

#flo #ret #hw

1 | Problem 21!

Suppose V is finite-dimensional and $T \in L(V, W)$. Prove that T is injective if and only if there exists $S \in L(W, V)$ such that ST is the identity map on V .

3.16 injectivity is equivalent to null space equals $\{0\}$ 3.15 injective: $T: V \rightarrow W$ is injective if $Tu = Tv$ implied $u = v$ 3.8 product of linear maps:

identity map on v : $Iv = v$

product of linear maps:

Suppose $S, T \in L(V, W)$ and $\lambda \in F$. The *sum* of $S + T$ and the *product* λT are the linear maps from V to W defined by

$$(S + T)(v) = Sv + Tv$$

and

$$(\lambda T)(v) = \lambda(Tv)$$

for all $v \in V$