Here are four easy integrals.

## 1 | Single Value Function

$$f_1: \mathbb{R}^2 \to \mathbb{R}^1 \tag{1}$$

$$f_1(x,y) = 0 (2)$$

What's the area of this function?

We can take the area of the shape, essentially by taking the volume by height 1: that is, for a rectangle of l, w, h, its top-area is simply  $l \cdot w$ , also known as  $lw \cdot 1$ . Therefore:

$$\int_0^7 \int_0^5 1 dx \, dy = 35 \tag{3}$$

The area of the shape is therefore 35.

## 2 | Area of the Plane

We want to first figure the correction per every given slice  $dA = n \ dV$  to setup a surface integral. By pythagoras (i.e. projecting the changes to the parallelity of the surface), we have that:

$$dA = \sqrt{1 + \left(\frac{\partial f}{\partial x}\right) + \left(\frac{\partial f}{\partial y}\right)} \, dV \tag{4}$$

Therefore: