## 1 | the equation

The goal is to add a bunch of slices,  $d\theta$ . For instance, you can approximate each slice as a sector of a circle:

$$dA = \underbrace{\left(\pi r^2\right)}_{\text{Area of the full circle Fraction of the circle}} \underbrace{\frac{d\theta}{2\pi}}_{\text{Fraction of the circle}}$$
 
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where The area of the full circle

The portion of the circle covered by  $d\theta$ 

And so, the full equation would be

$$A = \int_0^{2\pi} \frac{1}{2} r^2 d\theta$$

Make sure you pick the bounds such that it only goes once around! If it's a cardiod with overlappy bits then you gotta make sure you know what area you're talking about.

## 1.1 | alternative formulation

You could also formulate the circle slice as an icosolese triangle, where the base is  $rd\theta$  and the height is r. Then, the area of the triangle is

$$dA = \frac{1}{2}bh = \frac{1}{2}r^2d\theta$$

Which results in the same equation as above.

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