#ret

1. Suppose A = $\begin{pmatrix} 1 & 3 \\ 2 & -1 \end{pmatrix}$ and B = $\begin{pmatrix} 0 & -1 \\ 2 & 1 \end{pmatrix}$. Multiply AB and BA. What do you notice???

Nothing. Matrix multiplication is not commutative.

$$\begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \begin{bmatrix} x = 2 \\ x + 3y \end{bmatrix} = \begin{bmatrix} 14 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} 7x \\ x + 3y \end{bmatrix} = \begin{bmatrix} 14 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} \frac{7}{7} & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 7x \\ x + 3y \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 7x \\ x + 3y \end{bmatrix} = \begin{bmatrix} 2 \\ 5 \\ x + 3y \end{bmatrix} = \begin{bmatrix} 2 \\ 5 \\ 5 \end{bmatrix}$$

$$\begin{bmatrix} x \\ x + 3y \end{bmatrix} = \begin{bmatrix} 2 \\ 5 \end{bmatrix}$$

$$x = 2$$

$$x = 2$$

rest of it with matrices, so I'll just do it normally: $\ [2+3y=5\]$ 3. > Do 2x2 matrices form a group under > 3y=3 y=1

x + 3y = 5

a. addition? > b. multiplication?

See KBe2020math530refGroups I'll assume that our matrices have real numbers in them.

Operation Property	Closed	Identity	Inverse	Associative?	Final
Addition	Yes	$e = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$	$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} -a & -b \\ -c & -d \end{bmatrix} = e$	"Inherits from addition"	Yes
Multiplication	Yes	$e = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	Maybe?	Yes, see below	Undecided

I can't figure out if 2x2 matrices have multiplicative inverses... I tried to work it out using algebra but kept proving identities. Not sure what the right way to go about this is...

I spent far too long on this assignment (1.6h), so I probably won't spend as much time LaTeXing my homework in the future.