

We first set up the same set of basic assumptions and variables.

```
GRAV <- 9.8 # gravity (m/s^2)
MASS <- 1 # mass (kg)
I_CM <- 1/12 # rotational inertia (kg m^2)
PHI <- 0.1 # angle of Ft relative to floor (parallel) (rad)
L <- 0.5 # distance from the center of mass (of rotation point) to tension (m)
FT <- 11 # tension force (N)
OMEGA <- 0.1 # angle of line orthogonal to floor relative to gravity (rad) (because shifted axis)
```

Additionally, we set the time interval and seed values for all values that's tallied:

```
dt <- 0.0001
t_max <- 5

vx <- 0
vy <- 0

time <- 0
theta <- 0
thetadot <- 0
```

Great. Let's start writing the loop now by setting up a bunch of arrays and writing their values in.

```
cTime = NULL
cTorqueNet = NULL
cDDTheta = NULL
cDTheta = NULL
cTheta = NULL

cAccelX = NULL
cAccelY = NULL
cVelX = NULL
cVelY = NULL

cFNetX = NULL
cFNetY = NULL

cKERot = NULL
cKETrans = NULL
```

Awesome, we will start tallying, then!

```
for (i in 0:(t_max/dt)) {
  # write down standard values
  cTime[i] = time
  cTheta[i] = theta

  # torque is calculated via the dot product between the vector of the radius projected out
  # and also the angle at which the thing is at (so like theta + phi)
  #
  # note that, unlike the tabled version, L here represents distance from CoM to tension
  # application
```

```

torque <- FT*L*cos(theta+PHI)
cTorqueNet[i] = torque

# from knowing the torque, we could divide out the rotational inertia to figure the
# acceleration of rotation
thetadotdot <- torque/I_CM
cDDTheta[i] <- thetadotdot

# from this, we could of course tally for the velocity of theta as well
thetadot <- dt*thetadotdot + thetadot
cDTheta[i] <- thetadot

# After knowing the value for theta, we could use it to calculate the net forces in
# both components.
# we define up as +, down as -, right as +, left as -
fnet_x <- FT*cos(PHI) + MASS*GRAV*sin(OMEGA)
fnet_y <- FT*sin(PHI) - MASS*GRAV*cos(OMEGA)
# "I think ax and ay will be constant with time" --- Mark

cFNetX[i] = fnet_x
cFNetY[i] = fnet_y

# Dividing the mass out, we could get accelerations
ax <- fnet_x/MASS
ay <- fnet_y/MASS

# We also tally the components seperately for velocity
vx <- ax*dt + vx
vy <- ay*dt + vy

# And we add them together to tally
cAccelX[i] = ax
cAccelY[i] = ay

cVelX[i] = ax
cVelY[i] = ay

cKERot[i] = 0.5 * I_CM * thetadot^2
cKETrans[i] = 0.5 * MASS * (vx^2+vy^2)

# We increment the time and theta based on the tallying variable
time <- dt + time
theta <- dt*thetadot + theta
}

rotating_link <- data.frame(cTime,
  cTheta,
  cDTheta,
  cDDTheta,
  cTorqueNet,
  cAccelX,
  cAccelY,
  cKERot,
  cKETrans)

```

```
names(rotating_link) <- c("time",
  "theta",
  "d.theta",
  "dd.theta",
  "net.torque",
  "accel.x",
  "accel.y",
  "ke.rot",
  "ke.trans")
```

Let's import some visualization tools, etc.

```
library(tidyverse)
```

Let's first see the head of this table:

```
head(rotating_link)
```

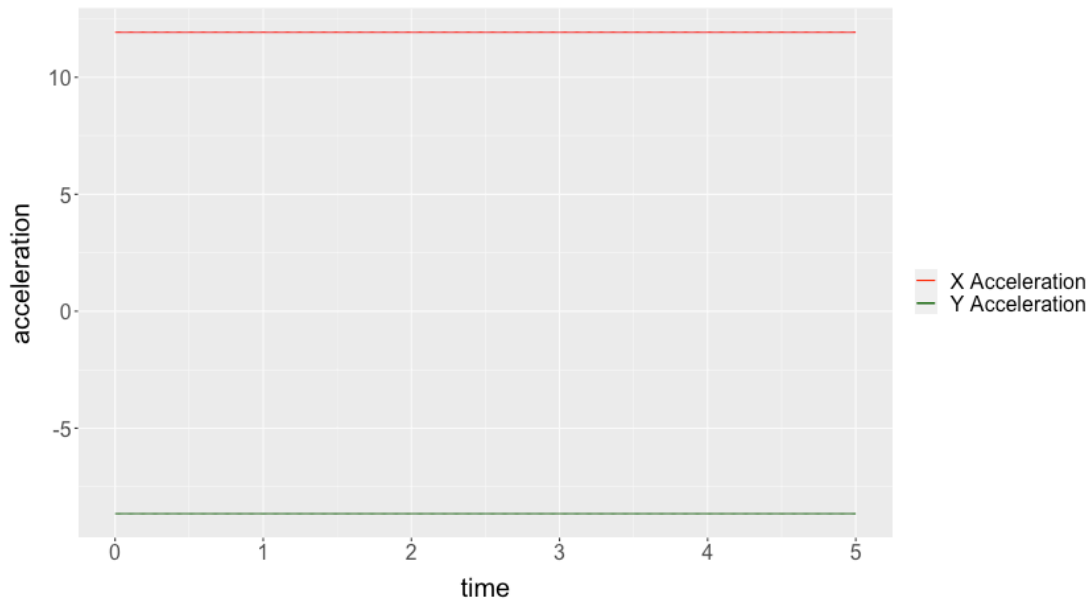
1e-04	6.56702749083497e-07	0.0131340545489667	65.6702705813175	5.47252254844313	11.9234133011972
-8.65287323660954	7.18764120396806e-06	4.3408e-06			
2e-04	1.97010820398017e-06	0.0197010807416836	65.6702619271685	5.47252182726404	11.9234133011972
-8.65287323660954	1.61721909329306e-05	9.7668e-06			
3e-04	3.94021627814853e-06	0.0262681056362569	65.6702489457332	5.47252074547777	11.9234133011972
-8.65287323660954	2.87505572382313e-05	1.73632e-05			
4e-04	6.56702684177422e-06	0.0328351287999327	65.6702316367577	5.47251930306314	11.9234133011972
-8.65287323660954	4.4922736804507e-05	2.713e-05			
5e-04	9.85053972176748e-06	0.039402149799923	65.6702099999032	5.47251749999193	11.9234133011972
-8.65287323660954	6.46887253689821e-05	3.90672e-05			
6e-04	1.37907547017598e-05	0.0459691682033976	65.6701840347464	5.47251533622887	11.9234133011972
-8.65287323660954	8.80485177213443e-05	5.31748e-05			

Before we start graphing, let's set a common graph theme.

```
default.theme <- theme(text = element_text(size=20), axis.title.y = element_text(margin = margin(t = 0,
```

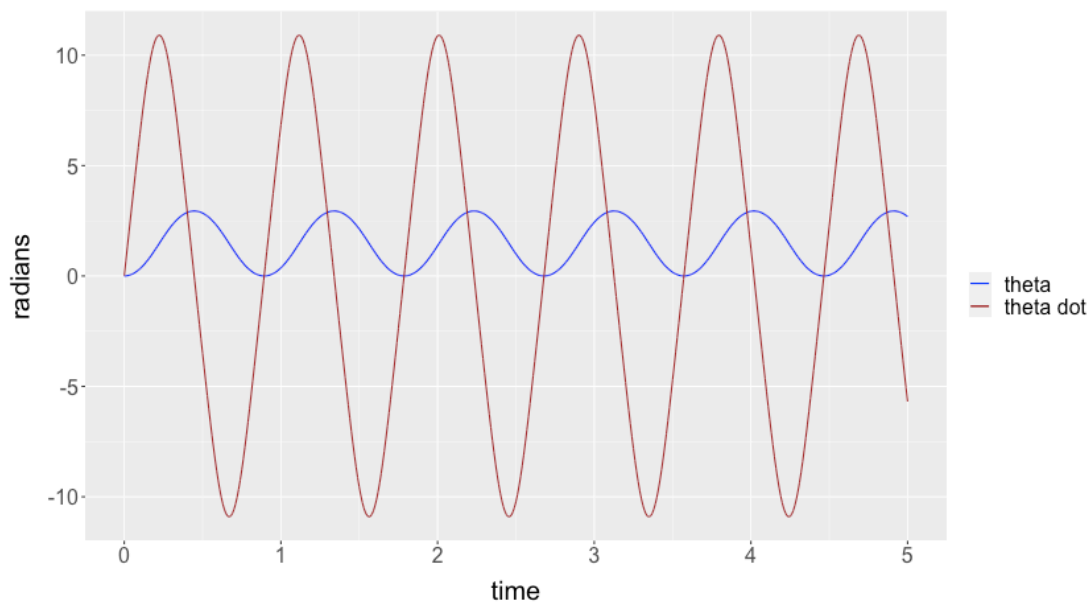
We will graph ax and ay on top of each other:

```
rotating_link %>% ggplot() + geom_line(aes(x=time, y=accel.x, colour="X Acceleration")) + geom_line(aes
```



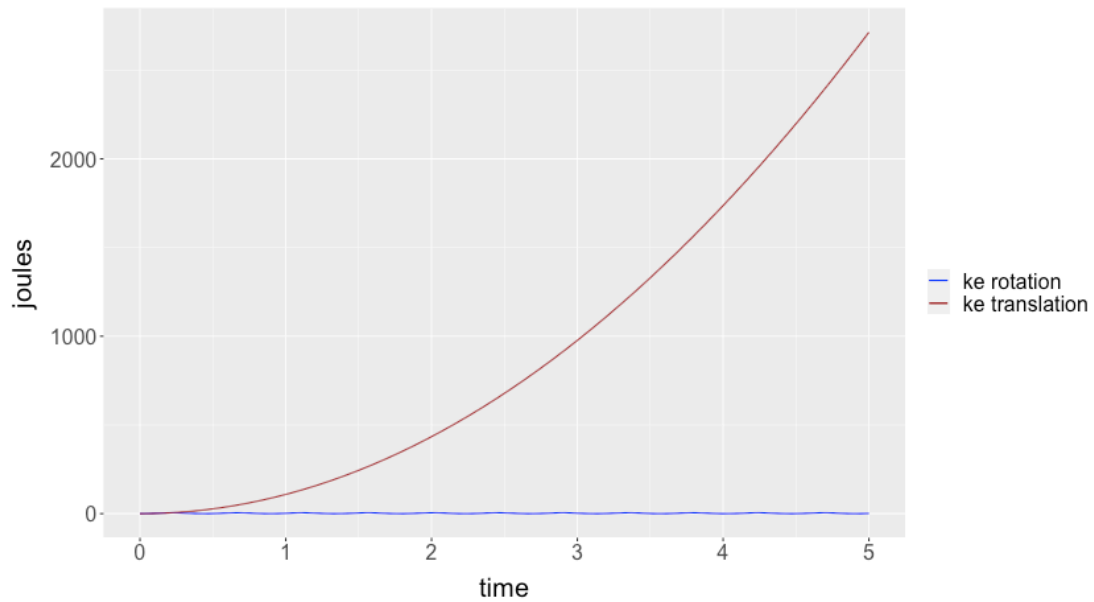
Theta dot atop theta:

```
rotating_link %>% ggplot() + geom_line(aes(x=time, y=theta, colour="theta")) + geom_line(aes(x=time, y=theta_dot, colour="theta dot"))
```



We finally, plot KE rotation and translation

```
rotating_link %>% ggplot() + geom_line(aes(x=time, y=ke.rot, colour="ke rotation")) + geom_line(aes(x=time, y=ke.trans, colour="ke translation"))
```



Let's also plot torque as well.

```
rotating_link %>% ggplot() + geom_line(aes(x=time, y=net.torque)) + default.theme
```

