1 | inner product space **def**

An *inner product space* is a vector space V along with an inner product on V.

When $V =^n$, assume the inner product is the Euclidean inner product

$$\langle (w_1, \ldots, w_n), (z_1, \ldots, z_n) \rangle = w_1\overline{z_1} + \cdots w_n\overline{z_n}$$

2 | results

2.1 | Axler6.7 properties

2.1.1 | For each fixed $u \in V$, the function that takes v to $\langle v, u \rangle$ is a linear map from V to

2.1.2 | $\langle 0, u \rangle = 0 = \langle u, 0 \rangle \forall u \in V$

2.1.3 | $\langle u, v + w \rangle = \langle u, v \rangle + \langle u, w \rangle$ for all $u, v, w \in V$

2.1.4 | $\langle u, \lambda v \rangle = \overline{\lambda} \langle u, v \rangle$ for all $\lambda \in$ and $u, v \in V$