## 1 | A surface integral

We are defining a function:

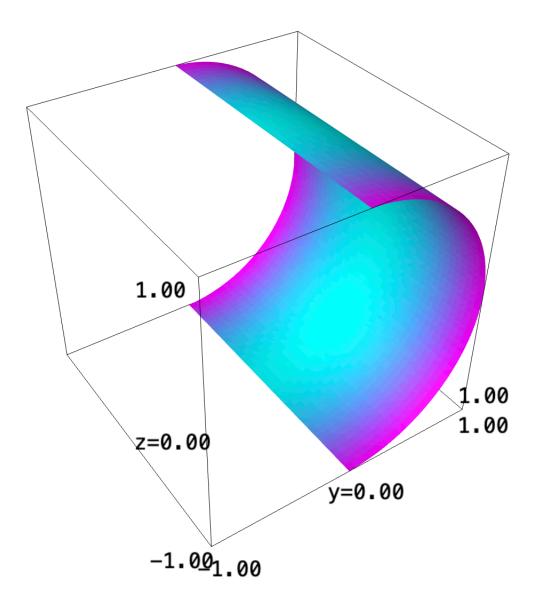
$$f(x, y, z) = y^2 \tag{1}$$

and slicing out a vertical organ pipe shape with a sliced edge. That is:

$$x^2 + z^2 = 1 (2)$$

bounded by y > 0 and y < 3 - x.

Let's plot this:



that's honestly pretty cool!

Great, now let's take the actual surface integral.

Looking at the actual function for which we are taking the integral, we have:

$$x^2 + z^2 = 1 (3)$$

We will rearrange this expression in terms of z:

$$z = \sqrt{1 - x^2} \tag{4}$$

Fortunately, we see already that the function's derivative w.r.t. y is 0; indeed, it doesn't change along the y direction (the cylinder is centered around it after all.)