## 1 | Isomorphism

def

An isomorphism is an invertible linear map

# 2 | Isomorphic def

Two vector spaces are called *isomorphic* if there is an isomorphism from one vector space into the other

## 2.1 | intuition

Can be thought of as relabeling each element v from one space into an element Tv in the other.

#### 2.2 | results

#### 2.2.1 | equal dimension iff isomorphic Axler3.59

Two vector spaces over some field  $\mathbb{F}$  are isomorphic iff they have the same dimension.

### 2.2.2 $|\mathcal{L}(V,W)|$ and $\mathbb{F}^{m,n}$ are isomorphic

Given two bases of V and W,  $\mathcal{M}$  is an isomorphism between  $\mathcal{L}(V,W)$  and  $\mathbb{F}^{m,n}$ 

## 2.2.3 | Axler3.61 dim $\mathcal{L}(V,W) = (\dim V) (\dim V)$

#### 2.3 | intuition

Not only do two isomorphic spaces have a one to one correspondence between them, that coresspondence is linear which means that they way the elements interact on one side is the same on the other.

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