## 1 | Openstax Calc vol 1 chap 2.4 ex 134

$$g(t) = \frac{1}{t} + 1$$

which is basically  $\frac{1}{x}$  shied up by one, so there is an infinite discontinuity at x=0

#### 2 | 136

There is a jump discontinuity at x=2, because normally  $y=\frac{x}{x}$  simplifies to y=1, but the sign flips at x=2.

#### 3 | 142

$$f(y) = \frac{\sin(\pi y)}{\tan(\pi y)} = \frac{\sin(\pi y)\cos(\pi y)}{\sin(\pi y)}$$

So there is a removable discontinuity at y=1, because there is a discontinuity but it can be removed with algebra.

### 4 | 148

$$e^{4k} = 4 + 3$$
$$e^{4k} = 7$$
$$4k = \ln(7)$$
$$k = \frac{\ln(7)}{4}$$

# 5 | **TODO 174**

Prove f(x) is continues everywhere, meaning show that  $\forall c \in \mathbb{R}$ 

$$\lim_{x\to c} f(x) = f(c)$$

Because we can always evaluate f(x), the limit always exists.

## 6 | Paul's online math notes Section 2-9: 23

The IVT states that when a function is continuous over a closed interval [a,b], then for all  $\min\{f(a),f(b)\} \le y \le \max\{f(a),f(b)\}$  there exists some  $a \le c \le b$  s.t. f(c)=y. In this case, we have f(4)=193 and f(8)=-511. f(x) is a polynomial, so it is continuous over the range. Because our values stradle zero, there must be some value  $4 \le c \le 8$  s.t. f(c)=0.

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# 7 | Boundedness theorem

Given a function f(x) that is continuous on a closed interval [a,b], there exists some  $M \in \mathbb{R}$  s.t.  $f(c) \leq M$  for all  $a \leq c \leq b$  aka M is an upper bound on f(x) over the interval [a,b]. There's also one that's less than all c. Doesn't work for open intervals.

7.1  $\mid$  (0, 1]: not continuous, not a closed interval

7.2  $\mid [0, 1)$ : not a closed interval

7.3  $\mid$  (0, 1]: not a closed interval

7.4  $\mid (0, 1]$ : not continuous, not a closed interval

7.5 |  $f(x) = \frac{1}{x}$ : not continuous

## 8 | Epilouge

Other than Problem 5, this took roughly 40 minutes. I still don't know how to do problem 5...

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