- · Discussion Results: what is a number?
  - Something about group theory
    - \* This is more like a way of telling us how to use numbers, not really a good definition.
    - \* Set up bounds to define things
  - Different classes (natural, real, imaginary)
  - Where do you draw the boundaries between objects?
  - A way to quantify the nature of living and reality
- Number Systems
  - We want them to be desirable and group-like
  - Types

## \* Natural Numbers

- · Integers greater than zero
- \* Whole Numbers
  - · Natural Numbers + 0
  - · 0 is the hole.
- \* Integers
  - $\{\ldots, -2, -1, 0, 1, 2, \ldots\}$
  - · Good for algebra, we'll see later
- \* Rationals
  - · Like  $\frac{1}{2}$ .
  - · A ratio/fraction/quotient of integers
- \* Real
  - · Like  $\pi$
  - · A number on the number line
  - · A number that can be a distance to something.
  - · A good enough definition that isn't "real analysis"

## \* Complex Numbers

- · Like 5i
- · There will be many complex numbers
- $\cdot$  Matrices with complex numbers can be different from real numbers
- · Complex plane
- \* Hamaltonian numbers music video? #curiosity
- Why do we want more numbers?
  - \* Why Zero?
    - · Additive identity
    - · Zero vector = identity vector
    - · Frame of reference, starting point, nice and neutral
  - \* Zintegers?
    - Why negatives?
    - · So you can make zero

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- $\cdot\,$  Undo each other, undo a +5
- · Inverse
- $\cdot \ -a$  and a are additive *inverses*
- That's all we need to get to a group: KBe2020math530refGroups

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