

# Derivatives

## Abstract

*The Derivative of any function  $f(x)$  is the function  $f'(x)$  for which  $\forall$*

## The Limit Definition of Derivatives

$$\frac{d}{dx}f(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow a} \frac{f(h) - f(a)}{h - a}$$

## Derivative Rules

- $\frac{d}{dx}x^a = ax^{a-1}$
- $\frac{d}{dx}f(x)g(x) = f'(x)g(x) + f(x)g'(x)$
- $\frac{d}{dx}f(g(x)) = f'(g(x))g'(x)$
- $\frac{d}{dx}\sin(x) = \cos(x)$
- $\frac{d}{dx}e^x = e^x$
- $\frac{d}{dx}a^x = a^x \ln(a)$
- $\frac{d}{dx}f(x) \pm g(x) \pm \dots = f'(x) \pm g'(x) \pm \dots$
- $\frac{d}{dx} \frac{f(x)}{g(x)} = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$
- $\frac{d}{dx}f^{-1}(x) = \frac{1}{f'(f^{-1}(x))}$
- $\frac{d}{dx}\cos(x) = -\sin x$
- $\frac{d}{dx}\ln(x) = \frac{1}{x}$