

The dot product is a projection of a vector onto a column space. (It's kind of like the closest vector to the out-of-range one that is in range). We can find this vector for the column space of  $A$  by taking  $A^T b$ . Thus, when we see this

$$AA^T x$$

we are somehow 'projecting'  $x$  on to  $A$ .