

1 | Calculating Derivatives

unit1::derivatives

1.1 | Types of Formulas

Two kinds of formulas, specific (for specific functions) and general. Both are needed to solve polynomials.

1.2 | Derivative of $\sin(x)$

This only works with radians! Loose summary of derivation:

- $\lim_{x \rightarrow 0} \frac{\sin(x+\Delta x) - f(x)}{\Delta x}$
- Use trigonometric identities to expand the $\sin(x+\Delta x)$ term. $\sin(a+b) = \sin(a)\cos(b) + \cos(a)\sin(b)$.
- Group the terms by plugging in the derivative at $x = 0$ such that the resulting quotients end up cancelling.

$\sin(x) \left(\frac{\cos(\Delta x) - 1}{\Delta x} \right) + \cos(x) \left(\frac{\sin(\Delta x)}{\Delta x} \right)$ Right side's quotient goes to 1, left side goes to 0, so the entire equation goes to $\cos(x)$ The derivatives of sin and cosine at $x = 0$ give all values of the derivative of sine and cosine.

1.3 | Derivative of $\cos(x)$

Similar derivation to above which yields $-\sin(x)$.

1.4 | Some General Rules

- Product rule: $(uv)' = u'v + uv'$
- Quotient rule: $\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$

2 | Links

Differentiation Rules builds upon this.