## 1 | Problem 1

1.1 | (1*a*)

PE=-W \[  $W=\int_{R_e}^{\infty}F(r)\,dr$  \] We know that the force applied to a point mass m by the gravitational field of the

earth (with mass  $M_e$ ) with distance x is modeled by

$$\begin{split} F(r) &= \frac{GmM_e}{r^2} \\ W &= \int_{R_e}^{\infty} \frac{GmM_e}{r^2} \, dr \\ &= GmM_e \int_{R_e}^{\infty} \frac{1}{r^2} \, dr \\ \text{ed to be } \backslash [ &= GmM_e [-\frac{1}{r}]_{R_e}^{\infty} \quad \backslash ] \end{split}$$

. Therefore, our work integral can be modified to be  $\[\]$ 

$$[ = GmM_e[-\frac{1}{r}]_{R_e}^{\infty} \ \ ]$$

$$= -\frac{GmM_e}{R_e}$$

$$PE = \frac{GmM_e}{R_e}$$

1.2 | (1*b*)

**1.3** | (1*c*)

$$\begin{split} v &= \sqrt{\frac{2GM_e}{R_e}} \\ \backslash [ &= \sqrt{\frac{2 \cdot 6.674 \cdot 10^{-11} \cdot 5.972 \times 10^{24}}{6.371 \cdot 10^6}} \ \backslash ] \\ &= 11185.7 m/s \\ &= 25020.1 mph \end{split}$$

## 2 | Problem 2

$$\sum_{i=1}^n \vec{F}_{net,i} = (\sum_{i=1}^n m_i) \ddot{\vec{r}}_{CM}$$
 
$$\sum_{i=1}^n m_i \ddot{\vec{r}}_i = (\sum_{i=1}^n m_i) \ddot{\vec{r}}_{CM}$$
 \[ \int \int \sum\_{i=1}^n m\_i \dot{\vec{r}}\_i \dot dt \dt = \int \int (\sum\_{i=1}^n m\_i) \dot{\vec{r}}\_{CM} \dt dt \dt \] \] Both constants are the same constant on both sides of 
$$\int \sum_{i=1}^n m_i \dot{\vec{r}}_i \, dt + C_1 = \int (\sum_{i=1}^n m_i) \dot{\vec{r}}_{CM} \, dt + C_1$$
 
$$\sum_{i=1}^n m_i \vec{r}_i + C_1 t + C_2 = (\sum_{i=1}^n m_i) \vec{r}_{CM} + C_1 t + C_2$$

the equation so they will cancel out. The sum of all mass is just M.  $\setminus [\vec{r}_{CM} = \frac{1}{M} \sum_{i=1}^{n} m_i \vec{r}_i \setminus ]$ 

## 3 | Problem 3

Any force within a system will have an opposite force applied as well (Newton's 3rd law). Therefore, forces within a system will cancel out and will have no effect on the center of mass.

## 4 | Problem 4

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