1 | Axler5.22 matrix of an operator, $\mathcal{M}(T)$

def

Suppose $T \in \mathcal{L}(V)$ and v_1, \dots, v_n is a basis of V. The *matrix of* T wrt this basis is the *n*-by-*n* matrix

$$\mathcal{M}(T) = \begin{pmatrix} A_{1,1} & \cdots & A_{1,n} \\ \vdots & \ddots & \vdots \\ A_{n,1} & \cdots & A_{n,n} \end{pmatrix}$$

whose entries $A_{i,k}$ are defined by

$$Tv_k = A_{1,k}v_1 + \dots + A_{n,k}v_n$$

Specify a basis with $\mathcal{M}(T,(v_1,\ldots,v_n))$

- 1.1 | intuition
- 1.1.1 | each column is where the map takes a basis vector
- 2 | Simplifying The Matrix Representation
- 2.1 | 'A central goal of linear algebra is to show that given an operator $T\in\mathcal{L}(V)$, there exists a basis of V wrt which T has a reasonably simple matrix'
- 2.2 | If by simple we mean "has many zeros" or RREF, then we know enough to ensure that there exists a basis s.t. the first column has zeros everywhere except the first row.

$$\begin{tabular}{ll} λ \\ 0 & * \\ \vdots \\ 0 \end{tabular} \begin{tabular}{ll} λ by taking the lone eigenvalue and letting λ is a property of the lone of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and letting λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of the lone eigenvalue and λ is a property of λ is a pro$$

it's eigenvector be the first basis vector.

Taproot • 2021-2022