

#flo #hw

## 1 | Linear Maps

no one gets excited about vector spaces -axler

the interesting part: linear maps!

title: learning objectives

- fundamentals theorem of linear maps
- matrix of linear map w.r.t. given bases
- isomorphic vec spaces
- product spaces
- quotient spaces
- duals spaces
  - vector space
  - linear map

## 2 | The vector space of linear maps

key definition!

title: linear map

aka \*linear transformation.\*

a \*linear map\* from  $V$  to  $W$  is a function  $T: V \rightarrow W$  with the following properties:

**\*\*additivity\*\***

$T(u+v) = Tu + Tv$  for all  $u, v \in V$ ;

**\*\*homogeneity\*\***

$T(\lambda v) = \lambda T(v)$  for all  $\lambda \in F$  and  $v \in V$ .

the functional notation  $T(V)$  is the same as the notation  $Tv$  when talking about linear maps.

title: notation --  $L(V, W)$

the set of all linear maps from  $V$  to  $W$ .

### 2.0.1 | examples of linear maps

- 0?
  - 0 is the func that takes each ele from some vec space to the additive iden of another vec space.
    - \*  $0v = 0$
    - \* left: func from  $V$  to  $W$ , right: additive iden in  $W$
    - \* #question what does it mean for it to be a function from  $V$  to  $W$ ?
- identity, denoted  $I$ 
  - $Iv = v$
  - maps each element to itself linear transformation like a .map? code!! this is some code!