



# Something about Cryptography

1phan

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# What is cryptography?

- 什么是密码学?
- 需要了解什么?
- 常用的工具?



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# CONTENTS

- 
- A large, stylized silhouette of a human head in profile, facing left. The interior of the head is filled with various white icons representing different concepts: a picture, a magnifying glass, a folder, an alarm clock, a film strip, a camera, a smartphone, a lightbulb, and a microscope. The silhouette is outlined with a dashed yellow border.
- 1 流加密
- 2 块加密
- 3 分组密码模式
- 4 公钥算法 (RSA)
- 5 RSA算法使用中较容易犯的错误





# XMAN XMAN

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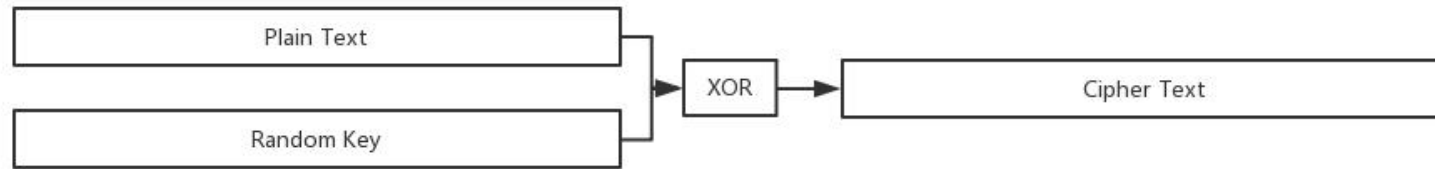
流加密

What is?

# OTP



- OTP——完善保密性



# OTP



- 为什么它是绝对安全的？
- 随机数 XOR 0 == ?
- 随机数 XOR 1 == ?

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# 熵



- 不确定性的量度
- 如英语有26个字母，假如每个字母在文章中出现次数平均的话，每个字母的讯息量为？（4.7）

$$H(X) = E[I(X)] = E[-\ln(P(X))]$$

$$H(X) = \sum_i P(x_i) I(x_i) = - \sum_i P(x_i) \log_b P(x_i).$$



# TEST



- 现有一段128bits长的随机数，一段128bits长的明文（这段明文包含了72bits的信息）
- 将他们 XOR 成一段128bits的密文
- 密文中包括了多少bits的信息？

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- 信息不会凭空产生！
- 也不会凭空消失！

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# OTP VS Pseudorandom generator



- 安全
- 密钥过长

- 密钥足够短
- 不是信息论安全的

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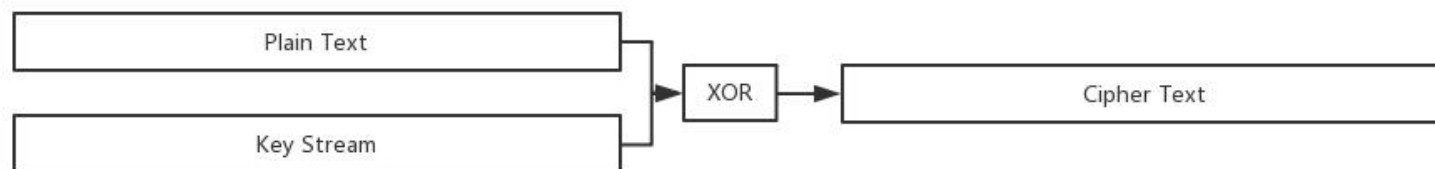
我们想要一个安全性与可用性之间的平衡



# 流加密



- 一个伪随机数生成器
- 一个简单的运算 (XOR)





# 伪随机数生成器



- glibc rand ?

```
seeding_stage() // (code omitted here, see the description from above link)

for (i=344; i<MAX; i++)
{
    r[i] = r[i-31] + r[i-3];
    val = ((unsigned int) r[i]) >> 1;
}
```

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# 伪随机数生成器



- 线性同余?

$$N_{j+1} \equiv (A \times N_j + B) \pmod{M}$$

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# 统计学伪随机数生成器VS密码学安全伪随机数生成器



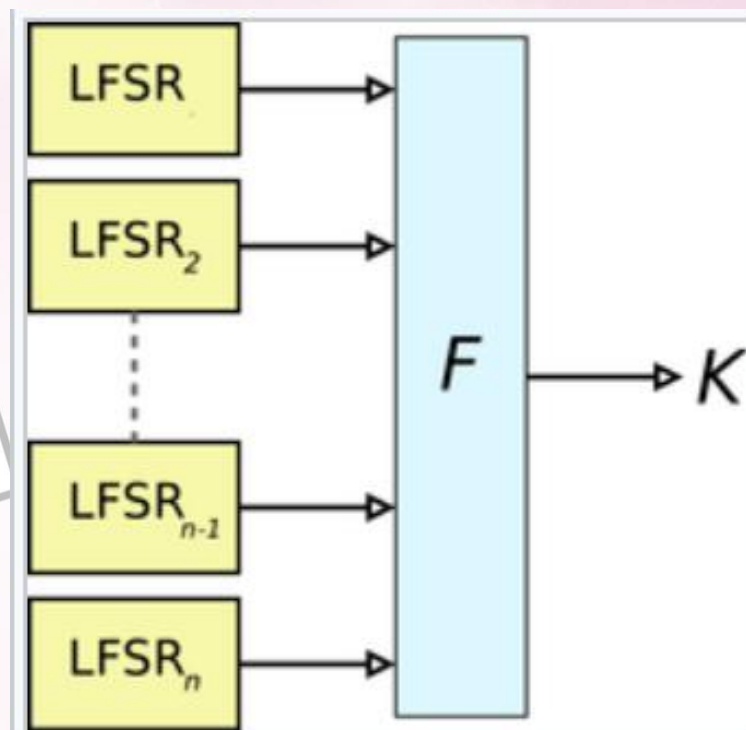
- 伪随机数生成器的内部状态可否轻易地由其输出演算得知

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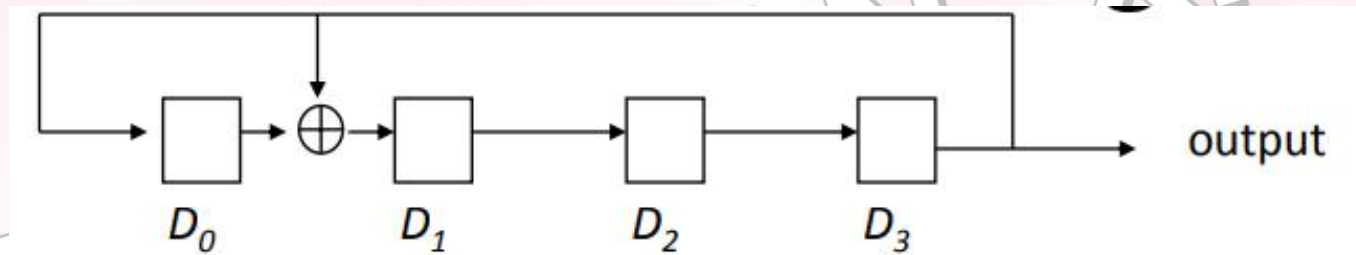
# 安全的随机数生成器



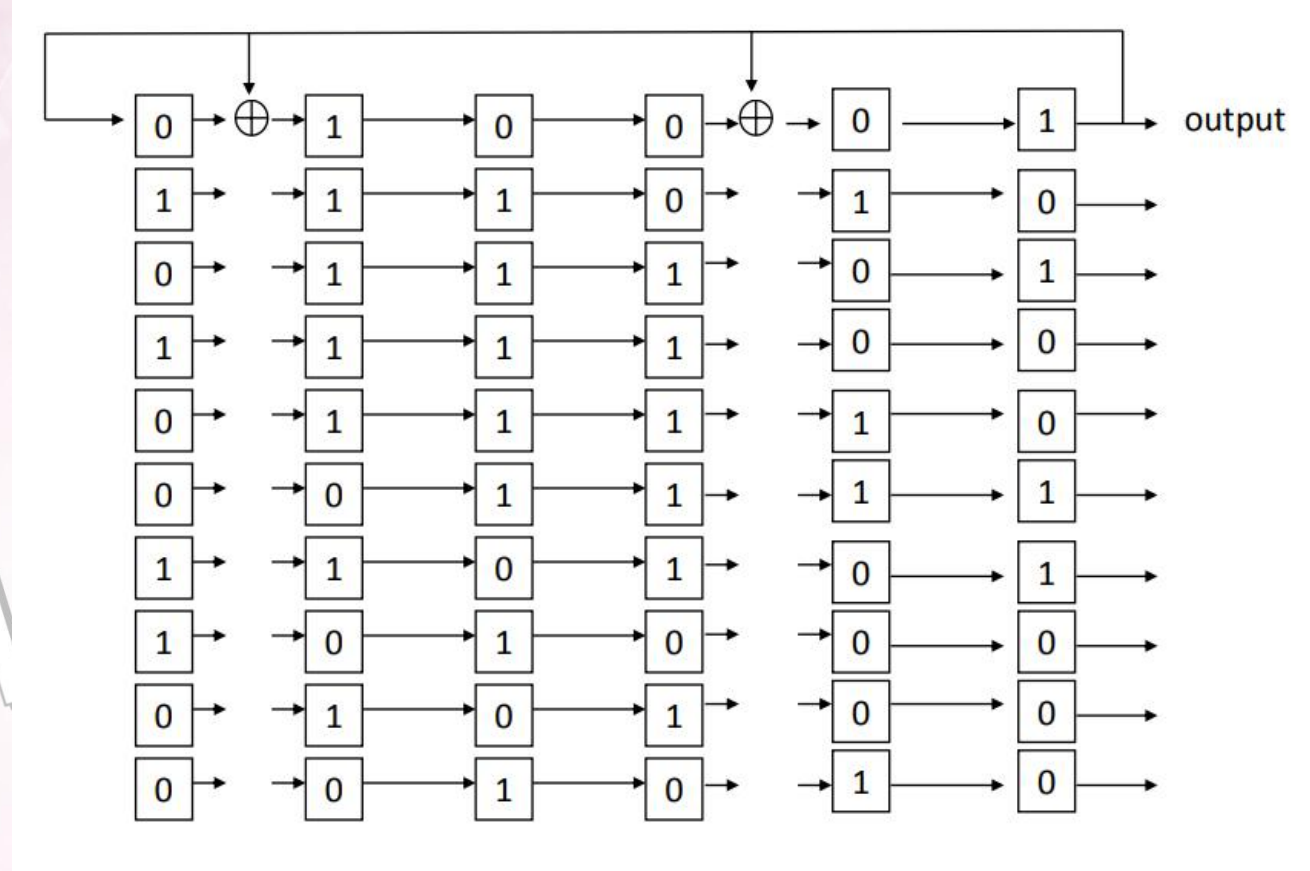


# LFSR（线性反馈移位寄存器）

- 因为寄存器具有有限数量的可能状态，所以它最终必须进入重复循环。然而，具有良好选择的反馈功能的LFSR可以产生随机出现且具有非常长周期的比特序列。



- seed: 1111
- 1011-->1
- 1001-->1
- 1000-->1



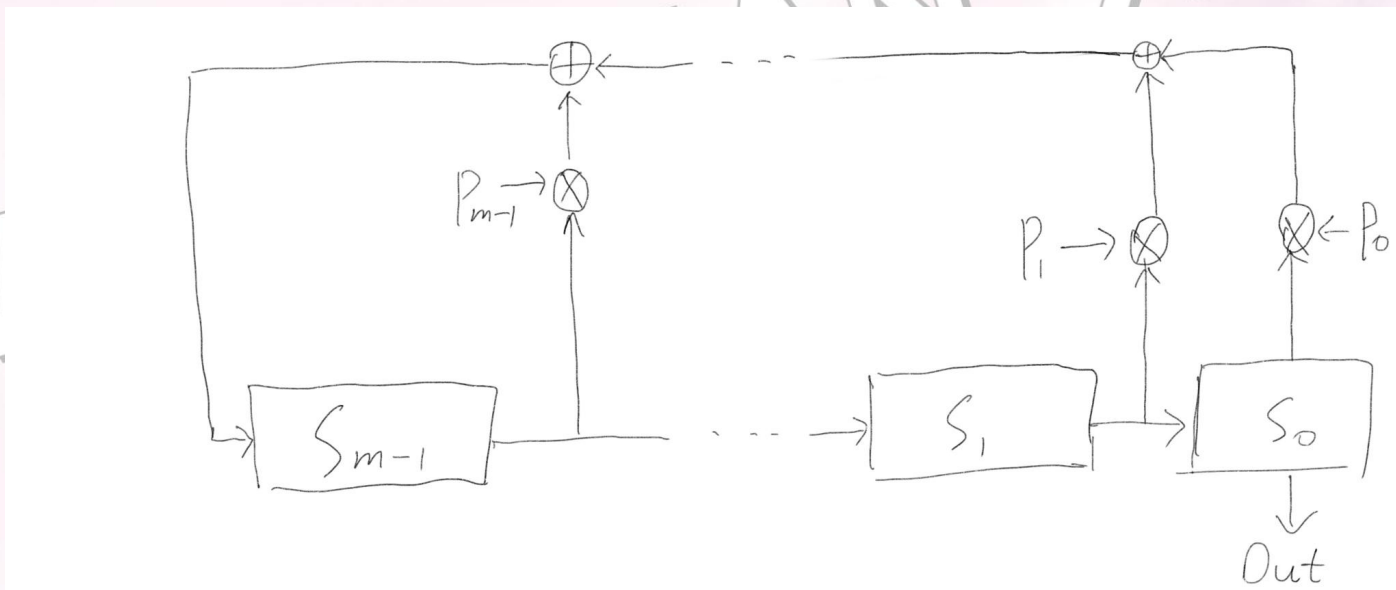




# LFSR的数学描述

- 得到最长LFSR  $\iff P(X)$ 为本原多项式

$$P(x) = x^m + p_{m-1}x^{m-1} + \dots + p_1x + p_0$$



# LFSR不同长度的例子

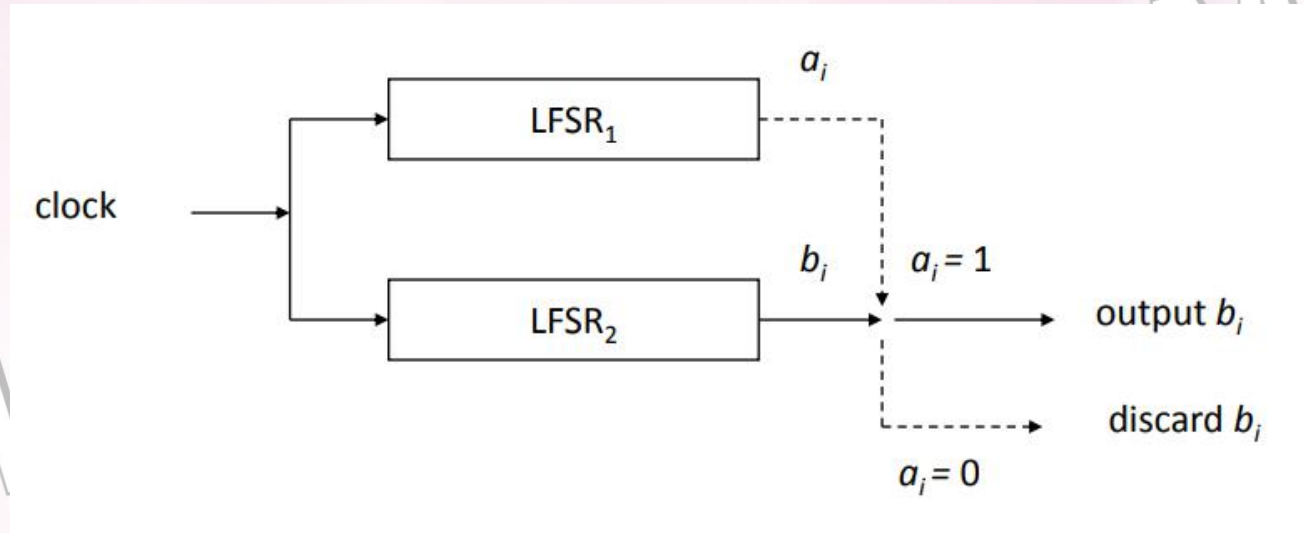
- $X^4 + X + 1$
- $X^4 + X^3 + X^2 + X + 1$



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# Shrinking Generator

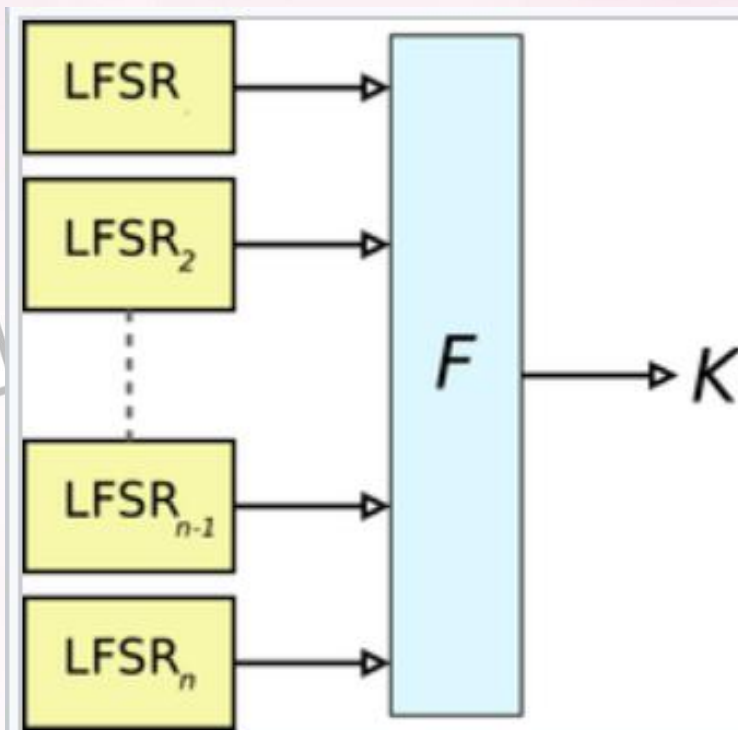




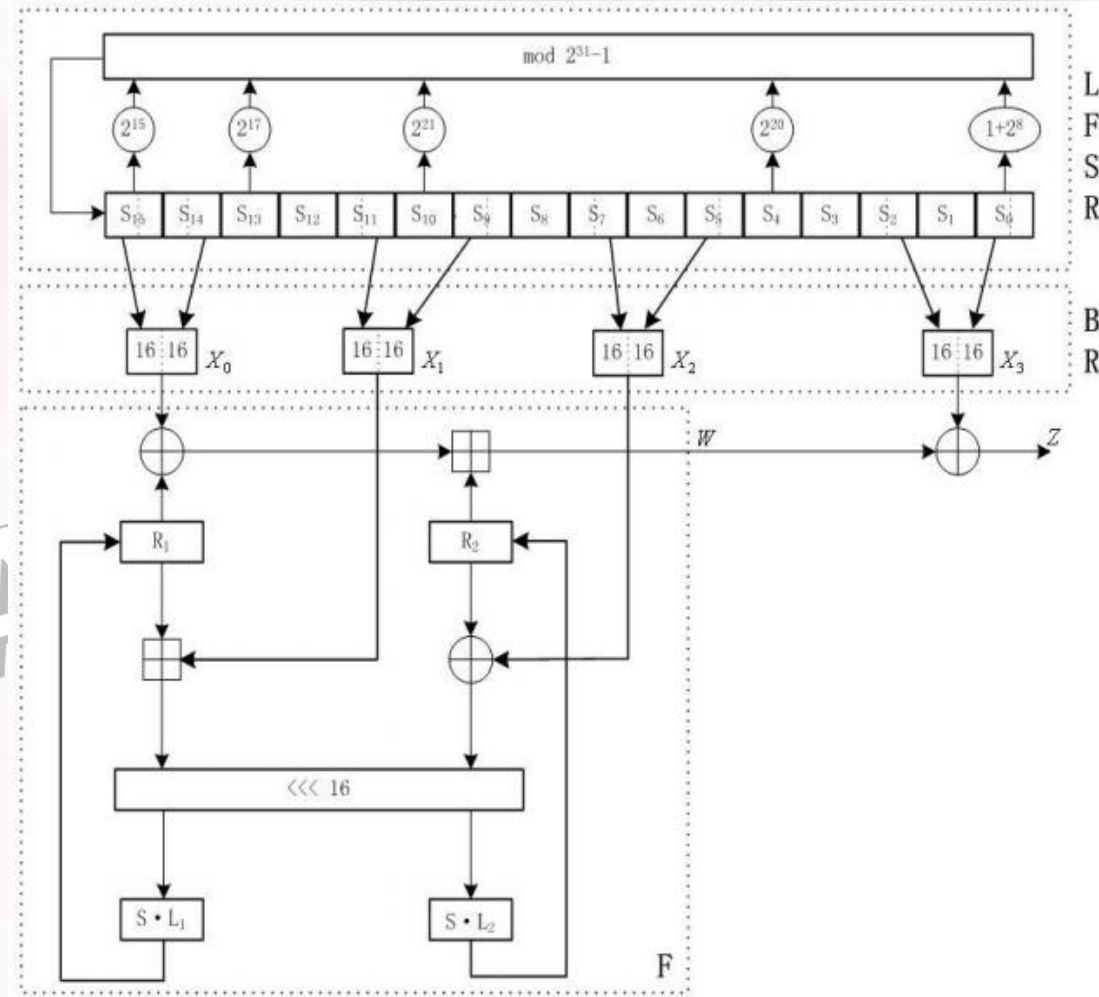
# 只用LFSR可以么？



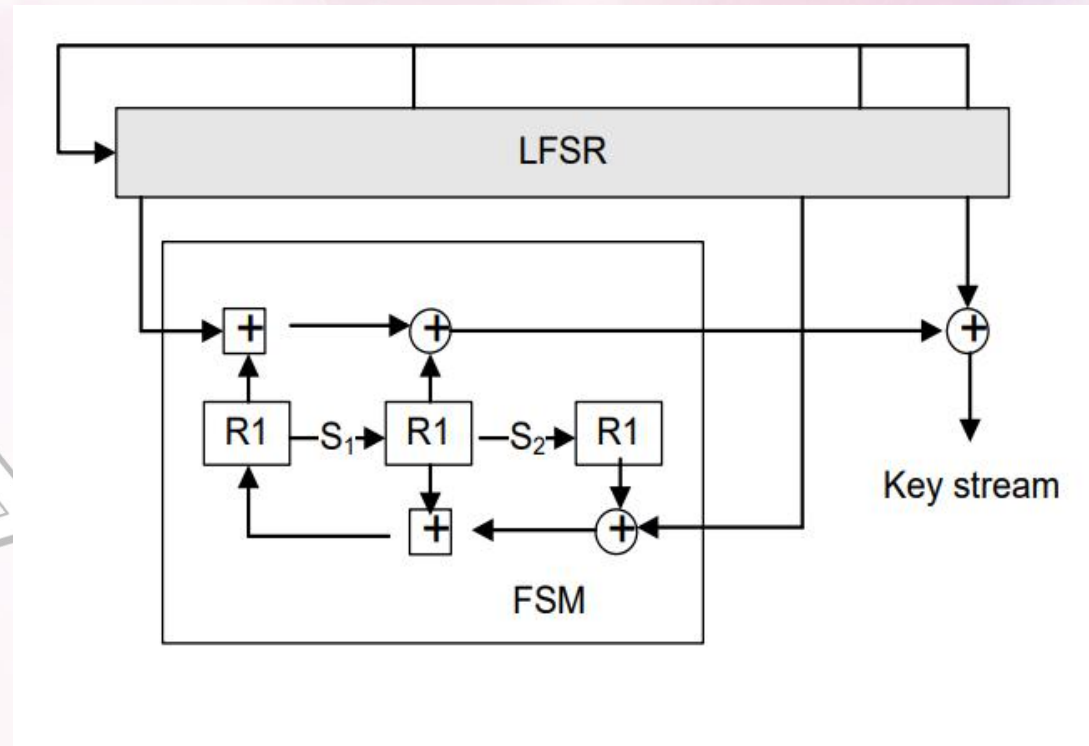
- NO!
- LFSR是可以根据输出反推回去的，我们需要一个非线性函数



ZUC

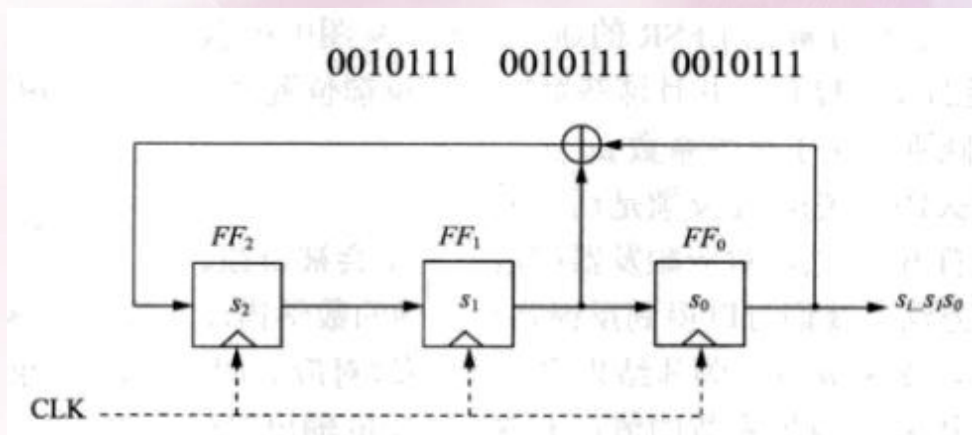


# SNOW3G





# LFSR已知明文攻击



$$s_3 \equiv s_1 + s_0 \pmod{2}$$

$$s_4 \equiv s_2 + s_1 \pmod{2}$$

$$s_5 \equiv s_3 + s_2 \pmod{2}$$

$\vdots$

$$s_{i+3} \equiv s_{i+1} + s_i \pmod{2}$$

# LFSR已知明文攻击



1 0 1 0 0 1 1 0 0 0 1 0  
0 1 2 3 4 5 6 7 8 9 10 11

0 0 0 1 0 1  
↑            ↑

1 1 0 0 0 0

$$\left. \begin{array}{l} ① 1 = P_5 + P_2 + P_0 \\ ② 0 = P_5 + P_4 + P_1 \\ ③ 0 = P_4 + P_3 + P_0 \\ ④ 0 = P_3 + P_2 \\ ⑤ 1 = P_2 + P_1 \\ ⑥ 0 = P_5 + P_1 + P_0 \end{array} \right\} \rightarrow \text{mod } 2$$

$$⑥ + ② = P_4 + P_0 = 0 =$$

$$⑤ + ② + ③ = P_3 = 0$$

$$P_2 = 0 ; P_1 = 1$$

$$\begin{cases} P_5 + P_0 = 1 & P_5 = 1 \\ P_5 + P_4 = 1 & P_0 = P_4 = 0 \\ P_4 + P_0 = 0 \end{cases}$$

$$X_m = X_{m-1} + X_{m-5}$$

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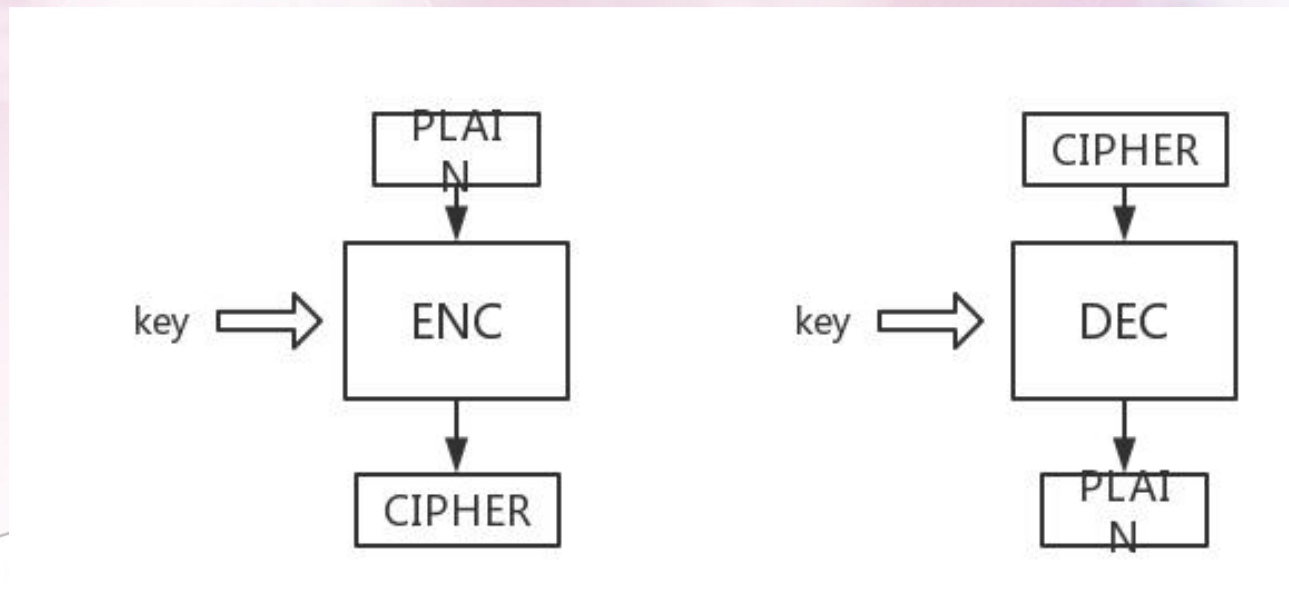
2

# 块加密

What is?



# 块加密



# 块加密



加密:

$$E_K(P) := E(K, P) : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$$

解密:

$$E_K^{-1}(C) := D_K(C) = D(K, C) : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$$



# 混淆与扩散

- 混淆, Confusion, 将密文与密钥之间的统计关系变得尽可能复杂, 使得攻击者即使获取了密文的一些统计特性, 也无法推测密钥。
- 扩散, Diffusion, 使得明文中的每一位影响密文中的许多位。

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# 块加密



- 大部分分组密码都是迭代分组密码
- what is?

$$M_0 = M \oplus K_0$$

$$M_i = R_{K_i}(M_{i-1}) ; i = 1 \dots r$$

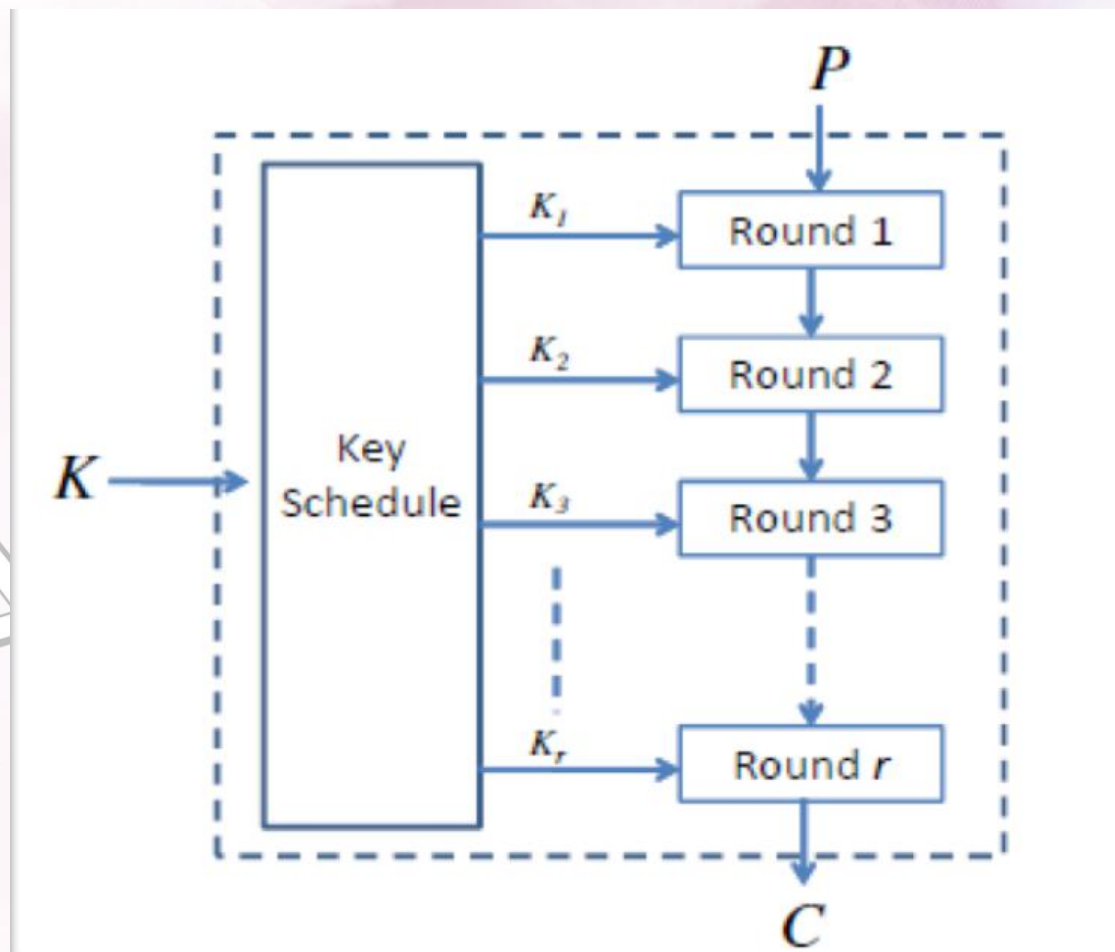
$$C = M_r \oplus K_{r+1}$$

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# 迭代分组密码



# 轮函数构造

- Feistel Network
- Substitution-Permutation Network



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# Feistel Cipher



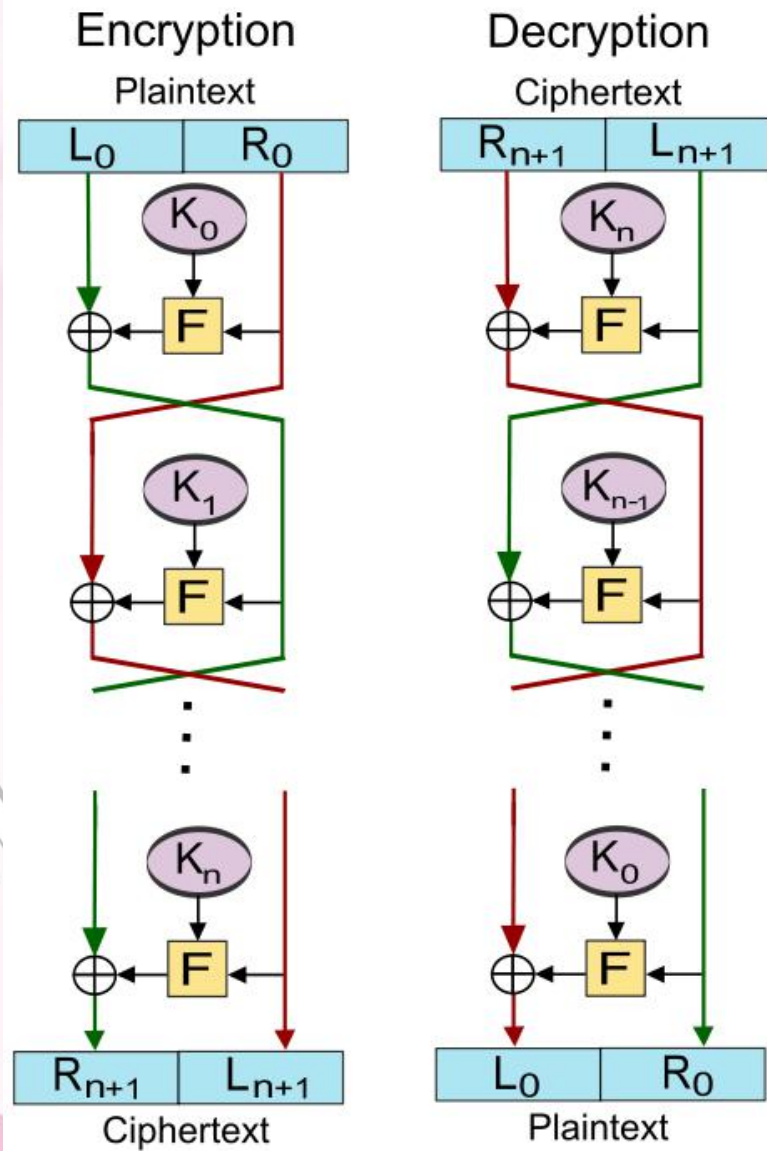
- 在密码学中，Feistel密码是用于构造分组密码的对称结构，它以在为IBM（美国）工作时做了开创性的研究的德国物理学家和密码学家Horst Feistel的名字命名；它通常也被称为Feistel网络。大部分分组密码使用该方案，包括数据加密标准（DES）。
- Feistel结构的优点是加密和解密操作非常相似，在某些情况下甚至相同，只需要反转子密钥的顺序。因此，实现这种密码所需的代码或电路的大小几乎减半。

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$$i = 0, 1, \dots, n$$

$$L_{i+1} = R_i$$

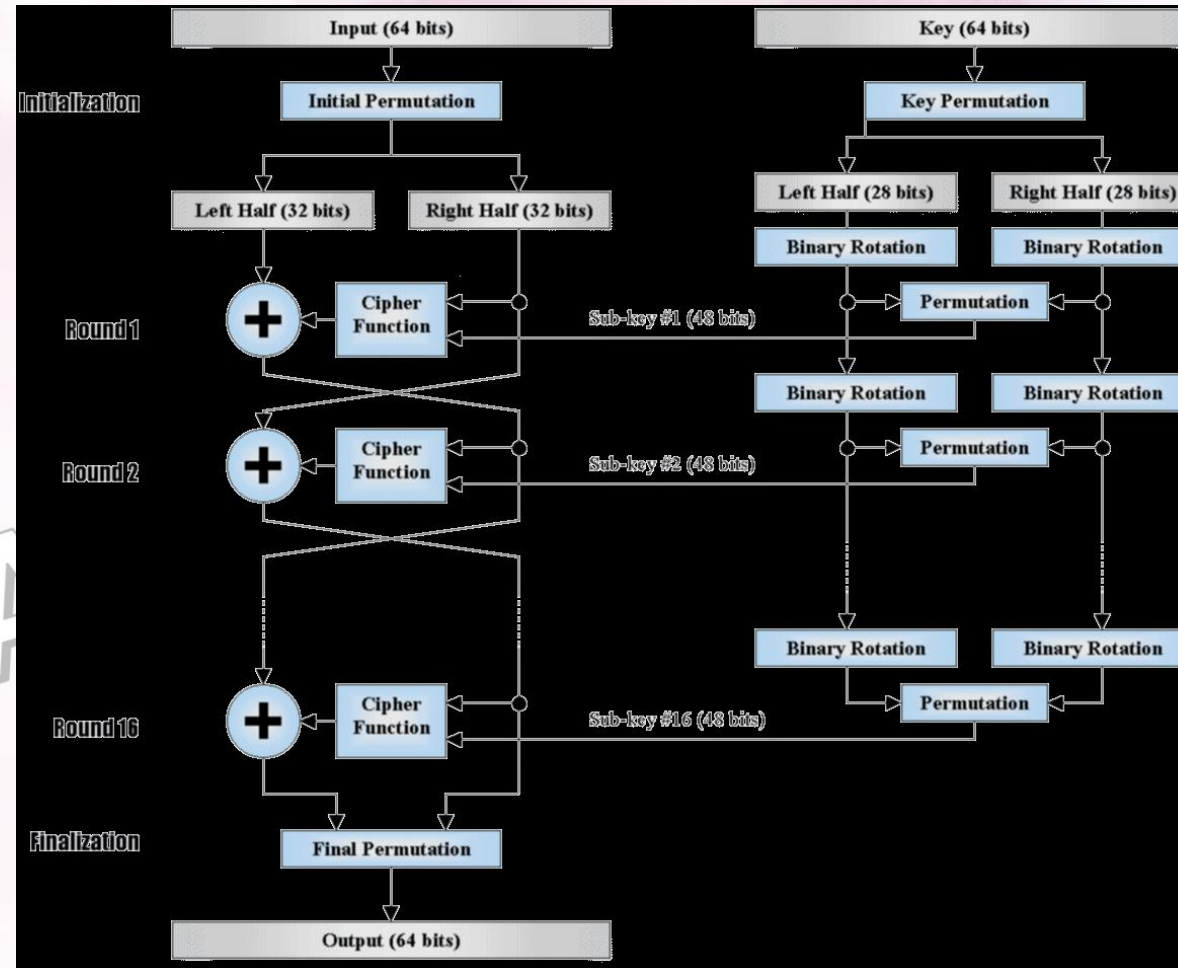
$$R_{i+1} = L_i \oplus F(R_i, K_i)$$

$$i = n, n-1, \dots, 0$$

$$R_i = L_{i+1}$$

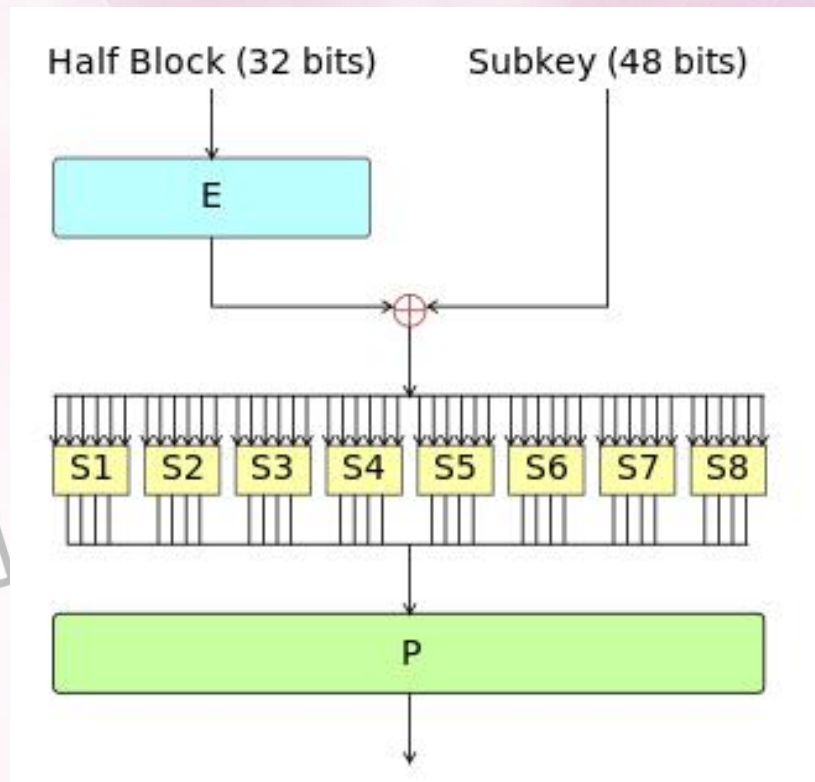
$$L_i = R_{i+1} \oplus F(L_{i+1}, K_i).$$

# DES





# F函数



IP



IP

IP-1

58 50 42 34 26 18 10 2  
60 52 44 36 28 20 12 4  
62 54 46 38 30 22 14 6  
64 56 48 40 32 24 16 8  
57 49 41 33 25 17 9 1  
59 51 43 35 27 19 11 3  
61 53 45 37 29 21 13 5  
63 55 47 39 31 23 15 7

40 8 48 16 56 24 64 32  
39 7 47 15 55 23 63 31  
38 6 46 14 54 22 62 30  
37 5 45 13 53 21 61 29  
36 4 44 12 52 20 60 28  
35 3 43 11 51 19 59 27  
34 2 42 10 50 18 58 26  
33 1 41 9 49 17 57 25

XN

N



# Initial Key Permutation



## Initial Key Permutation

57	49	41	33	25	17	9
1	58	50	42	34	26	18
10	2	59	51	43	35	27
19	11	3	60	52	44	36
63	55	47	39	31	23	15
7	62	54	46	38	30	22
14	6	61	53	45	37	29
21	13	5	28	20	12	4

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# Key Shifting



Round	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
Shifts	1	1	2	2	2	2	2	2	1	2	2	2	2	2	2	1

# Subkey Permutation



## Subkey Permutation

14	17	11	24	1	5
3	28	15	6	21	10
23	19	12	4	26	8
16	7	27	20	13	2
41	52	31	37	47	55
30	40	51	45	33	48
44	49	39	56	34	53
46	42	50	36	29	32

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# 48 bits key V.S. 32 bits block?



- Cipher expansion!





# 轮函数&弱密钥

- 针对子密钥生成器
- DES的4个弱密钥 0&F



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# Feistel Challenge

- 给Feistel网络写解密函数



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# 3DES



$$C = E_{k3}(D_{k2}(E_{k1}(P)))$$

$$P = D_{k1}(E_{k2}(D_{k3}(C)))$$

X-MEN





# 生日悖论<--->2DES



- 中间相遇攻击
- $P \xrightarrow{k_1} M \xrightarrow{k_2} C$

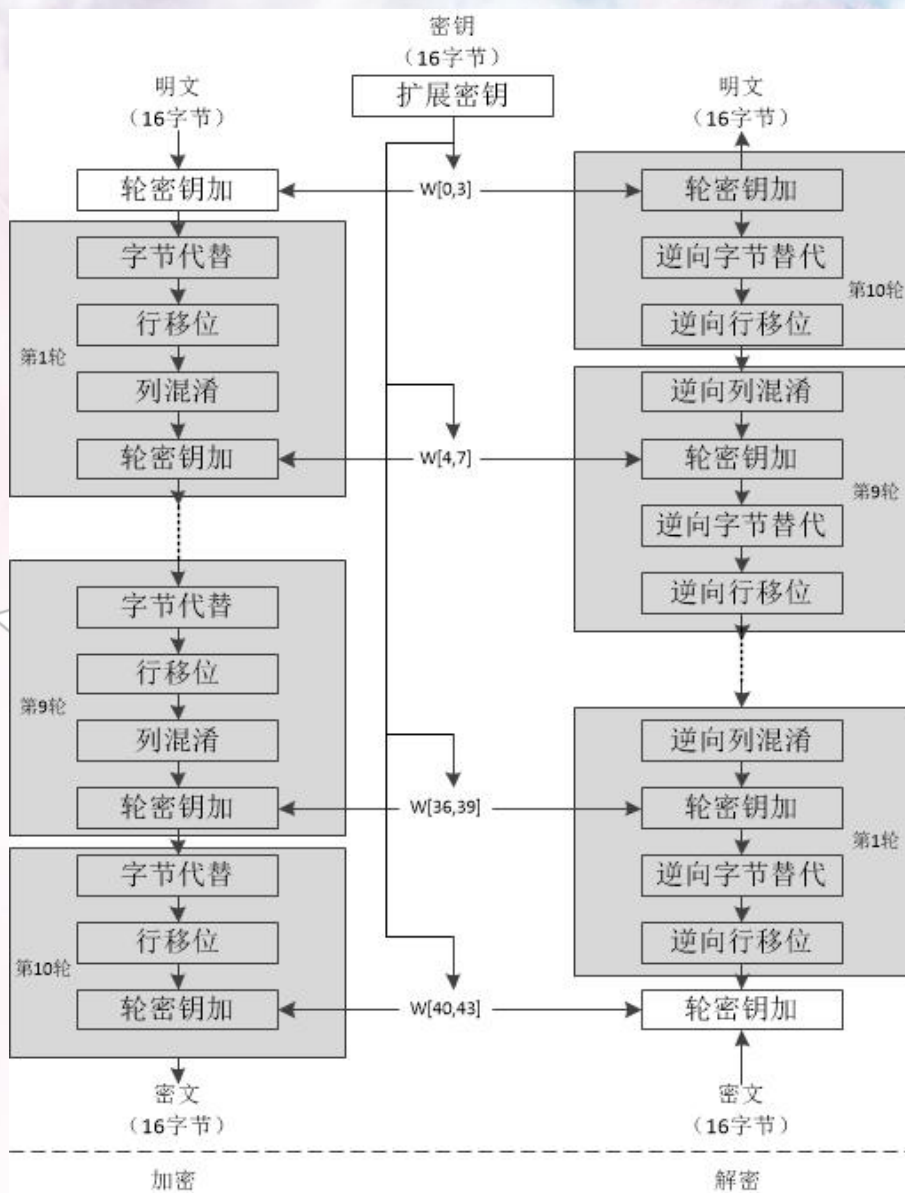
$$C = E_{k_2}(E_{k_1}(P))$$

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XMAN



# AES



# AES

- 动画&手写解释列混淆



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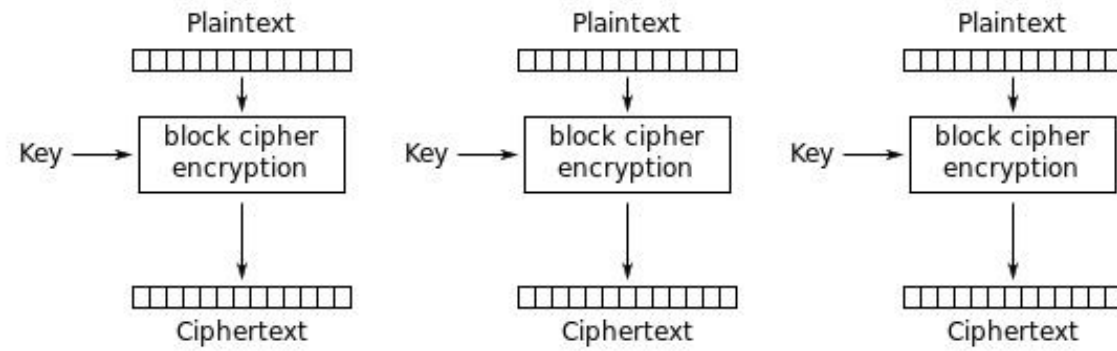


3

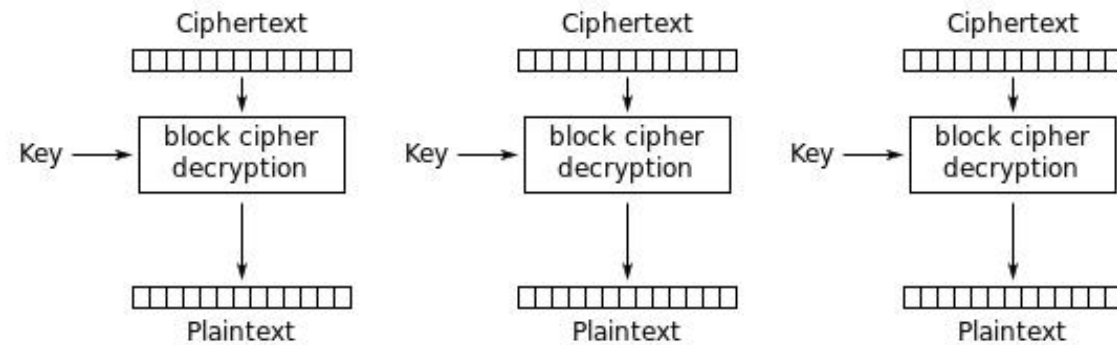
# 分组密码加密模式

What is?

# ECB



Electronic Codebook (ECB) mode encryption



# ECB



- 实现简单。
- 不同明文分组的加密可以并行计算，速度很快。
- 同样的明文块会被加密成相同的密文块  
(lack of diffusion)

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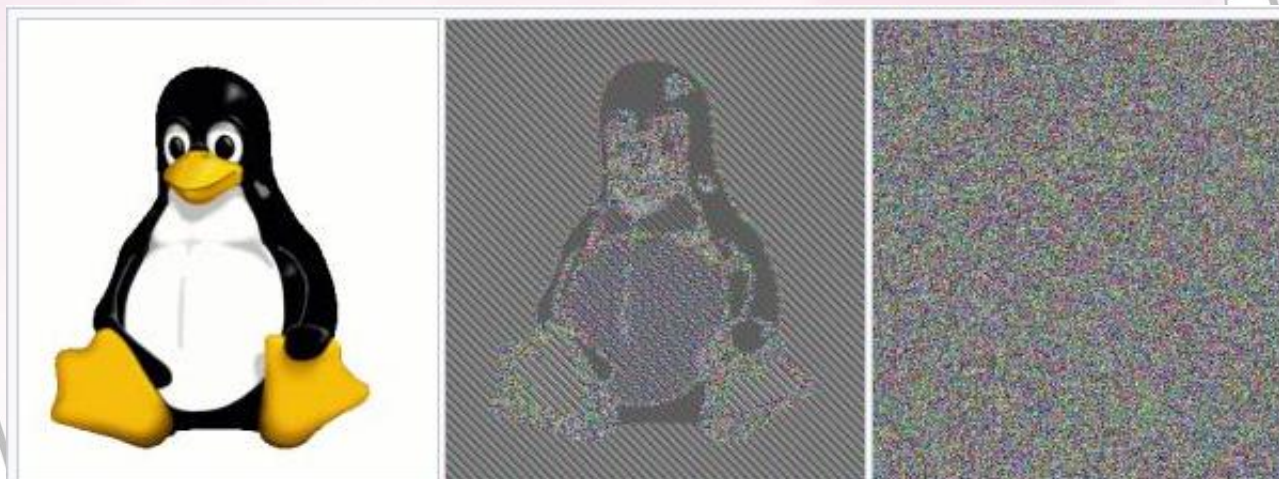




# ECB



- 加密模式存在的意义



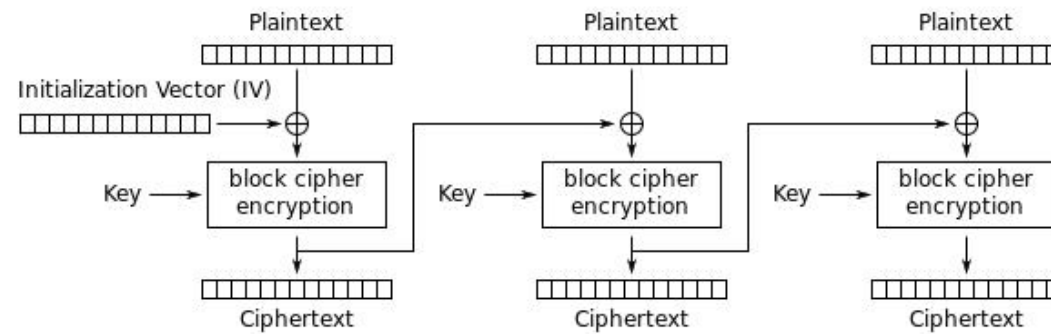
Original image

Encrypted using ECB mode

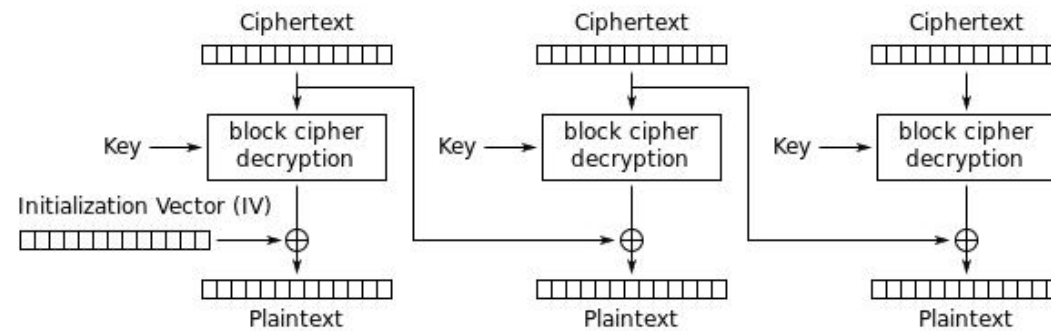
Modes other than ECB result in pseudo-randomness

The image on the right is how the image might appear encrypted with CBC, CTR or any of the other more secure modes—indistinguishable from random noise. Note that the random appearance of the image on the right does not ensure that the image has been securely encrypted; many kinds of insecure encryption have been developed which would produce output just as "random-looking".

# CBC (PCBC)



Cipher Block Chaining (CBC) mode encryption



Cipher Block Chaining (CBC) mode decryption



CBC



- IV 必须是不可预测的，而且要保证完整性
- 两步错误传播特性
- 明文统计特性的隐藏
- 并行解密

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# 针对CBC的攻击

- 字节反转攻击
- Padding Oracle Attack



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# Padding Oracle Attack



	1	2	3	4	5	6	7	8
Encrypted Input	0xF8	0x51	0xD6	0xCC	0x68	0xFC	0x95	0x37
	↓	↓	↓	↓	↓	↓	↓	↓
	TRIPLE DES							
	↓	↓	↓	↓	↓	↓	↓	↓
Intermediary Value	0x39	0x73	0x23	0x22	0x07	0x6a	0x26	0x3D
	⊕	⊕	⊕	⊕	⊕	⊕	⊕	⊕
Initialization Vector	0x6D	0x36	0x70	0x76	0x03	0x6E	0x22	0x39
	↓	↓	↓	↓	↓	↓	↓	↓
Decrypted Value	T	E	S	T	0x04	0x04	0x04	0x04

我们输入的密文

加/解密算法 例如DES

计算的中间结果 这是只要的攻击需要的 我们给它一个名字  
Intermediary Value

我们输入的初始化向量IV

解密的明文



# Padding Oracle Attack



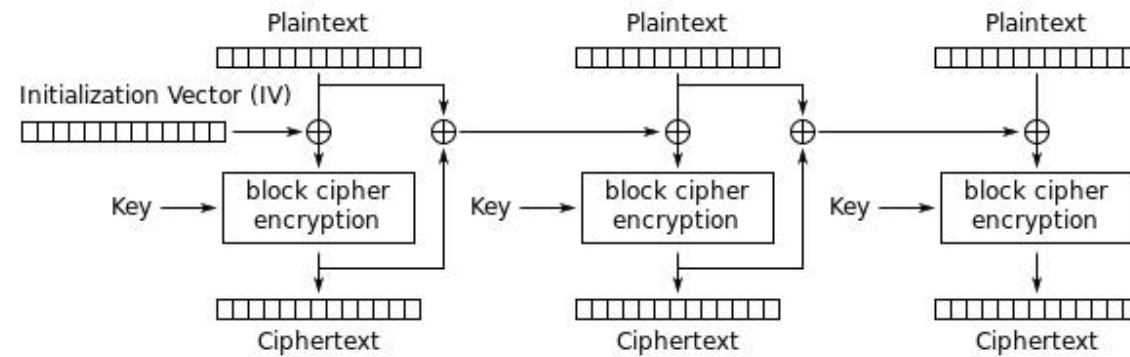
Block 1 of 1								
	1	2	3	4	5	6	7	8
Encrypted Input	0xF8	0x51	0xD6	0xCC	0x68	0xFC	0x95	0x37
	↓	↓	↓	↓	↓	↓	↓	↓
	TRIPLE DES							
	↓	↓	↓	↓	↓	↓	↓	↓
Intermediary Value	0x39	0x73	0x23	0x22	0x07	0x6a	0x26	0x67
	⊕	⊕	⊕	⊕	⊕	⊕	⊕	⊕
Initialization Vector	0x00	0x00	0x00	0x00	0x00	0x00	0x00	0x66
	↓	↓	↓	↓	↓	↓	↓	↓
Decrypted Value	0x39	0x73	0x23	0x22	0x07	0x6a	0x26	0x01

VALID PADDING

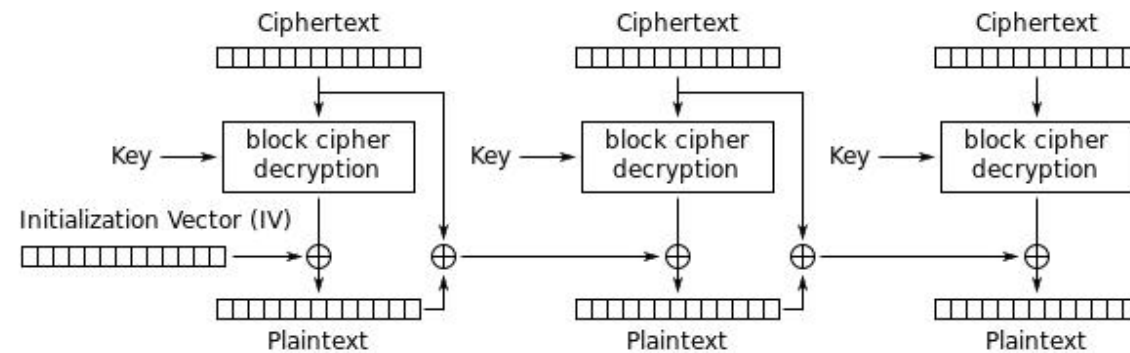




# PCBC

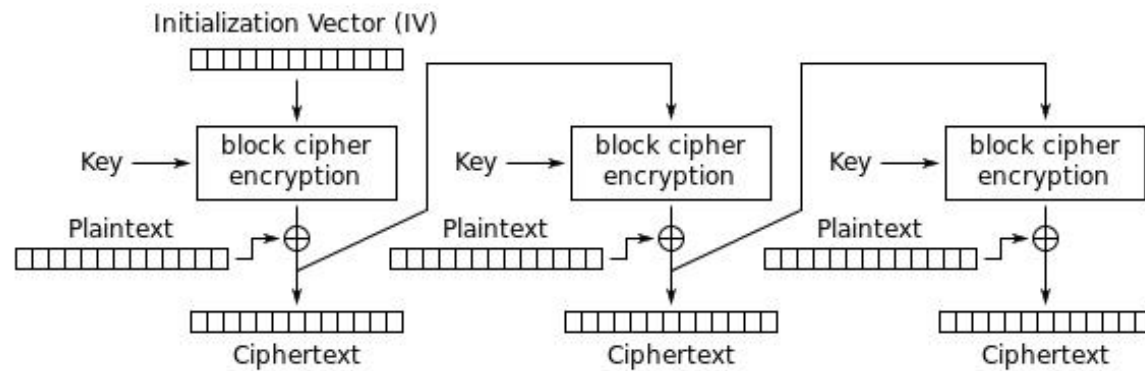


Propagating Cipher Block Chaining (PCBC) mode encryption

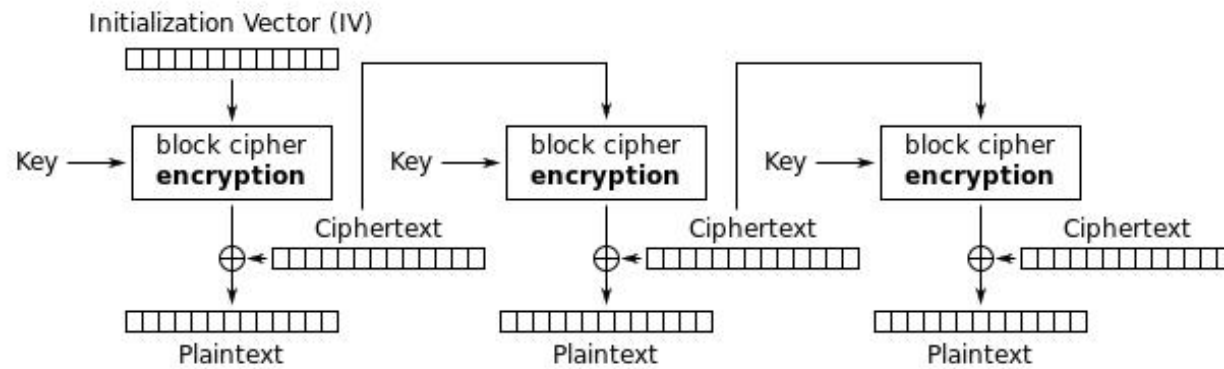


Propagating Cipher Block Chaining (PCBC) mode decryption

# CFB



Cipher Feedback (CFB) mode encryption



Cipher Feedback (CFB) mode decryption

# CFB



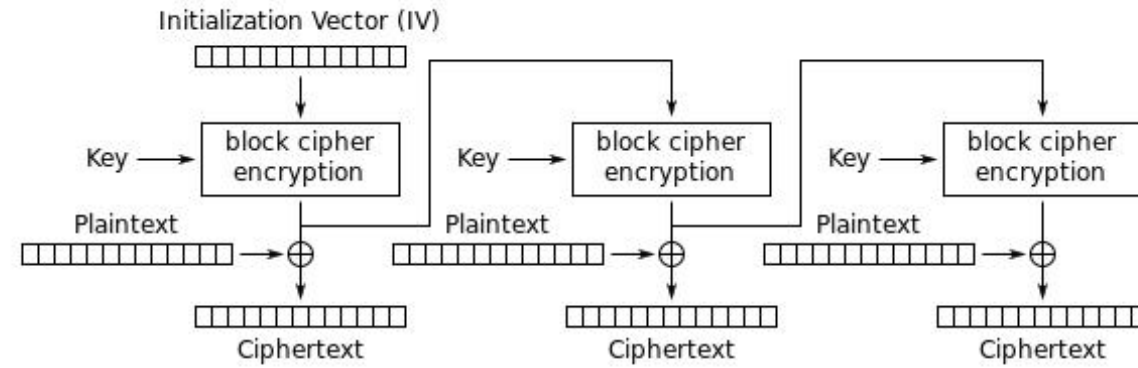
- 并行状况与CBC相同
- 不需要padding

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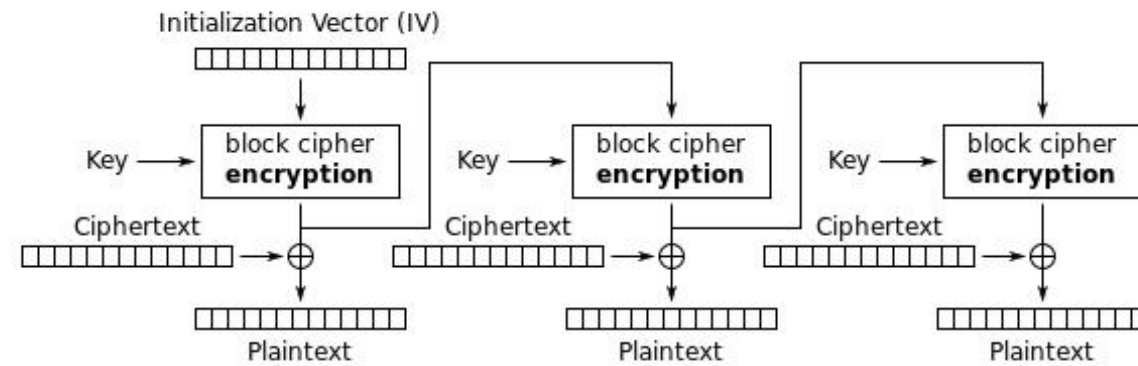




# OFB



Output Feedback (OFB) mode encryption



Output Feedback (OFB) mode decryption



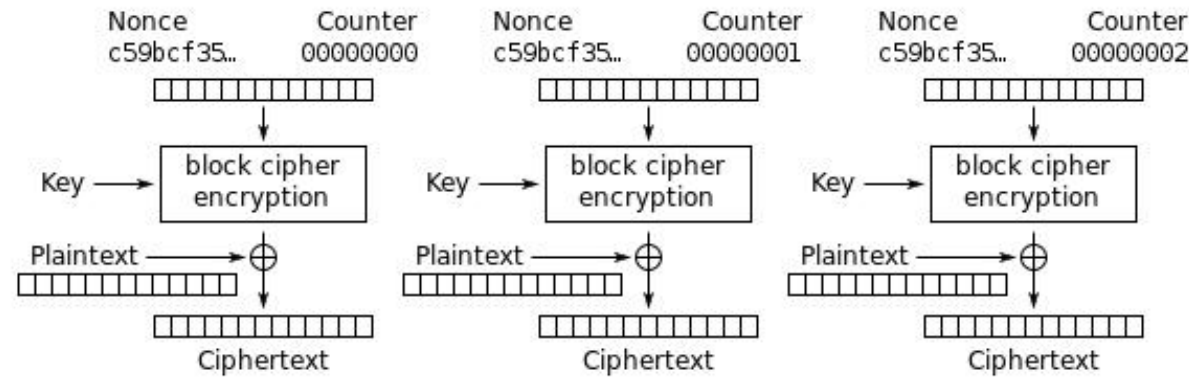
- 可以预先计算key stream

- 加解密均不能并行
- 可能存在cycle

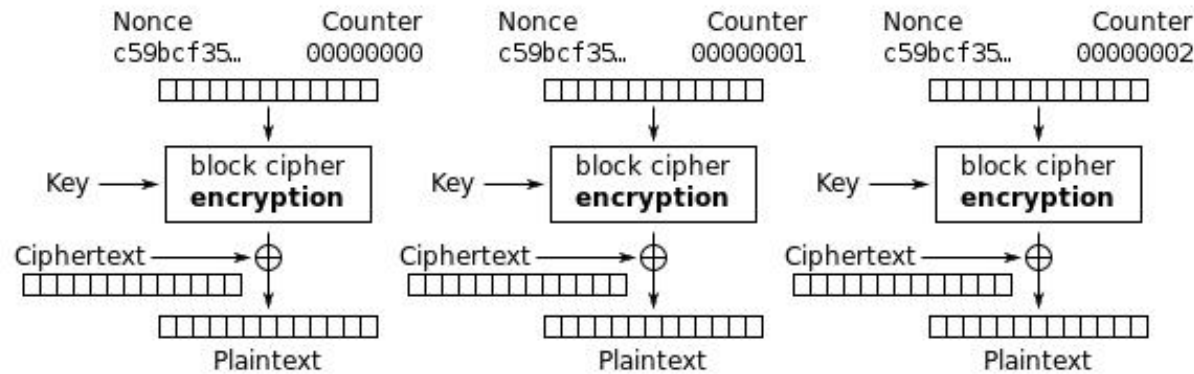
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# CTR



Counter (CTR) mode encryption



Counter (CTR) mode decryption



# 加密模式间的比较



- 总结一下
- Please use GCM
- Message Authentic Code

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3.5

# Padding

What is?

# Padding

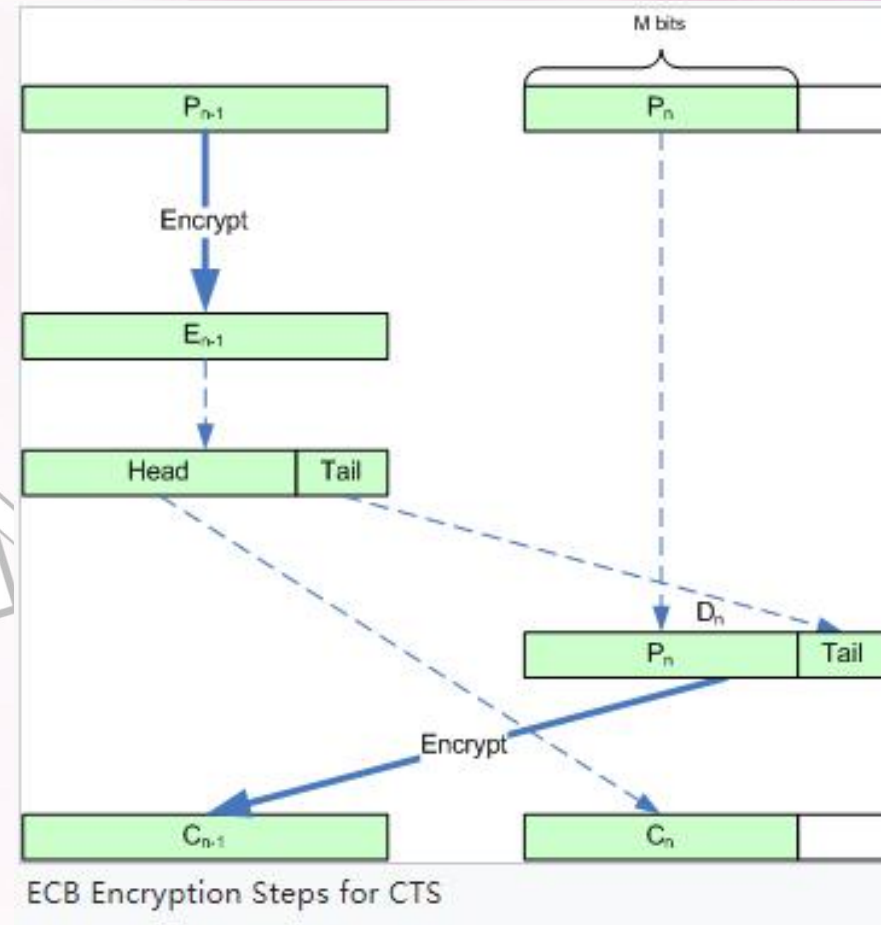
- PKCS#5



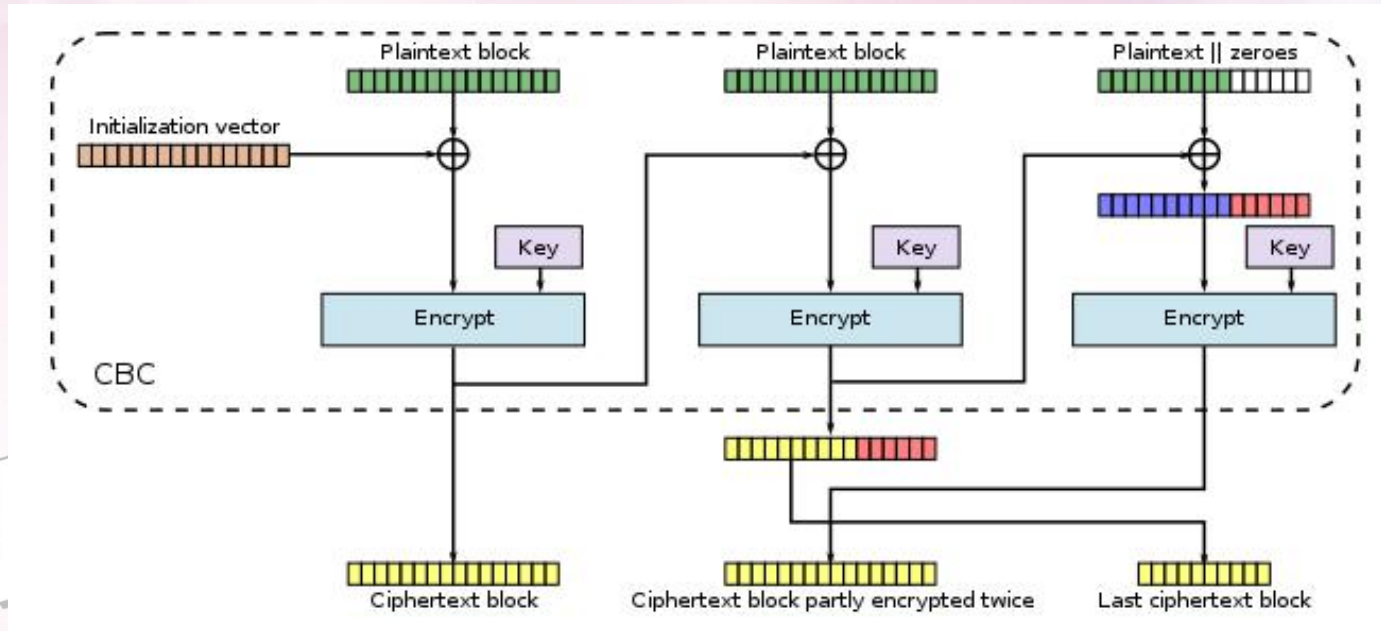
	BLOCK #1								BLOCK #2							
	1	2	3	4	5	6	7	8	1	2	3	4	5	6	7	8
Ex 1	F	I	G													
Ex 1 (Padded)	F	I	G	0x05	0x05	0x05	0x05	0x05								
Ex 2	B	A	N	A	N	A										
Ex 2 (Padded)	B	A	N	A	N	A	0x02	0x02								
Ex 3	A	V	O	C	A	D	O									
Ex 3 (Padded)	A	V	O	C	A	D	O	0x01								
Ex 4	P	L	A	N	T	A	I	N								
Ex 4 (Padded)	P	L	A	N	T	A	I	N	0x08	0x08	0x08	0x08	0x08	0x08	0x08	0x08
Ex 5	P	A	S	S	I	O	N	F	R	U	I	T				
Ex 5 (Padded)	P	A	S	S	I	O	N	F	R	U	I	T	0x04	0x04	0x04	0x04



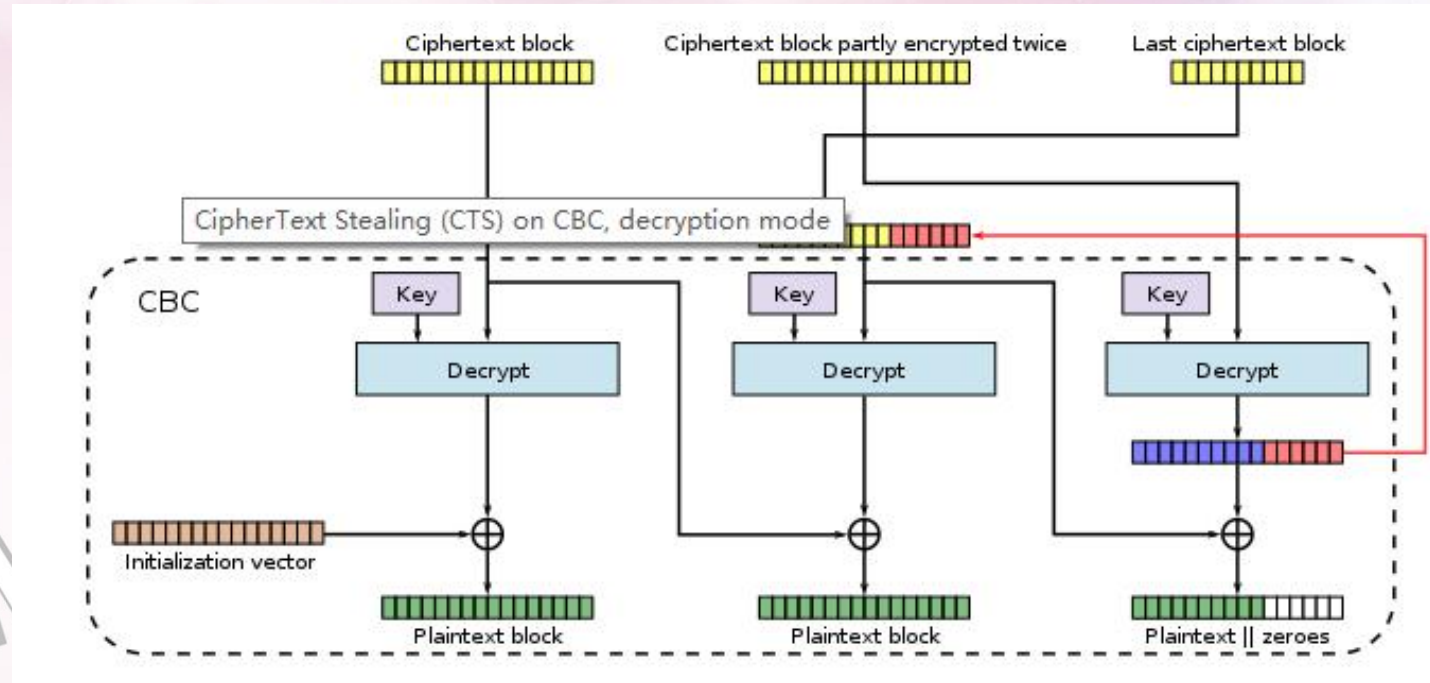
# Ciphertext stealing for ECB



# Ciphertext stealing for CBC



# Ciphertext stealing for CBC







4

# 公钥算法

What is?

# 公钥算法



- 公钥算法存在的意义
  - 公开信道上的通信
  - 更灵活的协议设计

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# 公钥算法的安全性来源



- Discrete log problem (DLP)

- CDH
- DDH
- ...

- Integer factorization

- RSA problem

- ...

- Final Report on Main Computational Assumptions in Cryptography



# RSA



- 根据一定条件随机选择两个不同的大质数 $p$ 和 $q$ ，计算 $N = p * q$
- 根据欧拉函数， $\varphi(N) = \varphi(p) * \varphi(q) = (p-1) * (q-1)$
- 选择一个与 $\varphi(N)$ 互素的数字 $e$ ，并求得 $e$ 的逆元 $d$
- Public Key:  $(N, e)$
- Secret Key  $(N, d)$

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# ENC & DEC



- $C = \text{pow}(M, e, N)$
- $M = \text{pow}(C, d, N)$

- $M = \text{pow}(C, d, N)$   
=  $\text{pow}(\text{pow}(M, e, N), d, N)$   
=  $\text{pow}(M, e \cdot d, N)$   
=  $\text{pow}(M, k \cdot \phi(N) + 1, N)$

# 费马小定理



- $\text{pow}(a, \varphi(N), N) = 1$
- $N, a$  为正整数;  $N, a$  互质

• 证明:

$$X_1 \dots X_{\varphi n} == a_1 \dots a_{\varphi n}$$

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# 快速幂算法



```
def fastExp(m, d, N):  
    ret = 1  
    while d > 0:  
        if d&1:  
            ret = ret * m % N  
        d = d // 2  
        m = pow(m, 2, N)  
    return ret
```





# 中国剩余定理加速法

- 已知  $p, q, e, c$
- $cp = c \bmod p$
- $cq = c \bmod q$
- $dp = d \bmod (p-1)$
- $dq = d \bmod (q-1)$
- $pp = \text{pow}(cp, dp, p)$
- $pq = \text{pow}(cq, dq, q)$
- $p = q * \text{inv}(q, p) * pp + p * \text{inv}(p, q) * pq \bmod (p*q)$
- [举个例子]



# 中国剩余定理



$$(S) : \begin{cases} x \equiv a_1 \pmod{m_1} \\ x \equiv a_2 \pmod{m_2} \\ \vdots \\ x \equiv a_n \pmod{m_n} \end{cases}$$

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# 中国剩余定理



$$M = m_1 \times m_2 \times \cdots \times m_n = \prod_{i=1}^n m_i$$

$$M_i = M/m_i, \quad \forall i \in \{1, 2, \cdots, n\}$$

$$t_i M_i \equiv 1 \pmod{m_i}, \quad \forall i \in \{1, 2, \cdots, n\}$$

$$x = a_1 t_1 M_1 + a_2 t_2 M_2 + \cdots + a_n t_n M_n + kM = kM + \sum_{i=1}^n a_i t_i M_i$$

$$x = \sum_{i=1}^n a_i t_i M_i$$

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# CTF中的RSA



- pem格式的证书
  - openssl rsautl -encrypt -in FLAG -inkey public.pem -pubin -out flag.enc
  - openssl rsa -pubin -text -modulus -in warmup -in public.pem
- pcap流量包
- nc端口交互 pwntools
- $N=*****$ ;  $e=*****$  ...

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5

# RSA使用中常见的错误





# SHOULD NOT DO THIS

- 过小的 $N$
- 过小的 $d$
- 过小的 $e$
- 重复使用 $p, q$
- 不恰当的 $pq$ 特征
- 广播同一段明文的不同密文
- 不同的 $e$ 共用 $n$
- 提供 Padding Oracle

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# 过小的N



- 素数分解问题是困难的，但是可以通过计算机进行暴力分解。
- 针对RSA最流行的攻击一般是基于大数因数分解。1999年，RSA-155 (512 bits)被成功分解，花了五个月时间（约8000 MIPS年）和224 CPU hours在一台有3.2G中央内存的Cray C916计算机上完成。
- 2009年12月12日，编号为RSA-768（768 bits, 232 digits）数也被成功分解。这一事件威胁了现通行的1024-bit密钥的安全性，普遍认为用户应尽快升级到2048-bit或以上。
- 2010年，又提出了一些针对1024bit的n的分解的途径，但是没有正面分解成功。

# 过小的N



- 一般认为2048bit以上的n是安全的。现在一般的公钥证书都是4096bit的证书。

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# 过小的N



- online DB: <http://factordb.com>

Search Sequences Report results Factor tables Status Downloads

123456789052364653459784654135468764354873475634768764661 Factorize! (?)

**Result:**

status (?)	digits	number
FF	57 (show)	<a href="#">1234567890...61</a> <sub>&lt;57&gt;</sub> = $3 \cdot 7 \cdot 11 \cdot 13 \cdot 17 \cdot 23 \cdot 41 \cdot 3301 \cdot 776879222921624175777642745962496986583004477$ <sub>&lt;45&gt;</sub>

**More information** ↗

**ECM** ↗

factordb.com - 11 queries to generate this page (0.01 seconds) ([limits](#)) ([Imprint](#)) ([Privacy Policy](#))

# 过小的N



- 本机: RSATool, yafu

```
$ ./yafu-x64.exe
factor(123456789052364653459784654135468764354873475634768764661)

fac: factoring 123456789052364653459784654135468764354873475634768764661
fac: using pretesting plan: normal
fac: no tune info: using qs/gnfs crossover of 95 digits
div: primes less than 10000
fmt: 1000000 iterations
Total factoring time = 0.0430 seconds
factordb.com - 11 queries to genera

***factors found***
P1 = 3
P1 = 7
P2 = 11
P2 = 13
P2 = 17
P2 = 23
P2 = 41
P4 = 3301
P45 = 776879222921624175777642745962496986583004477

ans = 1
```

## 过小的e

- $\text{pow}(m, e) < N$  ( $e == 3$ )
- $\text{Cipher Text} = \text{pow}(m, e) + k * N$  ( $e == 3$ )



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# 过小的d

- rsa-wiener-attack
- <https://github.com/pablocelayes/rsa-wiener-attack>



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# 重复使用PQ

- $N1 = p1 * q1$
- $N2 = p1 * q2$
- $\gcd(N1, N2) = p1$



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# 不恰当的pq特征

- Fermat方法 & Pollard rho方法
- 在 $p$ ,  $q$ 的取值差异过大, 或者 $p$ ,  $q$ 的取值过于相近的时候, Fermat方法与Pollard rho方法都可以很快将 $n$ 分解成功。
- Just Yafu it

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# 广播攻击



- $C1 = \text{pow}(m, e, N1)$
- $C2 = \text{pow}(m, e, N2)$
- $C3 = \text{pow}(m, e, N3)$
- $C\_ = \text{pow}(m, e, N1*N2*N3)$
- (中国剩余定理)

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## 共模攻击

- $C1 = \text{pow}(m, e1, N)$
- $C2 = \text{pow}(m, e2, N)$
- if  $\text{gcd}(e1, e2) == 1 \rightarrow e1*r1 + e2*r2 == 1 \ (r1*r2 < 0)$
- $m = \text{pow}(C1, r1, N) * \text{pow}(C2, r2, N)$   
 $= \text{pow}(m, e1*r1 + e2*r2, N)$

# Padding Oracle



- SSL with PKCS#1 v1.5
- 0x00 0x02 [some non-zero bytes] 0x00 [here goes M]

0002	09ad829ffb3a98b91a1b ... 089333f7ca7b4070f272	00	68656c6c6f20776f726c6421
------	-----------------------------------------------	----	--------------------------

- $C' = C * \text{pow}(s, e, N) \% N$
- $m' = m * s \% N$
- Randomly choose s (once every 30000 to 130000 attempts got a padded value)
- After a few million connections in all, the attacker learned enough to pinpoint the exact m



# An easier scenario



- 0b 1 [here goes M]
- server will return an error when Plain Text start with 0 at 1023's bit

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# Padding Oracle's paper & realization



- Chosen Ciphertext Attacks Against Protocols Based on the RSA Encryption Standard PKCS #1
- <https://github.com/RUB-NDS/TLS-Attacker>
- Plz use OAEP!

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# ATTACK ON RSA



- Coppersmith Attack
- Side channel

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# Coppersmith's Theorem



- Coppersmith method, proposed by Don Coppersmith 是一种主要利用 Lenstra–Lenstra–Lovász lattice basis reduction algorithm (LLL) 找到低系数多项式根的算法
- 在密码学中，Coppersmith方法主要用于攻击RSA

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# Stereotyped Messages Attack

- Plain Text --> "The PassWord is: \*\*\*\*\*"
- Attacker knows:  $M = M_0 + x$
- Attacker has to solve:
  - $F(x_0) = (M_0 + x_0)^e - C = 0 \pmod{N}$
- 如果 $x_0$ 和 $e$ 足够小的话, LLL算法可以以线性的时间复杂度解决这个问题
  - $x_0 < X$
  - $d = e$

$$X = N^{\frac{1}{d}-\epsilon} \text{ for } \frac{1}{d} > \epsilon > 0$$



# Factoring with high bits known

- $p(x, y) == 0$
- $p(x_0, y_0) == P * Q - N == 0$

$$\begin{aligned}P &= P_0 + x_0 \\Q &= Q_0 + y_0 \\|x_0| &< X = P_0 / N^{(1/4)+\epsilon} \\|y_0| &< Y = Q_0 / N^{(1/4)+\epsilon} \\p(x, y) &= (P_0 + x)(Q_0 + y) - N \\&= (P_0 Q_0 - N) + Q_0 x + P_0 y + xy\end{aligned}$$

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# LLL的实现



- <https://github.com/mimoo/RSA-and-LLL-attacks>

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# side-channel attack



- RSA被能量攻击的点在?
  - 快速幂算法
  - 中国剩余定理加速解密

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# 快速幂算法



```
def fastExp(m, d, N):  
    ret = 1  
    while d > 0:  
        if d&1:  
            ret = ret * m % N  
        d = d // 2  
        m = pow(m, 2, N)  
    return ret
```







# 中国剩余定理加速法

- 已知  $p, q, e, c$
- $cp = c \bmod p$
- $cq = c \bmod q$
- $dp = d \bmod (p-1)$
- $dq = d \bmod (q-1)$
- $pp = \text{pow}(cp, dp, p)$
- $pq = \text{pow}(cq, dq, q)$
- $p = q * \text{inv}(q, p) * pp + p * \text{inv}(p, q) * pq \bmod (p*q)$
- [举个例子]



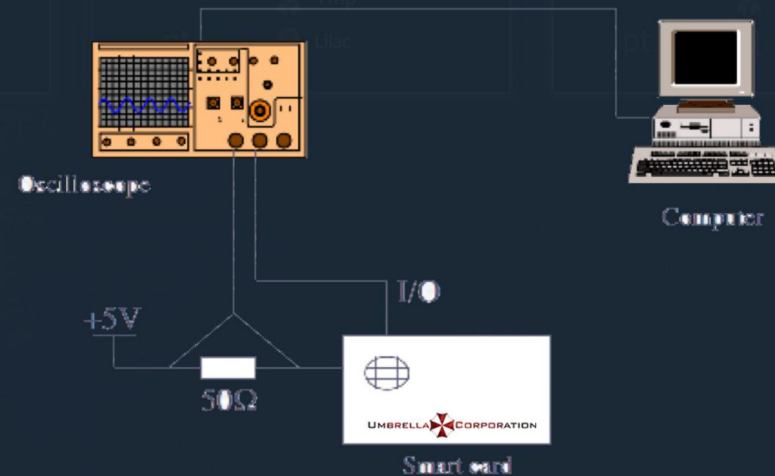


## HACK IN THE CARD I

Welcome to work for C.I.A. Our agent 47 has successfully penetrated to an evil company and sent this secret smart card to us. Intelligence department said the crypto chip on this card is doing RSA operation and the public key we got is here(attachments - > publickey.pem). Your mission is to extract the private key embedded in this smart card and decrypt the following hex-encoded ciphertext.

014b05e1a09668c83e13fda8be28d148568a2342aed833e0ad646bd45461da2decf9d538c2d3ab245b272873beb112586bb7b17dc4b30f0c5408d8b03cfbc8388b2bd579fb419a1cac38798da1c3da75dc9a74a90d98c8f986fd8ab8b2dc539768beb339cad13383c62b5223a50e050cb9c6b759072962c2b2cf21b4421ca73394d9e12cfbc958fc5f6b596da368923121e55a3c6a7b12fdca127ecc0e8470463f6e04f27cd4bb3de30555b6c701f524c8c032fa51d719901e7c75cc72764ac00976ac6427a1f483779f61cee455ed319ee9071abefae4473e7c637760b4b3131f25e5eb9950dd9d37666e129640c82a4b01b8bdc1a78b007f8ec71e7bad48046

The progress of hacking was going well until it got stuck, what we did so far is that as you can see the smartcard, an oscilloscope, a computer (act as the card reader) and a resistor are plugged into a circuit board. The circuit diagram is given as follows.



We finally managed to decrypt a crafted message and captured voltage variation(<http://47.74.147.53:20015/index.html>) of the resistor during the whole process. Now we are counting on you to do the rest...

[Download Attachments](#)

# side-channel attack





# Tools

- Github



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THANK YOU

FOR YOUR  
ATTENTION

