PS#24: More easy 2D areas!

Nueva Multivariable Calculus

Boy! All these higher-dimensional areas and volumes have been such a pain. Last week, we took a chill break from those septuple integrals to do an easy single integral, $\int_{-}^{+} e^{-x^2} dx$. Let's do some more easy single integrals that beget simple 2D areas!

(Do all these problems without looking up any advice or formulas or help!

1. What's the area of a rectangle with corners at the origin and (5,7)? Or, phrased more complicatedly (for symmetry with the rest of the problems), consider the function:

$$f_1: \mathbb{R}^2 \to \mathbb{R}^1$$

$$f_1(x,y) = 0$$

What's the area of this function, above a rectangle with corners at the origin and at (5,7)?

2. Consider the plane:

$$f_2: \mathbb{R}^2 \to \mathbb{R}^1$$

$$f_2(x,y) = 2x + 3y + 10$$

What's the area (as in, like, the one-sided surface area) of this function, above a rectangle with corners at the origin and at (5,7)?

3. Consider the stretched-out parabola:

$$f_3: \mathbb{R}^2 \to \mathbb{R}^1$$

$$f_3(x,y) = x^2$$

What's the surface area of the function, above a rectangle with corners at the origin and at (5,7)? (Again, by "surface area" here I just mean the area of one side, although if you feel compelled to double it, that doesn't fundamentally alter the problem.)

4. Consider the hyperbolic paraboloid:

$$f_4: \mathbb{R}^2 \to \mathbb{R}^1$$

$$f_4(x,y) = x^2 - y^2$$

Again, what's the area of this function, above a rectangle with corners at the origin and at (5,7)?