MVC 2 PS#28 Compiled May 9, 2022

1 | Evaluating a Cylindrical Integral

Considering the function:

$$f(x, y, z) = \sqrt{x^2 + y^2}$$
 (1)

To evaluate the integral, we will convert it to cylindrical coordinates. We note first that the integral is to be evaluated inside the cylinder of $x^2 + y^2 = 16$, which means that we wish to evaluate it in a circle with center at the origin with radius 4.

Furthermore, we understand that the bounds of the function are to be evaluated between [-5, -4].

If we set up the integral, we will get:

$$\int_{-5}^{-4} \int_{C} \sqrt{x^2 + y^2} \, dx \, dy \, dz \tag{2}$$

This is convenient. We can evaluate the inner integral first like in $\mathbb{R}^2 \to \mathbb{R}^1$, then simply evaluate the other integral after.

Let's do so.

Note that the inner integral is a normal cylindrical coordinate setup. Therefore, we can take the following substitution:

$$\sqrt{x^2 + y^2} = r \tag{3}$$

Furthermore, that:

$$dx dy = dr d\theta (4)$$