

LhARA linear optics documentation

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30 1 Introduction

The LhARA [1, 2] linear optics package was written to allow rapid calculations to initiate more detailed studies of the LhARA beam lines and for use as a tool to check issues as they arise. The package has been written in Python so that it is accessible and can readily be updated, modified and maintained. At present the code treats proton beams only.

35 This document presents the approximations and notation used and summarises the module, class and data structures that have been adopted.

2 Coordinate systems

2.1 Laboratory coordinate system

40 The origin of the LhARA coordinate system, the “laboratory coordinate system” or “laboratory reference frame”, is at the position of the laser focus at the laser-target interaction point [3]. The z axis is horizontal and parallel to the nominal capture axis, pointing in the downstream direction. The y axis points vertically upwards and the x axis completes a right-handed orthogonal coordinate system.

Unit vectors along the x , y and z axes are \mathbf{i} , \mathbf{j} and \mathbf{k} respectively. The position of the reference particle as well as its momentum and energy are described as functions of the distance it has travelled from the origin of coordinates. The distance the reference particle has travelled is s , making the position, \mathbf{r}_0 , momentum, \mathbf{p}_0 , and energy, E_0 , of the reference particle position, s :

$$\begin{aligned} \mathbf{r}_0 &= \mathbf{r}_0(s); \\ \mathbf{p}_0 &= \mathbf{p}_0(s); \text{ and} \\ E_0 &= E_0(s). \end{aligned} \tag{1}$$

The magnitude of the reference particle velocity is v_0 and the relativistic parameters that determine the reference particle energy and momentum are:

$$\begin{aligned} \beta_0 &= \frac{v_0}{c}; \text{ and} \\ \gamma_0 &= \frac{1}{\sqrt{1 - \beta_0^2}}; \end{aligned}$$

where c is the speed of light. The time, t , at which the reference particle is at s is also a function of s :

$$t = t(s) = \frac{s}{v_0} = \frac{s}{c} \frac{E_0}{cp_0}; \tag{2}$$

50 where $p_0 = |\mathbf{p}_0|$.

2.2 Reference particle local coordinate system

A coordinate system defined relative to the position of the reference particle, the “reference particle local coordinate” (RPLC) system, may be defined using the direction in which the particle is travelling. The position of the particle defines the origin of the RPLC system, see figure 1. The tangent to the reference particle trajectory at s defines the z_r axis with unit vector \mathbf{k}_r . In the laboratory frame, the presence of local electric or magnetic fields may cause the reference particle’s trajectory to change. In the neighbourhood of the particle, the curved trajectory may be described in terms of an arc of a circle. The x_r axis (with unit vector \mathbf{i}_r) is then taken to be in the direction pointing away from the centre of the circle. The third coordinate axis, y_r , is defined



Figure 1: Reference particle local coordinate system. The trajectory of the reference particle is shown as the red line. The distance the reference particle has travelled, measured from the origin of coordinates in the laboratory frame, is labelled s . The origin of the “reference particle local coordinate (RPLC) system is coincident with the position of the reference particle. The directions of unit vectors along each of three righthanded, orthogonal coordinate axes are shown as black arrows labelled \mathbf{i}_r , \mathbf{j}_r , and \mathbf{k}_r .

to complete the right-handed orthogonal coordinate system; the unit vector along the y_r axis being given by
 $\mathbf{j}_r = \mathbf{k}_r \times \mathbf{i}_r$.

The trajectory of the reference particle is a straight line as it traverses a drift space and a variety of beam-line elements. Examples of such beam-line elements include solenoids and quadrupoles. The reference trajectory is also undeviated by passage through an accelerating cavity placed such that the accelerating field is parallel to the reference-particle trajectory.

The RPLC coordinate system at $s = 0$ is taken to coincide with the laboratory coordinate system. Beam-line elements are placed sequentially along the trajectory of the reference particle. If necessary a coordinate transformation is performed to ensure that the RPLC system at the entrance to a particular beam-line element is consistent with the definition given above.

2.3 Transforming to and from reference particle local coordinates to laboratory coordinates

In the RPLC system, the trajectory of the reference particle, \mathbf{R}_0 , is:

$$\mathbf{R}_0(s) = \mathbf{0}. \quad (3)$$

The position of a test particle in the RPLC frame, \mathbf{R} , is described with reference to the position of the reference particle. In the laboratory frame, the position of the test particle is:

$$\mathbf{r}(s) = \mathbf{r}_0(s) + \delta\mathbf{r}(s); \quad (4)$$

where:

$$\delta\mathbf{r}(s) = \underline{\underline{R}}(s)\mathbf{R}(s); \text{ and} \quad (5)$$

75 $\underline{\underline{R}}(s)$ is a rotation matrix that takes the RPLCs at s to the laboratory frame coordinates.

In the laboratory frame, the unit vectors \mathbf{i}_r , \mathbf{j}_r and \mathbf{k}_r are given by:

$$\begin{aligned}\mathbf{i}_r &= \begin{pmatrix} i_{rx} \\ i_{ry} \\ i_{rz} \end{pmatrix}; \\ \mathbf{j}_r &= \begin{pmatrix} j_{rx} \\ j_{ry} \\ j_{rz} \end{pmatrix}; \text{ and} \\ \mathbf{k}_r &= \begin{pmatrix} k_{rx} \\ k_{ry} \\ k_{rz} \end{pmatrix}.\end{aligned}\tag{6}$$

The rotation matrix, $\underline{\underline{R}}$, may now be written:

$$\underline{\underline{R}}(s) = \begin{bmatrix} i_{rx} & j_{rx} & k_{rx} \\ i_{ry} & j_{ry} & k_{ry} \\ i_{rz} & j_{rz} & k_{rz} \end{bmatrix}.\tag{7}$$

3 Phase space and trace space

The motion of particles passing through an accelerator is most often described using classical Hamiltonian mechanics; quantum mechanics being required only in particular cases such as the description of spin polarisation in a storage ring. In classical Hamiltonian mechanics the equations of motion are solved to give the evolution of the position, momentum, and energy as functions of a single independent parameter. The independent parameter is often taken to be time.

80 Relativistic mechanics exploits four-vector position, $\underline{\mathcal{R}} = (\mathbf{r}, ct)$, and four-vector momentum, $\underline{\mathcal{P}} = (c\mathbf{p}, E)$. In the Hamiltonian description of particle dynamics, these four vectors become functions of the independent variable, i.e. $\underline{\mathcal{R}} = \underline{\mathcal{R}}(t)$ and $\underline{\mathcal{P}} = \underline{\mathcal{P}}(t)$. In the laboratory system, the position of the reference particle along its trajectory is directly related to the time coordinate by $t = c\beta_0 s$. This allows s to be taken as the independent variable and for the motion of particles in the beam to be derived as functions of s .

90 The 6D phase-space coordinates of a particle as a function of s are given by the position and momentum three vectors. The particle energy may be determined from the invariant mass and the time coordinate from the invariant interval between the origin and the position represented by s .

The “trace-space” coordinates of a particle are defined relative to the reference particle. Usually, a beam is understood to contain particles which follow trajectories that differ rather little from that of the reference particle. Trace space is defined such that the position, “momentum”, and “energy” coordinates are small for particles which follow trajectories close to that of the reference particle. The utility of this approach is that trace-space coordinates may be used to perform Taylor expansions of the Hamiltonian which may readily be solved to yield a description of particle transport using functions that are linear in the trace-space coordinates.

The notation used for the 6D phase and trace spaces are defined in this section.

3.1 Phase space

100 The 6D phase-space vector is defined in terms of the three-vector position and three vector momentum as:

$$\begin{bmatrix} \mathbf{r} \\ \mathbf{p} \end{bmatrix} = \begin{bmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} \\ \begin{pmatrix} p_x \\ p_y \\ p_z \end{pmatrix} \end{bmatrix} \quad (8)$$

The trajectory of the particle may be evaluated as a function of time or s .

3.2 Trace space

Trace space is defined to simplify the calculation of the trajectory of particles through the accelerator lattice and is derived from the phase space expressed in the RPLC frame. Consider a particle with position $\mathbf{r}_{\text{RPLC}} = (x_{\text{RPLC}}, y_{\text{RPLC}}, z_{\text{RPLC}})$ and momentum $\mathbf{p}_{\text{RPLC}} = (p_{x\text{RPLC}}, p_{y\text{RPLC}}, p_{z\text{RPLC}})$. Taking the magnitude of the momentum of the reference particle in the laboratory frame to be p_0 , the trace-space coordinates are given by:

$$\underline{\phi} = \begin{pmatrix} x_{\text{RPLC}} \\ x'_{\text{RPLC}} \\ y_{\text{RPLC}} \\ y'_{\text{RPLC}} \\ z_{\text{RPLC}} \\ \delta_{\text{RPLC}} \end{pmatrix}; \quad (9)$$

where:

$$x'_{\text{RPLC}} = \frac{\partial x}{\partial s} = \frac{cp_{x\text{RPLC}}}{cp_0}; \quad (10)$$

$$y'_{\text{RPLC}} = \frac{\partial y}{\partial s} = \frac{cp_{y\text{RPLC}}}{cp_0}; \quad (11)$$

$$z_{\text{RPLC}} = \frac{s}{\beta_0} - ct = \frac{\Delta s}{\beta_0}; \text{ and} \quad (12)$$

$$\delta_{\text{RPLC}} = \frac{E}{cp_0} - \frac{1}{\beta_0} = \frac{\Delta E}{cp_0}. \quad (13)$$

Here $\Delta s = s - s_0$ and $\Delta E = E - E_0$, where s_0 and E_0 are the reference particle position and energy respectively; E and s are the energy and position of a particular particle in the beam.

110 4 Transfer matrices

A beam line may be described as a series of beam-line elements arranged one after the other. A particle may then be transported through the beam line by transporting it through each element in turn. Taking advantage of the trace-space defined above, the transport of a particle across a particular beam-line element may be performed using a linear transformation:

$$\underline{\phi}_{\text{end}} = \underline{T} \underline{\phi}_{\text{start}}; \quad (14)$$

115 where $\underline{\phi}_{\text{start}}$ is the trace-space vector at the start of the beam-line element and $\underline{\phi}_{\text{end}}$ is the transformed trace-space vector at the end. The step across the beam-line element implies an increment, δs , to the s -coordinate given by:

$$s_{\text{end}} = s_{\text{start}} + \delta s; \quad (15)$$

where s_{start} and s_{end} are the coordinate along the reference particle trajectory at the start and end of the beam-line element respectively. There are many excellent descriptions of the derivation of the transfer matrices, \underline{T} , so only the results are quoted here. The notation used below is developed from that used in [4].

4.1 Drift

A “drift” space refers to a region in which the beam propagates in the absence of any electromagnetic fields. In a drift, particles propagate in straight lines, therefore:

$$\underline{T}_{\text{drift}} = \begin{pmatrix} 1 & l & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & l & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}; \quad (16)$$

where l is the length of the drift. The increment in the reference particle position is:

$$\delta s = l. \quad (17)$$

4.2 Quadrupole

The passage of a beam particle through a quadrupole magnet may be described by specifying the field gradient, g , within the magnet and the length, l_q , of the quadrupole measured along its axis. The impact of a quadrupole on the trajectory of a particle in the xy plane is independent of the impact of the magnet on the particle’s trajectory in the yz plane. In this sense quadrupole focusing in the xz and yz planes is said to be “uncoupled”.

If the field gradient along the x and y axes is identical, then:

$$g_x = \frac{\partial B_{qx}}{\partial x} = g_y = \frac{\partial B_{qy}}{\partial y} = g; \quad (18)$$

where the field in the quadrupole, \mathbf{B}_q , has components $(B_{qx}, B_{qy}, 0)$.

In the “hard-edge” approximation, where the field falls to zero at the start and end of the quadrupole, the transfer matrix for a quadrupole focusing in the xz plane (a “focusing quadrupole”) may be written:

$$\underline{T}_{\text{Fquad}} = \begin{pmatrix} \cos(\sqrt{k_q} l_q) & \frac{\sin(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 & 0 & 0 \\ -\sqrt{k_q} \sin(\sqrt{k_q} l_q) & \cos(\sqrt{k_q} l_q) & 0 & 0 & 0 & 0 \\ 0 & 0 & \cosh(\sqrt{k_q} l_q) & \frac{\sinh(\sqrt{k_q} l_q)}{\sqrt{k_q}} & 0 & 0 \\ 0 & 0 & \sqrt{k_q} \sinh(\sqrt{k_q} l_q) & \cosh(\sqrt{k_q} l_q) & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l_q}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}; \quad (19)$$

where:

$$k_q = \frac{gc}{p} \times 10^{-3} \text{ m}^{-2}, \quad (20)$$

c is the speed of light in metres per second, p is the magnitude of the momentum of the particle in MeV/c, and the field gradient, g , is given in T/m. As before, β_0 is the relativistic velocity of the reference particle and $\gamma_0 = (1 - \beta_0^2)^{-\frac{1}{2}}$. The increment in the reference particle position is:

$$\delta s = l_q. \quad (21)$$

It is important to include a description of the effect of dispersion on beam transport through the LhARA beam line since the laser-driven proton and ion source provides a broad energy spectrum. Reference [4] describes two methods for the description of dispersion in a linear approximation. The first is to use the reference momentum to calculate the quadrupole focusing strength ($k_{0q} = \frac{qc}{p_0} \times 10^{-3} \text{ m}^{-2}$) and to include terms in the expressions for x , x' , y , and y' dependent on δ . The second is to use equation 20 to calculate the effective quadrupole focusing strength, with k_q evaluated using p . The second approach has been adopted here.

In the same notation, the transfer matrix for a quadrupole focusing in the yz plane (a “defocusing quadrupole”) may be written:

$$\underline{T}_{\text{Dquad}} = \begin{pmatrix} \cosh(\sqrt{k_q}l_q) & \frac{\sinh(\sqrt{k_q}l_q)}{\sqrt{k_q}} & 0 & 0 & 0 & 0 \\ \sqrt{k_q} \sinh(\sqrt{k_q}l_q) & \cosh(\sqrt{k_q}l_q) & 0 & 0 & 0 & 0 \\ 0 & 0 & \cos(\sqrt{k_q}l_q) & \frac{\sin(\sqrt{k_q}l_q)}{\sqrt{k_q}} & 0 & 0 \\ 0 & 0 & -\sqrt{k_q} \sin(\sqrt{k_q}l_q) & \cos(\sqrt{k_q}l_q) & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l_q}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}. \quad (22)$$

4.3 Solenoid

The trajectory of a beam particle through a solenoid is determined by the magnetic field strength, B_s , within the solenoid and the length of the solenoid, l_s , measured along its axis. As the particle enters the solenoid, the fringe field imparts momentum transverse to the axis of the magnet. This results in the particle executing a helical trajectory, the axis of the helix being parallel to the solenoid axis. The sense of the rotation depends on the particle charge and the polarity of the field. The helical motion means that the evolution of the particle motion in the xz plane is coupled with the evolution of the particle motion in the yz plane.

In the “hard-edge” approximation, the magnetic field inside the magnet is given by $\mathbf{B}_s = (0, 0, B_{s0})$, where the solenoid axis lies along the z_{RPLC} axis. The solenoid field-strength parameter is then given by:

$$k_s = \left[\frac{B_{s0}c}{2p} \times 10^{-3} \right]^2 \text{ m}^{-2}; \quad (23)$$

where B_{s0} is measured in T, p in MeV/c and c in m/s.

The transfer matrix for passage of a positive particle through a solenoid with field pointing in the positive z_{RPLC} direction may be written:

$$\underline{T}_{\text{Sol}} = \begin{pmatrix} \cos^2(\sqrt{k_s}l_s) & \frac{1}{2\sqrt{k_s}} \sin(\sqrt{k_s}l_s) & \frac{1}{2} \sin(2\sqrt{k_s}l_s) & \frac{1}{\sqrt{k_s}} \sin^2(\sqrt{k_s}l_s) & 0 & 0 \\ -\frac{\sqrt{k_s}}{2} \sin(2\sqrt{k_s}l_s) & \cos^2(\sqrt{k_s}l_s) & -\sqrt{k_s} \sin^2(\sqrt{k_s}l_s) & \frac{1}{2} \sin(2\sqrt{k_s}l_s) & 0 & 0 \\ -\frac{1}{2} \sin(2\sqrt{k_s}l_s) & -\frac{1}{\sqrt{k_s}} \sin^2(\sqrt{k_s}l_s) & \cos^2(\sqrt{k_s}l_s) & \frac{1}{2\sqrt{k_s}} \sin(2\sqrt{k_s}l_s) & 0 & 0 \\ \sqrt{k_s} \sin^2(\sqrt{k_s}l_s) & -\frac{1}{2} \sin(2\sqrt{k_s}l_s) & -\frac{\sqrt{k_s}}{2} \sin(2\sqrt{k_s}l_s) & \cos^2(\sqrt{k_s}l_s) & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}. \quad (24)$$

As in the case of the quadrupoles, dispersion is accounted for by using p to calculate k_s (equation 23). The increment in the reference particle position is:

$$\delta s = l_s. \quad (25)$$

160 4.4 Non-neutral (electron) plasma (Gabor) lens

A dense gas of electrons confined in a Penning-Malmberg trap provides an electric field that can be used to focus a positive ion beam. The electron gas is confined axially in the lens by an electrostatic potential created using a central anode of length l_G . The gas is confined radially using the uniform field of a solenoid. Assuming a uniform electron density, n_e , the focusing parameter, k_G , may be written:

$$k_G = \frac{e}{2\epsilon_0} \frac{m_p \gamma}{p^2} n_e \quad \text{m}^{-2}; \quad (26)$$

165 where e is the charge on the electron, ϵ_0 is the permittivity of free space, and m_p is the proton mass. As in the case of the quadrupoles and solenoid, dispersion is accounted for by using p in equation 26. The force on a particle passing through the electron gas is towards the axis of the lens and is proportional to the radial distance of the particle from the axis. Focusing is therefore cylindrically symmetric and does not couple motion in the the xz and yz planes.

170 In the “hard-edge” approximation, the electric field inside the lens falls to zero at the end of the electron gas and the contribution of the magnetic field used to confine the electron gas in the transverse direction has a negligible effect on particles passing through the lens. The transfer matrix for the passage of a positive particle through the lens may be written:

$$\underline{T}_G = \begin{pmatrix} \cos(\sqrt{k_G} l_G) & \frac{\sin(\sqrt{k_G} l_G)}{\sqrt{k_G}} & 0 & 0 & 0 & 0 \\ -\sqrt{k_G} \sin(\sqrt{k_G} l_G) & \cos(\sqrt{k_G} l_G) & 0 & 0 & 0 & 0 \\ 0 & 0 & \cos(\sqrt{k_G} l_G) & \frac{\sin(\sqrt{k_G} l_G)}{\sqrt{k_G}} & 0 & 0 \\ 0 & 0 & -\sqrt{k_G} \sin(\sqrt{k_G} l_G) & \cos(\sqrt{k_G} l_G) & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & \frac{l}{\beta_0^2 \gamma_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}. \quad (27)$$

The increment in the reference particle position is:

$$\delta s = l_G. \quad (28)$$

175 4.5 Dipole

The reference particle trajectory in the beam-line elements described above passes along the axis of the element. In contrast, a dipole bends the reference trajectory so that it describes the arc of a circle (see figure 2). The code provides for transport through a “sector dipole” in the hard-edge approximation. In this case, the field within the magnet is taken to be constant and parallel to \hat{j}_{RPLC} , i.e. $\mathbf{B}_D = (0, B_{D0}, 0)$. No edge focusing is considered.

180 The passage of particles through a dipole may be described by defining the parameter, k_D :

$$k_D = \left[\frac{B_{D0} c}{p} \times 10^{-3} \right]^2 \text{m}^{-2}. \quad (29)$$

The momentum of the reference particle is related to the curvature. ρ , by:

$$p_0 = B_{D0} \rho; \quad (30)$$

so:

$$k_D = \frac{1}{\rho}; \quad (31)$$

and the angle ϕ is given by:

$$\phi = \frac{l_D}{\rho}. \quad (32)$$

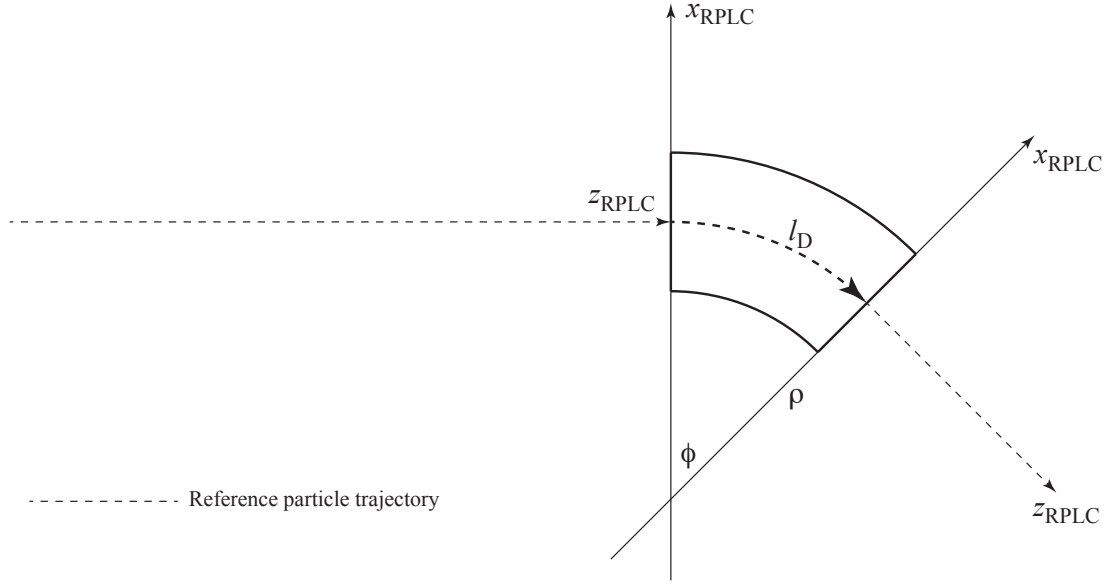


Figure 2: Schematic representation of the passage of the reference particle through a sector dipole. The outline of the sector dipole is shown by the solid black lines. The trajectory of the reference particle is shown as the dashed line. The length of the reference-particle trajectory inside the field of the sector dipole is l_D . The x_{RPLC} and z_{RPLC} coordinate axes at the entry and exit of the sector dipole are shown. The radius of curvature of the reference particle trajectory inside the magnet is ρ and the angle through which the x_{RPLC} is rotated is ϕ .

185 With these definitions the transfer matrix for passage through a dipole may be written:

$$T_D = \begin{pmatrix} \cos(\phi) & \rho \sin(\phi) & 0 & 0 & 0 & \frac{\rho}{\beta_0} (1 - \cos(\phi)) \\ -\frac{\sin(\phi)}{\rho} & \cos(\phi) & 0 & 0 & 0 & \frac{\sin(\phi)}{\beta_0} \\ 0 & 0 & 1 & l & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ -\frac{\sin(\phi)}{\beta_0} & -\frac{\rho}{\beta_0} (1 - \cos(\phi)) & 0 & 0 & 1 & \frac{l}{\beta^2 \gamma^2} - \frac{l - \rho \sin(\phi)}{\beta_0^2} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}. \quad (33)$$

The increment in the reference particle position is:

$$\delta s = l_D. \quad (34)$$

5 Source

A variety of options for the generation of the particle distribution at source are included in the package (see section ??). The principal, and the default, option is the target-normal sheath acceleration (TNSA) model presented in [5]. The implementation of this model is summarised below. The laboratory and RPLC reference frames coincide at the target, therefore trace- and phase-coordinates are not distinguished in the presentation of the particle-production model.

5.1 Energy distribution

190 The typical kinetic energy spectrum produced in target-normal sheath acceleration falls rapidly with kinetic energy before dropping rapidly to zero above a maximum “cut off” energy ε_{max} . The kinetic-energy spectrum

of the TNSA model presented in [5] is given by:

$$\frac{dN}{d\varepsilon} = \frac{n_{e0}c_s t_{laser} S_{sheath}}{\sqrt{2\varepsilon T_e}} \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right); \quad (35)$$

where N is the number of protons or ions produced per unit solid angle, ε is the ion kinetic energy, n_{e0} and T_e are the hot electron density and temperature respectively, c_s is the ion acoustic velocity, t_{laser} is the duration of the laser pulse, and S_{sheath} is the effective area over which the TNSA mechanism takes place. The variables and the units in which they are expressed are presented in table 1.

Equation 35 is based on time-limited fluid-dynamical models which are unable to predict the cut-off kinetic energy accurately. The cut-off energy is taken to be that given by the model described in [6] in which the time over which the laser pulse creates the conditions necessary for acceleration is derived. The kinetic energy cut-off is given by:

$$\varepsilon_{max} = X^2 \varepsilon_{i,\infty}; \quad (36)$$

where X is obtained by solving:

$$\frac{t_{laser}}{t_0} = X \left(1 + \frac{1}{2} \frac{1}{1 - X^2}\right) + \frac{1}{4} \ln \left(\frac{1 + X}{1 - X}\right). \quad (37)$$

Here t_0 is the time over which the ion acceleration may be treated as ballistic and $\varepsilon_{i,\infty}$ is given in table 1.

To generate the kinetic energy spectrum, the probability density function, $g(\varepsilon)$, is defined such that the probability, $\delta\mathcal{P}$, of a particle being generated in the interval $\varepsilon \rightarrow \varepsilon + \delta\varepsilon$ is given by:

$$\delta\mathcal{P} = g(\varepsilon) \delta\varepsilon. \quad (38)$$

$g(\varepsilon)$ can be written in terms of the differential spectrum given in equation 35 through the introduction of a normalisation constant \mathcal{N} :

$$g(\varepsilon) = \frac{1}{\mathcal{N}} \frac{dN}{d\varepsilon}. \quad (39)$$

The cumulative distribution function, $G(\varepsilon)$, is given by:

$$G(\varepsilon) = \int_{\varepsilon_{\min}}^{\varepsilon_{\max}} g(\varepsilon) d\varepsilon; \quad (40)$$

where ε_{\min} is the minimum kinetic energy and the normalisation constant, \mathcal{N} , is set so that $G(\varepsilon_{\max}) = 1$. Carrying out the integration yields:

$$G(\varepsilon) = \frac{2}{\mathcal{N}} \frac{n_{e0}c_s t_{laser} S_{sheath}}{\sqrt{2T_e}} \sqrt{\frac{T_e}{2}} \left[\exp\left(-\sqrt{\frac{2\varepsilon_{\min}}{T_e}}\right) - \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right) \right]; \quad (41)$$

and the normalisation constant is given by:

$$\mathcal{N} = 2 \frac{n_{e0}c_s t_{laser} S_{sheath}}{\sqrt{2T_e}} \sqrt{\frac{T_e}{2}} \left[\exp\left(-\sqrt{\frac{2\varepsilon_{\min}}{T_e}}\right) - \exp\left(-\sqrt{\frac{2\varepsilon}{T_e}}\right) \right]. \quad (42)$$

The kinetic energy spectrum may now be obtained by choosing a value for $G(\varepsilon)$ using a probability distribution uniform over the range $0 < G(\varepsilon) < 1$. The generated value of ε is obtained by evaluating:

$$\varepsilon = \left[\sqrt{\varepsilon_{\min}} - \sqrt{\frac{T_e}{2}} \ln \left(1 - \frac{G(\varepsilon)}{G(\varepsilon_{\max})}\right) \right]^2. \quad (43)$$

Table 1: Parameters present in the analytical expression, equation 35, describing target normal sheath acceleration (TNSA).

| Parameter | Definition | Value | Unit |
|--------------------------|--------------------------------|---|------------------------|
| N | Ion number | - | - |
| ε | Ion kinetic energy | - | J |
| n_{e0} | Hot electron density | $\frac{N_E}{ct_{laser}S_{sheath}}$ | pp/m^3 |
| N_e | Accelerated electron number | $\frac{fE_{laser}}{T_e}$ | - |
| E_{laser} | Laser energy | 70 | J |
| f | Energy conversion efficiency | $1.2 \times 10^{-15} I^{0.75}$, max=0.5 | - |
| I | Laser intensity | 4×10^{20} | W/cm^2 |
| T_e | Hot electron temperature | $m_e c^2 [\sqrt{1 + \frac{I\lambda^2}{1.37 \times 10^{18}}} - 1]$ | J |
| m_e | Electron mass | 9.11×10^{-31} | Kg |
| c | Speed of light | 3×10^8 | m/s |
| λ | Laser wavelength | 0.8 | μm |
| t_{laser} | Laser pulse duration | 28×10^{-15} | s |
| B | Radius of electron bunch | $B = r_0 + dtan(\theta)$ | m |
| S_{sheath} | Electron acceleration area | πB^2 | m^2 |
| r_0 | Laser spot radius | $\sqrt{\frac{P_{laser}}{I\pi}}$, I in W/m^2 | m |
| d | Target thickness | $400 - 600 \times 10^{-9}$ | m |
| θ | Electron half angle divergence | 0.436 | rad |
| P_{laser} | Laser power | 2.5×10^{15} , $P_{laser} = \frac{E_{laser}}{t_{laser}}$ | W |
| c_s | Ion-acoustic velocity | $(\frac{Zk_B T_e}{m_i})^{\frac{1}{2}}$ | m/s |
| Z | Ion charge number | 1 | - |
| k_B | Boltzmann constant | 1.380649×10^{-23} | $m^2 kg s^{-2} K^{-1}$ |
| m_i | Proton mass | 1.67×10^{-27} | Kg |
| P_R | Relativistic power unit | $\frac{m_e c^2}{r_e} = 8.71 \times 10^9$ | W |
| r_e | Electron radius | 2.82×10^{-15} | m |
| $\varepsilon_{i,\infty}$ | Maximum ion kinetic energy | $2Zm_e c^2 \sqrt{\frac{fP_{laser}}{P_R}}$ | MeV |
| t_0 | Ballistic time | $\frac{B}{v(\infty)}$ | s |
| $v(\infty)$ | Ballistic velocity | $\sqrt{\frac{2\varepsilon_{i,\infty}}{m_i}}$ | m/s |

5.2 Angular Distribution

The angular distribution of the flux of protons and ions produced by the TNSA mechanism may be described as a cone centred on the normal to the foil surface [7]. Radiochromic film has been used to observe the opening angle, 2α , of the cone as a function of energy. The envelope angle, α , defined such that, at a particular energy, all particles are contained within $\pm\alpha(\varepsilon)$ of the z axis. The opening angle is observed to decrease as the ion energy increases.

The distribution of the polar angle, θ_S , at which particles are produced at the laser-driven source is generated by defining r' such that:

$$r' = \frac{\partial r}{\partial s}; \quad (44)$$

where $r = \sin \theta_S$. x' and y' are sampled independently from the probability density function:

$$g(r') = \frac{3}{4r_m'^2} (r_m'^2 - r'^2); \quad (45)$$

where $r_m' = \sin \alpha$. At low kinetic energy ($\varepsilon \sim \varepsilon_{\min}$), $\alpha(\varepsilon)$ is taken to be $\sim 20^\circ$. $\alpha(\varepsilon)$ is assumed to decrease linearly with energy such that:

$$\alpha(\varepsilon) = 20^\circ - 15^\circ \frac{\varepsilon}{\varepsilon_{\max}}; \quad (46)$$

i.e. $\alpha(\varepsilon)$ decreases from 20° at $\varepsilon = 0$ to 5° at ε_{\max} . Finally, the azimuthal angle, ϕ_S , is chose from a distribution uniform over the range $0 < \phi_S < 2\pi$.

5.3 Spatial distribution

The x and y distributions at production are assumed to be independent and Gaussianly distributed with a standard deviation given by the radius of the laser spot focused on the target.

5.4 Simulated distributions

Distributions 10^6 protons produced by the TNSA mechanism using the algorithm described above are shown in figure 4. The parameters used in the algorithm are presented in table 2. The generated distribution of kinetic energy is in good agreement with the distribution implied by equation 35. The width of the generated polar-angle distribution is observed to fall with kinetic energy and the kinetic-energy dependence of the RMS calculated from the generated particles is in good agreement with that expected from equation 46. As a result, the distribution of θ_S is approximately Gaussian with a width dominated by the contribution of protons with kinetic energy close to ε_{\min} . The generated ϕ_S distribution is flat in the range $0^\circ < \phi_S < 360^\circ$ and the (x, y) distribution is Gaussian in both the x and y projections.

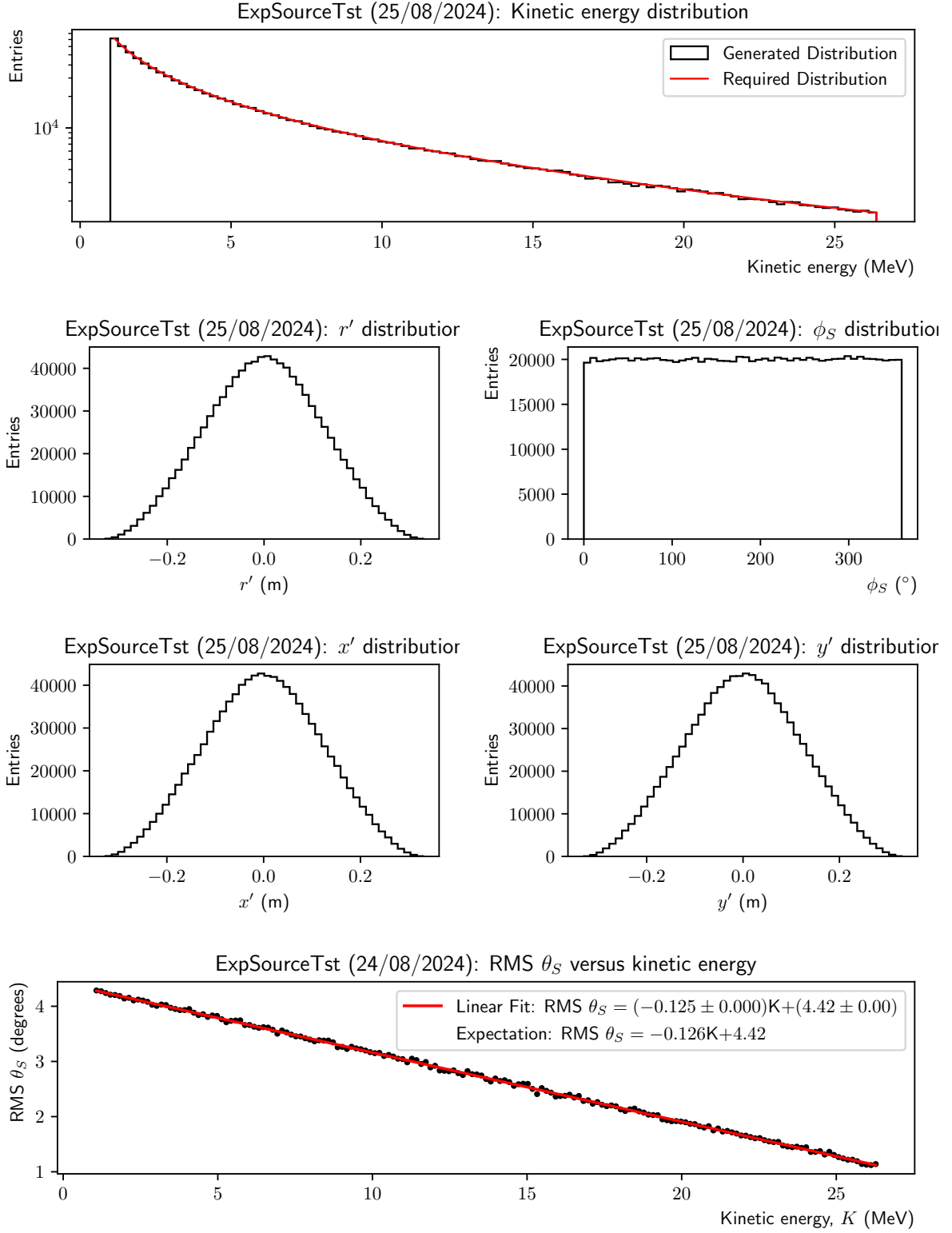
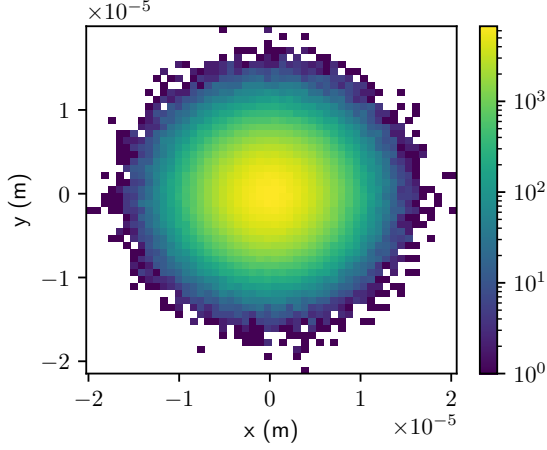
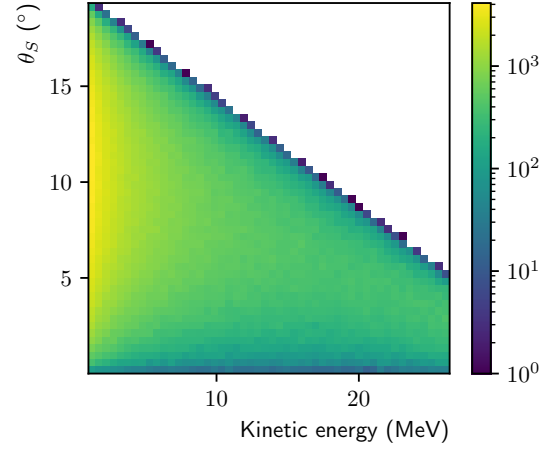


Figure 3: Kinematic distributions of particles at the point of production. Top: The generated kinetic energy distribution is shown as the solid histogram. The required distribution (equation 35), normalised to the lowest kinetic-energy bin, is shown as the solid red line. Second row: Generated r' and ϕ_S distributions. Third row: Generated x' and y' distributions. Bottom: RMS of the θ_S distribution versus kinetic energy. The solid circles are calculated using slices of width 0.15 MeV. The red line shows the result of a straight line fit to the data. The expected dependence from integration of equation 46 is presented in the legend.

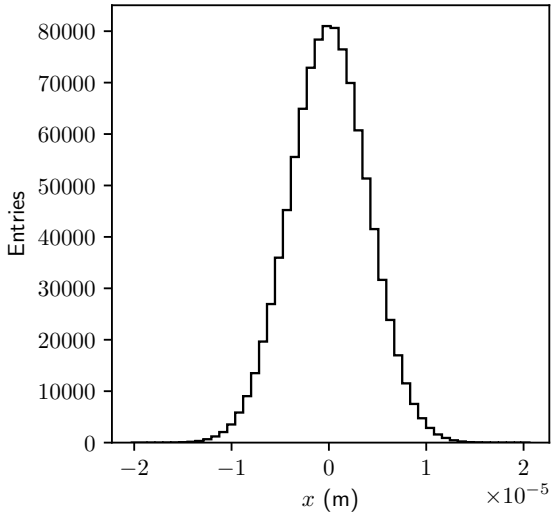
ExpSourceTst (25/08/2024): (x, y) distribution



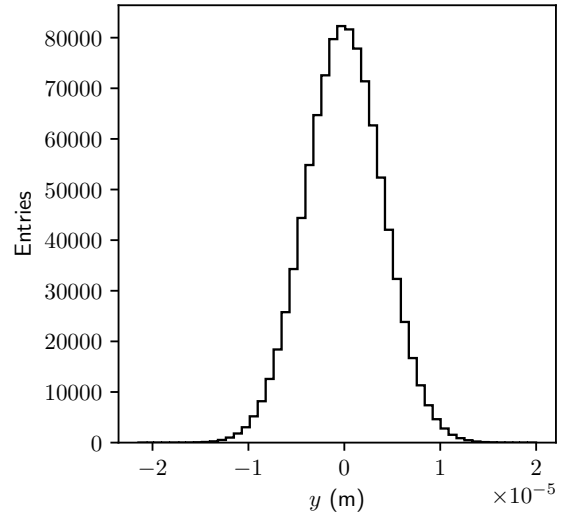
ExpSourceTst (25/08/2024): (θ_S, K) distribution



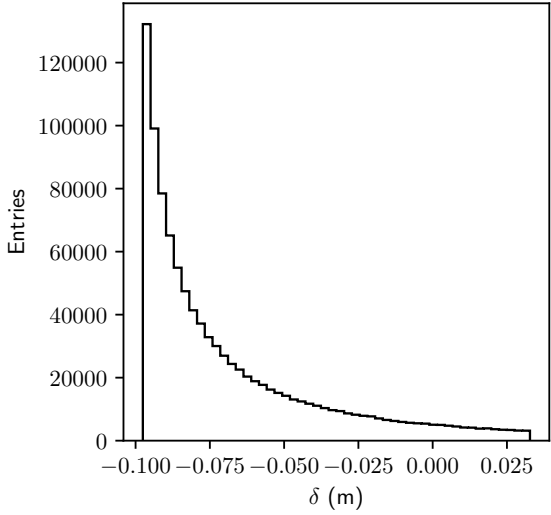
ExpSourceTst (25/08/2024): x distribution



ExpSourceTst (25/08/2024): y distribution



ExpSourceTst (25/08/2024): δ distribution



ExpSourceTst (25/08/2024): θ_S distribution

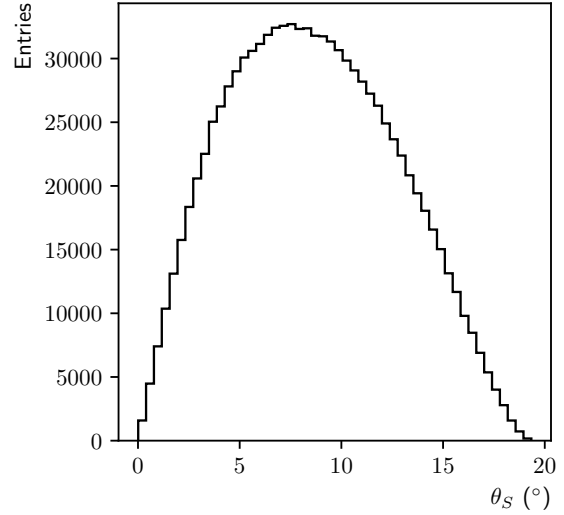


Figure 4: Top left: Generated (x, y) distribution of the particle-production point. Top right: The distribution of θ_S versus kinetic energy. Centre left, right: Generated distributions of x' and y' . Bottom left: Generated distribution of δ . Bottom right: Generated distribution of θ_S .

Table 2: Parameterised laser driven

| Parameter | Value | Unit |
|---|--------------------|-----------------------|
| σ_x | 4e-06 | μm |
| σ_y | 4e-06 | μm |
| $\cos \theta_S _{\min}$ | 0.998 | |
| ε_{\min} | 1.0 | MeV |
| ε_{\max} | 25.0 | MeV |
| nPnts | 1000 | |
| Laser power | 2500000000000000.0 | W |
| Laser energy | 70.0 | J |
| Laser wavelength | 0.8 | μm |
| Laser pulse duration | 2.8e-14 | s |
| Laser spot size | 4e-07 | μm |
| Laser intensity | 4e+20 | J/m^2 |
| Electron divergence angle | 25.0 | degrees |
| RMS θ_S at $K = 0 \text{ MeV}$ | 20 | degrees |
| Scaled slope of RMS θ_S versus K | 15 | degrees |

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A Module, class and data structures

The linear optics package has been written in object-oriented Python and is broken down in four principal modules:

- BeamLineElement: provides the various beam-line elements required to build a description of the beam line. Each individual element, such as a drift, quadrupole, etc., is described in a class derived from the `BeamLineElement` parent class.
- BeamLine: provides code to assemble the elements into a coherent beam line. `BeamLine` is a singleton class to ensure that two beam lines can not be simulated in a single run of the package. The `extrapolateBeam` class is derived from the `Beam` class to handle the propagation of beam envelopes without the need to track individual particles.
- Beam: provides code to calculate ensemble properties of the beam such as emittance. The ensemble properties are stored as instance attributes of the `Beam` class.
- Particle: provides code to record beam particles at positions along the beam line. The module provides the singleton `ReferenceParticle` class derived from the `Particle` class.

Other modules: `BeamIO`, `LaTeX`, `PhysicalConstants`, `Report`, `Simulation`, `UserFramework`, `Utilities`, and `Visualise` support the principal modules or provide services. The data structure is implemented as attributes of the instances of the various classes. This section describes the implementation of the various modules, the classes of which they are composed, and how access to the data is provided.

- Each class has methods by which to access a list of the class instances and a Boolean flag by which to generate debug print out (see table 3).

Table 3: Methods by which to set and access class attributes.

| Method | Argument | Return | Comment |
|------------------------------|----------|----------------------------|---|
| <code>getinstances()</code> | Boolean | List of instances of class | For singleton classes such as <code>BeamLine</code> , <code>getinstances()</code> returns a single instance rather than a list. |
| <code>setDebug(Debug)</code> | | Boolean debug flag | Sets flag to generate debug print-out |
| <code>getDebug()</code> | | | If True, generate debug print-out |
| <code>setAll2None()</code> | | String | Set all instance attributes to <code>None</code> at start of instantiation. |
| <code>SummaryStr()</code> | | | Text string to record parameters in debug print out. |

A.1 BeamLine

BeamLine is a singleton class that sets up the beam line geometry and provides methods to track particles through the beam line using the transfer matrices defined in section A.4. The beam-line geometry is provided in the form of a “csv” file read using pandas. The format of the “csv” file is defined in section ?? . Alternatively, if a data file written using the BeamIO package is being read, the beam-line geometry is read from the top of the data file. The instance of the BeamLine class is created when the first record of the data file is read.

A.1.1 Instantiation

The call to instantiate the BeamLineElement class is:

```
BeamLine(BeamLineSpecificationCSVfile, readDataFile)
```

BeamLineSpecificationCSVfile is the full path of the CSV file containing the beam-line specification. readDataFile is a boolean flag. If readDataFile is set to True, then the BeamLine instance will be created and the beam-line geometry will be read from the header of the BeamIO data file. If readDataFile is not set or is set to False, the beam-line geometry will be read from BeamLineSpecificationCSVfile.

A.1.2 Instance attributes and access methods

The instance attributes are presented in table 4 and the access methods are summarised in table 5.

Table 4: Definition of attributes of instances of the BeamLine class.

| Attribute | Type | Comment |
|-------------------------------|-----------|--|
| BeamLineSpecificationCSVfile* | path | Full path to beam-line specification csv file. |
| BeamLineParamPandasInstance | dataframe | Pandas data frame containing beam-line specification. |
| Element | list | List of instances of BeamLineElement class containing pointers to the elements that make up the beam line. |

A.1.3 Processing methods

Table 6 presents the processing methods provided in the BeamLine class.

A.1.4 I/o methods

Table 7 presents the i/o methods provided in the BeamLine class.

A.1.5 Utilities

Table 8 presents the utilities provided in the `BeamLine` class.

Table 5: Definition of access methods for the BeamLine class.

| Set method | Get method | Comment |
|--------------------------|---------------------------------|--|
| setSrcTrcSpc (SrcTrcSpc) | getSrcTrcSpc () | Set trace space at source; SrcTrcSpc presented as (1, 6) np.ndarray. |
| | getinsance () | Get instance of BeamLine class. |
| | BeamLineSpecificationCSVfile () | Get beam line specification csv file. |
| | (getBeamLineParamPandas) | Get pandas dat from containing beam-line specification. |
| | getElement () | get list of BeamLineElement instances. |

Table 6: Processing methods provided by the BeamLine class.

| Method | Argument(s) | Return | Comment |
|----------------------------------|-------------|-------------------|--|
| addBeamLine () | | Success | Loops through pandas data frame and manages parsing and instantiation of the beam line elements defined in the specification csv file. Returns Success (bool) which is True if the beamline has been set up OK and is False otherwise. |
| addFacility () | | | Manages the extraction of the facility parameters from the pandas data frame and the creation of the single instance of Facility (BeamLineElement). |
| addSource () | | | Manages the extraction of the source parameters from the pandas data frame and the creation of the single instance of Source (BeamLineElement). |
| parseFacility () | | Name, K0, VCMVr | Parses pandas data frame to extract facility parameters. Returns the facility Name (str), the kinetic energy of the reference particle, K0 (float) in MeV, and the vacuum chamber mother volume radius, VCMVr (float) in m. |
| parseSource () | | Name, Mode, Param | Parses pandas data frame to extract source parameters. Returns Name (str), Mode (int) Param (list) containing the parameters required to instantiate source Mode. |
| addBeamLineElement (iBLE) | | | Adds BeamLineElement instance iBLE to the list of instances of BeamLineElement that make up the beam line. |
| checkConsistency () | | Consistent | Checks the consistency of the beam line representation in memory with that requested in the specification csv file. Returns Consistent (bool) which is True if the beamline is consistent is False otherwise. |
| trackBeamn (NEvts, particleFILE) | | | Generates NEvts (int) particles and tracks them through the beam line. |

Table 7: I/o methods provided by the BeamLine class.

| Method | Argument(s) | Return | Comment |
|---------------------|-------------|------------------|---|
| csv2pandas(csvFILE) | Path | pandas dataframe | Read CSV file to create pandas data frame. csvFILE (path) is the full path to the csv |
| pandasBeamLine() | | pandas dataframe | Create pandas dataframe from BeamLine instance. |
| getHeader() | | List | Prepares list of header fields for pandasBeamLine. |
| readBeamLine(file) | Path | Boolean | Called from BeamIO. Reads BeamLine from data file. |

Table 8: Utilities provided by the BeamLine class.

| Method | Argument(s) | Return | Comment |
|-----------------|-------------|--------|--|
| cleaninstance() | | List | Remove BeamLine instance. |
| fixsz() | | | Loop through BeamLineElement instances to set s and z at exit. |

A.2 Particle and ReferenceParticle

The `Particle` class provides methods to transport particles through the beam line. The trace and phase space is recorded at the start and end of each element. The `ReferenceParticle` derived class is a singleton and records the trajectory of the reference particle.

A.2.1 Particle

A.2.1.1 Instantiation

The call to instantiate the `Particle` class is:

```
Particle(Species)
```

`Species`, the type of particle to be propagated, is a string containing the particle name. At present valid particle species are proton, pion, and muon.

A.2.1.2 Instance attributes and access methods

The instance attributes are presented in table 9 and the access methods are summarised in table 10.

Table 9: Definition of attributes of instances of the `Particle` class.

| Attribute | Type | Comment |
|----------------------------|------|--|
| <code>Species</code> | str | Particle species; proton, muon or pion. |
| <code>Location</code> | list | List of strings containing the unique Name of the <code>BeamLineElement</code> at the particle position is reported. |
| <code>s</code> | list | List of floats recording <code>s</code> coordinate at which particle position is reported. |
| <code>TraceSpace</code> | list | List of <code>np.ndarray</code> containing 6D trace space of particle at <code>s</code> . |
| <code>PhaseSpace</code> | list | List of <code>np.ndarray</code> containing 6D phase space (RPLC) of particle at <code>s</code> . |
| <code>LabPhaseSpace</code> | list | List of <code>np.ndarray</code> containing 6D phase space (Lab) of particle at <code>s</code> . |

A.2.1.3 Processing methods

Table 11 presents the processing methods provided in the `Particle` class.

A.2.1.4 I/o methods

The i/o methods provided by the `Particle` class are listed in table 12.

A.2.1.5 Utilities

The utilities provided by the `Particle` class are listed in table 13.

Table 10: Definition of access methods for the `Particle` class.

| Set method | Get method | Comment |
|--|---|--|
| <code>setSpecies</code> <code>setLocation</code> <code>sets</code> <code>setTraceSpace</code> <code>setRPLCPhaseSpace</code> <code>setLabPhaseSpace</code> <code>resetParticleInstances</code> <code>recordParticle (Loc, z, s, TrcSpc)</code> <code>setSourceTraceSpace (TrcSpc)</code> | <code>getSpecies</code> <code>getLocation</code> <code>gets</code> <code>getTraceSpace</code> <code>setRPLCPhaseSpace</code> <code>getLabPhaseSpace</code> | <code>Set/get particle species.</code> <code>Set/get list of locations location.</code> <code>Set/get list of s coordinates.</code> <code>Set/get list of trace-space vectors.</code> <code>Set/get list of phase-space vectirs in RPLC coordinates.</code> <code>Set/get list of phase-space vectirs in Lab coordinates.</code> <code>Resets list of particle instances preserving reference parti-</code> <code>cle as firt instance in the list.</code> <code>Records particle attributes. Arguments: Loc=Location,</code> <code>z= z, s= s, and TrcSpc=trace space.</code> <code>Sets TrcSpc=trace space at source.</code> |

Table 11: Processing methods provided by the `Particle` class.

| Method | Argument(s) | Return | Comment |
|---|-------------------|------------|---|
| <code>fillPhaseSpaceAll()</code> | | Boolean | Fill phase space for all <code>Particle</code> instances. Class Method. Return <code>True</code> if successful. |
| <code>fillPhaseSpace()</code> | | Boolean | Fill phase space for current <code>Particle</code> instance. Return <code>True</code> if successful. |
| <code>initialiseSums()</code> | Particle instance | | Initialises sums used to calculate covariance matrix. |
| <code>incrementSums(iPrtcl)</code> | | | Increment sums used to calculate covariance matrix. |
| <code>calcCovarianceMatrix()</code> | | | Calculate covariance matrix. |
| <code>evaluateBeam()</code> | | | Work through locations and calculate parameters from covariance matrix. |
| <code>calcRPLCPHasesSpace(nLoc)</code> | Int | np.ndarray | Calculate and return phase space in RPLCs at location <code>nLoc</code> . |
| <code>RPLCTraceSpace2PhaseSpace(TrcSpc)</code> | np.ndarray | np.ndarray | Transform trace space to phase space in RPLCs. |
| <code>RPLCPHasesSpace2TraceSpace(TrcSpc)</code> | np.ndarray | np.ndarray | Transform phase space to trace space in RPLCs. |

Table 12: I/o methods provided by the `Particle` class.

| Method | Argument(s) | Return | Comment |
|--|------------------------|---------|---|
| <code>createParticleFile(path, file)</code> | Path, Str | Path | Class method, kept for backward compatibility. |
| <code>flushNcloseParticleFile(file)</code> | Path | | Class method, kept for backward compatibility. |
| <code>openParticleFile(path, file)</code> | Path, Str | | Class method, kept for backward compatibility. |
| <code>closeParticleFile(path, file)</code> | Path, Str | | Class method, kept for backward compatibility. |
| <code>readParticle(file)</code> | Path | Boolean | Read particle from input stream. Called from <code>BeamIO.file</code> is full path to file. Return <code>True</code> if end of file. |
| <code>writeParticle(file, clean)</code> | Path, boolean | | Write particle to output stream. <code>file</code> is full path to file. If <code>clean</code> , then clean particle instance after write. |
| <code>writeParticleBDSIM(file, iLoc, clean)</code> | Path, integer, boolean | | Write particle to BDSIM ascii file. <code>file</code> is full path to file. <code>iLoc</code> is the location along the beam line at which to write the particle coordinates. If <code>clean</code> , then clean particle instance after write. |

Table 13: Utilities provided by the Particle class.

| Method | Argument(s) | Return | Comment |
|---|-------------|--------|---|
| <code>cleanAllParticles ()</code> | | | Delete all Particle instances including <code>ReferenceParticle</code> . |
| <code>cleanParticles ()</code> | | | Delete all Particle instances except <code>ReferenceParticle</code> . |
| <code>plotTraceSpaceProgression ()</code> | | | Plot transverse trace space at each location. Class method. Writes file to <code>99-Scratch/</code> . |
| <code>plotLongitudinalTraceSpaceProgression ()</code> | | | Plot longitudinal trace space at each location. Class method. Writes file to <code>99-Scratch/</code> . |
| <code>printProgression ()</code> | | | Print particle parameters at each location. |
| <code>getLines ()</code> | | | Returns lines to be used to create summary pandas data frame. |
| <code>createReport ()</code> | | | Creates <code>csv</code> file containing summary of beam progression. |

A.2.2 ReferenceParticle

A.2.2.1 Instantiation

`ReferenceParticle` is a singleton derived class. The call to instantiate the `ReferenceParticle` class is:

```
ReferenceParticle(Species)
```

`Species`, the type of particle to be propagated, is a string containing the particle name. At present valid particle species are `proton`, `pion`, and `muon`.

A.2.2.2 Instance attributes and access methods

In addition to the instance attributes inherited from the parent class, the `ReferenceParticle` class provides the instance attributes presented in table 14 and the access methods are summarised in table 15.

Table 14: Definition of attributes of instances of the `ReferenceParticle` class.

| Attribute | Type | Comment |
|----------------------------|------|---|
| <code>_sIn[]</code> | list | List of floats containing the s coordinates at the entrance to the beam line elements along the locus of the reference particle trajectory. |
| <code>_sOut[]</code> | list | List of floats containing the s coordinates at the exit to the beam line elements along the locus of the reference particle trajectory. |
| <code>_RrIn[]</code> | list | List of ndarrays containing the four-vector position in laboratory coordinates at the entrance to the beam line elements along the locus of the reference particle trajectory. |
| <code>_RrOut[]</code> | list | List of ndarrays containing the four-vector position in laboratory coordinates at the exit to the beam line elements along the locus of the reference particle trajectory. |
| <code>_PrIn[]</code> | list | List of ndarrays containing the four-vector momentum in laboratory coordinates at the entrance to the beam line elements along the locus of the reference particle trajectory. |
| <code>_PrOut[]</code> | list | List of ndarrays containing the four-vector momentum in laboratory coordinates at the exit to the beam line elements along the locus of the reference particle trajectory. |
| <code>_Rot2LabIn[]</code> | list | List of ndarrays containing the rotation matrices taking RPLC to laboratory coordinates at the entrance to the beam line elements along the locus of the reference particle trajectory. |
| <code>_Rot2LabOut[]</code> | list | List of ndarrays containing the rotation matrices taking RPLC to laboratory coordinates at the exit to the beam line elements along the locus of the reference particle trajectory. |

Table 15: Definition of access methods for the ReferenceParticle class.

| Set method | Get method | Comment |
|---------------|-----------------------|---|
| setRPDebug | getRPDebug | Set/get ReferenceParticle debug flag. |
| setsIn | getsIn | Set/get <code>_sIn</code> |
| setsOut | getsOut | Set/get <code>_sOut</code> |
| setRrIn | getRrIn | Set/get <code>_RrIn</code> |
| setRrOut | getRrOut | Set/get <code>_RrOut</code> |
| setPrIn | getPrIn | Set/get <code>_PrIn</code> |
| setPrOut | getPrOut | Set/get <code>_PrOut</code> |
| | getMomentumIn (iLoc) | Get magnitude of three-vector momentum at entrance of location iLoc |
| | getMomentumOut (iLoc) | Get magnitude of three-vector momentum at exit of location iLoc |
| setRot2LabIn | getRot2LabIn | Set/get <code>_Rot2LabIn</code> |
| setRot2LabOut | getRot2LabOut | Set/get <code>_Rot2LabOut</code> |
| | getb0 (iLoc) | Get β_0 . |
| | getg0b0 (iLoc) | Get $\gamma_0\beta_0$. |
| setAllRP2None | | Set all ReferenceParticle attributes to None. |

Table 16: Processing methods provided by the ReferenceParticle class.

| Method | Argument(s) | Return | Comment |
|------------------------------------|-------------|---------|---|
| setReferenceParticleAtSource () | BLE | boolean | Set ReferenceParticle attributes at source. Returns True if success. |
| setReferenceParticleAtDrift (iBLE) | | boolean | Set ReferenceParticle attributes at BeamLineElement (BLE) instance iBLE. Returns True if success. |

A.2.2.3 Processing methods

Table 16 presents the processing methods provided in the `ReferenceParticle` class.

A.2.2.4 I/o methods

The `ReferenceParticle` class provides no additional i/o methods.

345 A.2.2.5 Utilities

The `ReferenceParticle` class provides no additional utilities.

A.3 Beam and extrapolateBeam

The Beam class is in some sense a "sister" class to Particle. Whereas an instance of Particle records the passage of a particle travelling through the beam line, an instance of Beam records the collective properties of the beam such as emittance, as the beam progresses through the beam line. The beam parameters reported in the attributes of an instance of Beam are obtained by summing over nEvtMax particles to evaluate the covariance matrices by location.

The extrapolatedBeam class is derived from Beam. An instance of extrapolatedBeam calculates the covariance matrix at a location along the beam line and then uses the transfer matrices to propagate the beam envelope.

A.3.1 Beam

A.3.1.1 Instantiation

The call to instantiate the Beam class is:

```
Beam(InputDatafile, nEvtMax, outputCSVfile, startlocation,  
      beamlineSpecificationCSVfile))
```

InputDatafile is either the full path to a data file in one of the formats specified in BeamIO or an instance of the BeamIO class that refers to an existing data file that can be read. nEvtMax is the maximum number of events to read or process using the Beam instance. outputCSVfile is the full path to the output file, in CSV format, containing the beam parameters at the locations traversed by the beam. startlocation is the location along the beam line at which propagation will start; if startlocation is absent or None propagation will start at the source. beamlineSpecificationCSVfile is the CSV file specifying the beam line. beamlineSpecificationCSVfile is kept for backward compatibility. If the first record of InputDatafile contains the specification of the beam line, beamlineSpecificationCSVfile is not required.

A.3.1.2 Instance attributes and access methods

The instance attributes are presented in table 17 and the access methods are summarised in table 18.

A.3.1.3 Processing methods

Table 19 presents the processing methods provided in the Beam class.

A.3.1.4 I/o methods

The Beam class has no i/o methods.

A.3.1.5 Utilities

The utilities provided by the Beam class are listed in table 20.

Table 17: Definition of attributes of instances of the Beam class.

| Attribute | Type | Comment |
|---------------------|-------------|--|
| InputDataFile | Path/BeamIO | Path to, or BeamIO instance of input file. |
| nEvtMax | int | Maximum number of particles to read and process. |
| outputCSVfile | Path | Path to output CSV file to contain beam parameters by location. |
| startlocation | int | Location at which to start beam propagation. |
| BLspecCSVfile | Path | beamlineSpecificationCSVfile, kept for backward compatibility. |
| Location[iLoc] | List | List of locations (int) at which beam parameters are recorded. |
| s[iLoc] | List | List of s coordinates of reference particle at locations at which beam parameters are recorded. |
| nParticles[iLoc] | List | List of number of particles (int) recorded at location iLoc. |
| CovMtrx[iLoc][6, 6] | List | List of covariance matrices (ndarray) by location. |
| sigmaxy[iLoc][2] | List | List of $\sigma_x = \text{sigmaxy}[\text{iLoc}][0]$ and $\sigma_y = \text{sigmaxy}[\text{iLoc}][1]$ (float). |
| emittance[iLoc][5] | List | List of emittance by location: $\epsilon_x = \text{emittance}[\text{iLoc}][0]$, $\epsilon_y = \text{emittance}[\text{iLoc}][1]$, $\epsilon_L = \text{emittance}[\text{iLoc}][2]$, $\epsilon_{4D} = \text{emittance}[\text{iLoc}][3]$, $\epsilon_{6D} = \text{emittance}[\text{iLoc}][4]$. |
| Twiss[iLoc][2][3] | List | List of Twiss parameters by location: $\text{Twiss}[\text{iLoc}][0][0:2] = [\alpha_x, \beta_x, \gamma_x]$, $\text{Twiss}[\text{iLoc}][1][0:2] = [\alpha_y, \beta_y, \gamma_y]$. |

Table 18: Definition of access methods for the Beam class.

| Set method | Get method | Comment |
|---|---|--|
| setInputDataFile setBeamIOread setEvtMax setoutputCSVfile setstartlocation setbeamlineSpecificationCSVfile sets setsigmaxy setEmittance setTwiss resetBeamInstances | getInputDataFile getBeamIOread getEvtMax getoutputCSVfile getstartlocation getbeamlineSpecificationCSVfile sets setsigmaxy setEmittance setTwiss getCovSums getCovMtrx getnParticles getCovarianceMatrix getCovMtrx | Set path to input file. Set instance of BeamIO for input file. Set maximum number of particles to deal with. Set path to output CSV file. Set start location. Set beam line specification file. Set s by location. Set $\sigma_{x,y}$ by location. Set emittance list by location. Set Twiss parameter list by location. Set list of beam instances to []. Get list of sums used to calculate covariance matrices. Get list of covariance matrices by location. Get number of particles entering covariance sums by location. Get list of covariance matrices by location. Get list of covariance matrices by location. |

Table 19: Processing methods provided by the Beam class.

| Method | Argument(s) | Return | Comment |
|-------------------------------|-------------|--------|--|
| initialiseSums() | | | Initialise sums to be used to calculate covariance matrices by location. |
| incrementSums(iPrtcl) | Particle | | Increment sums for covariance matrix calculation for Particle instance iPrtcl. |
| calcCovarianceMatrix() | | | Calculate covariance matrices by location. |
| evaluateBeam(TrackBeam=False) | boolean | | Loop over nEvtMax particles to calculate beam parameters by location. If TrackBeam is True, particles are transported through the beam line. If TrackBeam is False, covariance matrices stored as Beam instance attributes are used. |

Table 20: Utilities provided by the Beam class.

| Method | Argument(s) | Return | Comment |
|--------------------------------|-------------|---------|---|
| cleanBeams () | | boolean | Delete all Beam instances, returns True if successful. |
| printProgression () | | | Print beam parameters by location. |
| getHeader () | | list | Prepare header for CSV file containing beam parameters by location. |
| getLines () | | list | Prepare lines for CSV file containing beam parameters by location. |
| createReport () | | | Interface to Report class to make beam parameter CSV file. |
| plotBeamProgression (plotFILE) | | path | Plot beam parameters by location; plotFILE is full path to plot file. |

A.3.2 extrapolateBeam

A.3.2.1 Instantiation

The call to instantiate the `extrapolateBeam` class is:

```
Beam(InputDatafile, nEvtMax, outputCSVfile, startlocation,  
      beamlineSpecificationCSVfile)
```

The arguments are passed directly to a call to instantiate the parent `Beam` class. In the execution of `extrapolateBeam`, the covariance matrices are calculated from `nEvtMax` at `startlocation`. If `startlocation`, the last location provided in the input data file is used as the source.

A.3.2.2 Instance attributes and access methods

Instance attributes are inherited from `Beam` (table 17). Access methods are also inherited from `Beam` (table 18). The method `resetextrapolateBeamInstances` is provided to reset only the list of instances of `extrapolateBeam`.

A.3.2.3 Processing methods

Table 21 presents the processing methods provided in the `extrapolateBeam` class.

Table 21: Processing methods provided by the `extrapolateBeam` class.

| Method | Argument(s) | Return | Comment |
|--|-------------|--------|--|
| <code>initialiseSums()</code> | Particle | | Initialise sums to be used to calculate covariance matrices at <code>startlocation</code> . |
| <code>incfementSums(iPrtcl)</code> | | | Increment sums for covariance matrix calculation for Particle instance <code>iPrtcl</code> at <code>startlocation</code> . |
| <code>extrapolateCovarianceMatrix()</code> | | | Extrapolate covariance matrices along the beam line by location. |
| <code>extrapolateBeam()</code> | | | Estrapolate beam envelope and beam parameters along the beam line by location. |

A.3.2.4 I/o methods

The `extrapolateBeam` class has no i/o methods.

A.3.2.5 Utilities

The utilities provided by the `extrapolateBeam` class are listed in table 22.

Table 22: Utilities provided by the `extrapolateBeam` class.

| Method | Argument(s) | Return | Comment |
|--------------------------------------|-------------|---------|--|
| <code>cleanextrapolateBeams()</code> | | boolean | Delete all <code>extrapolateBeam</code> instances, returns True if successful. |

A.4 BeamLineElement

A.4.1 Parent class

A.4.1.1 Instantiation

The call to instantiate the `BeamLineElement` class is:

```
400         BeamLineElement(Name, rStrt, vStrt, drStrt, dvStrt)
```

where:

`Name`: (string) is the unique name of the element;

`rStrt`: (`numpy.ndarray(3)`) is the three-vector position in laboratory coordinates of the start of the element;

`vStrt`: (`numpy.ndarray(1,2)`) is the polar, θ , and azimuthal, ϕ , angles that define the y ($i = 0$) and z ($i = 1$)
405 axes of the RPLC coordinate system at the start of the element (`vStrt = [[i], [θ, φ]]`);

`drStrt`: (`numpy.ndarray(3)`) error in the three-vector position with respect to the nominal position; and

`dvStrt`: (`numpy.ndarray(1,2)`) error in the polar and azimuthal angles defining RLPC the y and z axes.

All arguments are required.

A.4.1.2 Instance attributes and access methods

410 Properties common to all beam-line elements are stored as instance attributes of the parent `BeamLineElement` class. The instance attributes are defined in table 23. The attributes are accessed and set using the methods defined in table 24.

A.4.1.3 Processing methods

Table 25 presents the processing methods provided in the `BeamLineElement` class.

415 A.4.1.4 I/o methods

Methods to read and write instance attributes to the files defined using the `BeamIO` package (see section ?? are provided. The calls are:

```
readElement(dataFILE)    and    writeElement(dataFILE);
```

where `dataFILE` is `BeamIO` instance.

A.4.1.5 Utilities

420 Table 26 presents the utilities provided in the `BeamLineElement` class.

Table 23: Definition of attributes of instances of the `BeamLineElement` class. The attributes marked * above the dividing line are required in the call to instantiate the element. The attributes marked † below the dividing line are calculated.

| Attribute | Type | Unit | Comment |
|-------------|---------------|------|--|
| Name* | String | | Name of beam-line element. |
| rStrt* | numpy.ndarray | m | $[x, y, z]$ position of entrance to element in laboratory coordinate system. |
| vStrt* | numpy.ndarray | rad | $[[i], [\theta, \phi]]$ (polar and azimuthal angles) of RPLC y and z axes ($i = 0, 1$ respectively) at start. |
| drStrt* | numpy.ndarray | m | “Error”, $[x, y, z]$, displacement of start from nominal position (not yet implemented). |
| dvStrt* | numpy.ndarray | rad | “Error”, $[[i], [\theta, \phi]]$, deviation in θ and ϕ from nominal axis (not yet implemented). |
| Strt2End† | numpy.ndarray | | 1×3 translation from start of element to end; in laboratory coordinates. Set in derived class. |
| Rot2LbStrt† | numpy.ndarray | | 3×3 rotation matrix that takes RPLC axes to laboratory axes at start. |
| Rot2LbEnd† | numpy.ndarray | | 3×3 rotation matrix that takes RPLC axes to laboratory axes at end. Set in derived class. |
| TrnsMtrx† | numpy.ndarray | | 3×3 transfer matrix. Set in derived class. |

Table 24: Definition of access methods for the BeamLineElement class.

| Set method | Get method | Comment |
|--------------------|----------------------|---|
| setName (Name) | getName () | Set/get name of beam-line element. |
| setStrt (rStrt) | getStrt () | Set/get laboratory $[x, y, z]$ position of entrance. |
| setvStrt (vStrt) | getvStrt () | Set/get RPLC $[\theta, \phi]$ of principal axis at start of element. |
| | getvEnd () | Set/get RPLC $[\theta, \phi]$ of principal axis at end of element. |
| setdrStrt (drStrt) | getdrStrt () | Set/get “error” displacement. |
| setdvStrt (dvStrt) | getdvStrt () | Set/get “error” deviation in $[\theta, \phi]$. |
| setLength (length) | getLength | Set/get increment in s across element, (length for elements that do not bend beam). |
| setRot2LbStrt () | getRot2LbStrt () | Set/get rotation matrix from RPLC axes to laboratory. |
| setRot2LabStrt () | getRot2LabStrt () | Set/get rotation matrix from RPLC to laboratory at start. |
| setStrt2End (t) | getStrt2End () | Set/get displacement vector start to end in laboratory coordinates. setStrt2End takes 1 argument, t, a 1D np.ndarray containing the translation from the start to the end of the element in RPLC. |
| setRot2LbEnd (R) | getRot2LbEnd () | Set/get rotation matrix from RPLC to laboratory at end. setRot2LbEnd takes 1 argument, R, a 2D np.array containing the rotation matrix to be set. |
| | getTransferMatrix () | Get transfer matrix set in derived class. |
| | getLines () | Get lines to write LaTeX specification of element. |

Table 25: Processing methods provided by the BeamLineElement class.

| Method | Argument(s) | Return | Comment |
|----------------------------|-------------------------|-------------------------|--|
| OutsideBeamPipe (R) | Float | Boolean | Returns False if particle is inside beam pipe. If R, radial distance from z axis in RPLC, falls outside beam pipe, returns True. |
| ExpansionParameterFail (R) | Float | Boolean | Calculates an approximate expansion parameter and returns False if the parameter is large (> 1). Not yet used in Transport. |
| Transport (V) | 6×1 np.ndarray | 6×1 np.ndarray | Transport 6D trace-space vector, V, across element. Final trace-space vector returned. |
| Shit2Local (V) | 6×1 np.ndarray | 6×1 np.ndarray | Transform 6D trace-space vector, V, from RPLC to laboratory coordinates. Phase-space vector in laboratory frame returned. |
| Shit2Laboratory (U) | 6×1 np.ndarray | 6×1 np.ndarray | Transform 6D phase-space vector, U, from laboratory coordinates to trace-space coordinates in the RPLC frame. Trace-space vector in RLPC frame returned. |

Table 26: Utilities provided by the BeamLineElement class.

| Method | Argument(s) | Return | Comment |
|---------------------------------|--|--------|--|
| cleaninstances () | | | Delete (using “del”) all instances of the BeamLineElement class. Reset instances list. |
| removeInstance (inst) | Instance of BLE | | Remove instance inst and remove from list of instances of BeamLineElement. |
| visualise (axs, CoordSys, Proj) | axs – Matplotlib “axes” instance CoordSys – string Proj – string | | Manages plotting (visualisation) of element. “Lab” or “RPLC”, coordinate system in which to visualise element. “xz” or “yz” projection to visualise. |

A.4.2 Derived class: Facility (BeamLineElement)

A.4.2.1 Instantiation

The call to instantiate the `Facility` derived class is:

```
FacilityName, rStrt, vStrt, drStrt, dvStrt, p0, VCMV)
```

425 Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`. The `Facility` arguments are translated into instance attributes as described in section A.4.2.2 and defined in table 27.

A.4.2.2 Instance attributes and access methods

The instance attributes are defined in table 27. The attributes are accessed and set using the methods defined in table 28.

Table 27: Definition of attributes of instances of the `Facility (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-------------------|-------|------|---|
| <code>p0</code> | float | MeV | Kinetic energy of reference particle. |
| <code>VCMV</code> | float | m | Radius of vacuum-chamber mother volume. The radius defines edge of the volume at which a particle trajectory is terminated. It may be necessary to introduce a beam pipe later. |

Table 28: Definition of access methods for the `Facility` derived class.

| Set method | Get method | Comment |
|-----------------------------|--------------------------|--|
| <code>setp0 (Name)</code> | <code>getp0 ()</code> | Set/get momentum of reference particle (in MeV). |
| <code>setVCMV (VCMV)</code> | <code>getrVCMV ()</code> | Set/get radius of vacuum chamber mother volume. |

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A.4.2.3 Processing methods

The `Facility` derived class has no processing methods other than those inherited from the parent class.

A.4.2.4 I/o methods

The `Facility` derived class has no i/o methods other than those inherited from the parent class.

435 A.4.2.5 Utilities

The `Facility` derived class has no utilities other than those inherited from the parent class.

A.4.3 Derived class: Drift (BeamLineElement)

A.4.3.1 Instantiation

The call to instantiate the `Drift` derived class is:

440 `Drift(Name, rStrt, vStrt, drStrt, dvStrt, Length)`

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`.

A.4.3.2 Instance attributes and access methods

The instance attributes are defined in table 29. The attributes are accessed and set using the methods defined in table 30.

Table 29: Definition of attributes of instances of the `Drift(BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|---------------------|-------|------|------------------|
| <code>Length</code> | float | m | Length of drift. |

Table 30: Definition of access methods for the `Facility` derived class.

| Set method | Get method | Comment |
|----------------------------------|--------------------------|---------------------------------|
| <code>setLength(Length)</code> | <code>getLength()</code> | Set/get length of drift (in m). |
| <code>setTransferMatrix()</code> | | Set transfer matrix. |

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A.4.3.3 Processing methods

The `Drift` derived class has no processing methods other than those inherited from the parent class.

A.4.3.4 I/o methods

The `Drift` derived class has no i/o methods other than those inherited from the parent class.

450 **A.4.3.5 Utilities**

The `Drift` derived class has no utilities other than those inherited from the parent class.

A.4.4 Derived class: `Aperture(BeamLineElement)`

A.4.4.1 Instantiation

The call to instantiate the `Aperture` derived class is:

455 `Aperture(Name, rStrt, vStrt, drStrt, dvStrt, ParamList)`

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`.

A.4.4.2 Instance attributes and access methods

The instance attributes are defined in table 31. The attributes are accessed and set using the methods defined in table 33.

460

A.4.4.3 Processing methods

The `Aperture` processing method is defined in table 33.

Table 31: Definition of attributes of instances of the `Aperture (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|---|--|--|--|
| <code>ParamList</code> | <code>[]</code> | | List containing aperture parameters. The first parameter is an <code>int</code> and defines the aperture “Type”. The remaining elements in the parameter list are <code>floats</code> with meanings that depend on Type. |
| <code>ParamList[0]</code> <code>ParamList[1]</code> | <code>int</code> <code>float</code> | <code>m</code> | Type= 0; circular Radius of circular aperture |
| <code>ParamList[0]</code> <code>ParamList[1]</code> <code>ParamList[2]</code> | <code>int</code> <code>float</code> <code>float</code> | <code>m</code> <code>m</code> <code>m</code> | Type= 1; Elliptical Radius of elliptical aperture along x_{RPLC} axis Radius of elliptical aperture along y_{RPLC} axis |
| <code>ParamList[0]</code> <code>ParamList[1]</code> <code>ParamList[2]</code> | <code>int</code> <code>float</code> <code>float</code> | <code>m</code> <code>m</code> <code>m</code> | Type= 2; Rectangular Size of aperture along x_{RPLC} axis Size of aperture along y_{RPLC} axis |

Table 32: Definition of access methods for the `Aperture` derived class.

| Set method | Get method | Comment |
|--|--|---|
| <code>setApertureParameters (ParamList)</code> | <code>getType ()</code> <code>getParams ()</code> | Set aperture parameters. Sets Type and parameters depending on Type. Get Type of aperture. Get aperture parameters. |

Table 33: Utilities provided by the `Aperture` derived class.

| Method | Argument(s) | Return | Comment |
|----------------------------|-------------------------|--|---|
| <code>Transport (V)</code> | <code>np.ndarray</code> | <code>np.ndarray</code> or <code>None</code> | Transport trace-space vector <code>V</code> . If <code>V</code> falls outside of the aperture, return <code>None</code> . |

A.4.4.4 I/o methods

The `Aperture` derived class has no i/o methods other than those inherited from the parent class.

A.4.4.5 Utilities

The `Aperture` derived class has no utilities other than those inherited from the parent class.

A.4.5 Derived class: `FocusQuadrupole (BeamLineElement)`

A.4.5.1 Instantiation

The call to instantiate the `FocusQuadrupole` derived class is:

```
FocusQuadrupole (Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength,
                  kFQ)
```

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`. The quadrupole `Length` is required together with either the field gradient, `Strength` (equation 18), or the quadrupole k parameter, `kFQ` (equation 20).

A.4.5.2 Instance attributes and access methods

The instance attributes are defined in table 34. The attributes are accessed and set using the methods defined in table 36.

Table 34: Definition of attributes of instances of the `FocusQuadrupole (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------------------|-------|-----------------|---|
| <code>FQmode</code> | int | | If 0, use particle momentum in calculation of transfer matrix; if 1, use reference particle momentum. |
| <code>Length</code> | float | m | Effective length of quadrupole. |
| <code>Strength</code> | float | T/m | Magnetic field gradient; required if <code>kFQ</code> is not given. |
| <code>kFQ</code> | float | m^{-2} | Quadrupole k parameter. |

Table 35: Definition of access methods for the `FocusQuadrupole` derived class.

| Set method | Get method | Comment |
|-----------------------------------|-----------------------------|--|
| <code>setFQmode (FQmode)</code> | <code>getFQmode ()</code> | Set/get <code>FQmode</code> . |
| <code>setLength (Length)</code> | <code>getLength ()</code> | Set/get length. |
| <code>setStrength (Length)</code> | <code>getStrength ()</code> | Set/get strength (field gradient). |
| <code>setKfQ (Length)</code> | <code>getKfQ ()</code> | Set/get <code>kFQ</code> , quadrupole k parameter. |

A.4.5.3 Processing methods

The `FocusQuadrupole` processing methods are defined in table 36.

A.4.5.4 I/o methods

The `Focusquadrupole` derived class has no i/o methods other than those inherited from the parent class.

Table 36: Utilities provided by the `FocusQuadrupole` derived class.

| Method | Argument(s) | Return | Comment |
|-----------------------------|-------------|--------|---|
| <code>calcKfQ()</code> | | float | Calculates <code>kFQ</code> if strength is given in instance attributes. |
| <code>calcStrength()</code> | | float | Calculates <code>Strength</code> if <code>kFQ</code> is given in instance attributes. |

A.4.5.5 Utilities

The `FocusQuadrupole` derived class has no utilities other than those inherited from the parent class.

A.4.6 Derived class: `DefocusQuadrupole (BeamLineElement)`

A.4.6.1 Instantiation

The call to instantiate the `DefocusQuadrupole` derived class is:

```
DefocusQuadrupole(Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength,
                  kDQ)
```

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`. The quadrupole `Length` is required together with either the field gradient, `Strength` (equation 18), or the quadrupole k parameter, `kDQ` (equation 20).

A.4.6.2 Instance attributes and access methods

The instance attributes are defined in table 37. The attributes are accessed and set using the methods defined in table 39.

Table 37: Definition of attributes of instances of the `DefocusQuadrupole (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------------------|-------|-----------------|---|
| <code>DQmode</code> | int | | If 0, use particle momentum in calculation of transfer matrix; if 1, use reference particle momentum. |
| <code>Length</code> | float | m | Effective length of quadrupole. |
| <code>Strength</code> | float | T/m | Magnetic field gradient; required if <code>kDQ</code> is not given. |
| <code>kDQ</code> | float | m^{-2} | Quadrupole k parameter. |

A.4.6.3 Processing methods

The `DefocusQuadrupole` processing methods are defined in table 39.

A.4.6.4 I/o methods

The `Defocusquadrupole` derived class has no i/o methods other than those inherited from the parent class.

A.4.6.5 Utilities

The `Defocusquadrupole` derived class has no utilities other than those inherited from the parent class.

Table 38: Definition of access methods for the `DefocusQuadrupole` derived class.

| Set method | Get method | Comment |
|----------------------------------|----------------------------|--|
| <code>setDQmode(DQmode)</code> | <code>getDQmode()</code> | Set/get DQmode. |
| <code>setLength(Length)</code> | <code>getLength()</code> | Set/get length. |
| <code>setStrength(Length)</code> | <code>getStrength()</code> | Set/get strength (field gradient). |
| <code>setKDQ(Length)</code> | <code>getKDQ()</code> | Set/get kDQ, quadrupole k parameter. |

Table 39: Utilities provided by the `DefocusQuadrupole` derived class.

| Method | Argument(s) | Return | Comment |
|-----------------------------|-------------|--------|--|
| <code>calcKDQ()</code> | | float | Calculates kDQ if strength is specified. |
| <code>calcStrength()</code> | | float | Calculates Strength if kDQ is specified. |

A.4.7 Derived class: `SectorDipole` (`BeamLineElement`)

A.4.7.1 Instantiation

The call to instantiate the `SectorDipole` derived class is:

```
SectorDipole(Name, rStrt, vStrt, drStrt, dvStrt, Angle, B)
```

505 Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`.

The orientation of the RLPC coordinate axes with respect to those of the laboratory frame changes from the start of sector dipole to its end. Referring to figure 2, the vector, \mathbf{v}_{ES} , that translates the origin of the RLPC coordinate system at the start of the sector dipole to the origin of the RLPC coordinate system at its end is given
510 by:

$$\mathbf{v}_{\text{ES}} = 2\rho_0 \sin\left(\frac{\phi}{2}\right) \begin{pmatrix} \sin\left(\frac{\phi}{2}\right) \\ 0 \\ \cos\left(\frac{\phi}{2}\right) \end{pmatrix}; \quad (47)$$

where ρ_0 is the radius of the circular locus of the trajectory of the reference particle. If the rotation matrix taking the RPLC axes at the start of the sector dipole to the laboratory coordinate axes is $\underline{\underline{R}}_{\text{S}}$, then the vector, $\mathbf{v}_{\text{ES}}^{\text{lab}}$, that translates from the start of the sector dipole to its end in laboratory coordinates is given by:

$$\mathbf{v}_{\text{ES}}^{\text{lab}} = \underline{\underline{R}}_{\text{S}} \mathbf{v}_{\text{ES}}. \quad (48)$$

515 The rotation matrix that transforms from the RPLC system at the end of the sector dipole to the laboratory coordinate system, $\underline{\underline{R}}_{\text{E}}$ is given by:

$$\underline{\underline{R}}_{\text{E}} = \underline{\underline{R}}_{\text{S}} \underline{\underline{R}}; \quad (49)$$

where:

$$\underline{\underline{R}} = \begin{pmatrix} \cos \phi & 0 & -\sin \phi \\ 0 & 1 & 0 \\ \sin \phi & 0 & \cos \phi \end{pmatrix}. \quad (50)$$

A.4.7.2 Instance attributes and access methods

The instance attributes are defined in table 40. The attributes are accessed and set using the methods defined in table 41.

Table 40: Definition of attributes of instances of the `SectorDipole (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|------|--|
| Angle | float | rad | Angle through which sector dipole bends positive reference particle. |
| B | float | T | Magnetic field. |

Table 41: Definition of access methods for the `SectorDipole` derived class.

| Set method | Get method | Comment |
|-------------------------------|---------------------------|---|
| <code>setAngle (Angle)</code> | <code>getAngle ()</code> | Set/get bending angle. |
| <code>setB (B)</code> | <code>getB ()</code> | Set/get dipole magnetic field. |
| <code>setLength ()</code> | <code>getLength ()</code> | Set/get length of reference particle trajectory through sector dipole (arc length). |

A.4.7.3 Processing methods

The `SectorDipole` derived class has no processing methods other than those inherited from the parent class.

A.4.7.4 I/o methods

The `SectorDipole` derived class has no i/o methods other than those inherited from the parent class.

A.4.7.5 Utilities

The `SectorDipole` derived class has no utilities other than those inherited from the parent class.

A.4.8 Derived class: `Solenoid (BeamLineElement)`

A.4.8.1 Instantiation

The call to instantiate the `Solenoid` derived class is:

```
Solenoid (Name, rStrt, vStrt, drStrt, dvStrt, Length, Strength, kSol)
```

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`. The solenoid `Length` is required together with either the magnetic field strength, `Strength` or the solenoid k parameter, `kSol` (equation 23).

A.4.8.2 Instance attributes and access methods

The instance attributes are defined in table 42. The attributes are accessed and set using the methods defined in table 44.

A.4.8.3 Processing methods

The `Solenoid` processing method is defined in table 44.

A.4.8.4 I/o methods

The `Solenoid` derived class has no i/o methods other than those inherited from the parent class.

Table 42: Definition of attributes of instances of the `Solenoid(BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|-----------------|--|
| Length | float | m | Effective length of solenoid. |
| Strength | float | T/m | Magnetic field gradient; required if kSol is not given. |
| kSol | float | m ⁻² | GaborLens <i>k</i> parameter required if Strength not given. |

Table 43: Definition of access methods for the `Solenoid` derived class.

| Set method | Get method | Comment |
|-------------------|---------------|---|
| setLength(Length) | getLength() | Set/get length. |
| setStrength(B) | getStrength() | Set/get strength (solenoid magnetic field). |
| setKSol(Length) | getKFQ() | Set/get kSol, solenoid <i>k</i> parameter. |

A.4.8.5 Utilities

The `Solenoid` derived class has no utilities other than those inherited from the parent class.

Table 44: Utilities provided by the `Solenoid` derived class.

| Method | Argument(s) | Return | Comment |
|----------------|-------------|--------|---|
| calckSol() | | float | Calculates kSol if strength is specified. |
| calcStrength() | | float | Calculates Strength if kSol is specified. |

A.4.9 Derived class: `GaborLens(BeamLineElement)`

A.4.9.1 Instantiation

545 The call to instantiate the `GaborLens` derived class is:

```
GaborLens(Name, rStrt, vStrt, drStrt, dvStrt, Bz, VA, RA, Rp, Length,
          kSol)
```

550 Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`. The Gabor lens `Length` is required together with either the parameters `Bz`, `VA`, `RA`, and `Rp` corresponding, respectively, to the parameters B_z , V_A , V_A and R_p defined in section 4.4, or `kSol`, the solenoid strength parameter of the equivalent solenoid (see section 4.4). The effective electron number density inside the trap is calculated using either `Bz`, `VA`, `RA` and `Rp` or `kSol`.

A.4.9.2 Instance attributes and access methods

555 The instance attributes are defined in table 45. The attributes are accessed and set using the methods defined in table 46.

A.4.9.3 Processing methods

The `GaborLens` processing method is defined in table 44.

Table 45: Definition of attributes of instances of the `GaborLens (BeamLineElement)` derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-----------|-------|-----------------|---|
| Bz | float | T | Effective length of Gabor lens. |
| VA | float | V | Effective length of Gabor lens. |
| RA | float | m | Effective length of Gabor lens. |
| RP | float | m | Effective length of Gabor lens. |
| Length | float | m | Effective length of Gabor lens. |
| Strength | float | T/m | Magnetic field gradient; required if kSol is not given. |
| kSol | float | m ⁻² | <i>k</i> parameter of the solenoid with the equivalent focusing strength. |

Table 46: Definition of access methods for the `GaborLens` derived class.

| Set method | Get method | Comment |
|------------------------|-----------------------|--|
| setBz (Bz) | getBz () | Set/get magnetic field of the Penning-Malmberg trap. |
| setVA (VA) | getVA () | Set/get anode voltage of the Penning-Malmberg trap. |
| setRA (RA) | getRA () | Set/get radius of the anode of the Penning-Malmberg trap. |
| setRP (RP) | getRP () | Set/get magnetic effective radius of the plasma confined within the Penning-Malmberg trap. |
| setLength (Length) | getLength () | Set/get effective length of the lens. |
| setStrength (Strength) | getStrength () | Set/get k-parameter of the solenoid with the equivalent focal length. |
| setElectronDensity () | getElectronDensity () | Set/get electron density. |

A.4.9.4 I/o methods

The `GaborLens` derived class has no i/o methods other than those inherited from the parent class.

A.4.9.5 Utilities

The `GaborLens` derived class has no utilities other than those inherited from the parent class.

A.4.10 Derived class: `CylindricalRFCavity (BeamLineElement)`

A.4.10.1 Instantiation

The call to instantiate the `CylindricalRFCavity` derived class is:

```
CylindricalRFCavity (Name, rStrt, vStrt, drStrt, dvStrt, Gradient,
                     Frequency, Phase)
```

Parent class arguments `Name`, `rStrt`, `vStrt`, `drStrt`, and `dvStrt` are described in section A.4.1.2. These arguments are passed directly to `BeamLineElement`.

A.4.10.2 Instance attributes and access methods

570 The instance attributes are defined in table 47. The attributes are accessed and set using the methods defined in table 48.

Table 47: Definition of attributes of instances of the `CylindricalRFCavity` (`BeamLineElement`) derived class. All attributes are required in the call to instantiate the element.

| Attribute | Type | Unit | Comment |
|-------------------|-------|------|---|
| Gradient | float | MV/m | Peak electric field gradient on axis. |
| Frequency | float | MHz | Resonant frequency. |
| Phase | float | rad | Phase cavity at time reference particle crosses centre of cavity, “linac convention”. |
| TransitTimeFactor | float | MV | Transit time factor (equation ??). |
| V0 | float | | Peak voltage. |
| alpha | float | | α parameter defined in equation ??. |
| wperp | float | | ω_{\perp} parameter defined in equation ??. |
| cperp | float | | c_{\perp} parameter defined in equation ??. |
| sperp | float | | s_{\perp} parameter defined in equation ??. |
| wprll | float | | ω_{\parallel} parameter defined in equation ??. |
| cprll | float | | c_{\parallel} parameter defined in equation ??. |
| sprll | float | | s_{\parallel} parameter defined in equation ??. |

A.4.10.3 Processing methods

The `CylindricalRFCavity` derived class has no processing methods other than those inherited from the parent class.

575 A.4.10.4 I/o methods

The `CylindricalRFCavity` derived class has no i/o methods other than those inherited from the parent class.

A.4.10.5 Utilities

The `CylindricalRFCavity` derived class has no utilities other than those inherited from the parent class.

580 A.4.10.6 Processing methods

The `CylindricalRFCavity` dericed class has no processing methods.

Table 48: Definition of access methods for the `CylindricalRFCavity` derived class.

| Set method | Get method | Comment |
|---|--------------------------------------|---------------------------------------|
| <code>setGradient (Gradient)</code> | <code>getGradient ()</code> | Set/get peak electric field gradient. |
| <code>setFrequency (Frequency)</code> | <code>getFrequency ()</code> | Set/get frequency. |
| <code>setAngularFrequency (AngFreq)</code> | <code>getAngularFrequency ()</code> | Set/get angular frequency. |
| <code>setPhase (Phase)</code> | <code>getPhase ()</code> | Set/get phase. |
| <code>setWaveNumber (WaveNumber)</code> | <code>getWaveNumber ()</code> | Set/get wavenumber. |
| <code>setLength (Length)</code> | <code>getLength ()</code> | Set/get Length. |
| <code>setRadius (Radius)</code> | <code>getRadius ()</code> | Set/get Radius. |
| <code>setTransitTimeFactor (TransitTimeFactor)</code> | <code>getTransitTimeFactor ()</code> | Set/get TransitTimeFactor. |
| <code>setV0 (V0)</code> | <code>getV0 ()</code> | Set/get peak voltage. |
| <code>setalpha (alpha)</code> | <code>getalpha ()</code> | Set/get alpha. |
| <code>setwperp (wperp)</code> | <code>getwperp ()</code> | Set/get wperp. |
| <code>setcperp (cperp)</code> | <code>getcperp ()</code> | Set/get cperp. |
| <code>setsperp (sperp)</code> | <code>getsperp ()</code> | Set/get sperp. |
| <code>setwprll (wprll)</code> | <code>getwprll ()</code> | Set/get wprll. |
| <code>setcprll (cprll)</code> | <code>getcprll ()</code> | Set/get cprll. |
| <code>setsprll (sprll)</code> | <code>getsprll ()</code> | Set/get sprll. |
| <code>setmrf (mrf)</code> | <code>getmrf ()</code> | Set/get mrf. |

A.5 UserFramework

`UserFramework` is a module that provides a set of methods used in the code provided to allow users easy access to the code and data. The following methods are provided:

`startAnalysis (argv)`: processes input flags passed in call to run script.

Argument:

`argv`: list of arguments passed to `main` by call to run script.

Returns:

`Success`: (boolean) True if processing successful.

`Debug`: (boolean) Set to True if flag `-d` is set to True.

`inputfile`: (path) full path to input file; set using flag `-y`.

`outputfile`: (path) full path to output file; set using flag `-o`.

`nEvts`: (integer) number of events to process; set using flag `-n`.

`bdsimfile`: (path) full path to bdsim format file; set using flag `-z`.

`beamspecfile`: (path) full path to beam specification CSV file; set using flag `-b`.

`handleFILES (beamspecfile, inputfile, outputfile, bdsimFILE=False)`: File handling method to check files exist and create relevant `BeamIO` instances.

Arguments:

`beamspecfile`: (path) full path to beam specification CSV file;

inputfile: (path) full path to input file;
outputfile: (path) full path to output file;
bdsimfile: (path) full path to bdsim format file.

Returns:

Success: (boolean) True if file handling successful.
ibmIOOr: (BeamIO) instance of BeamIO class for file to be read.
ibmIOw: (BeamIO) instance of BeamIO class for file to be written.

EventLoop(iUsrAnl, ibmIOOr, ibmIOw, nEvtsIn): executes loop over nEvtsIn events. Reads event record or generates event if ibmIOOr=None, and handles end-of-file. Passes control to UserAnal.EventLoop

Arguments:

iUsrAnl: (UserAnal) instance.
ibmIOOr: (BeamIO) instance of BeamIO class for file to be read.
ibmIOw: (BeamIO) instance of BeamIO class for file to be written.
nEvtsIn: (integer) number of events to process.

Returns:

Success: (boolean) True if successful.

A.6 visualise

The visualise class manages the visualisation of the beam line and particles traversing it.

A.6.1 Instantiation

The call to instantiate the visualise class is:

```
Beam(CoordSys, Projection)
```

CoordSys (string) is either “RPLC” to visualise the beam line in the reference particle local coordinate system or “Lab”. Projection (string) is either “xs” (RPLC) or “xz” (lab) to visualise the xs or xz projecton and eithed “ys” (RPLC) or “yz” (lab) to visualise the xs or xz projecton.

A.6.2 Instance attributes and access methods

The instance attributes are presented in table 49 and the access methods are summarised in table 50.

Table 49: Definition of attributes of instances of the visualise class.

| Attribute | Type | Comment |
|------------|--------|--|
| CoordSys | String | Either “RPLC” to visualise the in the reference particle local coordinate system or “Lab”. |
| Projection | String | Either “xs” (RPLC) or “xz” (lab) to visualise the xs or xz projecton and eithed “ys” (RPLC) or “yz” (lab) to visualise the xs or xz projecton. |

A.6.3 Processing methods

Table 51 presents the processing methods provided in the visualise class.

Table 50: Definition of access methods for the `visualise` class.

| Set method | Get method | Comment |
|----------------------------|----------------------------|--|
| <code>setCoordSys</code> | <code>getCoordSys</code> | Set coordinate system for visualisation. |
| <code>setProjection</code> | <code>setProjection</code> | Set projection for visualisation. |

Table 51: Processing methods provided by the `visualise` class.

| Method | Argument(s) | Return | Comment |
|--------------------------------------|---------------|--------|--|
| <code>Particles(axes, nPrtcl)</code> | plot, integer | | Manage plotting of <code>nPrtcl</code> particles on <code>matplotlib axes</code> instance. |
| <code>BeamLine(axes)</code> | plot | | Manage plotting of beam line on <code>matplotlib axes</code> instance. |

A.6.4 I/o methods

The `visualise` class has no i/o methods.

A.6.5 Utilities

The `visualise` class has no i/o methods.

635 A.7 BeamIO

The `BeamIO` class provides interfaces to the reading and writing of beam specification and beam data files. Each file is managed through an instance of the `BeamIO` class or a class derived from it.

A.7.1 Instantiation

The call to instantiate the `BeamIO` class is:

640 `BeamIO(datafilePath, datafileName, create, BDSIMfile)`

`datafilePath`: (string) Path to directory in which input file is to be found, or, in which output file is to be created. `datafilePath` can be set to `None` if the full path is specified in `datafileName`.

`datafileName`: (string) File name (string) which, when appended to `datafilePath` gives the full path to the input or output data file, or. full path to the input or output file.

645 `create`: (boolean) if true indicates that the file must be created. If a file exists at the location specified by `datafilePath` and `datafileName` it will be overwritten.

`BDSIMfile`: (boolean) If True then the file is to be read or written in `BDSIMfile` format.

A.7.2 Instance attributes and access methods

The `BeamIO` instance attributes are presented in table 52 and the access methods are summarised in table 53.

Table 52: Definition of attributes of instances of the BeamIO class.

| Attribute | Type | Comment |
|-----------------|---------|--|
| dataFILE | Path | Full path to data file. |
| Read1stRecord | Boolean | True if first record has been read from file. |
| dataFILEVersion | Integer | For BeamIO files version number identifying file format. |
| create | Boolean | True if data file is to be created. |
| BDSIMfile | Boolean | True id reading or writing a BDSim file. |

Table 53: Definition of access methods for the BeamIO class.

| Set method | Get method | Comment |
|--------------------|--------------------|---|
| setpathFILE | getpathFILE | Set/get path to directory containing data file. |
| setdataFILE | getdataFILE | Set/get full path to data file. |
| setReadFirstRecord | getReadFirstRecord | Set/get flag indicating whether the first record has been read. |
| setcreate | getcreate | Set/get flag indicating whether data file is to be created. |
| setdataFILEVersion | getdataFILEVersion | Set/get BeamIO version number. |
| setBDSIMfile | getBDSIMfile | Set/get flag indicating whether the data file is in BDSIM format. |

650 A.7.3 Processing methods

The BeamIO class has no processing methods.

A.7.4 I/o methods

Table 54 presents the i/o methods provided by the BeamIO class.

A.7.5 Utilities

655 Table 55 presents the utilities provided by the BeamIO class.

Table 54: I/o methods provided by the BeamIO class.

| Method | Argument(s) | Return | Comment |
|--|-------------|---------|--|
| <code>readBeamDataRecord()</code> | Path | Boolean | Manages reading/writing of a record from/to the data file. Returns a boolean, EOF, set to True of end of file has been detected. |
| <code>readVersion()</code> | | Integer | Reads data-file format version number from file. Returns integer version number. |
| <code>flushNclosedataFile(dataFILE)</code> | | | Flush and close data dataFILE at end of processing. |

Table 55: Utilities provided by the BeamIO class.

| Method | Argument(s) | Return | Comment |
|---------------------------------|-------------|--------|--|
| <code>resetinstances()</code> | | | Class method. Sets list of instances to []. |
| <code>cleanBeamIOfiles()</code> | | | Class method. Delete BeamIO instances and reset list of instances. |

B Set-up and run

Introduction

This section summarises the steps needed to set-up and run the linear optics simulation of the LhARA beam line. A summary of the tasks that the software suite performs will be documented in due course. The code has been developed in python; python 3 is assumed.

Getting the code

The linear optics package is maintained using the GitHub version-control system. The latest release can be downloaded from:

```
\centerline{
  \href{https://github.com/ImperialCollegeLondon/LhARALinearOptics.git}{https://}
}
```

Dependencies and required packages

The linear optics code requires the following packages:

- Python modules: `scipy` and `matplotlib`.

It may be convenient to run the package in a “virtual environment”. To set this up, after updating your python installation to python 3.9, execute the following commands:

1. `python3 -m venv --system-site-packages venv`
 - This creates the director `venv` that contains files related to the virtual environment.
2. `source venv/bin/activate`
3. `python -m pip install pandas scipy matplotlib`

To exit from the virtual environment, execute the command `deactivate`. The command `source venv/bin/activate` places you back into the virtual environment.

The Imperial HEP linux cluster provides python 3.9.18 by default.

Unpacking the code, directories, and running the tests

After downloading the package from GitHub, or cloning the repository, you will find a “`README.md`” file which provides some orientation and instructions to run the code. In particular, a bash script “`startup.bash`” is provided which:

- Sets the “`LhARAOpticsPATH`” environment variable so that the files that hold constants etc. required by the code can be located; and
- Adds “`01-Code`” (see below) to the `PYTHONPATH`. The scripts in “`02-Tests`” (see below) may then be run with the command “`python 02-Tests/<filename>.py`”.

Below the top directory, the directory structure in which the code is presented is:

`01-Code`: contains the python implementation as a series of modules. Each module contains a single class or a related set of methods.

`02-Tests`: contains self-contained test scripts that run the various methods and simulation packages defined in the code directory.

`11-Parameters`: contains the parameter set used to specify the various beam lines presently implemented.

The instructions in the `README.md` file should be followed to set up and run the code.

695 Running the code

Execute "startup.bash" from the top directory (i.e. run the bash command "source startup.bash"). This will:

- Set up "LhARAOpticsPATH"; and
- Add "01-Code" to the PYTHONPATH. The scripts in "02-Tests" may then be run with the command
700 "python 02-Tests/<filename>.py";
- Example scripts are provided in "03-Scripts", these can be used first to "Run" the simulation and then to "Read" the data file produced. Example scripts are provided for the DRACO, LION, and LhARA Stage 1 beam lines.