## 1 | boatman problem

Target displacement: (3km, 2km)

We are working with the velocities of the boat and the river. The velocity of the river is defined as  $r = \langle 0, -3.5 \rangle$ . We want to find vector  $v = \langle v_x, v_y \rangle$  s.t.

$$|v|=13 \ \text{km/h}$$
 
$$\lambda(v+r)=\langle 3,2\rangle$$

 $v_x^2 + v_y^2 = 13^2$ 

Where the trip will take  $\lambda$  hours

$$\lambda(v_x + 0) = 3$$

$$\lambda(v_y + -3.5) = 2$$

$$v_x = \frac{3}{\lambda}$$

$$v_y = \frac{2}{\lambda} + 3.5$$

$$\frac{3^2}{\lambda^2} + \left(\frac{2}{\lambda} + 3.5\right)^2 = 13^2$$

$$\frac{3^2}{\lambda^2} + \frac{2^2}{\lambda^2} + 3.5^2 + \frac{4(3.5)}{\lambda} = 13^2$$

$$\frac{3^2 + 2^2}{\lambda^2} + \frac{4(3.5)}{\lambda} = 13^2 - 3.5^2$$

$$3^2 + 2^2 + 4(3.5)\lambda = \lambda^2 \left(13^2 - 3.5^2\right)$$

 $13 + 4(3.5)\lambda = \lambda^2 (156.75)$ 

 $-156.75\lambda^2 + 14^2 + 13 = 0$ 

 $\frac{-14 \pm \sqrt{14^2 + 4(13)156.75}}{-2(156.75)}$ 

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