

#flo #hw

## 1 | Linear Maps

no one gets excited about vector spaces -axler

the interesting part: linear maps!

```
title: learning objectives
- fundamentals theorem of linear maps
- matrix of linear map w.r.t. given bases
- isomorphic vec spaces
- product spaces
- quotient spaces
- duals spaces
  - vector space
  - linear map
```

## 2 | The vector space of linear maps

**key definition!**

```
title: linear map
aka *linear transformation.*
```

a *linear map* from  $V$  to  $W$  is a function  $T: V \rightarrow W$  with the following properties:

**\*\*additivity\*\***

$T(u+v) = Tu + Tv$  for all  $u, v \in V$ ;

**\*\*homogeneity\*\***

$T(\lambda v) = \lambda(Tv)$  for all  $\lambda \in F$  and  $v \in V$ .

the functional notation  $T(V)$  is the same as the notation  $Tv$  when talking about linear maps.

```
title: notation --  $L(V, W)$ 
```

the set of all linear maps from  $V$  to  $W$ .

### 2.0.1 | examples of linear maps

- 0?
- 0 is the func that takes each ele from some vec space to the additive iden of another vec space.
  - \*  $0v = 0$
  - \*