

**Solutions:**

**Problem 1:**

Test case table:

Test Case	Current State	Next State	Inputs				Exp outputs			
			D	G	P	Z	B	I	T	X
1	Start	OFF	0	0	0	0	0	0	0	0
2	OFF	OFF	0	0	0	1	0	0	0	0
3	OFF	U	0	0	1	0	1	0	0	1
4	OFF	L	0	1	0	0	1	0	1	0
5	OFF	OFF	1	0	0	0	0	0	0	0
6	L	L	0	0	0	1	1	0	1	0
7	L	OFF	0	0	1	0	0	0	0	0
8	L	L	0	1	0	0	1	0	1	0
9	L	L	1	0	0	0	1	0	1	0
10	U	X5	0	0	0	1	1	0	0	2
11	U	OFF	0	0	1	0	0	0	0	0
12	U	U	0	1	0	0	1	0	0	1
13	U	U	1	0	0	0	1	0	0	1
14	X5	X10	0	0	0	1	1	0	0	3
15	X5	X5	0	0	1	0	1	0	0	2
16	X5	X5	0	1	0	0	1	0	0	2
17	X5	N	1	0	0	0	1	1	0	2
18	X10	U	0	0	0	1	1	0	0	1
19	X10	X10	0	0	1	0	1	0	0	3
20	X10	X10	0	1	0	0	1	0	0	3
21	X10	X10	1	0	0	0	1	0	0	3
22	N	N	0	0	0	1	1	1	0	2
23	N	N	0	0	1	0	1	1	0	2
24	N	N	0	1	0	0	1	1	0	2
25	N	X5	1	0	0	0	1	0	0	2

Sequence Enumeration Table:

Test Case Number	Length	Sequence	Response	Equivalence	Carry to next level
1	0	Idle	B=0, I=0, T=0, X=0	-	
2	1	D	B=0, I=0, T=0, X=0	Idle	
3	1	G	T=1, B=1, I=0, X=0	-	Yes
4	1	P	X=1, B=1, I=0, T=0	-	Yes
5	1	Z	B=0, I=0, T=0, X=0	Idle	
6	2	GD	T=1, B=1, I=0, X=0	G	
7	2	GG	T=1, B=1, I=0, X=0	G	
8	2	GP	B=0, I=0, T=0, X=0	Idle	
9	2	GZ	T=1, B=1, I=0, X=0	G	
10	2	PD	X=1, B=1, I=0, T=0	P	
11	2	PG	X=1, B=1, I=0, T=0	P	
12	2	PP	B=0, I=0, T=0, X=0	Idle	
13	2	PZ	B=1, X=2, T=0, I=0	-	Yes
14	3	PZD	I=1, X=2, B=1, T=0	-	Yes
15	3	PZG	X=2, I=0, B=1, T=0	PZ	
16	3	PZP	X=2, I=0, B=1, T=0	PZ	
17	3	PZZ	B=1, I=0, T=0, X=3	-	Yes
18	4	PZDD	I=0, X=2, B=1, T=0	PZ	
19	4	PZDG	I=1, X=2, B=1, T=0	PZD	
20	4	PZDP	I=1, X=2, B=1, T=0	PZD	
21	4	PZDZ	I=1, X=2, B=1, T=0	PZD	
22	4	PZZD	X=3, B=1, I=0, T=0	PZZ	
23	4	PZZG	X=3, B=1, I=0, T=0	PZZ	
24	4	PZZP	X=3, B=1, I=0, T=0	PZZ	
25	4	PZZZ	X=1, B=1, I=0, T=0	PZZ	

Canonical sequences are: G, P, PZ, PZD, PZZ

## Problem 2.

Answer in excels

**Problem 3.**

a.  $a'b'c' + abc + abc'd' + a'b'cd' + a'bc'd + a'bcd + ab'c'd$

On converting 3 variable terms to 4 variable terms.

$a'b'c'd + a'b'c'd' + abcd + abcd' + abc'd' + a'b'cd' + a'bc'd + a'bcd + ab'c'd$

	cd	00	01	11	10
ab					
00		1	1	0	1
01		0	1	1	0
11		1	0	1	1
10		0	1	0	0

Solution:  $a'b'd' + a'c'd + bcd + abd' + b'c'd$

b.  $a'b'c' + a'cd' + ac'd' + ab'c + a'b'cd + abcd' + ab'c'd + a'bc'd'$

On converting 3 variable terms to 4 variable terms.

$$a'b'c'd' + a'b'c'd + a'bcd' + a'b'cd' + abc'd' + ab'c'd' + ab'cd + ab'cd' + a'b'cd + abcd' + ab'c'd + a'bc'd'$$

ab \ cd	00	01	11	10
00	1	1	1	1
01	1	0	0	1
11	1	0	0	1
10	1	1	1	1

Solution:  $b' + d'$

c.  $cd + a'b'c'd' + a'b'c'd + ab'cd + a'bcd + a'b'cd' + ab'c'd' + a'bc'd' + ab$

On converting 3 variable terms to 4 variable terms.

$$abcd + a'bcd + a'b'cd + abcd' + abc'd + abc'd' + a'b'c'd' + a'b'c'd + ab'cd + a'b'cd' + ab'c'd' + a'bc'd'$$

ab \ cd	00	01	11	10
00	1	1	1	1
01	1	0	1	0
11	1	1	1	1
10	1	0	1	0

Solution:  $c'd' + cd + ab + a'b'$

d.  $a'b'c'd + abcd + a'b'cd + abc'd + a'bc'd + ab'cd + a'bcd + ab'c'd$

ab \ cd	00	01	11	10
00	0	1	1	0
01	0	1	1	0
11	0	1	1	0
10	0	1	1	0

Solution:  $d$

**Problem 4.**

**a.  $a+b'c'$**

Truth table:

a	b	c	$a+b'c'$
F	F	F	T
F	F	T	F
F	T	F	F
F	T	T	F
T	F	F	T
T	F	T	T
T	T	F	T
T	T	T	T

1)

- Condition Decision Coverage Pairs(c/d) = FTT, TFF
- Condition (only) Coverage Pairs(c) = FFF, TTT (considered FFF because other are in c/g)
- Decision (only) Coverage Pair(d) = FFF, FTF

2)

- Term Omission Faults (TOF's): a, b'c'
- Term Negation Faults (TNF's):  $a'+b'c'$ ,  $a+(b'c')'$

**b.  $a(c + d)$**

On converting given problem:  $ac + ad$

Truth table:

a	c	d	$ac + ad$
F	F	F	F
F	F	T	F
F	T	F	F
F	T	T	F
T	F	F	F
T	F	T	T
T	T	F	T
T	T	T	T

1)

- Condition Decision Coverage Pairs(c/d) = FFT, TTF
- Condition (only) Coverage Pairs(c) = FTT, TFF
- Decision (only) Coverage Pair(d) = FFF, TFT

2)

- Term Omission Faults (TOF's): ac, ad
- Term Negation Faults (TNF's):  $ac+(ad)'$ ,  $(ac)'+ad$

**c.  $ab + c' + d$**

a	b	c	d	$ab + c' + d$
F	F	F	F	T
F	F	F	T	T
F	F	T	F	F
F	F	T	T	T
F	T	F	F	T
F	T	F	T	T
F	T	T	F	F
F	T	T	T	T
T	F	F	F	T
T	F	F	T	T
T	F	T	F	F
T	F	T	T	T
T	T	F	F	T
T	T	F	T	T
T	T	T	F	T
T	T	T	T	T

1)

- Condition Decision Coverage Pairs(c/d) = FTTF, TFFT
- Condition (only) Coverage Pairs(c) = FFFT, TTTF
- Decision (only) Coverage Pair(d) = FFFF, FFTF

2)

- Term Omission Faults (TOF's):  $c'+d$ ,  $ab+d$ ,  $ab+c'$
- Term Negation Faults (TNF's):  $ab+c+d$ ,  $ab+c'+d'$ ,  $(ab)'+c'+d$

**d.  $ab \text{ XOR } (a + b)$**

$$\begin{aligned} &= (ab)(a+b)' + (ab)'(a+b) \\ &= (ab)(a'b') + (a'+b')(a+b) \\ &= aa' + a'b + ab' + bb' \\ &= a'b + ab' \end{aligned}$$

a	b	$a'b + ab'$
F	F	F
F	T	T
T	F	T
T	T	F

1)

- Condition Decision Coverage Pairs(c/d) = No c/d coverage
- Condition (only) Coverage Pairs(c) = FT, TF
- Decision (only) Coverage Pair(d) = FF, FT

2)

- Term Omission Faults (TOF's):  $a'b, ab'$
- Term Negation Faults (TNF's):  $(a'b)' + ab', a'b + (ab')'$

**Problem 5.**

**SOLUTION:**

**Question 1:**

**a.  $ab' + c$**

Condition of interest of a (COI's of a): XFF

Condition of interest of b (COI's of b): TXF

Condition of interest of c (COI's of c): FTX, FFX, TTX

Base set (BS) => TFF, FFF, TTF

Unique Cause Solution 1(UC 1): TFF, FFF, TTF, FFT

Unique Cause Solution 2(UC 2): TFF, FFF, TTF, TTT

**b.  $a' + b + c$**

Condition of interest of a (COI's of a): XFF

Condition of interest of b (COI's of b): TXF

Condition of interest of c (COI's of c): TFX



Base set (BS): TFF, FFF, TTF, TFT

Unique Cause Solution 1(UC 1): TFF, FFF, TTF, FFT

c.  $a + bc + d'$

Condition of interest of a (COI's of a): XFTT, XTFT, XFFT

Condition of interest of b (COI's of b): FXTT

Condition of interest of c (COI's of c): FTXT

Condition of interest of d (COI's of d): FFTX, FTFX, FFFX

Base set (BS): FTTT, FFTT, FTFT

Unique Cause Solution 1(UC 1): FTTT, FFTT, FTFT, TFFT, FFTF

Unique Cause Solution 2(UC 2): FTTT, FFTT, FTFT, TTFT, FTFF

## Question 2:

a.  $abc \text{ XOR } (ab'c)'$

Solving given problem:

$$= (abc)(ab'c') + (abc)'(ab'c)'$$

$$= (abc)'(ab'c)'$$

$$= ((ab)' + c')((ab')' + c)$$

$$= (a' + b' + c')(a' + b + c)$$

$$= a' + b'c + bc'$$

Truth table for  $a' + b'c + bc'$ :

a	b	c	$a' + b'c + bc'$
F	F	F	T
F	F	T	T
F	T	F	T
F	T	T	T
T	F	F	F
T	F	T	T
T	T	F	T
T	T	T	F

1)

- Condition Decision Coverage Pairs(c/d) = FTT, TFF
- Condition (only) Coverage Pairs(c) = FFT, TTF
- Decision (only) Coverage Pair(d) = FFF, TFF

2)

- Term Omission Faults (TOF's):  $a'+b'c, a'+bc', b'c+bc'$
- Term Negation Faults (TNF's):  $a+b'c+bc', a'+(b'c)'+bc', a'+b'c+(bc')'$

**b.  $((a+b)(b'+c))'$**

Solving given problem:

$$=(a+b)' + (b'+c)'$$

$$=a'b'+bc'$$

Truth Table:

a	b	c	$a'b'+bc'$
F	F	F	T
F	F	T	T
F	T	F	T
F	T	T	F
T	F	F	F
T	F	T	F
T	T	F	T
T	T	T	F

1)

- Condition Decision Coverage Pairs(c/d) = FTF, TFT
- Condition (only) Coverage Pairs(c) = FFT, TTF
- Decision (only) Coverage Pair(d) = FFF, FTT

2)

- Term Omission Faults (TOF's):  $bc', a'b'$
- Term Negation Faults (TNF's):  $(a'b')'+bc', a'b'+(bc')'$

**c.  $(ab' + ac + c'd)'$**

Solving given problem:

$$=(ab')' + (ac)' + (c'd)'$$

$$=(a'+b)(a'+c')(c+d)'$$

$$=(a'a'+a'c'+ba'+bc')(c+d)'$$

$$=(a'+bc')(c+d)'$$

$$=a'c+a'd'+bc'c+bc'd'$$

$$=a'c+a'd'+bc'd'$$

Truth Table:

a	b	c	d	$a'c+a'd'+bc'd'$
F	F	F	F	T
F	F	F	T	F
F	F	T	F	T
F	F	T	T	T
F	T	F	F	T
F	T	F	T	F
F	T	T	F	T
F	T	T	T	T
T	F	F	F	F
T	F	F	T	F
T	F	T	F	F
T	F	T	T	F
T	T	F	F	T
T	T	F	T	F
T	T	T	F	F
T	T	T	T	F

1)

- Condition Decision Coverage Pairs(c/d) = FFTF, TTFT
- Condition (only) Coverage Pairs(c) = FFFT, TTTF
- Decision (only) Coverage Pair(d) = FFFF, FFFT

2)

- Term Omission Faults (TOF's):  $a'd'+bc'd'$ ,  $a'c+bc'd'$ ,  $a'c+a'd'$
- Term Negation Faults (TNF's):  $(a'c)+a'd'+bc'd'$ ,  $a'c+(a'd')'+bc'd'$ ,  $a'c+a'd'+(bc'd')'$

Question 3:

a.  $(a'b'c' + a'b'd')'$

Solving given problem:

$$= (a'b'c')' (a'b'd')'$$

$$\begin{aligned}
&= ((a'b')'+c) ((a'b')'+d) \\
&= (a+b+c)(a+b+d) \\
&= a+b+cd
\end{aligned}$$

Condition of interest of a (COI's of a): XFFT, XFTF, XFFF

Condition of interest of b (COI's of b): FXFT, FXTF, FXFF

Condition of interest of c (COI's of c): FFXT

Condition of interest of d (COI's of d): FFTX

Base Set (BS) – FFFT, FFTT, FFTF

Unique Cause Solution 1(UC 1) - FFFT, FFTT, FFTF, TTFT, FTFT

Unique Cause Solution 2(UC 2) - FFFT, FFTT, FFTF, TTFT, FTFT

Unique Cause Solution 3(UC 3) - FFFT, FFTT, FFTF, TTFT, FTFT

Unique Cause Solution 4(UC 4) - FFFT, FFTT, FFTF, TTFT, FTFT

**b.  $(a'c' + a'd' + a'b)'$**

Solving given problem:

$$= (a'c' + a'd')' (a'b)'$$

$$= (a'c')' (a'd')' (a'b)'$$

$$= (a+c)(a+d)(a+b')$$

$$= a+b'cd$$

Condition of interest of a (COI's of a): XFFF, XFFT, XFTF, XTFF, XFTT, XTTF, XTTF

Condition of interest of b (COI's of b): FXFF,FXFT,FXTF

Condition of interest of c (COI's of c): FTXF,FFXT,FTXT

Condition of interest of d (COI's of d): FFFX,FTFX,FTTX

Base Set (BS) – FTTF,FTTF,FFTF,FFTF

Unique Cause Solution 1(UC 1) - FTTF,FTTF,FFTF,FFTF,TTFT

Unique Cause Solution 2(UC 2) - FTTF,FTTF,FFTF,FFTF,TTFT

Unique Cause Solution 3(UC 3) - FTTF,FTTF,FFTF,FFTF,TTFT

**c.  $(abd + acd)'$**

Solving given problem:

$$= (abd)' (acd)'$$

$$= (a'+b'+d')(a'+c'+d')$$

$$= a' + b'c' + d'$$

Condition of interest of a (COI's of a): XTTF,XTTF,XFTT

Condition of interest of b (COI's of b): TXFT

Condition of interest of c (COI's of c): TFXF

Condition of interest of d (COI's of d): TTFX,TTFX,TFTX

Base Set (BS) – TTFT,TFTT,TFTT

Unique Cause Solution 1 - TTFT,TFTT,TFFT,FTFT,TTFF  
 Unique Cause Solution 2 - TTFT,TFTT,TFFT,FTFT,TFTF  
 Unique Cause Solution 3 - TTFT,TFTT,TFFT,FFTT,TTFF  
 Unique Cause Solution 4 - TTFT,TFTT,TFFT,FFTT,TFTF

### Bonus Point questions

Extra credits:

Problem b1)

**a)  $ab' + c' + d'$**

Condition of interest of a (COI's of a): XFTT

Condition of interest of b (COI's of b): TXTT

Condition of interest of c (COI's of c): FFXT, FTXT, TTXT

Condition of interest of d (COI's of d): FFTX, FTTX, TTTX

Base Set (BS) – TFTT, FFTT, TTTT

Unique Cause Solution 1(UC 1) - TFTT, FFTT, TTTT, TTFT, TTTF

Unique Cause Solution 2(UC 2) - TFTT, FFTT, TTTT, FFFT, FTFE

Masking Solution 1 - TFTT, FFTT, TTTT, FTFT, FTTF

**b)  $a + bc + d'$**

Condition of interest of a (COI's of a): XFFT, XFTT, XTFT

Condition of interest of b (COI's of b): FXTT

Condition of interest of c (COI's of c): FTXT

Condition of interest of d (COI's of d): FFFX, FFTX, FTFX

Base Set (BS) – FTTT, FFTT, FTFT

Unique Cause Solution 1(UC 1) - FTTT, FFTT, FTFT, TFFT, FTFE

Unique Cause Solution 2(UC 2) - FTTT, FFTT, FTFT, TTFT, FTFF

Masking Solution 1 - FTTT, FFTT, FTFT, TFFT, FFFT

Problem b2)

**a.  $a = (b < 0) \vee c$**

From the above condition, Boundary values of b = -1,0.

	Inputs		Expected Outputs
Test Case	b	c	a
1	0	F	F
2	-1	T	T
3	-1	F	T

**b.  $a = b \ \&\& \ (c < 5)$**

From the above condition, Boundary values of  $c = 4, 5$ .

	Inputs		Expected Outputs
Test Case	b	c	a
1	T	5	F
2	F	4	F
3	T	4	T

**c.  $a = (b > 5) \ \&\& \ (c < 8)$**

From the above condition, Boundary values of  $b = 5, 6$ .

From the above condition, Boundary values of  $c = 7, 8$ .

	Inputs		Expected Outputs
Test Case	b	c	a
1	5	7	F
2	6	8	F
3	6	7	T

**d.  $a = (b > 5) \ \&\& \ (b < 10)$**

From the above condition, Boundary values of first  $b(b > 5) = 5, 6$ .

From the above condition, Boundary values of second  $b(b < 10) = 9, 10$ .

	Input	Expected Outputs
Test Case	b	a
1	5	F
2	6 or 9	T
3	10	F
4	9 or 6	T

