

1 | Dot product:

- Name: dot product
- Result: Scalar
- Interpretation (what it measures): parallelity
 - the more parallel the larger the dot product
- Magnitude (with sign): $|\vec{a}||\vec{b}|\cos(\theta)$
- Geometric magnitude: $|\vec{a}||\vec{b}_{\parallel\vec{a}}|$
- Direction: no direction
- Algebraic form: $a_x b_x + a_y b_y + a_z b_z$
- Algebraic properties:
 - commutative
 - associative
 - distributive across addition

2 | Cross product:

- Name: Cross product
- Result: Vector
- Interpretation (what it measures): Orthgonality
 - the more orthogonal the longer the cross product
- Magnitude (with sign): $|\vec{a}||\vec{b}|\sin(\theta)$
- Geometric Magnitude: $|\vec{a}||\vec{b}_{\perp\vec{a}}|$
- Direction: perpendicular to the two vectors
 - by the right hand rule by rotating the first vector into the second vector

3 | Application of cross product:

- In physics there is something called torque, notated τ
 - Torque is the net force of things that rotate, so:
 - * $F_{net} = ma$
 - * $\tau_{net} = I\omega$
- Somethings to note about τ :
 - It increases with a longer lever
 - It increases with a greater force

- ★ that is perpendicular to the lever
- Given these requirements we can make a formula:
 - $|\tau| = |\vec{r}||\vec{F}_{\perp\vec{r}}|$, where \vec{F} is the force applied to the door, and \vec{r} is the radius of the lever.
 - this, the right side of the equation, can be described using the dot product: $|\tau| = \vec{r} \times \vec{F}$