#flo #hw

## 1 | Linear Maps

```
no one get's excited about vector spaces -axler

the interesting part: linear maps!

title: learning objectives
- fundementals theorem of linear maps
- matrix of linear map w.r.t. given bases
- isomorphic vec spaces
- product spaces
- quotient spaces
- duals spaces
- vector space
- linear map
```

# 2 | The vector space of linear maps

#### key definition!

### 2.0.1 | examples of linear maps

- 0?
  - 0 is the func that takes each ele from some vec space to the additive iden of another vec space.
    - \* 0v = 0
    - \* left: func from V to W, right: additive iden in W
    - \* #question what does it mean for it to be a function from V to W?
- identity, denoted I
  - -Iv=v
  - maps each element to itself linear transformation like a .map?

- · differentiation and integration!
- multiplication by  $x^2$  (on polynomials)
- shifts! defined as,  $T(x_1, x_2, x_3, ...) = (x_2, x_3, ...)$ 
  - #question this is an example, but how do we define it as a transformation? or is giving an example in the general case the same thing as defining a transformation?
- from  $R^3 \to R^2$  ? #question what? how does this work?
- · #review how this dimension shift works...
- 1. linear maps and basis of domain

```
title: linear maps and basis of domain Suppose v_1, \dots , v_n is a basis of v_1, \dots , v_1 is a basis of v_1, \dots , v_1 in v_1. Then there exists a unit v_1 is v_2 if v_3 for each v_1, \dots v_2.
```

we can uniquely map between the basis of a subspace and a list of equal len in a diff subspace? #question wait how does the uniquess proof work here at the end?

## 2.0.2 | algebraic operations on L(V, W)

```
title: addition and SCAMUL Suppose S,T \in L(V,W) and \lambda \in F. The *sum* of S+T and the *product* \lambda \in S(S+T)(v) = V + Tv and S(\lambda \in T)(v) = \lambda \in Tv for all v \in V
```

oh jeez..

```
title: L(V,W) is a vector space! with the operations of addition and SCAMUL as defined above, L(V,W) is a [[file:KBe20math530refVector]]
```

and another one.

1. product of linear maps

```
title: product of linear maps if T \in L(U,V) and L(U,W), then the *product* T \in L(U,W) is defined by S(T)(u)=S(Tu) for all U \in U.
```

S dot T?? what is this symbol? it's a composition sign!! \circ -> 0

```
title: albraic props of products of linear maps
- associative
```

- idenity
- distributive properties

multiplication of linear maps is not commutative! ie. ST = TS isn't always true.

```
title: linear maps take 0 to 0 suppose $T$ is a linear map from $V$ to $W$. Then $T(0) = 0$
```

#review this chapter...

bassically all just result blocks and nothing else

i don't have an intuitive understanding of the concept of a map. perhaps look into 3b1b vid on line