We first set up the basic assumptions and variables.

```
GRAV <- 9.8 # gravity (m/s^2)

MASS <- 1 # mass (kg)

I_ROT <- 1 # roational inertia (kg m^2)

L1 <- 0.5 # distance from rotation point to CoM (m)

L2 <- 1 # distance from rotation ponit to tension (m)

PHI <- 0 # angle of Ft relative to floor orthogoal (rad)

FT <- 11 # tension force (N)

OMEGA <- 0 # angle of line orthogonal to floor relative to gravity (rad) (because shifted axis)
```

Additionally, we set the time interval and seed values for time and theta (distance from flat):

```
dt <- 0.0001
t_max <- 5

vx <- 0
vy <- 0

theta <- 0
thetadot <- 0
time <- 0</pre>
```

First, let's create a function for torque in terms of theta (and the constants above:

```
net_torque <- function(theta) {
    return(L2 * FT * cos(theta + PHI) - L1 * MASS * GRAV * cos(theta - OMEGA))
}</pre>
```

Great. Let's start generating the table! We essentially write a for loop to appends to a few different vectors. Variables appended with c reflect the column vectors that we will put together.

```
cTime = NULL
cTheta = NULL
cDDTheta = NULL
cDTheta = NULL
cTorqueNet = NULL
cAccelX = NULL
cAccelY = NULL
cVelX = NULL
cVelY = NULL
cFFriction = NULL
cFNormal = NULL
# debugging values
cFNetY = NULL
cFTensionPhiComponent = NULL
cFGravityPhiComponent = NULL
cMuStatic = NULL
cKERot = NULL
cKETrans = NULL
```

Awesome. Let's now run a lovely little for loop to actually populate the values recursively.

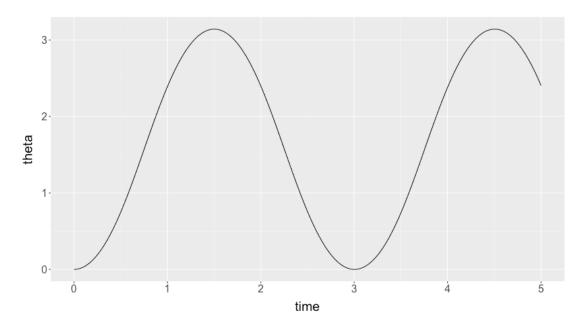
```
for (i in 0:(t max/dt)) {
    # We first populate the time column with the time, theta column with theta
    cTime[i] = time
    cTheta[i] = theta
    torque <- net_torque(theta)</pre>
    # Given the theta value, we calculate the net torque and set that
    cTorqueNet[i] = torque
    # Now that we know the net torque, we could know how much the angular
    # acceleration is by just dividing out the rotational inertia
    thetadotdot <- torque/I_ROT
    cDDTheta[i] = thetadotdot
    # We could also multiply the theta acceleration by time to get the
    # velocity at that point
    thetadot <- dt*thetadotdot + thetadot</pre>
    cDTheta[i] = thetadot
    # We could therefore component-ize the acceleration in theta into
    # ax and av
    ax \leftarrow -1 * L1 * sin(theta) * thetadotdot
    cAccelX[i] = ax
    ay <- L1 * cos(theta) * thetadotdot
    cAccelY[i] = ay # @mark isn't sin and cos backwards?
    # We also tally the components seperately for velocity
    vx \leftarrow ax*dt + vx
    vy \leftarrow ay*dt + vy
    # Based on these accelerations, we therefore could calculate the relative
    # force of friction and normal force by subtracting the force in that direction
    # out of net
    ffriction <- FT*sin(PHI) + MASS*GRAV*sin(OMEGA)-MASS*ax
    fnormal <- MASS*ay-FT*cos(PHI)+MASS*GRAV*cos(OMEGA)</pre>
    cFNetY[i] = MASS*ay
    cFTensionPhiComponent[i] = FT*cos(PHI)
    cFGravityPhiComponent[i] = -MASS*GRAV*cos(OMEGA)
    cFFriction[i] = ffriction
    cFNormal[i] = fnormal
    # Then, we calculate the energies
    cKERot[i] = 0.5 * I ROT * thetadot^2
    cKETrans[i] = 0.5 * MASS * (vx^2+vy^2)
    # Dividing the friction force by the normal force, of course, will result in
    # the (min?) friction coeff
    cMuStatic[i] = ffriction/fnormal
    # We incriment the time and also increment theta by multiplying the velocity
    # by dt to get change in the next increment
    time <- dt + time
    theta <- dt*thetadot + theta
}
```

We now put all of this together in a dataframe.

```
rotating_link <- data.frame(cTime,</pre>
   cTheta.
   cDTheta,
   cDDTheta,
   cTorqueNet,
   cAccelX,
   cAccelY.
   cFFriction,
   cFNormal.
   cMuStatic,
   cKERot,
   cKETrans)
names(rotating_link) <- c("time",</pre>
 "theta",
 "d.theta"
 "dd.theta"
 "net.torque",
 "accel.x",
 "accel.y",
 "friction.force",
 "normal.force",
 "friction.coeff",
 "ke.rot".
 "ke.trans")
Let's import some visualization tools, etc.
library(tidyverse)
Let's first see the head of this table:
head(rotating_link)
1e-04 6.1e-08 0.00122 6.099999999999 6.099999999999 -1.8605e-07 3.049999999999 1.8605e-07
5.5814999999987e-07 1.849999999999 3.01702702702712e-07 1.6744499999998e-06 4.18612499999992e-07
3e-04 3.65999999999e-07 0.002439999999995 6.0999999999 6.0999999999 -1.1162999999999e-06
3.049999999999 1.116299999999e-06 1.849999999999 6.03405405405483e-07 2.97679999999987e-06
7.4419999999953e-07
4e-04 6.099999999994e-07 0.0030499999999983 6.0999999999887 6.0999999999887 -1.86049999999952e-06
3.0499999999887 1.86049999999952e-06 1.8499999999887 1.00567567567603e-06 4.65124999999949e-06
1.16281249999982e-06
5e-04 9.149999999977e-07 0.0036599999999958 6.099999999745 6.0999999999745 -2.79074999999837e-06
3.0499999999745 2.79074999999837e-06 1.8499999999745 1.50851351351472e-06 6.69779999999846e-06
1.67444999999944e-06
6e-04 1.280999999999e-06 0.0042699999999998 6.099999999999 6.099999999999 -3.90704999999553e-06
3.0499999999499 3.90704999999553e-06 1.849999999995 2.11191891892221e-06 9.116449999999606e-06
2.27911249999858e-06
Before we start graphing, let's set a common graph there.
default.theme <- theme(text = element_text(size=20), axis.title.y = element_text(margin = margin(t = 0,
```

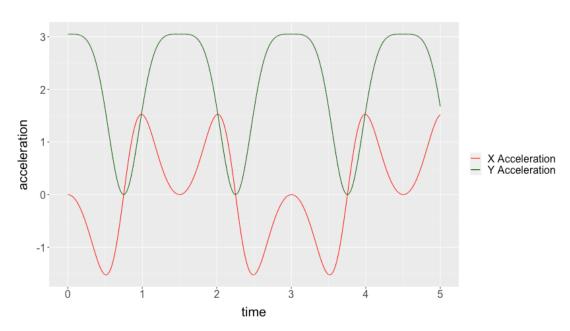
Cool! We could first graph a function for theta over time.

rotating_link %>% ggplot() + geom_line(aes(x=time, y=theta)) + default.theme



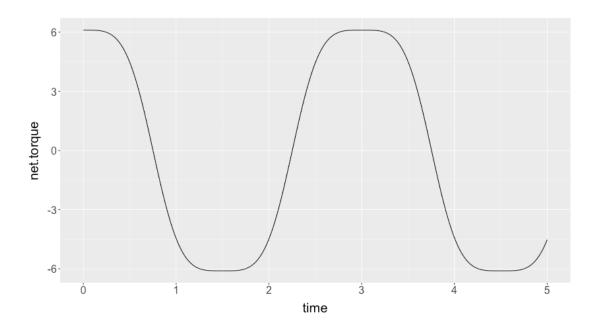
And, similarly, we will graph ax and ay on top of each other:

rotating_link %>% ggplot() + geom_line(aes(x=time, y=accel.x, colour="X Acceleration")) + geom_line(aes



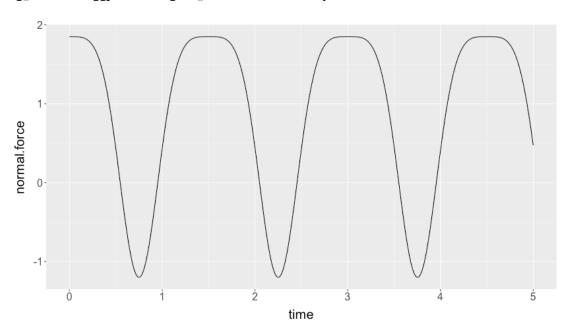
Let's also plot torque as well.

rotating_link %>% ggplot() + geom_line(aes(x=time, y=net.torque)) + default.theme



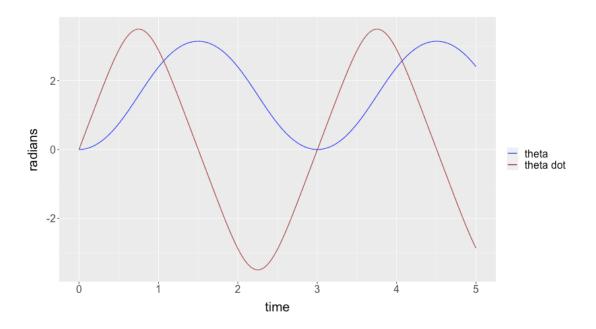
And. Most importantly! Let's plot the normal force.

 $\verb|rotating_link \%>\%| ggplot() + geom_line(aes(x=time, y=normal.force)) + default.theme|$



Obviously, after the normal force becomes negative, this graph stops being useful. Theta dot atop theta:

rotating_link %>% ggplot() + geom_line(aes(x=time, y=theta, colour="theta")) + geom_line(aes(x=time, y=theta, tolour="theta")) + geom_line(aes(x=time, y=theta, tolour="theta")) + geom_line(aes(x=time, y=theta, tolour="theta")) + geom_line(aes(x=time, y=theta, y=theta, tolour="theta")) + geom_line(aes(x=time, y=theta, y=the



We finally, plot KE rotation and translation

 $\verb|rotating_link| \%>\% | \texttt{ggplot()} + \texttt{geom_line(aes(x=time, y=ke.rot, colour="ke rotation"))} + \texttt{geom_line(aes(x=time, y=ke.rot, colour="ke rotation")} + \texttt{geom_line(aes(x=time, y=ke.rot, colour="ke rotation")} + \texttt{geom_line(aes(x=time, y=ke.$

