#ret #hw

1 | Cryptography

Done prior:

- Try turning on two-factor authentication, if you have that option.
- Think about how secure your password is, relative to how attackers would try guessing. Is it a dict
- Generate a public/private key pair for yourself. Put the public key on our test laptop so that you

1.1 | Creating a custom hash function

Hey Wes, this is a bit of a weirder one.

1.1.1 | Requirements

What are the requirements for a hash function?

- Source
 - No preimage: given y, it should not be feasible to find x such that h(x) = y.
 - No second preimage: given x_1 , it should not be feasible to find x_2 (distinct from x_1) such that $h(x_1) = h(x_2)$.
 - No collision: it should not be feasible to find any x_1 and x_2 (distinct from each other) such that $h(x_1) = h(x_2)$.

What if we just.. use a neural network?

1.1.2 | NN hash

Intuitively, using a neural network as a hash function seems like it won't work. In fact, I believe it doesn't work, I just don't know why it doesn't work. * Of course, a vanilla neural network won't work because we can just train a model to reverse its mapping. To solve this problem, we can use something I call permute layers.

- 1. Permute Layers **Concept** Fundamentally, the concept of permute layers is to take an input, and do some operation on it such that a non-continuous output space is generated. The goal would be that: Similar inputs lead to vastly different outputs Make there no guarantee that an adversarial NN's guess of x is closer to $x + \epsilon_0$ than it is to $x + \frac{1}{\epsilon_0}$ As in, we can't train a NN to reverse it!
 - **Implementation** One possible implementation of these permute layers would be simply permuting the bits that make up our tensors.

1.1.3 | Proof of concept

The code below is meant as proof of concept – or rather, demonstration of concept. It is messy and surely error ridden, but it seems to work.

Outline: - Create a deep neural network with randomly initialized weights. - Ensure that it is deterministic with a set seed. This seed could potentially be carried with the hash. - Add permute layers in between the The code can also be found here.

```
#####################
       SETUP
######################
# imports
import torch
import torch.nn as nn
import torch.nn.functional as F
import math
import struct
from codecs import decode
import numpy as np
import string
INP = [0.1, 0.0, 1.01] # our input!
SAFE = 8 # don't permute the first 8 bits, so we don't get infs and 0
# makes things deterministic
np.random.seed(0)
torch.manual_seed(0)
torch.set_default_dtype(torch.float64) # make sure we use the right datatype!
###########################
       BASE NN
###########################
class Net(nn.Module): # define the model
   def __init__(self):
        super(Net, self).__init__()
        self.11 = nn.Linear(3, 128) # linear layer, with input size 3
        self.pl1 = PermuteLayer(128,256) # custom permute layer
        self.12 = nn.Linear(256, 512)
        self.pl2 = PermuteLayer(512, 512)
        self.13 = nn.Linear(512, 256)
        self.pl3 = PermuteLayer(256, 256)
        self.14 = nn.Linear(256, 128)
        self.pl4 = PermuteLayer(128, 8) # output a tensor with 8 floats
```

```
def forward(self, x): # run it through!
       x = [100*(y+1) \text{ for y in x}] \text{ # add 1 and multiply by 100 for each input element}
       x = torch.tensor(x) # then convert it to a tensor
       x = self.ll(x) # run it through the layers
       x = x.view(-1, 128)
       x = self.pl1(x)
       x = self.12(x)
       x = self.pl2(x)
       x = self.13(x)
       x = self.pl3(x)
       x = self.14(x)
       x = self.pl4(x)
       return x
CUSTOM PERMUTE LAYER
class PermuteLayer(nn.Module): # not my code! default linear code comes from https://auro-227.medium.com
   # after modification, acts as a normal linear layer except it permutes the bits.
   def __init__(self, size_in, size_out):
       super().__init__()
       self.size_in, self.size_out = size_in, size_out
       weights = torch.Tensor(size_out, size_in)
       self.weights = nn.Parameter(weights) # nn.Parameter is a Tensor that's a module parameter.
       bias = torch.Tensor(size_out)
       self.bias = nn.Parameter(bias)
       # initialize weights and biases
       nn.init.kaiming_uniform_(self.weights, a=math.sqrt(5)) # weight init
       fan_in, _ = nn.init._calculate_fan_in_and_fan_out(self.weights)
       bound = 1 / math.sqrt(fan_in)
       nn.init.uniform_(self.bias, -bound, bound) # bias init
   def forward(self, x): # where the permuting happens
       # this part isn't pretty..
       # but according to Dr. Brian Dean, we don't need to constant factor optimize!
       bits = "" # store bits in a char array
       saved = [] # save the bits we want to protect
       for i,v in enumerate(x[0]): # loop through the floats
           tnsr = float_to_bin(v) # convert them to binary
           saved.append(tnsr[:SAFE]) # save what we need to
           bits += tnsr[SAFE:] # and add to the char array
       p = np.random.permutation([x for x in bits]) # permute it!
       p = ''.join(map(str, p)) # and then.. join it back together
       converted = []
```

```
# loop through p, chunk it into segments
       for i in range(len(p)//(64-SAFE)):
            # convert segment to floats
            item = bin_to_float(saved[i]+p[(64-SAFE)*i:((64-SAFE)*i)+(64-SAFE)])
            converted.append(item)
        converted = torch.tensor([converted]) # change it back to a tensor
       x = converted
       w_times_x= torch.mm(x, self.weights.t()) # matrix multiply them
       return torch.add(w_times_x, self.bias) # w times x + b
#############################
       HELPERS
############################
# not my code! from https://stackoverflow.com/questions/16444726/binary-representation-of-float-in-pyth
def bin_to_float(b):
   """ Convert binary string to a float. """
   bf = int_to_bytes(int(b, 2), 8) # 8 bytes needed for IEEE 754 binary64.
   return struct.unpack('>d', bf)[0]
def int_to_bytes(n, length): # Helper function
    """ Int/long to byte string.
       Python 3.2+ has a built-in int.to_bytes() method that could be used
        instead, but the following works in earlier versions including 2.x.
   return decode('%%0%dx' % (length << 1) % n, 'hex')[-length:]
def float_to_bin(value): # For testing.
    """ Convert float to 64-bit binary string. """
    [d] = struct.unpack(">Q", struct.pack(">d", value))
   return '{:064b}'.format(d)
def int2base(x, base): # not my code! modified from https://stackoverflow.com/questions/2267362/how-to-
   if x < 0: sign = -1
   elif x == 0: return digs[0]
                sign = 1
   else:
   x *= sign
   digits = []
   while x:
       digits.append(digs[x % base])
       x = x // base
    if sign < 0: digits.append('-')</pre>
   digits.reverse()
   return ''.join(digits)
digs = string.digits + string.ascii_letters
#########################
       OUTPUT
```

```
model = Net()
result = list(model(INP).detach().numpy()[0]) # convert output to list
output_bits = ''
for i in result:
    # convert to bits, then take the second half
    # because it's more shuffled
    output_bits += float_to_bin(i)[32:]
print(int2base(int(output_bits, 2), 16)) # clean the output up and print it out
```