#flo #disorganized #incomplete

# 1 | Administrative bits

- Will present problems from 2.B and/or 2.C next week
- · Mini quiz, stop yourself after an hour
- · and give your subconscious a chance to think about things
- · No need to say "clearly", "obviously", "evidently"

# 2 | #icr Axler2.C

#source Axler Linear Algebra Done Right 2.C ## Polynomials are vectors - because you can add and scale them and they are kind of nice in general

### 2.1 | The box under 2.38

- You can't understand a vector space just by knowing the vectors inside
  - you also need to know the field that you are in
  - See 2.A ex5
- The field that you are over changes your dimension: usually we think of  $\mathbb C$  as a vector space over  $\mathbb R$ , but in this class we think of it as over  $\mathbb C$ , which means dim  $\mathbb C=1$

#### 2.2 | **Axler2.41**

• It's my question! See KBe20math530floQuestions

### 2.3 | Axler2.42

- #tip If it's a spanning list that's the right length, then it's a basis and therefore linearly independent.
- If it's a linearly independent list and it's the right length, then it's a basis and therefore spanning.

### 2.4 | Axler2.43 Dimension of a Sum

#### 2.4.1 | **An Example**

- If you have two planes in 3 space, and they intersect at exactly one line, then you can't just add the dimension of the two planes (2+2 = 4 which is more than 3 space can allow).
  - If the planes are parallel, and both subspaces, then we know they both go through the origin and thus are the same plane.

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## 2.4.2 | Some tips

- Usually easiest to get a basis of a subspace by building on instead of taking out
  - for example if you have a slanty plane in 3 space, and you start with standard basis, then you won't even get the slanty plane.

## 2.4.3 |The span is $U_1+U_2$

- · Because it's a double containment
  - $span \subset U_1 + U_2$
  - $v \in span \implies v = a_1u_1 + \ldots + a_mb_m + b_1v_1 + \ldots$
  - For all u. in the span, you can write it as something in  $U_1$ 
    - $\star \ \ \text{something in} \ U_2$

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