

#flo #hw #reading

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## 1 | Bases !

- types of lists, so far
  - linearly independent lists
  - spanning lists
    - \* list of vecs, that when span()-ed, contains all the elements of the vector space.
    - \* ie. you can use linear combo of the original list to get to every element in the vector space

title: basis

a *basis* of  $V$  is a list of vectors in  $V$  that is [linearly independant] (KBxLinearIndependence) and [spanning]

such as,

standard basis of  $\mathbb{F}^n$  is  $(1, 0, \dots, 0), (0, 1, \dots, 0), \dots, (0, \dots, 0, 1)$   
 $(1, 2), (3, 5)$  -> basis of  $\mathbb{F}^2$

- things can have many basis!

### 1.0.1 | criterion for basis

title: criterion for basis

a list  $v_1, \dots, v_n$  of vectors in  $V$  is a basis of  $V$  iff every  $v \in V$  can be written uniquely in

$$v = a_1 v_1 + \dots + a_n v_n$$

where  $a_1, \dots, a_n \in \mathbb{F}$ 

essentially, for a list of vectors in  $V$  to be a basis of  $V$ , every element in  $V$  has to be written uniquely as the linear combo of the org list of vectors. uh, #review

### 1.0.2 | spanning lists and basis

- spanning list isn't necessarily a basis cuz they don't need to be linearly independent
  - but, each spanning list does contain a basis
- each spanning list can be converted to a basis through the removal of some number of elements
- but also, every linearly independent list extends to a basis
  - can be extended to a basis