1 | Tiling the Pringlehouse

As a review, our pringles shaped house has the following parametres:

$$\begin{cases} x(t) = 30cos(t) \\ y(t) = 20sin(t) \end{cases} \tag{1}$$

and the roof is defined by:

$$r(x,y) = \frac{1}{400} \left(\sqrt{3}x - y\right)^2 - \frac{1}{400} \left(\sqrt{3}y - x\right)^2 + 10 \tag{2}$$

We will first convert the above function into rectangular bounds to take the area of.

$$x = 30\cos(t) \tag{3}$$

$$\Rightarrow \frac{x}{30} = \cos(t) \tag{4}$$

$$\Rightarrow t = \arccos\left(\frac{x}{30}\right) \tag{5}$$

Supplying this back to the original expression for y:

$$y = 20sin\left(arccos\left(\frac{x}{30}\right)\right) \tag{6}$$

$$=20\sqrt{1-\left(\frac{x}{30}\right)^2}\tag{7}$$

Therefore, the actual integral:

$$\int_{-30}^{30} \int_{-20\sqrt{1-\left(\frac{x}{30}\right)^2}}^{20\sqrt{1-\left(\frac{x}{30}\right)^2}} 1dy \, dx \tag{8}$$

We will endeavor now to use technology.

$$var("x y")$$

 $f(x,y) = 1$
 $f.integrate(y, -20*sqrt(1-(x/30)^2), 20*sqrt(1-(x/30)^2)).integrate(x, -30,30)$

It appears that the area of the floor is 600π .

We can do this something for the function of the roof. We will first figure correction factor dA, then take the integral as prescribed.

$$dA = \sqrt{1 + \left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2} \tag{9}$$

At this point, we realize that the actual function will turn to be much too complicated to integrate by hand at this moment; therefore, we will create the expression digitally.

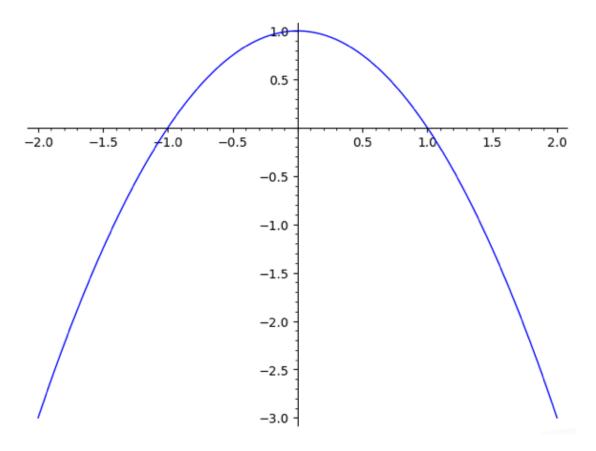
Looks like the result is converting to about 2002.2 for this shape.

2 | Three Dimensional Region!

Slowly adding up the arguments to this figure reveals its general shape:

$$f(x) = 1-x^2$$

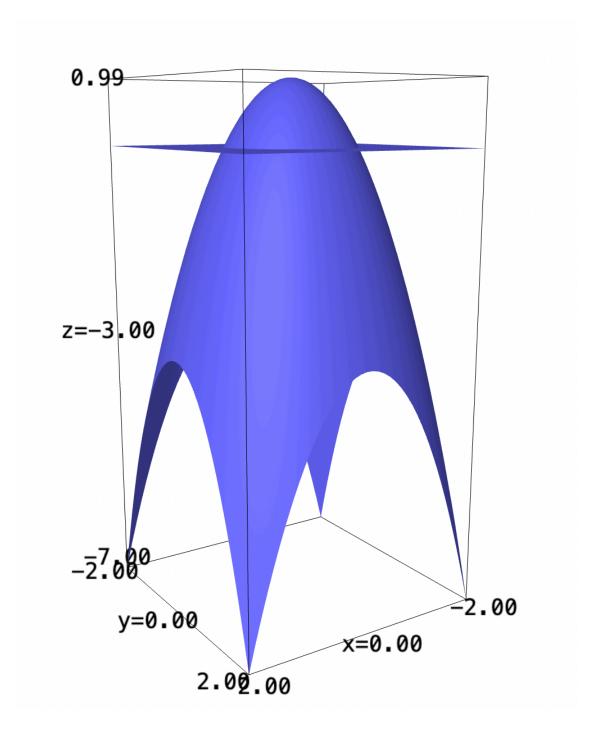
plot(f, -2, 2)



And, adding up the y component:

$$f(x,y) = 1-x^2-y^2$$

plot3d(f, (x,-2,2), (y,-2,2)) + plot3d(0, (x,-2,2), (y,-2,2))



We can see that the positive component exists at x = [-1, 1], y = [-1, 1]. If the same pattern holds, then, the maximum volume would be over areas:

$$x = [-1, 1], y = [-1, 1], z = [-1, 1]$$
 (10)

Taking the actual integral:

$$a(x,y,z) = 1-x^2-y^2-z^2$$

a.integrate(x,-1,1).integrate(y,-1,1).integrate(z,-1,1)

Shockingly, the resulting integral is 0. However, we can actually move the bounds to see that all other manifestations about this point would actually result in even more negative values.

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a(x,y,z) = 1-x^2-y^2-z^2
a.integrate(x,-1,1).integrate(y,-1,1).integrate(z,-1,2)
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