

#flo #hw

1 | Finite-Dimensional Vector Spaces

title: Review

F denotes \mathbb{R} or \mathbb{C}

V denotes a [\[\[file:KBe20math530refVectorSpace.org\]\]](http://file.KBe20math530refVectorSpace.org) [\[KBe20math530refVectorSpace\]](#) over F

- lin alg does not focus on arbitrary vector spaces
- it focuses on finite-dimensional vector spaces!

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title: learning objectives for the chapter
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- span //covered in section
- linear independence //covered in section
- bases
- dimension

- **notation:**
 - lists of vectors:
 - * $(2,1,4),(3,2,5)$
 - list len 2 of vectors in \mathbb{R}^3
 - * n-tuples without surrounding parens
- *linear combination*
 - a linear combination of x and y would be any expression of the form $ax + by$, where a and b are constants ~wiki
 - multiply each element in a list of vectors by an element in F
 - and then add them up!
 - any relation between the element scalar and what's being multiplied? can the scalars repeat?
#question
 - * yes, yes they can.
- *span*
 - the set of all linear combos of a list of vectors
 - * denoted: $\text{span}(v_1, \dots, v_m)$
 - span of empty list is $\{0\}$
 - aka. linear span
- *KBxSpansLinAlg*

the span of a list of vectors in V is the smallest subspace of V containing all the vectors in the list

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```ad-question
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but don't you get out a single vector at the end..? because you add them? #question no! because it's the

- \*finite-dimensional vector space
  - a vector space is called finite-dimensional if some list of vectors in it spans the space
    - \* spans the space..?
    - \* ????
- linear independence
  - a list of vectors in  $V$  where the only choice of  $a_1 \dots a_m$  in  $F$  that makes  $a_1 v_1 + \dots + a_m v_m = 0$  is  $a_1 = \dots = a_m = 0$
  - unique way to get 0?
- linearly dependent
  - opposite, can get to 0 with non-zero scalars
- KBxLinearIndependence

#review the end here #todo some exercises