

## 1 | Practice Problems

The relevant questions can be found here.

1. One should use a one-sided limit, more specifically a right-hand limit because  $\sqrt{x}$  is only defined for  $x \geq 0$ .

$$\lim_{x \rightarrow 0^+} \sqrt{x} = 0$$

2. One should use a one-sided limit because  $\frac{1}{x+1}$  has an infinite discontinuity with asymptotes at  $x = -1$ . Either side will work.  $\lim_{x \rightarrow 0^+} \frac{1}{x+1} = \infty$   $\lim_{x \rightarrow 0^-} \frac{1}{x+1} = -\infty$

3. One should use a two-sided limit because  $\frac{1}{(x-1)^4}$  goes to infinity as  $x$  tends toward one from either side due to its even asymptote.

$$\lim_{x \rightarrow 1} \frac{1}{(x-1)^4} = \infty$$

4. One should use a two-sided limit because  $|\sin(x)|$  is continuous.  $\lim_{x \rightarrow 1} |\sin(x)| = 0$

5. One should use a one-sided limit as the function  $\frac{|x|}{x}$  has a jump discontinuity at  $x = 0$  and the left and right hand limits are not equal. Either side will work.  $\lim_{x \rightarrow 0^+} \frac{|x|}{x} = 1$   $\lim_{x \rightarrow 0^-} \frac{|x|}{x} = -1$