

# 1 | Derivatives

## 1.1 | Common

function	derivative
$\sin x$	$\cos x$
$\cos x$	$-\sin x$
$\tan x$	$\frac{1}{\sin^2 x}$
$\sin x^{-1}$	$-\frac{1}{\sqrt{1-x^2}}$
$\cos x^{-1}$	$\frac{1}{\sqrt{1-x^2}}$
$\tan x^{-1}$	$-\frac{1}{1+x^2}$
$a^x$	$\ln(a)a^x$
$\log_a x$	$\frac{1}{\ln(a)x}$

## 1.2 | Rules

### 1.2.1 | Add/Subtract

$$\frac{d}{dx} f(x) + g(x) = \frac{d}{dx} f(x) + \frac{d}{dx} g(x)$$

### 1.2.2 | Multiply

$$\frac{d}{dx} (f(x)g(x)) = \left( \frac{d}{dx} f(x) \right) g(x) + f(x) \left( \frac{d}{dx} g(x) \right)$$

### 1.2.3 | Divide

$$\frac{d}{dx} \frac{f(x)}{g(x)} = \frac{g(x) \frac{d}{dx} f(x) - f(x) \frac{d}{dx} g(x)}{g^2(x)}$$

### 1.2.4 | Chain Rule

$$\frac{d}{dx} f(g(x)) = \left( \frac{d}{dx} f \right) (g(x)) \left( \frac{d}{dx} g(x) \right)$$

### 1.2.5 | Power Rule (ONLY TAKE OUT CONST MULTIPLES)

$$\frac{d}{dx} x^n = nx^{n-1}$$

## 2 | Approximation

### 2.1 | Linear Approximation at a Point

$$y = f(a) + f'(a)(x - a)$$

(First order Taylor series)

### 2.2 | Differentials

$$dy = f'(x)dx$$

Basically use the slope of the linear approximation to approximate the change ( $dy$ ) in the function given a change in  $x$  ( $dx$ ).

## 3 | Implicit Differentiation

REMEMBER that  $y$  is  $f(x)$  which means it's a function of  $x$ ! Use the chain rule!

Then solve for  $f'(x)$  and if necessary, plug in the original definition of  $f(x)$ .

Use point slope form to find tangent lines.

## 4 | Derivative of Inverse Functions

$$f^{-1}'(x) = \frac{1}{f'(f^{-1}(x))}$$