1 | Problem 1

$$\begin{split} KE_{total} &= \sum_{i=1}^{N} \frac{1}{2} m_i v_i^2 \\ &= \sum_{i=1}^{N} \frac{1}{2} m_i (\vec{v}_i \cdot \vec{v}_i) \\ &= \sum_{i=1}^{N} \frac{1}{2} m_i (\vec{V}_{CM}(t)^2 + 2 \vec{V}_{CM}(t) \vec{v}_i'(t) + \vec{v}_i'(t)^2) \\ &\setminus [\\ &= \sum_{i=1}^{N} \frac{1}{2} m_i (\vec{V}_{CM}(t)^2 + 2 \vec{V}_{CM}(t) \vec{v}_i'(t)) + \sum_{i=1}^{N} \frac{1}{2} m_i (v_i'^2) \\ &= \frac{1}{2} M V_{CM}^2 + V_{CM} \cdot \sum_{i=1}^{N} m_i \vec{v}_i' + \sum_{i=1}^{N} \frac{1}{2} m_i (v_i'^2) \\ &= \frac{1}{2} M v_{CM}^2 + \frac{1}{2} \sum_{i=1}^{N} m_i (v_i'^2) \end{split}$$