the quadrupole, B_q , has components $(B_{qx}, B_{qy}, 0)$.

In the "hard-edge" approximation, where the field falls to zero at the start and end of the quadrupole, the transfer matrix for a quadrupole focusing in the xz plane (a "focusing quadrupole") may be written:

$$\underline{\underline{T}}_{\text{Fquad}} = \begin{pmatrix}
\cos(\sqrt{k_q} l_q) & \frac{\sin(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 & 0 & 0 \\
-\sqrt{k_q} \sin(\sqrt{k_q} l_q) & \cos(\sqrt{k_q} l_q) & 0 & 0 & 0 & 0 \\
0 & 0 & \cosh(\sqrt{k_q} l_q) & \frac{\sinh(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 \\
0 & 0 & \sqrt{k_q} \sinh(\sqrt{k_q} l_q) & \cosh(\sqrt{k_q} l_q) & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & \frac{l_q}{\beta_0^2 \gamma_0^2} \\
0 & 0 & 0 & 0 & 0 & 1
\end{pmatrix}; (28)$$

where:

155

$$k_q = \frac{gc}{p} \times 10^{-3} \,\mathrm{m}^{-2} \,,$$
 (29)

c is the speed of light in metres per second, p is the magnitude of the momentum of the particle in MeV/c, and the field gradient, g, is given in T/m. As before, β_0 is the relativistic velocity of the reference particle and $\gamma_0 = (1 - \beta_0^2)^{-\frac{1}{2}}$. The increment in the reference particle position is:

$$\delta s = l_a \,. \tag{30}$$

It is important to include a description of the effect of dispersion on beam transport through the LhARA beam line since the laser-driven proton and ion source provides a broad energy spectrum. Reference [4] describes two methods for the description of dispersion in a linear approximation. The first is to use the reference momentum to calculate the quadrupole focusing strength ($k_{0q} = \frac{gc}{p_0} \times 10^{-3} \,\mathrm{m}^{-2}$) and to include terms in the expressions for x, x', y, and y' dependent on δ . The second is to use equation 29 to calculate the effective quadrupole focusing strength, with k_q evaluated using p. The second approach has been adopted here.

In the same notation, the transfer matrix for a quadrupole focusing in the yz plane (a "defocusing quadrupole") may be written:

$$\underline{\underline{T}}_{\text{Dquad}} = \begin{pmatrix}
\cosh(\sqrt{k_q} l_q) & \frac{\sinh(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 & 0 & 0 \\
\sqrt{k_q} \sinh(\sqrt{k_q} l_q) & \cosh(\sqrt{k_q} l_q) & 0 & 0 & 0 & 0 \\
0 & 0 & \cos(\sqrt{k_q} l_q) & \frac{\sin(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 \\
0 & 0 & -\sqrt{k_q} \sin(\sqrt{k_q} l_q) & \cos(\sqrt{k_q} l_q) & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & \frac{l_q}{\beta_0^2 \gamma_0^2} \\
0 & 0 & 0 & 0 & 0 & 1
\end{pmatrix}.$$
(31)

4.3 Solenoid

The trajectory of a beam particle through a solenoid is determined by the magnetic field strength, B_s , within the solenoid and the length of the solenoid, l_s , measured along its axis. As the particle enters the solenoid, the fringe field imparts momentum transverse to the axis of the magnet. This results in the particle executing a helical trajectory, the axis of the helix being parallel to the solenoid axis. The sense of the rotation depends on the particle charge and the polarity of the field. The helical motion means that the evolution of the particle motion in the yz plane is coupled with the evolution of the particle motion in the yz plane.

In the "hard-edge" approximation, the magnetic field inside the magnet is given by $\mathbf{B}_s = (0, 0, B_{s0})$, where the solenoid axis lies along the z_{RPLC} axis. The solenoid field-strength parameter is then given by:

$$k_s = \left[\frac{B_{s0}c}{2p} \times 10^{-3}\right]^2 \text{ m}^{-2};$$
 (32)

where B_{s0} is measured in T, p in MeV/c and c in m/s.

The transfer matrix for passage of a positive particle through a solenoid with field pointing in the positive z_{RPLC} direction may be written:

$$\underline{T}_{Sol} = \begin{pmatrix} \cos^{2}(\sqrt{k_{s}}l_{s}) & \frac{1}{2\sqrt{k_{s}}}\sin(\sqrt{k_{s}}l_{s}) & \frac{1}{2}\sin(2\sqrt{k_{s}}l_{s}) & \frac{1}{\sqrt{k_{s}}}\sin^{2}(\sqrt{k_{s}}l_{s}) & 0 & 0\\ -\frac{\sqrt{k_{s}}}{2}\sin(2\sqrt{k_{s}}l_{s}) & \cos^{2}(\sqrt{k_{s}}l_{s}) & -\sqrt{k_{s}}\sin^{2}(\sqrt{k_{s}}l_{s}) & \frac{1}{2}\sin(2\sqrt{k_{s}}l_{s}) & 0 & 0\\ -\frac{1}{2}\sin(2\sqrt{k_{s}}l_{s}) & -\frac{1}{\sqrt{k_{s}}}\sin^{2}(\sqrt{k_{s}}l_{s}) & \cos^{2}(\sqrt{k_{s}}l_{s}) & \frac{1}{2\sqrt{k_{s}}}\sin(2\sqrt{k_{s}}l_{s}) & 0 & 0\\ \sqrt{k_{s}}\sin^{2}(\sqrt{k_{s}}l_{s}) & -\frac{1}{2}\sin(2\sqrt{k_{s}}l_{s}) & -\frac{\sqrt{k_{s}}}{2}\sin(2\sqrt{k_{s}}l_{s}) & \cos^{2}(\sqrt{k_{s}}l_{s}) & 0 & 0\\ 0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_{0}^{2}\gamma_{0}^{2}}\\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}.$$

$$(33)$$

As in the case of the quadrupoles, dispersion is accounted for by using p to calculate k_s (equation 32). The increment in the reference particle position is:

$$\delta s = l_s \,. \tag{34}$$

4.4 Non-neutral (electron) plasma (Gabor) lens

A dense gas of electrons confined in a Penning-Malmberg trap provides an electric field that can be used to focus a positive ion beam. The electron gas is confined axially in the lens by an electrostatic potential created using a central anode of length l_G . The gas is confined radially using the uniform field of a solenoid. Assuming a uniform electron density, n_e , the focusing parameter, k_G , may be written:

$$k_G = \frac{e}{2\epsilon_0} \frac{m_p \gamma}{p^2} n_e \quad \text{m}^{-2};$$
(35)

where e is the charge on the electron, ϵ_0 is the permittivity of free space, and m_p is the proton mass. As in the case of the quadrupoles and solenoid, dispersion is accounted for by using p in equation 35. The force on a particle passing through the electron gas is towards the axis of the lens and is proportional to the radial distance of the particle from the axis. Focusing is therefore cylindrically symmetric and does not couple motion in the the xz and yz planes.

In the "hard-edge" approximation, the electric field inside the lens falls to zero at the end of the electron gas and the contribution of the magnetic field used to confine the electron gas in the transverse direction has a negligible effect on particles passing through the lens. The transfer matrix for the passage of a positive particle

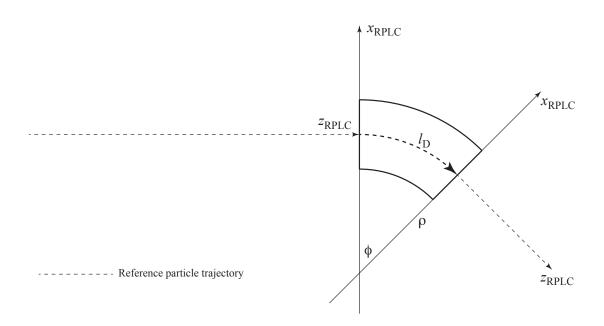


Figure 2: Schematic representation of the passage of the reference particle through a sector dipole. The outline of the sector dipole is shown by the solid black lines. The trajectory of the reference particle is shown as the dashed line. The length of the reference-particle trajectory inside the field of the sector dipole is l_D . The $x_{\rm RPLC}$ and $z_{\rm RPLC}$ coordinate axes at the entry and exit of the sector dipole are shown. The radius of curvature of the reference particle trajectory inside the magnet is ρ and the angle through which the $x_{\rm RPLC}$ is rotated is ϕ .

through the lens may be written:

$$\underline{\underline{T}}_{G} = \begin{pmatrix}
\cos(\sqrt{k_{G}}l_{G}) & \frac{\sin(\sqrt{k_{G}}l_{G})}{\sqrt{k_{G}}} & 0 & 0 & 0 & 0 \\
-\sqrt{k_{G}}\sin(\sqrt{k_{G}}l_{G}) & \cos(\sqrt{k_{G}}l_{G}) & 0 & 0 & 0 & 0 \\
0 & 0 & \cos(\sqrt{k_{G}}l_{G}) & \frac{\sin(\sqrt{k_{G}}l_{G})}{\sqrt{k_{G}}} & 0 & 0 \\
0 & 0 & -\sqrt{k_{G}}\sin(\sqrt{k_{G}}l_{G}) & \cos(\sqrt{k_{G}}l_{G}) & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_{0}^{2}\gamma_{0}^{2}} \\
0 & 0 & 0 & 0 & 0 & 1
\end{pmatrix}.$$
(36)

The increment in the reference particle position is:

$$\delta s = l_G. \tag{37}$$

4.5 Dipole

The reference particle trajectory in the beam-line elements described above passes along the axis of the element. In contrast, a dipole bends the reference trajectory so that it describes the arc of a circle (see figure 2). The code provides for transport through a "sector dipole" in the hard-edge approximation. In this case, the field within the magnet is taken to be constant and parallel to j_{RPLC} , i.e. $B_D = (0, B_{D0}, 0)$. No edge focusing is considered.

The passage of particles through a dipole may be described by defining the parameter, k_D :

$$k_D = \left[\frac{B_{D0}c}{p} \times 10^{-3}\right]^2 \,\mathrm{m}^{-2}\,.$$
 (38)

The momentum of the reference particle is related to the curvature. ρ , by:

$$p_0 = B_{D0}\rho; (39)$$

so:

$$k_D = \frac{1}{\rho};\tag{40}$$

and the angle ϕ is given by:

$$\phi = \frac{l_D}{\rho} \,. \tag{41}$$

With these definitions the transfer matrix for passage through a dipole may be written:

$$\underline{\underline{T}}_{D} = \begin{pmatrix}
\cos(\phi) & \rho \sin(\phi) & 0 & 0 & 0 & \frac{\rho}{\beta_{0}} (1 - \cos(\phi)) \\
-\frac{\sin(\phi)}{\rho} & \cos(\phi) & 0 & 0 & 0 & \frac{\sin(\phi)}{\beta_{0}} \\
0 & 0 & 1 & l & 0 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 \\
-\frac{\sin(\phi)}{\beta_{0}} & -\frac{\rho}{\beta_{0}} (1 - \cos(\phi)) & 0 & 0 & 1 & \frac{l}{\beta^{2} \gamma^{2}} - \frac{l - \rho \sin(\phi)}{\beta_{0}^{2}} \\
0 & 0 & 0 & 0 & 0 & 1
\end{pmatrix} .$$
(42)

The increment in the reference particle position is:

$$\delta s = l_D. \tag{43}$$

5 Source

A variety of options for the generation of the particle distribution at source are included in the package (see section ??). The principal, and the default, option is the target-normal sheath acceleration (TNSA) model presented in [5]. The implementation of this model is summarised below. The laboratory and RPLC reference frames coincide at the target, therefore trace- and phase-coordinates are not distinguished in the presentation of the particle-production model.

5.1 Energy distribution

The typical kinetic energy spectrum produced in target-normal sheath acceleration falls rapidly with kinetic energy before dropping rapidly to zero above a maximum "cut off" energy ε_{max} . The kinetic-energy spectrum of the TNSA model presented in [5] is given by:

$$\frac{dN}{d\varepsilon} = \frac{n_{e0}c_s t_{laser} S_{sheath}}{\sqrt{2\varepsilon T_e}} \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right); \tag{44}$$

where N is the number of protons or ions produced per unit solid angle, ε is the ion kinetic energy, n_{e0} and T_e are the hot electron density and temperature respectively, c_s is the ion acoustic velocity, $t_{\rm laser}$ is the duration of the laser pulse, and $S_{\rm sheath}$ is the effective area over which the TNSA mechanism takes place. The variables and the units in which they are expressed are presented in table 1.

Equation 44 is based on time-limited fluid-dynamical models which are unable to predict the cut-off kinetic energy accurately. The cut-off energy is taken to be that given by the model described in [6] in which the time over which the laser pulse creates the conditions necessary for acceleration is derived. The kinetic energy cut-off is given by:

$$\varepsilon_{max} = X^2 \varepsilon_{i,\infty}; \tag{45}$$

Table 1: Parameters present in the analytical expression, equation 44, describing target normal sheath acceleration (TNSA).

| Parameter | Definition | Value | Unit |
|------------------------|--------------------------------|--|---------------------|
| N | Ion number | - | - |
| ε | Ion kinetic energy | - | J |
| n_{e0} | Hot electron density | $\frac{N_E}{ct_{laser}S_{sheath}}$ | pp/m^3 |
| N_e | Accelerated electron number | $\frac{fE_{laser}}{T_e}$ | - |
| E_{laser} | Laser energy | 70 | J |
| f | Energy conversion efficiency | $1.2 \times 10^{-15} I^{0.75}$, max=0.5 | - |
| I | Laser intensity | 4×10^{20} | W/cm^2 |
| T_e | Hot electron temperature | $m_e c^2 \left[\sqrt{1 + \frac{I\lambda^2}{1.37 \times 10^{18}} - 1} \right]$ | J |
| m_e | Electron mass | 9.11×10^{-31} | Kg |
| c | Speed of light | 3×10^8 | m/s |
| λ | Laser wavelength | 0.8 | μ m |
| t_{laser} | Laser pulse duration | 28×10^{-15} | S |
| B | Radius of electron bunch | $B = r_0 + dtan(\theta)$ | m |
| S_{sheath} | Electron acceleration area | πB^2 | m^2 |
| r_0 | Laser spot radius | $\sqrt{rac{P_{laser}}{I\pi}}$, I in W/m^2 | m |
| d | Target thickness | $400 - 600 \times 10^{-9}$ | m |
| heta | Electron half angle divergence | 0.436 | rad |
| P_{laser} | Laser power | 2.5×10^{15} , $P_{laser} = \frac{E_{laser}}{t_{laser}}$ | W |
| c_s | Ion-acoustic velocity | $(\frac{Zk_BT_e}{m_i})^{\frac{1}{2}}$ | m/s |
| Z | Ion charge number | 1 | - |
| k_B | Boltzmann constant | 1.380649×10^{-23} | $m^2kgs^{-2}K^{-1}$ |
| m_i | Proton mass | 1.67×10^{-27} | Kg |
| P_R | Relativistic power unit | $\frac{m_e c^2}{r_e} = 8.71 \times 10^9$ | W |
| r_e | Electron radius | 2.82×10^{-15} | m |
| $arepsilon_{i,\infty}$ | Maximum ion kinetic energy | $2Zm_ec^2\sqrt{rac{fP_{laser}}{P_R}}$ | MeV |
| t_0 | Ballistic time | $rac{B}{v(\infty)}$ | S |
| $v(\infty)$ | Ballistic velocity | $\sqrt{rac{2arepsilon_{i,\infty}}{m_{i}}}$ | m/s |

where *X* is obtained by solving:

230

$$\frac{t_{laser}}{t_0} = X \left(1 + \frac{1}{2} \frac{1}{1 - X^2} \right) + \frac{1}{4} \ln \left(\frac{1 + X}{1 - X} \right). \tag{46}$$

Here t_0 is the time over which the ion acceleration may be treated as ballistic and $\varepsilon_{i,\infty}$ is given in table 1.

To generate the kinetic energy spectrum, the probability density function, $g(\varepsilon)$, is defined such that the probability, $\delta \mathcal{P}$, of a particle being generated in the interval $\varepsilon \to \varepsilon + \delta \varepsilon$ is given by:

$$\delta \mathcal{P} = g\left(\varepsilon\right)\delta\varepsilon. \tag{47}$$

 $g(\varepsilon)$ can be written in terms of the differential spectrum given in equation 44 through the introduction of a normalisation constant \mathcal{N} :

$$g(\varepsilon) = \frac{1}{N} \frac{dN}{d\varepsilon} \,. \tag{48}$$

The cumulative distribution funtion, $G(\varepsilon)$, is given by:

$$G(\varepsilon) = \int_{\varepsilon_{\min}}^{\varepsilon_{\max}} g(\varepsilon) d\varepsilon; \qquad (49)$$

where ε_{\min} is the minimum kinetic energy and the normalisation constant, \mathcal{N} , is set so that $G(\varepsilon_{\max}) = 1$. Carrying out the integration yields:

$$G(\varepsilon) = \frac{2}{N} \frac{n_{e0}c_s t_{laser} S_{sheath}}{\sqrt{2T_e}} \sqrt{\frac{T_e}{2}} \left[\exp\left(-\sqrt{\frac{2\varepsilon_{\min}}{T_e}}\right) - \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right) \right]; \tag{50}$$

and the normalisation constant is given by:

$$\mathcal{N} = 2 \frac{n_{e0} c_s t_{laser} S_{sheath}}{\sqrt{2T_e}} \sqrt{\frac{T_e}{2}} \left[\exp\left(-\sqrt{\frac{2\varepsilon_{\min}}{T_e}}\right) - \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right) \right]. \tag{51}$$

The kinetic energy spectrum may now be obtained by choosing a value for $G(\varepsilon)$ using a probability distribution uniform over the range $0 < G(\varepsilon) < 1$. The generated value of ε is obtained by evaluating:

$$\varepsilon = \left[\sqrt{\varepsilon_{\min}} - \sqrt{\frac{T_e}{2}} \ln \left(1 - \frac{G(\varepsilon)}{G(\varepsilon_{\max})} \right) \right]^2.$$
 (52)

240 5.2 Angular Distribution

The angular distribution of the flux of protons and ions produced by the TNSA mechanism may be described as a cone centred on the normal to the foil surface [7]. Radiochromic film has been used to observe the opening angle, 2α , of the cone as a function of energy. The envelope angle, α , defined such that, at a particular energy, all particles are contained within $\pm \alpha(\varepsilon)$ of the z axis. The opening angle is observed to decrease as the ion energy increases.

The distribution of the polar angle, θ_S , at which particles are produced at the laser-driven source is generated by defining r' such that:

$$r' = \frac{\partial r}{\partial s}; (53)$$

where $r = \sin \theta_S$. x' and y' are sampled independently from the probability density function:

$$g(r') = \frac{3}{4r_m'^2} \left(r_m'^2 - r'^2 \right) ; \tag{54}$$

Table 2: Parameterised laser driven

| Parameter | Value | Unit |
|---|---|---------|
| σ_x | 4e-06 | μ m |
| $\mid \sigma_y \mid$ | 4e-06 | μ m |
| $ \cos 	heta_S _{	ext{min}}$ | 0.998 | |
| $arepsilon_{	ext{min}}$ | 1.0 | MeV |
| $arepsilon_{	ext{max}}$ | 25.0 | MeV |
| nPnts | 1000 | |
| Laser power | 250000000000000000000000000000000000000 | W |
| Laser energy | 70.0 | J |
| Laser wavelength | 0.8 | μ m |
| Laser pulse duration | 2.8e-14 | s |
| Laser spot size | 4e-07 | μ m |
| Laser intensity | 4e+20 | J/m^2 |
| Electron divergence angle | 25.0 | degrees |
| RMS θ_S at $K = 0 \mathrm{MeV}$ | 20 | degrees |
| Scaled slope of RMS θ_S versus K | 15 | degrees |

where $r'_m = \sin \alpha$. At low kinetic energy ($\varepsilon \sim \varepsilon_{\min}$), $\alpha(\varepsilon)$ is taken to be $\sim 20^{\circ}$. $\alpha(\varepsilon)$ is assumed to decrease linearly with energy such that:

$$\alpha(\varepsilon) = 20^{\circ} - 15^{\circ} \frac{\varepsilon}{\varepsilon_{max}}; \tag{55}$$

i.e. $\alpha(\varepsilon)$ decreases from 20° at $\varepsilon=0$ to 5° at ε_{max} . Finally, the azimuthal angle, ϕ_S , is chose from a distribution uniform over the range $0<\phi_S<2\pi$.

5.3 Spatial distribution

The x and y distributions at production are assumed to be independent and Gaussianly distributed with a standard deviation given by the radius of the laser spot focused on the target.

5.4 Simulated distributions

Distributions 10^6 protons produced by the TNSA mechanism using the algorithm described above are shown in figure 4. The parameters used in the algorithm are presented in table 2. The generated distribution of kinetic energy is in good agreement with the distribution implied by equation 44. The width of the generated polar-angle distribution is observed to fall with kinetic energy and the kinetic-energy dependence of the RMS calculated from the generated particles is in good agreement with that expected from equation 55. As a result, the distribution of θ_S is approximately Gaussian with a width dominated by the contribution of protons with kinetic energy close to ε_{\min} . The generated ϕ_S distribution is flat in the range $0^\circ < \phi_S < 360^\circ$ and the (x,y) distribution is Gaussian in both the x and y projections.

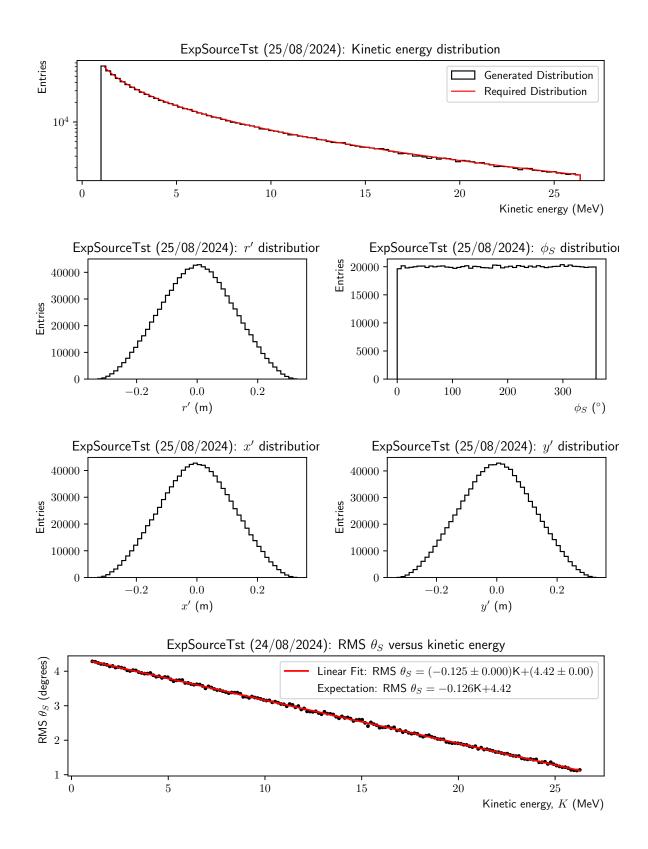


Figure 3: Kinematic distributions of particles at the point of production. <u>Top</u>: The generated kinetic energy disribution is shown as the solid histogram. The required distribution (equation 44), normalised to the lowest kinetic-energy bin, is shown as the solid red line. <u>Second row</u>: Generated r' and ϕ_S distributions. <u>Third row</u>: Generated x' and y' distributions. <u>Bottom</u>: RMS of the θ_S distribution versus kinetic energy. The solid circles are calculated using slices of width 0.15 MeV. The red line shows the result of a straight line fit to the data. The expected dependence from integration of equation 55 is presented in the legend.

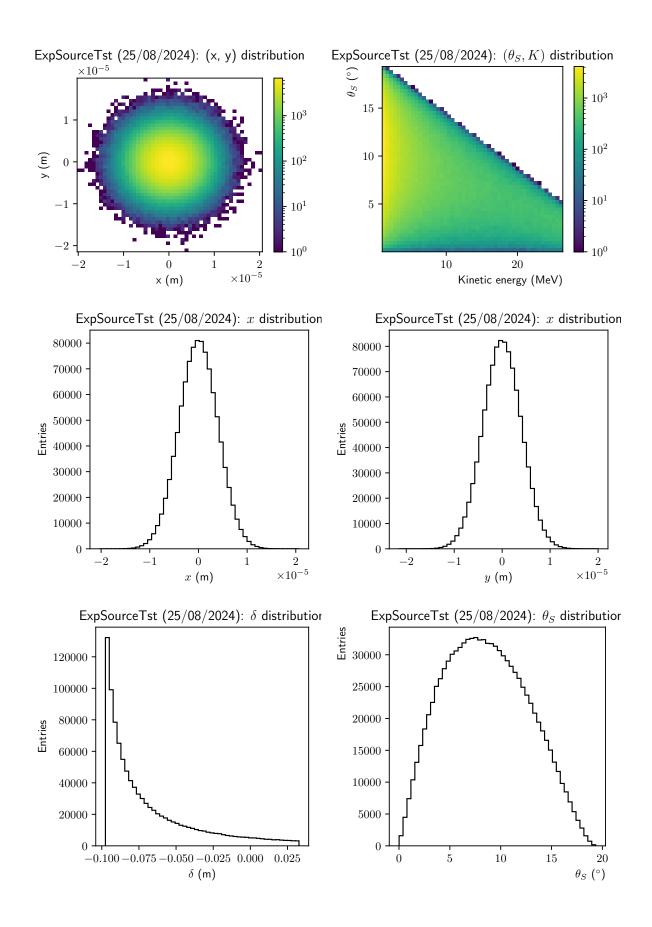


Figure 4: Top left: Generated (x, y) distribution of the particle-production point. Top right: The distribution of θ_S versus kinetic energy. Centre left, right: Generated distributions of x' and y'. Bottom left: Generated distribution of δ . Bottom right: Generated distribution of θ_S .

6 Beam-line specification and scripts

6.1 Beam-line specification

The specification is defined in the form of a parameter table. The table is loaded using a plain text file in CSV format. An example, specifying the PoPLaR beam line is shown in table 3. The simplest way to generate the CSV file is to use Excel to manipulate one of the examples provided in the 11-Parameters directory of the LinearOptics package. The parameter table is organised in 8 columns:

Stage: (integer) allows stages in the beam line to be defined. The number is arbitrary and is used only in the generation of a unique name for each element. Stage can be defined for clarity in labelling and presentation.

Section: (string) allows sections in the beam line to be distinguished. As in the case of Stage, Section may be defined for clarity and convenience. Section is used in the generation of the unique name of a particular element of the beam line.

Element: (string) indicates that the line will define one parameter for the particular beam-line element "Element'". Each beam-line element defined in appendix ?? is specified by a series of consecutive lines, each line defining one of the parameters that specifies the element. The lines required to specify each element are given in appendix ??.

Type: (string) specifies the type of Element that is to be used. For example, an Aperture along the beam line may be circular, elliptical, or rectangular. The Type keyword allows the required "type" of a particular beam-line element to be specified.

Parameter: (string) defines the parameter the value of which is specified by the line. For example, the length of an element is specified by setting the Parameter field to "Length".

Value: (float, integer) value of parameter.

Unit: (string) unit for parameter. Presently the code does not require Unit to be specified, it is included to record the unit of the value.

Comment: (string) free format comment.

The beam line is built by reading the file sequentially from the top. After the header fields, the first lines specify the Facility, giving its Name, the kinetic energy of the reference particle and radius of the "mother volume". The mother volume is a cylinder around the beam line, a particle hitting the boundary of the cylindrical volume is not propagated further along the beam line. The lines which follow specify each element of the beam line in turn, grouping them by Stage and Section as required.

295 **6.2 Scripts**

275

280

285

290

300

305

Scripts to perform common tasks are provided in the 03-Scripts directory. The scripts and the tasks they perform are;

runBeamSim.py -b <beamlinefile> -i <inputfile> -o <outputfile> -n <nEvts> uses the beam line specified in <beamlinefile> to generate <nEvts> and propagate them down the beam line. The output is written to <outputfile> in the format defined in the BeamIO class. If specified, <inputfile> is a BeamIO data file. In this case, beam transport starts from the most downstream element of the beam line defined in <inputfile>. Only one of <beamlinefile> and <inputfile> may be specified.

readBeamSim.py -i <inputfile> -o <outputfile> -n <nEvts>
reads <nEvts> events from the BeamIO-format data file <inputfile>. Two PDF files are written to 99-Scratch. The first, ParticleProgressionPlot.pdf, contains plots of the transverse trace space coordinates of the particles at the exit of each beamm line element. The second,

Table 3: Example beam-line specification file in Excel (xlsx) format.

| Stage | Section | Element | Туре | Parameter | Value | Unit | Comment |
|-------|----------|----------|--------------------|----------------------|-------------|---------|---|
| 0 | Facility | Global | Name | Name | PoPLaR | | |
| 0 | Facility | Global | Reference particle | Kinetic energy | 10 | MeV | |
| 0 | Facility | Global | Vacuum chamber | Mother volume radius | 0.5 | m | |
| 1 | Source | Source | Parameterised TNSA | SourceMode | 0 | | Mode |
| 1 | Source | Source | Parameterised TNSA | SigmaX | 0.000004 | m | Gaussian width, x |
| 1 | Source | Source | Parameterised TNSA | SigmaY | 0.000004 | m | Gaussian width, y |
| 1 | Source | Source | Parameterised TNSA | Emin | 1 | MeV | Minimum of energy distribution |
| 1 | Source | Source | Parameterised TNSA | Emax | 25 | MeV | Maximum of energy distribution |
| 1 | Source | Source | Parameterised TNSA | nPnts | 1000 | | Number of points to sample for integration of PDF |
| 1 | Source | Source | Parameterised TNSA | MinCTheta | 0.999691155 | | Maximum theta for flat cos theta |
| 1 | Source | Source | Parameterised TNSA | Power | 2.5E+15 | W | Laser power |
| 1 | Source | Source | Parameterised TNSA | Energy | 70 | J | Laser energy |
| 1 | Source | Source | Parameterised TNSA | Wavelength | 0.8 | um | Laser wavelength |
| 1 | Source | Source | Parameterised TNSA | Duration | 2.80E-14 | s | Laser pulse duration |
| 1 | Source | Source | Parameterised TNSA | Thickness | 0.0000004 | m | Target thickness |
| 1 | Source | Source | Parameterised TNSA | Intensity | 4.00E+20 | W/cm2 | Laser intensity |
| 1 | Source | Source | Parameterised TNSA | DivAngle | 25 | degrees | Electron divergence angle |
| 1 | Nozzle | Drift | | Length | 0.03 | m | |
| 1 | Nozzle | Aperture | Circular | Radius | 0.002 | m | |
| 1 | Nozzle | Drift | | Length | 0.003 | m | |
| 1 | Nozzle | Aperture | Circular | Radius | 0.002 | m | |
| 1 | Capture | Drift | | Length | 0.005 | m | |
| 1 | Capture | Aperture | Circular | Radius | 0.01 | m | |
| 1 | Capture | Fquad | | Length | 0.04 | m | |
| 1 | Capture | Fquad | | Strength | 150 | m | |
| 1 | Capture | Aperture | Circular | Radius | 0.01 | m | |
| 1 | Capture | Drift | | Length | 0.005 | m | |
| 1 | Capture | Aperture | Circular | Radius | 0.01 | m | |
| 1 | Capture | Dquad | | Length | 0.04 | m | |
| 1 | Capture | Dquad | | Strength | 150 | m | |
| 1 | Capture | Aperture | Circular | Radius | 0.01 | m | |
| 1 | Capture | Drift | | Length | 1.7 | m | |

ParticleLongiProgressionPlot.pdf, contains plots of the longitudina trace space coordinates of the particles at the exit of each beamm line element. The option -o <outputfile> has not yet been implemented.

310

315

325

calculates the covariance matrix of the trace-space coordinates at the exit from each vbean-line element and uses these covariance matrices to calculate the RMS beam size and Twiss parameters. A PDF file, BeamProgress.pdf, showing the evolution of these quantities along the is written to 99-Scratch. The calculations are performed on <nEvts> read from <inputfile>. If specified, a CSV file containing a summary of the beam evolution is written to <outputfile>. Optionally, if -1 is specified, the beam line evolution will be plotted from from location <startlocation>. The option -b

<br/

plotextrapolatedBeam.py -i <inputfile> -n <nEvts> -o <outputfile> -l <startlocation
[-b <beamlinefile>]

calculates the covariance matrix of the beam at location <startlocation> and then calculates the evolution of the covariance matrix and Twiss parameters using the beam-line element transfer matrices. The PDF file, extrapolatedBeamProgress.pdf, is created to contain plots of the beam evolution. If <startlocation> is not specified, the covariance matrix is calculated at the first element of the beam line and the propogation of the beam envelope starts at the beginning of the beam line. The

meaning of the other switches are as for plotBeam.py.

330

2BDSIM.py -i <inputfile> -o <outputfile> -l <start location> -n <nEvts> reads <nEvts> events from the BeamIO-format file <inputfile> and writes the ascii file <outputfile> in the format required by BDSIM. If specified, the BDSIM-format file is generated at location <start location>. If <start location> is not specified, the BDSIM-format is created with particles at the end of the beam line.

References

340

350

- [1] G. Aymar, T. Becker, *et al.*, "LhARA: The Laser-hybrid Accelerator for Radiobiological Applications," *Frontiers in Physics* **8** (2020) .
 - https://www.frontiersin.org/articles/10.3389/fphy.2020.567738.
 - [2] The LhARA consortium, "The Laser-hybrid Accelerator for Radiobiological Applications," Tech. Rep. CCAP-TN-01, The Centre for the Clinical Application of Particles, Imperial College London, 2020. https://ccap.hep.ph.ic.ac.uk/trac/raw-attachment/wiki/Communication/Notes/CCAP-TN-01.pdf.
 - [3] The LhARA collaboration, "Baseline for the LhARA design update," Tech. Rep. CCAP-TN-11, The Centre for the Clinical Application of Particles, Imperial College London, 2022.

 https://ccap.hep.ph.ic.ac.uk/trac/raw-attachment/wiki/Communication/Notes/CCAP-TN-11-LhARA-Design-Baseline.pdf.
- ³⁴⁵ [4] A. Wolski, *Beam dynamics in high energy particle accelerators*. Imperial College Press, 57 Shelton Street, Covent Garden, London WC2H 9HE, 2014.
 - [5] J. Fuchs, P. Antici, *et al.*, "Laser-driven proton scaling laws and new paths towards energy increase," *Nature Physics* **2** (01, 2006) .
 - [6] J. Schreiber, F. Bell, *et al.*, "Analytical Model for Ion Acceleration by High-Intensity Laser Pulses," *Physical review letters* **97** (08, 2006) 045005.
 - [7] F. Nürnberg, M. Schollmeier, et al., "Radiochromic film imaging spectroscopy of laser-accelerated proton beams," Review of Scientific Instruments 80 no. 3, (03, 2009) 033301, https://pubs.aip.org/aip/rsi/article-pdf/doi/10.1063/1.3086424/13601448/033301_1

https://doi.org/10.1063/1.3086424.

55 A Module, class and data structures

360

365

The linear optics package has been written in object-oriented Python and is broken down in four principal modules:

- BeamLineElement: provides the various beam-line elements required to build a description of the beam line. Each individual element, such as a drift, quadrupole, etc., is described in a class derived from the BeamLineElement parent class.
- <u>BeamLine</u>: provides code to assemble the elements into a coherent beam line. BeamLine is a singleton class to ensure that two beam lines can not be simulated in a single run of the package. The extrapolateBeam class is derived from the Beam class to handle the propagation of beam envelopes without the need to track individual particles.
- <u>Beam:</u> provides code to calculate ensemble properties of the beam such as emittance. The ensemble properties are stored as instance attributes of the Beam class.
- <u>Particle</u>: provides code to record beam particles at positions along the beam line. The module provides the singleton ReferenceParticle class derived from the Particle class.

Other modules: BeamIO, LaTeX, PhysicalConstants, Report, Simulation, UserFramework, and Visualise support the principal modules or provide services. The data structure is implemented as attributes of the instances of the various classes. This section describes the implementation of the various modules, the classes of which they are composed, and how access to the data is provided.

Each class has methods by which to access a list of the class instances and a Boolean flag by which to generate debug print out (see table 4).

Table 4: Methods by which to set and access class attributes.

| Method | Argument | Return | Comment |
|-----------------|----------|----------------------------|---|
| getinstances() | | List of instances of class | For singleton classes such as BeamLine, |
| | | | getinstances () returns a single instance |
| | | | rather than a list. |
| setDebug(Debug) | Boolean | | Sets flag to generate debug print-out |
| getDebug() | | Boolean debug flag | If True, generate debug print-out |
| setAll2None() | | | Set all instance attributes to None at start of |
| | | | instantiation. |
| SummaryStr() | | String | Text sring to record parameters in debug print |
| | | | out. |

375 A.1 BeamLine

BeamLine is a singleton class that sets up the beam line geometry and provides methods to track particles through the beam line using the transfer matarices defined in section A.4. The beam-line geometry is provided in the form of a "csv" file read using pandas. The format of the "csv" file is defined in section ??. Alternatively, if a data file written using the BeamIO package is being read, the beam-line geometry is read from the top of the data file. The instance of the BeamLine class is created when the first record of the data file is read.

A.1.1 Instantiation

The call to instantiate the BeamLineElenent class is:

BeamLine (BeamLineSpecificationCSVfile, readDataFile)

BeamLineSpecificationCSVfile is a the full path of the CSV file containing the beam-line specification. readDataFile is a boolean flag. If readDataFile is set to True, then the BeamLine instance will be created and the beam-line geometry will be read from the header of the BeamIO data file. If readDataFile is not set or is set to False, the beam-line geometry will be read from BeamLineSpecificationCSVfile.

A.1.2 Instance attributes and access methods

The instance attributes are presented in table 5 and the access methods are summarised in table 6.

Table 5: Definition of attributes of instances of the BeamLine class.

| Attribute | Type | Comment |
|-------------------------------|-----------|--|
| BeamLineSpecificationCSVfile* | path | Full path to beam-line specification csv file. |
| BeamLineParamPandasInstance | dataframe | Pandas data frame containing beam-line specification. |
| Element | list | List of instances of BeamLineElement class con- |
| | | taining pointers to the elements that make up the beam |
| | | line. |

A.1.3 Processing methods

Table 7 presents the processing methods provided in the BeamLine class.

A.1.4 I/o methods

Table 8 presents the i/o methods provided in the BeamLine class.

A.1.5 Utilities

400

Table 9 presents the utilities provided in the ${\tt BeamLine}$ class.

Table 6: Definition of access methods for the BeamLine class.

| Set method | Get method | Comment |
|-------------------------|---|--|
| setSrcTrcSpc(SrcTrcSpc) | <pre>getSrcTrcSpc()</pre> | Set trace space at source; SrcTrcSpc presented as (1, 6) |
| | | np.ndarray. |
| | getinsance() | Get instance of BeamLine class. |
| | <pre>BeamLineSpecificationCSVfile()</pre> | Get beam line specification csv file. |
| | (getBeamLineParamPandas) | Get pandas dat from containing beam-line specification. |
| | <pre>getElement()</pre> | get list of BeamLineElement instances. |

Table 7: Processing methods provided by the BeamLine class.

| Method | Argument(s) | Return | Comment |
|---------------------------------|-------------|-------------------|---|
| addBeamLine() | | Success | Loops through pandas data frame and manages parsing and in- |
| | | | stanciation of the beam line elements defined in the specification |
| | | | csv file. Returns Success (bool) which is True if the beam- |
| | | | line has been set up OK and is False otherwise. |
| addFacility() | | | Manages the extraction of the facility parameters from the |
| | | | pandas data frame and the creation of the single instance of |
| | | | Facility(BeamLineElement). |
| addSource() | | | Manages the extraction of the source parameters from the pan- |
| | | | das data frame and the creation of the single instance of |
| | | | Source(BeamLineElement). |
| parseFacility() | | Name, KO, VCMVr | Parses pandas data frane to extract facility parameters. Returns |
| | | | the facility Name (str), the kinetic energy of the reference parti- |
| | | | cle, K0 (float) in MeV, and the vacuum chamber mother volume |
| | | | radius, VCMVr (float) in m. |
| parseSource() | | Name, Mode, Param | Parses pandas data frane to extract source parameters. Returns |
| | | | Name (str), Mode (int) Param (list) containing the parameters |
| | | | required to instanciate source Mode. |
| addBeamLineElement(iBLE) | | | Adds BeamLineElement instance iBLE to the list of in- |
| | | | stances of BeamLineElement that make up the beam line. |
| checkConsistency() | | Consistent | Checks the consistency of the beam line representation in mem- |
| | | | ory with that requested in the specification csv file. Returns |
| | | | Consistent (bool) which is True if the beamline is consis- |
| | | | tent is False otherwise. |
| trackBeamn(NEvts, particleFILE) | | | Generates NEvts (int) particles and tracks them through the |
| | | | beam line. |

 $Table \ 8: \ I/o \ methods \ provided \ by \ the \ \texttt{BeamLine} \ class.$

| Method | Argument(s) | Return | Comment |
|---------------------|-------------|------------------|--|
| csv2pandas(csvFILE) | Path | pandas dataframe | Read CSV file to create pandas data frame. |
| | | | csvFILE (path) is the full path to the csv |
| pandasBeamLine() | | pandas dataframe | Create pandas dataframe from BeamLine |
| | | | instance. |
| getHeader() | | List | Prepares list of header fields for |
| | | | pandasBeamLine. |
| readBeamLine(file) | Path | Boolean | Called from BeamIO. Reads BeamLine |
| | | | from data file. |

 $Table \ 9: \ Utilities \ provided \ by \ the \ \texttt{BeamLine} \ class.$

| Method | Argument(s) | Return | Comment |
|-----------------|-------------|--------|-------------------------------------|
| cleaninstance() | | | Remove BeamLine instance. |
| fixsz() | | List | Loop through BeamLineElement in- |
| | | | stances to set s and z at exit. |

A.2 Particle and ReferenceParticle

The Particle class provides methods to transport particles through the beam line. The trace and phase space is recorded at the start and end of each element. The ReferenceParticle derived class is a singleton and records the trajectory of the reference particle.

A.2.1 Particle

A.2.1.1 Instantiation

The call to instantiate the Particle class is:

Particle (Species)

Species, the type of particle to be propagated, is a string containing the particle name. At present valid particle species are proton, pion, and muon.

A.2.1.2 Instance attributes and access methods

The instance attributes are presented in table 10 and the access methods are summarised in table 11.

Table 10: Definition of attributes of instances of the Particle class.

| Attribute | Type | Comment |
|---------------|------|---|
| Species | str | Particle species; proton, muon or pion. |
| Location | list | List of strings containing the unique Name of the BeamLineElement at the |
| | | particle position is reported. |
| S | list | List of floats recording s coordinate at which particle position is reported. |
| TraceSpace | list | List of np.ndarray containing 6D trace space of particle at s. |
| PhaseSpace | list | List of np.ndarray containing 6D phase space (RPLC) of particle at s. |
| LabPhaseSpace | list | List of np.ndarray containing 6D phase space (Lab) of particle at s. |

415

A.2.1.3 Processing methods

Table 12 presents the processing methods provided in the Particle class.

A.2.1.4 I/o methods

The i/o methods provided by the Particle class are listed in table 13.

A.2.1.5 Utilities

The utilities provided by the Particle class are listed in table 14.

Table 11: Definition of access methods for the Particle class.

| Sets TrcSpc=trace space at source. | | setSourceTraceSpace(TrcSpc) |
|---|-------------------|-----------------------------------|
| z=z, $s=s$, and TrcSpc=trace space. | | |
| Records particle attributes. Arguments: Loc=Location, | | recordParticle(Loc, z, s, TrcSpc) |
| cle as firt instance in the list. | | |
| Resets list of particle instances preserving reference parti- | | resetParticleInstances |
| Set/get list of phase-space vectirs in Lab coordinates. | getLabPhaseSpace | setLabPhaseSpace |
| Set/get list of phase-space vectirs in RPLC coordinates. | setRPLCPhaseSpace | setRPLCPhaseSpace |
| Set/get list of trace-space vectors. | getTraceSpace | setTraceSpace |
| Set/get list of s coordinates. | gets | sets |
| Set/get list of locations location. | getLocation | setLocation |
| Set/get particle species. | getSpecies | setSpecies |
| Comment | Get method | Set method |
| | | |

Table 12: Processing methods provided by the ${\tt Particle}$ class.

| Method | Argument(s) | Return | Comment |
|-----------------------------------|-------------------|------------|---|
| fillPhaseSpaceAll() | | Boolean | Fill phase space for all Particle instances. Class Method. Re- |
| | | | turn True if successful. |
| fillPhaseSpace() | | Boolean | Fill phase space for current Particle instance. Return True |
| | | | if successful. |
| initialiseSums() | | | Initialises sums used to calculate covariance matrix. |
| incrementSums (iPrtcl) | Particle instance | | Increment sums used to calculate covariance matrix. |
| calcCovarianceMatrix() | | | Calculate covariance matrix. |
| evaluateBeam() | | | Work through locations and calculate parameters from covariance |
| | | | matrix. |
| calcRPLCPhaseSpace(nLoc) | Int | np.ndarray | Calculate and return phase space in RPLCs at location nLoc. |
| RPLCTraceSpace2PhaseSpace(TrcSpc) | np.ndarray | np.ndarray | Transform trace space to phase space in RPLCs. |
| RPLCPhaseSpace2TraceSpace(TrcSpc) | np.ndarray | np.ndarray | Transform phase space to trace space in RPLCs. |

Table 13: Wo methods provided by the Particle class.

| Method | Argument(s) | Return | Comment |
|--|------------------------|---------|---|
| createParticleFile(path, file) | Path, Str | Path | Class method, kept for backward compatibility. |
| flushNcloseParticleFile(file) | Path | | Class method, kept for backward compatibility. |
| openParticleFile(path, file) | Path, Str | | Class method, kept for backward compatibility. |
| <pre>closeParticleFile(path, file)</pre> | Path, Str | | Class method, kept for backward compatibility. |
| readParticle(file) | Path | Boolean | Read particle from input stream. Called from BeamIO. file is |
| | | | full path to file. Return True if end of file. |
| writeParticle(file, clean) | Path, boolean | | Write particle to output stream. file is full path to file. If |
| | | | clean, then clean particle instance after write. |
| writeParticleBDSIM(file, iLoc, clean) | Path, integer, boolean | | Write particle to BDSIM ascii file. file is full path to file. iLoc |
| | | | is the location along the beamm line at which to write the particle |
| | | | coordinates. If clean, then clean particle instance after write. |
| | | | |

Table 14: Utilities provided by the Particle class.

| Method | Argument(s) Return Comment | Return | Comment | | | | |
|---|--------------------------------|--------|----------------------|-------------|--|------------------|------------|
| cleanAllParticles() | | | Delete | all | Particle | instances | including |
| | | | ReferenceParticle. | cePart | icle. | | |
| cleanParticles() | | | Delete | al1 | Particle | instances | except |
| | | | ReferenceParticle. | cePart | icle. | | |
| plotTraceSpaceProgression() | | | Plot transv | erse trace | Plot transverse trace space at each location. Class method. Writes | tion. Class meth | od. Writes |
| | | | file to 99-Scratch/. | Scratc | h/. | | |
| plotLongitudinalTraceSpaceProgression() | | | Plot longi | tudinal tr | Plot longitudinal trace space at each location. Class method. | location. Clas | s method. |
| | | | Writes file | to 99-S | Writes file to 99-Scratch/. | | |
| printProgression() | | | Print parti | cle param | Print particle parameters at each location. | ion. | |
| <pre>getLines()</pre> | | | Returns lir | ies to be u | Returns lines to be used to create summary pandas data frame. | mary pandas dat | a frame. |
| createReport() | | | Creates CS | s∨ file cor | Creates csv file containing summary of beam progression. | of beam progres | sion. |

A.2.2 ReferenceParticle

425 A.2.2.1 Instantiation

ReferenceParticle is a singleton derived class. The call to instantiate the ReferenceParticle class is:

ReferenceParticle(Species)

Species, the type of particle to be propagated, is a string containing the particle name. At present valid particle species are proton, pion, and muon.

A.2.2.2 Instance attributes and access methods

In addition to the instance attributes inheritted from the parent class, the ReferenceParticle class provides the instance attributes presented in table 15 and the access methods are summarised in table 16.

Table 15: Definition of attributes of instances of the ReferenceParticle class.

| Attribute | Type | Comment |
|---------------|------|---|
| _sIn[] | list | List of floats containing the s coordinates at the entrance to the beam line |
| | | elements along the locus of the reference particle trajectory. |
| _sOut[] | list | List of floats containing the s coordinates at the exit to the beam line elements |
| | | along the locus of the reference particle trajectory. |
| _RrIn[] | list | List of ndarrays containing the four-vector position in laboratory coordinates at |
| | | the entrance to the beam line elements along the locus of the reference particle |
| | | trajectory. |
| _RrOut[] | list | List of ndarrays containing the four-vector position in laboratory coordinates |
| | | at the exit to the beam line elements along the locus of the reference particle |
| | | trajectory. |
| _PrIn[] | list | List of ndarrays containing the four-vector momentum in laboratory coordi- |
| | | nates at the entrance to the beam line elements along the locus of the reference |
| | | particle trajectory. |
| _PrOut[] | list | List of ndarrays containing the four-vector momentum in laboratory coordi- |
| | | nates at the exit to the beam line elements along the locus of the reference |
| | | particle trajectory. |
| _Rot2LabIn[] | list | List of ndarrays containing the rotation matrices taking RPLC to laboratory |
| | | coordinates at the entrance to the beam line elements along the locus of the |
| | | reference particle trajectory. |
| _Rot2LabOut[] | list | List of ndarrays containing the rotation matrices taking RPLC to laboratory |
| | | coordinates at the exit to the beam line elements along the locus of the refer- |
| | | ence particle trajectory. |

Table 16: Definition of access methods for the ReferenceParticle class.

| Set method | Get method | Comment |
|---------------|----------------------|---|
| setRPDebug | getRPDebug | Set/get ReferenceParticle debug flag. |
| setsIn | getsIn | Set/get _sIn |
| setsOut | getsOut | Set/get _sOut |
| setRrIn | getRrIn | Set/get _RrIn |
| setRrOut | getRrOut | Set/get _RrOut |
| setPrIn | getPrIn | Set/get _PrIn |
| setPrOut | getPr0ut | Set/get _PrOut |
| | getMomentumIn(iLoc) | Get magnitude of three-vector momentum at |
| | | entrance of location iLoc |
| | getMomentumOut(iLoc) | Get magnitude of three-vector momentum at |
| | | exit of location iLoc |
| setRot2LabIn | getRot2LabIn | Set/get_Rot2LabIn |
| setRot2LabOut | getRot2LabOut | Set/get_Rot2LabOut |
| | getb0(iLoc) | Get β_0 . |
| | getg0b0(iLoc) | Get $\gamma_0\beta_0$. |
| setAllRP2None | | Set all ReferenceParticle attributes to |
| | | None. |

Table 17: Processing methods provided by the ReferenceParticle class.

| Method | Argument(s) | Return | Comment |
|-----------------------------------|-------------|---------|---------------------------|
| setReferenceParticleAtSource() | | boolean | Set |
| | | | ReferenceParticle |
| | | | attributes at source. Re- |
| | | | turns True if success. |
| setReferenceParticleAtDrift(iBLE) | BLE | boolean | Set |
| | | | ReferenceParticle |
| | | | attributes at |
| | | | BeamLineElement |
| | | | (BLE) instance iBLE. |
| | | | Returns True if success. |

A.2.2.3 Processing methods

Table 17 presents the processing methods provided in the ReferenceParticle class.

A.2.2.4 I/o methods

The $\ensuremath{\mathsf{ReferenceParticle}}$ class provides no additional i/o methods.

A.2.2.5 Utilities

The ReferenceParticle class provides no additional utilities.

440 A.3 Beam and extrapolateBeam

The Beam class is in some sense a "sister" class to Particle. Whereas an instance of Particle records the passage of a particle travelling through the beam line, an instance of Beam records the collective properties of the beam such as emittance, as the beam progresses through the beam line. The beam parameters reported in the attributes of an instance of Beam are obtained by summing over nEvtsMax particles to evaluate the covariance matrices by location.

The extrapolatedBeam class is derived from Beam. An instance of extrapolatedBeam calculates the covariance matrix at a location along the beam line and then uses the transfer matrices to propagate the beam envelope.

A.3.1 Beam

50 A.3.1.1 Instantiation

The call to instantiate the Beam class is:

InputDatafile is either the full path to a data file in one of the formats specified in BeamIO or an instance of the BeamIO class that refers to an existing data file that can be read. nEvtMax is the maximum number of events to read or process using the Beam instance. outputCSVfile is the full path to the output file, in CSV format, contining the beam parameters at the locations traversed by the beam. startlocation is the location along the beam line at which propagation will start; if startlocation is absent or None propagation will start at the source. beamlineSpecificationCSVfile is the CSV file specifying the beam line.

beamlineSpecificationCSVfile is kept for backward compatibilty. If the first record of InputDatafile contains the specification of the beam line, beamlineSpecificationCSVfile is not required.

A.3.1.2 Instance attributes and access methods

The instance attributes are presented in table 18 and the access methods are summarised in table 19.

465 A.3.1.3 Processing methods

Table 20 presents the processing methods provided in the Beam class.

A.3.1.4 I/o methods

The Beam class has no i/o methods.

A.3.1.5 Utilities

The utilities provided by the Beam class are listed in table 21.

Table 18: Definition of attributes of instances of the Beam class.

| Attribute | Type | Comment |
|-------------------------------|-------------|--|
| InputDataFile | Path/BeamIO | Path to, or BeamIO instance of input file. |
| nEvtMax | int | Maximum number of particles to read and process. |
| outputCSVfile | Path | Path to output CSV file to contain beam parmeters by location. |
| startlocation | int | Location at which to start beam propagation. |
| BLspecCSVfile | Path | beamlineSpecificationCSVfile, kept for backward compatibility. |
| Location[iLoc] | List | List of locations (int) at which beam parameters are recorded. |
| s[iLoc] | List | List of s coordinates of reference particle at locations at which beam parame- |
| | | ters are recorded. |
| nParticles[iLoc] | List | List of number of particles (int) recorded at location iLoc. |
| CovMtrx[iLoc][6,6] | List | List of covariance matrices (ndarray) by location. |
| <pre>sigmaxy[iLoc][2]</pre> | List | List of $\sigma_x = \text{sigmaxy[iLoc][0]}$ and $\sigma_y = \text{sigmaxy[iLoc][1]}$ |
| | | (float). |
| <pre>emittance[iLoc][5]</pre> | List | List of emittance by location: $\epsilon_x = \texttt{emittance[iLoc][0]}, \; \epsilon_y =$ |
| | | emittance[iLoc][1], ϵ_{L} = emittance[iLoc][2], ϵ_{4D} = |
| | | emittance[iLoc][3], $\epsilon_{6D}=$ emittance[iLoc][4]. |
| Twiss[iLoc][2][3] | List | List of Twiss parameters by location: Twiss[iLoc][0][0:2] = |
| | | $[lpha_x,eta_x,\gamma_x]$, Twiss[iLoc][1][0:2] $= [lpha_y,eta_y,\gamma_y]$. |

Table 19: Definition of access methods for the Beam class.

| | Get method | Comment |
|--------------------------------------|---------------------------------|---|
| setInputDataFile | getInputDataFile | Set path to input file. |
| setBeamIOread | getBeamIOread | Set instance of BeamIO for input file. |
| setnEvtMax | getnEvtMax | Set maximum number of particles to deal with. |
| setoutputCSVfile | getoutputCSVfile | Set pathh to output CSV file. |
| setstartlocation | getstartlocation | Set start location. |
| setbeamlineSpecificationCSVfile g@ | getbeamlineSpecificationCSVfile | Set beam line specification file. |
| sets | sets | Set s by location. |
| setsigmaxy | setsigmaxy | Set $\sigma_{x,y}$ by location. |
| setEmittance | setEmittance | Set emittance list by location. |
| setTwiss | setTwiss | Set Twiss paramter list by location. |
| resetBeamInstances | | Set list of beam instances to []. |
| | getCovSums | Get list of sums used to calculate covariance matrices. |
| | getCovMtrx | Get list of covariance matrices by location. |
| | getnParticles | Get number of particles entering covariance sums by loca- |
| | | tion. |
| | getCovarianceMatrix | Get list of covariance matrices by location. |
| | getCovMtrx | Get list of covariance matrices by location. |

Table 20: Processing methods provided by the Beam class.

| Method | Argument(s) Return Comment | Return | Comment |
|-----------------------------------|--------------------------------|--------|--|
| initialiseSums() | | | Initialise sums to be used to calculate covariance matrices by lo- |
| | | | cation. |
| <pre>incfementSums(iPrtcl)</pre> | Particle | | Increment sums for covariance matrix calculation for Particle |
| | | | instance iPrtcl. |
| <pre>calcCovarianceMatrix()</pre> | | | Calculate covariance matrices by location. |
| evaluateBeam(TrackBeam=False) | boolean | | Loop over nEvtMax partices to calculate beam parameters by lo- |
| | | | cation. If TrackBeam is True, particles are transported through |
| | | | the beam line. If TrackBeam is False, covariance matrices |
| | | | stored as Beam instance attributes are used. |

Table 21: Utilities provided by the Beam class.

| Method | Argument(s) Return Comment | Return | Comment |
|-------------------------------|--------------------------------|---------|--|
| cleanBeams() | | boolean | boolean Delete all Beam instances, returns True if successful. |
| printProgression() | | | Print beam parameters by location. |
| getHeader() | | list | Prepare header for CSV file containing beam parameters by loca- |
| | | | tion. |
| <pre>getLines()</pre> | | list | Prepare lines for CSV file containing beam parameters by loca- |
| | | | tion. |
| createReport() | | | Interface to Report class to make beam paramter CSV file. |
| plotBeamProgression(plotFILE) | | path | Plot beam parameters by location; plotFILE is full path to plot |
| | | | file. |

A.3.2 extrapolateBeam

A.3.2.1 Instantiation

475

The call to instantiate the extrapolateBeam class is:

The arguments are passed directly to a call to instantiate the parent Beam class. In the execution of extrapolateBeam, the covariance matrices are calculated from nEvtMax at startlocation. If startlocation, the last location provided in the input data file is used as the source.

A.3.2.2 Instance attributes and access methods

Instance attributes are inheritted from Beam (table 18). Access methods are also inheritted from Beam (table 19). The method resetextrapolateBeamInstances is provided to reset only the list of instances of extrapolateBeam.

A.3.2.3 Processing methods

Table 22 presents the processing methods provided in the extrapolateBeam class.

Table 22: Processing methods provided by the extrapolateBeam class.

| Method | Argument(s) | Return | Comment |
|-------------------------------|-------------|--------|----------------------------------|
| initialiseSums() | | | Initialise sums to be used to |
| | | | calculate covariance matrices at |
| | | | startlocation. |
| incfementSums(iPrtcl) | Particle | | Increment sums for covari- |
| | | | ance matrix calculation for |
| | | | Particle instance iPrtcl |
| | | | at startlocation. |
| extrapolateCovarianceMatrix() | | | Extrapolate covariance matrices |
| | | | along the beam line by location. |
| extrapolateBeam() | | | Estrapolate beam envelope and |
| | | | beam parameters along the beam |
| | | | line by location. |

485 **A.3.2.4 I/o** methods

The extrapolateBeam class has no i/o methods.

A.3.2.5 Utilities

The utilities provided by the extrapolateBeam class are listed in table 23.

Table 23: Utilities provided by the extrapolateBeam class.

| Method | Argument(s) | Return | Comment |
|-------------------------|-------------|---------|--------------------------------------|
| cleanextrapolateBeams() | | boolean | Delete all extrapolateBeam in- |
| | | | stances, returns True if successful. |

A.4 BeamLineElement

A.4.1 Parent class

A.4.1.1 Instantiation

The call to instantiate the BeamLineElenent class is:

BeamLineElement (Name, rStrt, vStrt, drStrt, dvStrt)

where:

500

Name: (string) is the unique name of the element;

rStrt: (numpy.ndarray(3)) is the three-vector position in laboratory coordinates of the start of the element;

vStrt: (numpy.ndarray(1,2)) is the polar, θ , and azimuthal, ϕ , angles that define the y (i = 0) and z (i = 1) axes of the RPLC coordinate system at the start of the element (vStrt = $[[i], [\theta, \phi]]$);

drStrt: (numpy.ndarray(3)) error in the three-vector position with respect to the nominal position; and

dvStrt: (numpy.ndarray(1,2)) error in the polar and azimuthal angles defining RLPC the y and z axes.

All arguments are required.

A.4.1.2 Instance attributes and access methods

Properties common to all beam-line elements are stored as instance attributes of the parent BeamLineElement class. The instance attributes are defined in table 24. The attributes are accessed and set using the methods defined in table 25.

A.4.1.3 Processing methods

Table 26 presents the processing methods provided in the BeamLineElement class.

A.4.1.4 I/o methods

Methods to read and write instance attributes to the files defined using the BeamIO package (see section ?? are provided. The calls are:

```
readElement(dataFILE) and writeElement(dataFILE);
```

where dataFILE is BeamIO instance.

A.4.1.5 Utilities

Table 27 presents the utilities provided in the BeamLineElement class.

Table 24: Definition of attributes of instances of the BeamLineElement class. The attributes marked * above the dividing line are required in the call to instantiate the element. The attributes marked † below the dividing line are calculated.

| Attribute | Type | Unit | Comment |
|-------------------------|---------------|------|--|
| Name* | String | | Name of beam-line element. |
| rStrt* | numpy.ndarray | m | [x, y, z] position of entrance to element in laboratory coordinate |
| | | | system. |
| vStrt* | numpy.ndarray | rad | $[[i], [\theta, \phi]]$ (polar and azimuthal angles) of RPLC y and z axes |
| | | | (i = 0, 1 respectively) at start. |
| drStrt* | numpy.ndarray | m | "Error", $[x, y, z]$, displacement of start from nominal position |
| | | | (not yet implemented). |
| dvStrt* | numpy.ndarray | rad | "Error", $[[i], [\theta, \phi]]$, deviation in θ and ϕ from nominal axis (not |
| | | | yet implemented). |
| Strt2End [†] | numpy.ndarray | | 1×3 translation from start of element to end; in laboratory |
| | | | coordinates. Set in derived class. |
| Rot2LbStrt [†] | numpy.ndarray | | 3×3 rotation matrix that takes RPLC axes to laboratory axes |
| | | | at start. |
| Rot2LbEnd [†] | numpy.ndarray | | 3×3 rotation matrix that takes RPLC axes to laboratory axes |
| | | | at end. Set in derived class. |
| TnrsMtrx [†] | numpy.ndarray | | 3×3 transfer matrix. Set in derived class. |

Table 25: Definition of access methods for the BeamLineElement class.

| Comment | Set/get name of beam-line element. | Set/get laboratory $[x, y, z]$ position of entrance. | Set/get RPLC $[\theta, \phi]$ of principal axis at start of element. | Set/get RPLC $[\theta, \phi]$ of principal axis at end of element. | Set/get "error" displacement. | Set/get "error" deviation in $[\theta, \phi]$. | Set/get increment in s across element, (length for elements that | do not bend beam). | Set/get rotation matrix from RPLC axes to laboratory. | Setget rotation matrix from RPLC to laboratory at start. | Set/get displacement vector start to end in laboratory coordinates. | setStrt2End takes 1 argument, t, a 1D np.ndarray containing the | translation from the start to the end of the element in RPLC. | Set/get rotation matrix from RPLC to laboratory at end. | setRot2LbEnd takes 1 argument, R, a 2D np.array containing the | rotation matrix to be set. | Get transfer matrix set in derived class. | Get lines to write LaTeX specification of element. |
|------------|------------------------------------|--|--|--|-------------------------------|---|--|--------------------|---|--|---|---|---|---|--|----------------------------|---|--|
| Get method | getName() | getrStrt() | getvStrt() | getvEnd() | <pre>getdrStrt()</pre> | getdvStrt() | getLength | | <pre>getRot2LbStrt()</pre> | <pre>getRot2LbStrt()</pre> | <pre>getStrt2End()</pre> | | | getRot2LbEnd() | | | <pre>getTransferMatrix()</pre> | getLines() |
| Set method | setName (Name) | setrStrt (rStrt) | setvStrt (vStrt) | | setdrStrt (drStrt) | setdvStrt (dvStrt) | setLength (length) | | setRot2LbStrt() | setRot2LabStrt() | setStrt2End(t) | | | setRot2LbEnd(R) | | | | |

Table 26: Processing methods provided by the BeamLineElement class.

| returned. | | | |
|--|-------------------------|-------------------------|---------------------------|
| space coordinates in the RPLC frame. Trace-space vector in RLPC frame | | | |
| 6×1 np.ndarray 6×1 np.ndarray Transform 6D phase-space vector, U, from laboratory coordinates to trace- | 6×1 np.ndarray | 6×1 np.ndarray | Shit2Laboratory(U) |
| Phase-space vector in laboratory frame returned. | | | |
| 6×1 np.ndarray $\mid 6 \times 1$ np.ndarray \mid Transform 6D trace-space vector, \vee , from RPLC to laboratory coordinates. | 6×1 np.ndarray | 6×1 np.ndarray | Shit2Local(V) |
| returned. | | | |
| 6×1 np.ndarray 6×1 np.ndarray Transport 6D trace-space vector, V , across element. Final trace-space vector | 6×1 np.ndarray | 6×1 np.ndarray | Transport (V) |
| rameter is large (> 1). Not yet used in Transport. | | | |
| Calculates an approximate expansion parameter and returns False if the pa- | Boolean | Float | ExpansionParameterFail(R) |
| in RPLC, falls outside beam pipe, returns True. | | | |
| Returns False if particle is inside beam pipe. If $\mathbb R$, radial distance from z axis | Boolean | Float | OutsideBeamPipe(R) |
| Comment | Return | Argument(s) | Method |

Table 27: Utilities provided by the BeamLineElement class.

| Method | Argument(s) | Return | Return Comment |
|--------------------------------|----------------------------------|--------|---|
| cleaninstances() | | | Delete (using "del") all instances of the BeamLineElement |
| | | | class. Reset instances list. |
| removeInstance(inst) | Instance of BLE | | Remove instance inst and remove from list of instances of |
| | | | BeamLineElement. |
| visualise(axs, CoordSys, Proj) | axs – MatPlotLib "axes" instance | | Manages plotting (visualisation) of element. |
| | CoordSys - string | | "Lab" or "RPLC", coordinate system in which to visualise ele- |
| | | | ment. |
| | Proj – string | | " xz " or " yz " projection to visualise. |

A.4.2 Derived class: Facility (BeamLineElement)

515 A.4.2.1 Instantiation

The call to instantiate the Facility derived class is:

FacilityName, rStrt, vStrt, drStrt, dvStrt, p0, VCMV)

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. The Facility arguments are translated into instance attributes as described in section A.4.2.2 and defined in table 28.

A.4.2.2 Instance attributes and access methods

The instance attributes are defined in table 28. The attributes are accessed and set using the methods defined in table 29.

Table 28: Definition of attributes of instances of the Facility (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|------|---|
| р0 | float | MeV | Kinetic energy of reference particle. |
| VCMV | float | m | Radius of vacuum-chamber mother volume. The radius defines |
| | | | edge of the volume at which a particle trajectory is terminated. It |
| | | | may be necessary to introduce a beam pipe later. |

Table 29: Definition of access methods for the Facility derived class.

| Set method | Get method | Comment |
|---------------|------------|--|
| setp0(Name) | getp0() | Set/get momentum of reference particle (in |
| | | MeV). |
| setVCMV(VCMV) | getrVCMV() | Set/get radius of vacuum chamber mother |
| | | volume. |

A.4.2.3 Processing methods

The Facility derived class has no processing methods other than those inheritted from the parent class.

A.4.2.4 I/o methods

The Facility derived class has no i/o methods other than those inheritted from the parent class.

A.4.2.5 Utilities

The Facility derived class has no utilities other than those inheritted from the parent class.

A.4.3 Derived class: Drift (BeamLineElement)

A.4.3.1 Instantiation

The call to instantiate the Drift derived class is:

```
Drift (Name, rStrt, vStrt, drStrt, dvStrt, Length)
```

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement.

A.4.3.2 Instance attributes and access methods

The instance attributes are defined in table 30. The attributes are accessed and set using the methods defined in table 31.

Table 30: Definition of attributes of instances of the Drift (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|------|------------------|
| Length | float | m | Length of drift. |

Table 31: Definition of access methods for the Facility derived class.

| Set method | Get method | Comment |
|--------------------------------|-------------|---------------------------------|
| setLength (Length) | getLength() | Set/get length of drift (in m). |
| <pre>setTransferMatrix()</pre> | | Set transfer matrix. |

A.4.3.3 Processing methods

The Drift derived class has no processing methods other than those inheritted from the parent class.

A.4.3.4 I/o methods

The Drift derived class has no i/o methods other than those inheritted from the parent class.

A.4.3.5 Utilities

The Drift derived class has no utilities other than those inheritted from the parent class.

A.4.4 Derived class: Aperture (BeamLineElement)

A.4.4.1 Instantiation

The call to instantiate the Aperture derived class is:

```
Aperture (Name, rStrt, vStrt, drStrt, dvStrt, ParamList)
```

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement.

A.4.4.2 Instance attributes and access methods

The instance attributes are defined in table 32. The attributes are accessed and set using the methods defined in table 34.

A.4.4.3 Processing methods

The Aperture processing method is defined in table 34.

Table 32: Definition of attributes of instances of the Aperture (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|--------------|-------|------|--|
| ParamList | [] | | List containing aperture parameters. The first parameter is an |
| | | | int and defines the aperture "Type". The remaining elements |
| | | | in the parameter list are floats with meanings that depend on |
| | | | Type. |
| ParamList[0] | int | | Type= 0; circular |
| ParamList[1] | float | m | Radius of circular aperture |
| ParamList[0] | int | | Type= 1; Elliptical |
| ParamList[1] | float | m | Radius of elliptical aperture along x_{RPLC} axis |
| ParamList[2] | float | m | Radius of elliptical aperture along y_{RPLC} axis |
| ParamList[0] | int | | Type= 2; Rectangular |
| ParamList[1] | float | m | Size of aperture along x_{RPLC} axis |
| ParamList[2] | float | m | Size of aperture along y_{RPLC} axis |

 $Table \ 33: \ Definition \ of \ access \ methods \ for \ the \ {\tt Aperture} \ derived \ class.$

| Set method | Get method | Comment |
|----------------------------------|-------------|--|
| setApertureParameters(ParamList) | | Set aperture parameters. Sets Type and pa- |
| | | rameters depending on Type. |
| | getType() | Get Type of aperture. |
| | getParams() | Get aperture parameters. |

Table 34: Utilities provided by the Aperture derived class.

| Method | Argument(s) | Return | Comment |
|---------------|-------------|--------------------|---|
| Transport (V) | np.ndarray | np.ndarray or None | Transport trace-space vector V. If V falls out- |
| | | | side of the aperture, return None. |

A.4.4.4 I/o methods

The Aperture derived class has no i/o methods other than those inheritted from the parent class.

A.4.4.5 Utilities

The Aperture derived class has no utilities other than those inheritted from the parent class.

A.4.5 Derived class: FocusQuadrupole (BeamLineElement)

A.4.5.1 Instantiation

The call to instantiate the FocusQuadrupole derived class is:

FocusQuadrupole(Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength,
$$kFQ$$
)

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. The quadrupole Length is required together with either the field gradient, Strength (equation 27), or the quadrupole k parameter, kFQ (equation 29).

A.4.5.2 Instance attributes and access methods

The instance attributes are defined in table 35. The attributes are accessed and set using the methods defined in table 37.

Table 35: Definition of attributes of instances of the FocusQuadrupole (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|-------------------|---|
| FQmode | int | | If 0, use particle momentum in calculation of transfer matrix; if |
| | | | 1, use reference particle momentum. |
| Length | float | m | Effective length of quadrupole. |
| Strength | float | T/m | Magnetic field gradient; required if kFQ is not given. |
| kFQ | float | m^{-2} | Quadrupole k parameter. |

Table 36: Definition of access methods for the FocusQuadrupole derived class.

| Set method | Get method | Comment |
|---------------------|---------------|--|
| setFQmode(FQmode) | getFQmode() | Set/get FQmode. |
| setLength(Length) | getLength() | Set/get length. |
| setStrength(Length) | getStrength() | Set/get strength (field gradient). |
| setKFQ(Length) | getKFQ() | Set/get kFQ, quadrupole k parameter. |

570

A.4.5.3 Processing methods

The FocusQuadrupole processing methods are defined in table 37.

A.4.5.4 I/o methods

The Focus quadrupole derived class has no i/o methods other than those inheritted from the parent class.

Table 37: Utilities provided by the FocusQuadrupole derived class.

| Method | Argument(s) | Return | Comment |
|----------------|-------------|--------|---|
| calckFQ() | | float | Calculates kFQ if strength is given in instance |
| | | | attributes. |
| calcStrength() | | float | Calculates Strength if kFQ is is given in |
| | | | instance attributes. |

575 **A.4.5.5 Utilities**

The Focusquadrupole derived class has no utilities other than those inheritted from the parent class.

A.4.6 Derived class: DefocusQuadrupole (BeamLineElement)

A.4.6.1 Instantiation

The call to instantiate the DefocusQuadrupole derived class is:

DefocusQuadrupole(Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength, kDQ)

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. The quadrupole Length is required together with either the field gradient, Strength (equation 27), or the quadrupole k parameter, kDQ (equation 29).

A.4.6.2 Instance attributes and access methods

The instance attributes are defined in table 38. The attributes are accessed and set using the methods defined in table 40.

Table 38: Definition of attributes of instances of the DefocusQuadrupole(BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|-------------------|---|
| DQmode | int | | If 0, use particle momentum in calculation of transfer matrix; if |
| | | | 1, use reference particle momentum. |
| Length | float | m | Effective length of quadrupole. |
| Strength | float | T/m | Magnetic field gradient; required if kDQ is not given. |
| kDQ | float | m^{-2} | Quadrupole k parameter. |

A.4.6.3 Processing methods

The DefocusQuadrupole processing methods are defined in table 40.

590 A.4.6.4 I/o methods

The Defocusquadrupole derived class has no i/o methods other than those inheritted from the parent class.

A.4.6.5 Utilities

The Defocusquadrupole derived class has no utilities other than those inheritted from the parent class.

Table 39: Definition of access methods for the DefocusQuadrupole derived class.

| Set method | Get method | Comment |
|---------------------|---------------|--|
| setDQmode(DQmode) | getDQmode() | Set/get DQmode. |
| setLength(Length) | getLength() | Set/get length. |
| setStrength(Length) | getStrength() | Set/get strength (field gradient). |
| setKDQ(Length) | getKDQ() | Set/get kDQ, quadrupole k parameter. |

Table 40: Utilities provided by the DefocusQuadrupole derived class.

| Method | Argument(s) | Return | Comment |
|----------------|-------------|--------|--|
| calckDQ() | | float | Calculates kDQ if strength is specified. |
| calcStrength() | | float | Calculates Strength if kDQ is specified. |

A.4.7 Derived class: SectorDipole (BeamLineElement)

A.4.7.1 Instantiation

The call to instantiate the SectorDipole derived class is:

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement.

The orientation of the RLPC coordinate axes with respect to those of the laboratory frame changes from the start of sector dipole to its end. Referring to figure 2, the vector, $v_{\rm ES}$, that translates the origin of the RLPC coordinate system at the start of the sector dipole to the origin of the RLPC coordinate system at its end is given by:

$$v_{\rm ES} = 2\rho_0 \sin\left(\frac{\phi}{2}\right) \begin{pmatrix} \sin\left(\frac{\phi}{2}\right) \\ 0 \\ \cos\left(\frac{\phi}{2}\right) \end{pmatrix};$$
 (56)

where ρ_0 is the radius of the circular locus of the trajectory of the reference particle. If the rotation matrix taking the RPLC axes at the start of the sector dipole to the laboratory coordinate axes is $\underline{\underline{R}}_{S}$, then the vector, v_{ES}^{lab} , that translates from the start of the sector dipole to its end in laboratory coordinates is given by:

$$v_{\rm ES}^{\rm lab} = \underline{R}_{\rm S} v_{\rm ES} \,.$$
 (57)

The rotation matrix that transforms from the RPLC system at the end of the sector dipole to the laboratory coordinate system, $\underline{\underline{R}}_{E}$ is given by:

$$\underline{\underline{R}}_{E} = \underline{\underline{R}}_{S}\underline{\underline{R}}; \tag{58}$$

where:

$$\underline{\underline{R}} = \begin{pmatrix} \cos \phi & 0 & -\sin \phi \\ 0 & 1 & 0 \\ \sin \phi & 0 & \cos \phi \end{pmatrix} . \tag{59}$$

A.4.7.2 Instance attributes and access methods

The instance attributes are defined in table 41. The attributes are accessed and set using the methods defined in table 42.

Table 41: Definition of attributes of instances of the SectorDipole (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|------|---|
| Angle | float | rad | Angle through which sector dipole bends positive reference par- |
| | | | ticle. |
| В | float | T | Magnetic field. |

Table 42: Definition of access methods for the SectorDipole derived class.

| Set method | Get method | Comment |
|-----------------|-------------|---|
| setAngle(Angle) | getAngle() | Set/get bending angle. |
| setB(B) | getB() | Set/get dipole magnetic field. |
| setLength() | getLength() | Set/get length of reference particle trajectory |
| | | through sector dipole (arc length). |

A.4.7.3 Processing methods

The SectorDipole derived class has no processing methods other than those inheritted from the parent class.

A.4.7.4 I/o methods

The SectorDipole derived class has no i/o methods other than those inheritted from the parent class.

A.4.7.5 Utilities

The SectorDipole derived class has no utilities other than those inheritted from the parent class.

A.4.8 Derived class: Solenoid (BeamLineElement)

A.4.8.1 Instantiation

The call to instantiate the Solenoid derived class is:

```
Solenoid (Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength, kSol)
```

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. The solenoid Length is required together with either the magnetic field strength, Strength or the solenoid k parameter, kSol (equation 32).

A.4.8.2 Instance attributes and access methods

The instance attributes are defined in table 43. The attributes are accessed and set using the methods defined in table 45.

A.4.8.3 Processing methods

The Solenoid processing method is defined in table 45.

A.4.8.4 I/o methods

The Solenoid derived class has no i/o methods other than those inheritted from the parent class.

Table 43: Definition of attributes of instances of the Solenoid (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|----------|---|
| Length | float | m | Effective length of solenoid. |
| Strength | float | T/m | Magnetic field gradient; required if kSol is not given. |
| kSol | float | m^{-2} | GaborLens k parameter required if Strength not given. |

Table 44: Definition of access methods for the Solenoid derived class.

| Set method | Get method | Comment |
|-------------------|---------------|---|
| setLength(Length) | getLength() | Set/get length. |
| setStrength(B) | getStrength() | Set/get strength (solenoid magnetic field). |
| setKSol(Length) | getKFQ() | Set/get kSol, solenoid k parameter. |

A.4.8.5 Utilities

The Solenoid derived class has no utilities other than those inheritted from the parent class.

Table 45: Utilities provided by the Solenoid derived class.

| Method | Argument(s) | Return | Comment |
|----------------|-------------|--------|---|
| calckSol() | | float | Calculates kSol if strength is specified. |
| calcStrength() | | float | Calculates Strength if kSol is specified. |

A.4.9 Derived class: GaborLens (BeamLineElement)

A.4.9.1 Instantiation

640

The call to instantiate the GaborLens derived class is:

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. The Gabor lens Length is required together with either the parameters Bz, VA, RA, and Rp corresponding, respectively, to the parameters B_z , V_A , V_A and R_p defined in section 4.4, or kSol, the solenoid strength parameter of the equaivalent solenoid (see section 4.4). The effective electon number density inside the trap is calculated using either Bz, VA, RA and Rp or kSol.

A.4.9.2 Instance attributes and access methods

The instance attributes are defined in table 46. The attributes are accessed and set using the methods defined in table 47.

A.4.9.3 Processing methods

The GaborLens processing method is defined in table 45.

Table 46: Definition of attributes of instances of the GaborLens (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|-------------------|--|
| Bz | float | Т | Effective length of Gabor lens. |
| VA | float | V | Effective length of Gabor lens. |
| RA | float | m | Effective length of Gabor lens. |
| RP | float | m | Effective length of Gabor lens. |
| Length | float | m | Effective length of Gabor lens. |
| Strength | float | T/m | Magnetic field gradient; required if kSol is not given. |
| kSol | float | m^{-2} | k parameter of the solenoid with the equivalent focusing strength. |

Table 47: Definition of access methods for the GaborLens derived class.

| Set method | Get method | Comment |
|-----------------------|---------------------------------|--|
| setBz(Bz) | getBz() | Set/get magnetic field of the Penning- |
| | | Malmberg trap. |
| setVA(VA) | getVA() | Set/get anode voltage of the Penning- |
| | | Malmberg trap. |
| setRA(RA) | getRA() | Set/get radius of the anode of the Penning- |
| | | Malmberg trap. |
| setRP(RP) | getRP() | Set/get magnetic effective radiius of the |
| | | plasma confined within the Penning- |
| | | Malmberg trap. |
| setLength(Length) | getLength() | Set/get effective length of the lens. |
| setStrength(Strength) | getStrength() | Set/get k-parameter of the solenoid with the |
| | | equivalent focal length. |
| setElectronDenisty() | <pre>getElectronDenisty()</pre> | Set/get electron density. |

A.4.9.4 I/o methods

The GaborLens derived class has no i/o methods other than those inheritted from the parent class.

A.4.9.5 Utilities

The GaborLens derived class has no utilities other than those inheritted from the parent class.

655 A.4.10 Derived class: CylindricalRFCavity (BeamLineElement)

A.4.10.1 Instantiation

The call to instantiate the CylindricalRFCavity derived class is:

```
CylindricalRFCavity(Name, rStrt, vStrt, drStrt, dvStrt, Gradient, Frequency, Phase)
```

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement.

A.4.10.2 Instance attributes and access methods

The instance attributes are defined in table 48. The attributes are accessed and set using the methods defined in table 49.

Table 48: Definition of attributes of instances of the CylindricalRFCavity (BeamLineElement) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-------------------|-------|------|---|
| Gradient | float | MV/m | Peak electric field gradient on axis. |
| Frequency | float | MHz | Resonant frequency. |
| Phase | float | rad | Phase cavity at time reference particle crosses centre of cavity, |
| | | | "linac convention". |
| TransitTimeFactor | float | | Transit time factor (equation ??). |
| VO | float | MV | Peak voltage. |
| alpha | float | | α parameter defined in equation ??. |
| wperp | float | | ω_{\perp} parameter defined in equation ??. |
| cperp | float | | c_{\perp} parameter defined in equation ??. |
| sperp | float | | s_{\perp} parameter defined in equation ??. |
| wprll | float | | $\omega_{ }$ parameter defined in equation ??. |
| cprll | float | | $c_{ }$ parameter defined in equation ??. |
| sprll | float | | $s_{ }$ parameter defined in equation ??. |

665 A.4.10.3 Processing methods

The CylindricalRFCavity derived class has no processing methods other than those inheritted from the parent class.

A.4.10.4 I/o methods

The CylindricalRFCavity derived class has no i/o methods other than those inheritted from the parent class.

A.4.10.5 Utilities

The CylindricalRFCavity derived class has no utilities other than those inheritted from the parent class.

A.4.10.6 Processing methods

The $\mbox{CylindricalRFCavity}$ derived class has no processing methods.

Table 49: Definition of access methods for the CylindricalRFCavity derived class.

| Set method | Get method | Comment |
|------------------------------|-----------------------------------|------------------------------------|
| setGradient(Gradient) | getGradient() | Set/get peak electric field gradi- |
| | | ent. |
| setFrequency(Frequency) | getFrequency() | Set/get frequency. |
| setAngularFrequency(AngFreq) | <pre>getAngularFrequency()</pre> | Set/get angular frequency. |
| setPhase (Phase) | getPhase() | Set/get phase. |
| setWaveNumber(WaveNumber) | getWaveNumber() | Set/get wavenumber. |
| setLength (Length) | getLength() | Set/get Length. |
| setRadius(Radius) | getRadius() | Set/get Radius. |
| setTransitTimeFactor | <pre>getTransitTimeFactor()</pre> | Set/get TransitTimeFactor. |
| (TransitTimeFactor) | | |
| setV0(V0) | getV0() | Set/get peak voltage. |
| setalpha(alpha) | getalpha() | Set/get alpha. |
| setwperp(wperp) | getwperp() | Set/get wperp. |
| setcperp(cperp) | getcperp() | Set/get cperp. |
| setsperp(sperp) | getsperp() | Set/get sperp. |
| setwprll(wprll) | getwprll() | Set/get wprll. |
| setcprll(cprll) | getcprll() | Set/get cprll. |
| setsprll(sprll) | getsprll() | Set/get sprll. |
| setmrf(mrf) | getmrf() | Set/get mrf. |

675 A.4.11 Derived class: Source (BeamLineElement)

A.4.11.1 Instantiation

The call to instantiate the Source derived class is:

```
Source (Name, rStrt, vStrt, drStrt, dvStrt, Mode, Parameters)
```

Parent class arguments Name, rStrt, vStrt, drStrt, and dvStrt are described in section A.4.1.2. These arguments are passed directly to BeamLineElement. Mode is an integer that transmits the type of source to be generated. The specification of the Parameters list depends on the value of Mode. The content of the Parameters list is transferred directly to the Param instance attribute.

A.4.11.2 Instance attributes and access methods

The instance attributes are defined in tables 50, 51, and 52, each table refers to a particular source Mode. The attributes are accessed and set using the methods defined in table 54.

A.4.11.3 Processing methods

The Source derived class has no processing methods other than those inheritted from the parent class.

A.4.11.4 I/o methods

The Source derived class has no i/o methods other than those inheritted from the parent class.

Table 50: Definition of attributes of instances of the Source (BeamLineElement) derived class for source Mode= 0, the parameterised TNSA model. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|---------|-------------------|--|
| Mode | integer | | Mode= 0; parameterised laser-driven source. |
| Param[0] | float | m | Standard deviation of normal distribution from which x coordi- |
| | | | nate is sampled. |
| Param[1] | float | m | Standard deviation of normal distribution from which y coordi- |
| | | | nate is sampled. |
| Param[2] | float | | Minimum $\cos \theta_S$. The specification of a minimum for $\cos \theta_S$ im- |
| | | | proves the efficiency of generation as it may be used to restrice |
| | | | generation to the set of partices that will enter the downstream |
| | | | acceptane. |
| Param[3] | float | MeV | Minimum kinetic energy (K_{\min} . |
| Param[4] | float | MeV | Maximum kinetic energy ($K_{\rm max}$. Value entered here is overwrit- |
| | | | ten when calculated in getLaserDrivenParticleEnergy |
| | | | during initialisation. |
| Param[5] | integer | | nPnts: Number of points to sample for integration of PDF (kept |
| | | | for backward compatibility). |
| Param[6] | float | W | P_L : Laser power. |
| Param[7] | float | J | E_L : Laser energy. |
| Param[8] | float | μ m | λ : Laser wavelength. |
| Param[9] | float | s | t_{laser} : Laser pulse duration. |
| Param[10] | float | m | d: Diameter of laser spot at focus. |
| Param[11] | float | W/cm ² | I: Laser intensity |
| Param[12] | float | 0 | $\theta_{ m degrees}$: Electron divergence angle. |
| Param[13] | float | 0 | Intercept of α , maximum half opening angle at $K=0$. |
| Param[14] | float | 0 | Scaled slope of $\alpha(K)$. |

690 A.4.11.5 Processing methods

The processing methods provided by the Source derived class are listed in table 55.

A.4.11.6 Utilities

The utilities provided by the Source derived class are listed in table 56.

Table 51: Definition of attributes of instances of the Source (BeamLineElement) derived class for source Mode=1 in which energy is sampled from a normal distribution. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|---------|------|--|
| Mode | integer | | Mode= 1; parameterised laser-driven source. |
| Param[0] | float | m | Standard deviation of normal distribution from which x coordi- |
| | | | nate is sampled. |
| Param[1] | float | m | Standard deviation of normal distribution from which y coordi- |
| | | | nate is sampled. |
| Param[2] | float | | Minimum $\cos \theta_S$. The specification of a minimum for $\cos \theta_S$ im- |
| | | | proves the efficiency of generation as it may be used to restrice |
| | | | generation to the set of partices that will enter the downstream |
| | | | acceptane. |
| Param[3] | float | MeV | Mean kinetic energy. |
| Param[4] | float | MeV | Standard deviation of kinetic energy distribution. |

Table 52: Definition of attributes of instances of the Source (BeamLineElement) derived class for source Mode=2 in which energy is sampled from a uniform distribution. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|---------|------|--|
| Mode | integer | | Mode= 2; parameterised laser-driven source. |
| Param[0] | float | m | Standard deviation of normal distribution from which x coordi- |
| | | | nate is sampled. |
| Param[1] | float | m | Standard deviation of normal distribution from which y coordi- |
| | | | nate is sampled. |
| Param[2] | float | | Minimum $\cos \theta_S$. The specification of a minimum for $\cos \theta_S$ im- |
| | | | proves the efficiency of generation as it may be used to restrice |
| | | | generation to the set of partices that will enter the downstream |
| | | | acceptane. |
| Param[3] | float | MeV | Mean kinetic energy. |
| Param[4] | float | MeV | Maximum kinetic energy. |

Table 53: Definition of attributes of instances of the Source (BeamLineElement) derived class for source Mode= 3 in which parameters of particle at source are read from an input file. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|---------|------|--|
| Mode | integer | | Mode= 3; partice trace space read from file. In this case no |
| | | | additional paramters are required. |

Table 54: Definition of access methods for the Source derived class.

| Set method | Get method | Comment |
|---------------------|-------------------------------|------------------------------------|
| setMode | getMode() | Set/get Mode. |
| setModeText | getModeText() | Set string with readable name |
| | | for mode. |
| setModeParamterText | <pre>getParameterText()</pre> | Set/get list of strings with read- |
| | | able name for paramter. |
| setParameters | getParameters() | Set/get parameters; list of |
| | | paramters as defined above. |
| setParameterUnit | <pre>getParameterUnit()</pre> | Set/get list of strings containing |
| | | parameter units. |

Table 55: Definition of processing methods provided by the Source derived class.

| Method | Arguments | Return | Comment |
|--|-----------|---------|---|
| getParticleFromSource() | | ndarray | Get trace space for particle at source, returns |
| | | | np.array. |
| getParticle() | | floats | Called from |
| | | | getParticleFromSource(), re- |
| | | | turns parameters used to create trace space of |
| | | | particle at source. |
| getFlatThetaPhi() | | floats | Called from getParticle() if flat $\cos \theta_S$, |
| | | | flat ϕ_S distribution is requested. |
| getgofrp(rpmax, xp, yp) | floats | float | Returns $g(r')$ given input r'_{max} , x' , and y' . |
| g_theta(Energy) | float | | Returns θ_S generated using a guassian distri- |
| | | | bution. Depricated. |
| angle_gemerator(Energy) | float | | Returns θ_S , ϕ_S using g-theta and uniform |
| | | | distribution for ϕ_S . Depricated. |
| getGaussianThetaPhi(Energy) | float | | Returns $\cos \theta_S$ and ϕ_S using |
| | | | angle_generator. |
| paramters(P, E, 1, t1, d, I, t) | floats | | Returns derived parameters used to generate |
| | | | TNSA proton kinetic energy spectrum. |
| equation(x, tl, t0) | floats | | Returns result of evaluation equation ??. |
| <pre>getLaserDrivenProtonEnergy()</pre> | | | Generates proton kinetic energy at source for |
| | | | paramterised TNSA model. |
| <pre>getLaserCumProbParam()</pre> | | | |
| <pre>getLaserCumProb()</pre> | | | |
| <pre>getLaserDrivenProtonEnergyProbDensity()</pre> | | | |
| <pre>getTraceSpace()</pre> | | | |

Table 56: Definition of utilities provided by the Source derived class.

| Method | Arguments | Return | Comment |
|-------------------------------|---------------|---------|-------------------------------|
| CheckSourceParam(Mode, Param) | Integer, list | boolean | Class method. Check that |
| | | | mode and parameters are |
| | | | valid. Calls CheckMode and |
| | | | CheckParam |
| CheckMode (Mode) | integer | boolean | Class method. Check is valid. |
| CheckParam | list | boolean | Class method. Check paramter |
| | | | list is valid. |
| tabulateParameters() | | | |

A.5 UserFramework

UserFramework is a module that provides a set of methods used in the code provided to allow users easy access to the code and data. The following methods are provided:

```
startAnalysis (argv): processes input flags passed in call to run script.
          Argument:
           argv: list of arguments passed to main by call to run script.
700
          Returns:
           Success: (boolean) True if processing successful.
           Debug: (boolean) Set to True if flag -d is set to True.
           inputfile: (path) full path to input file; set using flag -y.
           outputfile: (path) full path to output file; set using flag -o.
705
           nEvts: (integer) number of events to process; set using flag -n.
           bdsimfile: (path) full path to bdsim format file; set using flag -z.
           beamspecfile: (path) full path to beam specification CSV file; set using flag -b.
     handleFILES (beamspecfile, inputfile, outputfile, bdsimFILE=False): File han-
          dling method to check files exist and create relevant BeamIO instances.
          Arguments:
           beamspecfile: (path) full path to beam specification CSV file;
           inputfile: (path) full path to input file;
           outputfile: (path) full path to output file;
715
           bdsimfile: (path) full path to bdsim format file.
          Returns:
           Success: (boolean) True if file handling successful.
           ibmIOr: (BeamIO) instance of BeamIO class for file to be read.
           ibmIOw: (BeamIO) instance of BeamIO class for file to be written.
720
     EventLoop (iUsrAnl, ibmIOr, ibmIOw, nEvtsIn): executes loop over nEvtsIn events. Reads
          event record or generates event if ibmIOr=None, and handles end-of-file. Passes control to UserAnal. EventLoo
          Arguments:
           iUsrAnl: (UserAnal) instance.
725
           ibmIOr: (BeamIO) instance of BeamIO class for file to be read.
           ibmIOw: (BeamIO) instance of BeamIO class for file to be written.
           nEvtsIn: (integer) number of events to process.
          Returns:
           Success: (boolean) True if successful.
730
```

A.6 visualise

The visualise class manages the visualisation of the beam line and particles traversing it.

A.6.1 Instantiation

The call to instantiate the visualise class is:

Beam (CoordSys, Projection)

CoordSys (string) is either "RPLC" to visualise the beam line in the reference particle local coordinate system or "Lab". Projection (string) is either "xs" (RPLC) or "xz" (lab) to visualise the xs or xz projecton and eithed "ys" (RPLC) or "yz" (lab) to visualise the xs or xz projecton.

A.6.2 Instance attributes and access methods

The instance attributes are presented in table 57 and the access methods are summarised in table 58.

Table 57: Definition of attributes of instances of the visualise class.

| Attribute | Type | Comment |
|------------|--------|---|
| CoordSys | String | Either "RPLC" to visualise the in the reference particle local coordinate system |
| | | or "Lab". |
| Projection | String | Either " xs " (RPLC) or " xz " (lab) to visualise the xs or xz projecton and eithed |
| | | " ys " (RPLC) or " yz " (lab) to visualise the xs or xz projecton. |

Table 58: Definition of access methods for the visualise class.

| Set method | Get method | Comment |
|---------------|---------------|--|
| setCoordSys | getCoordSys | Set coordinate system for visualisation. |
| setProjection | setProjection | Set projection for visualisation. |

740

735

A.6.3 Processing methods

Table 59 presents the processing methods provided in the visualise class.

Table 59: Processing methods provided by the visualise class.

| Method | Argument(s) | Return | Comment |
|------------------------|---------------|--------|---------------------------------------|
| Particles(axs, nPrtcl) | plot, integer | | Manage ploting of nPrtcl particles on |
| | | | matplotlib axes instance. |
| BeamLine(axs) | plot | | Manage ploting of beam line on |
| | | | matplotlib axes instance. |

A.6.4 I/o methods

The visualise class has no i/o methods.

745 A.6.5 Utilities

The visualise class has no i/o methods.

A.7 BeamIO

The BeamIO class provides interfaces to the reading and writing of beam specification and beam data files.

A.7.1 Instantiation

The call to instantiate the Beam IO class is:

BeamIO(datafilePATH, datafileNAME, create, BDSIMfile)

datafilePATH: (string) Path to directory in which input file is to be found, or, in which output file is to be created. datafilePATH can be set to None if the full path is specified in datafileNAME.

datafileNAME: (string) File name (string) which, when appended to datafilePATH gives the full path to the input or output data file, or. full path to the input or output file.

create: (boolean) if true indicates that the file must be created. If a file exists at the location specified by datafilePATH and datafileNAME it will be overwritten.

BDSIMfile: (boolean) If True then the file is to be read or written in BDSIMfile format.

A.7.2 Instance attributes and access methods

The BeamIO instance attributes are presented in table 60 and the access methods are summarised in table 61.

Table 60: Definition of attributes of instances of the BeamIO class.

| Attribute | Type | Comment |
|-----------------|---------|--|
| dataFILE | Path | Full path to data file. |
| Read1stRecord | Boolean | True if first record has been read from file. |
| dataFILEversion | Integer | For BeamIO files version number identifying file format. |
| create | Boolean | True if data file is to be created. |
| BDSIMfile | Boolean | True id reading or writing a BDSim file. |

760

755

A.7.3 Processing methods

The BeamIO class has no processing methods.

A.7.4 I/o methods

Table 62 presents the i/o methods provided by the BeamIO class.

5 A.7.5 Utilities

Table 63 presents the utilities provided by the BeamIO class.

Table 61: Definition of access methods for the BeamIO class.

| Set method | Get method | Comment |
|--------------------|--------------------|---|
| setpathFILE | getpathFILE | Set/get path to directory containing data file. |
| setdataFILE | getdataFILE | Set/get full path to data file. |
| setReadFirstRecord | getReadFirstRecord | Set/get flag indicating whether the first record |
| | | has been read. |
| setcreate | getcreate | Set/get flag indicating whether data file is to be |
| | | created. |
| setdataFILEversion | getdataFILEversion | Set/get BeamIO version number. |
| setBDSIMfile | getBDSIMfile | Set/get flag indicating whether the data file is in |
| | | BDSIM format. |

Table 62: I/o methods provided by the BeamIO class.

| Method | Argument(s) | Return | Comment |
|-------------------------------|-------------|---------|-----------------------------------|
| readBeamDataRecord() | | Boolean | Manages reading/writing of a |
| | | | record from/to the data file. Re- |
| | | | turns a boolean, EoF, set to True |
| | | | of end of file has been detected. |
| readVersion() | | Integer | Reads data-file format version |
| | | | number from file. Returns inte- |
| | | | ger version number. |
| flushNclosedataFile(dataFILE) | Path | | Flush and close data dataFILE |
| | | | at end of processing. |

Table 63: Utilities provided by the BeamIO class.

| Method | Argument(s) | Return | Comment |
|-------------------------------|-------------|--------|---|
| resetinstances() | | | Class method. Sets list of instances to []. |
| <pre>cleanBeamIOfiles()</pre> | | | Class method. Delete BeamIO instances and |
| | | | reset list of instances. |

A.8 Simulation

The singleton Simulation class provides a framework and utilities for the simulation of the passage of particles through the beam lines defined through the classes described in this document. By default the seed for the random number generator is set using the system time.

A.8.1 Instantiation

780

The call to instantiate the Simulation class is:

NEvts: (integer) Number of events to generate.

BeamLineSpecificationCVSfile: (string) String containing path to the beam-line specification CVS file

dataFileDir: (string) String containing path to directory in which data file is to be written.

dataFileName: (string) Name of file to be written.

Simulation has two methods defined outside the class:

getRandom(): returns number between 0. and 1. drawn from a uniform distributin; and getParabolic (umax): returns number between —umax and umax drawn from a parabolic distribution with a maximum at 0.

A.8.2 Instance attributes and access methods

The Simulation instance attributes are presented in table 64 and the access methods are summarised in table 65.

| Attribute | Type | Comment | |
|---------------|----------|--|--|
| NEvt | integer | Number of events to generate. | |
| ParamFileName | string | Path to beam-line parameter CSV file. | |
| dataFileDir | string | Path to the directory in which data file is to be written. | |
| dataFileName | string | Name of file to be created. | |
| Facility | Facility | Instance of the derived Facility class derived from | |
| | | BeamLineElement. | |
| iBmIOw | BeamIO | Instance of the derived BeamIO class for the file to be written. | |
| ProgressPrint | boolean | If True the progress towards the NEvt requested events is printed. | |

Table 64: Definition of attributes of instances of the Simulation class.

A.8.3 Processing methods

The Simulation class provides one processing method:

RunSim()

which manages the generation of NEvts events. The specification of the beam line and the individual events are written to the output data file.

A.8.4 I/o methods

The Simulation class provides no i/o methods.

A.8.5 Utilities

795 The Simulation provides no utilities.

Table 65: Definition of access methods for the Simulation class.

| Set method | Get method | Comment |
|------------------------------|---|--|
| setNEvt | getNEvt | Set/get number of events to generate. |
| setBeamLineSpecificationFile | getBeamLineSpecificationFile Set/get full | Set/get full path to beam line specification file. |
| setdataFileDir | getdataFileDir | Set/get path to directory in which data file is to be written. |
| setdataFileName | getdataFileName | Set/get name of data file to be created. |
| setFacility | getFacility | Set/get Facility instance. |
| setiBmIOw | getiBmIOw | Set/get BeamIO instance specifying the file to be written. |
| setProgressPrint | getProgressPrint | Set/get flag that controls the progress printout. |

A.9 Physical constants

The PhysicalConstants class provides the physical constants that are required to carry out the linear optics calculations. The values are taken from, for example, the Particle Data Group book. The constants packages is implemented as a singleton class so that there is no ambiguity about which values are in use.

800 A.9.1 Instantiation

The call to instantiate the PhysicalConstants class is:

PhysicalConstants()

A.9.2 Instance attributes and access methods

The PhysicalConstants has no instance attributes. The access methods are summarised in table 66.

| Table 66: | Definition of access | methods for the Ph | ysicalConstants class. |
|-----------|----------------------|--------------------|------------------------|
|-----------|----------------------|--------------------|------------------------|

| Set method | Get method | Comment |
|------------|--------------------------|---|
| | getPDGref | Returns PDG reference used. |
| | getSoL | Returns speed of light in m/s. |
| | getSpecies | Returns list of particle species for which con- |
| | | stants are stored. |
| | getParticleMASS(Species) | Returns particle mass for Species. Species |
| | | is a list of strings: ["proton", "pion", |
| | | "muon", "neutrino"]. |
| | mp | Returns proton mass in MeV. |
| | getmPion | Returns pion mass in MeV. |
| | getmMuon | Returns muon mass in MeV. |
| | getmNeutrino | Returns 0, neutrino mass (for nuSIM). |
| | getm0 | Returns permittivity of free space. |

805 A.9.3 Processing methods

The PhysicalConstants class provides no processing methods.

A.9.4 I/o methods

The PhysicalConstants class provides no i/o methods.

A.9.5 Utilities

810 The Physical Constants provides no utilities.

A.10 Report

The Report parent class supports a collection of derived classes to generate reports, usually in the form of a CSV file, based on the data stored in the attributes of the Beam, BeamLine, BeamLineElement, Particle, and other classes.

815 A.10.1 Instantiation

820

The call to instantiate the Report class is:

Report (Name, ReportPath, FileName, Header, Lines)

Name: (string) Name of report;

ReportPath: (string) String containing path to the directory where report will be written;

FileName: (string) String containing name of the file in which report will be written.

Header: (list of strings) List containing strings that will form the header record of the report; and

Lines: (list of lists) The lines that will make up the lines of the report. List[i][j] provides the value of the item to be recorded in column j of row i of the report.

A.10.2 Instance attributes and access methods

The Report parent class supports a collection of derived classes to generate reports, usually in the form of a CSV file, based on the data stored in the attributes of the Beam, BeamLine, BeamLineElement, Particle, and other classes. instance attributes are presented in table 67 and the access methods are summarised in table 68.

Table 67: Definition of attributes of instances of the Report class.

| Attribute | Type | Comment | | |
|---------------|----------|--|--|--|
| NEvt | integer | Number of events to generate. | | |
| ParamFileName | string | Path to beam-line parameter CSV file. | | |
| dataFileDir | string | Path to the directory in which data file is to be written. | | |
| dataFileName | string | Name of file to be created. | | |
| Facility | Facility | Instance of the derived Facility class derived from | | |
| | | BeamLineElement. | | |
| iBmIOw | BeamIO | Instance of the derived BeamIO class for the file to be written. | | |
| ProgressPrint | boolean | If True the progress towards the NEvt requested events is printed. | | |

Table 68: Definition of access methods for the Report class.

| Set method | Get method | Comment |
|---------------|---------------|---|
| setName | getName | Set/get name of report. |
| setReportPath | getReportPath | Set/get path to director into which report file is to be written. |
| setFileName | getFileName | Set/get name of file to be written. |
| setHeader | getHeader | Set/get list of strings forming header fields. |
| setLines | getLines | Set/get list of lists containing report entries line by line. |

A.10.3 Processing methods

Table 70 presents the processing methods provided in the Report class.

Table 69: Processing methods provided by the Report class.

| Method | Argument(s) | Return | Comment |
|------------------------------------|-------------|---------------------|--------------------------------|
| <pre>createPandasDataFrame()</pre> | | Data frame instance | Create pandas data frame using |
| | | | the data contained in Header |
| | | | and Lines. The instance is re- |
| | | | turned. |

A.10.4 I/o methods

Table ?? presents the i/o methods provided in the Report class.

Table 70: I/o methods provided by the Report class.

| Method | Argument(s) | Return | Comment |
|----------------------|---------------------|--------|--|
| createCSV(DataFrame) | Data frame instance | | Create CSV file from pandas data |
| | | | DatsFrame frame using the data con- |
| | | | tained in Header and Lines. |
| asCSV() | | | Write pandas dataframe and write it to CSV |
| | | | file. |

A.11 LaTeX

The LaTeX module provides 2 methods to support the generation of LaTeX tables from data stored in the class and instance attributes. The first method, TableHeader, creates the header of LaTeX table. The method is accessed via the call:

TableHeader (FilePath, TabString, Caption)

where:

840

FilePath: (path) is the full path to the file to contain the table;

TabString: (string) is the string that defines the columns, e.g., '|c|c|', would result in a two-column table in which the contents of each column is centred; and

Caption: (string) Is the string to be used as the table caption; and

Each line in the table are entered with the call:

TableLine (FilePath, Line)

845 where:

FilePath: (path) is the full path to the file to contain the table;

Line: (string) is a list of strings that contain the contents of the line. A typical use case would be to create the table header, enter a line containing the header fields and then procede to add each line in the table in turn; and LaTeX commants are allowed, e.g. Line = \hline will produce a horizontal line.

The final lines of LaTeX code is entered with the call:

TableTrailer(FilePath)

where:

FilePath: (path) is the full path to the file to contain the table.

B Set-up and run

Introduction

This section summarises the steps needed to set-up and run the linear optics simulation of the LhARA beam line. A summary of the tasks that the software suite performs will be documented in due course. The code has been developed in python; python 3 is assumed.

Getting the code

865

885

890

The linear optics package is maintained using the GitHub version-control system. The latest release can be downloaded from:

```
\centerline{
  \href{https://github.com/ImperialCollegeLondon/LhARAlinearOptics.git}{https://e
}
```

Dependencies and required packages

The linear optics code requires the following packages:

• Python modules: scipy and matplotlib.

It may be convenient to run the package in a "virtual environment". To set this up, after updating your python installation to python 3.9, execute the following commands:

- 1. python3 -m venv --system-site-packages venv
 - This creates the director venv that contains files related to the virtual environment.
- 2. source venv/bin/activate
- 3. python -m pip install pandas scipy matplotlib

To exit from the virtual environment, execute the command deactivate. The command source venv/bin/activate places you back into the virtual environment.

The Imperial HEP linux cluster provides python 3.9.18 by default.

Unpacking the code, directories, and running the tests

After downloading the package from GitHub, or cloning the repository, you will find a "README.md" file which provides some orientation and instructions to run the code. In particular, a bash script "startup.bash" is provided which:

- Sets the "LhARAOpticsPATH" environment variable so that the files that hold constants etc. required by the code can be located; and
- Adds "01-Code" (see below) to the PYTHONPATH. The scripts in "02-Tests" (see below) may then be run with the command "python 02-Tests/<filename>.py".

Below the top directory, the directory structure in which the code is presented is:

- 01-Code: contains the python implementation as a series of modules. Each module contains a single class or a related set of methods.
- 02-Tests: contains self-contained test scripts that run the various methods and simulation packages defined in the code directory.
- 11-Parameters: contains the parameter set used to specify the various beam lines presently implemented. The instructions in the README.md file should be followed to set up and run the code.

Running the code

900

Execute "startup.bash" from the top directory (i.e. run the bash command "source startup.bash"). This will:

- Set up "LhARAOpticsPATH"; and
- Add "01-Code" to the PYTHONPATH. The scripts in "02-Tests" may then be run with the command "python 02-Tests/<filename>.py";
- Example scripts are provided in "03-Scripts", these can be used first to "Run" the simulation and then to "Read" the data file produced. Example scripts are provided for the DRACO, LION, and LhARA Stage 1 beam lines.