MVC 2 PS#26 Compiled May 2, 2022

1 | Tiling the Pringlehouse

As a review, our pringles shaped house has the following parametres:

$$\begin{cases} x(t) = 30cos(t) \\ y(t) = 20sin(t) \end{cases} \tag{1}$$

and the roof is defined by:

$$r(x,y) = \frac{1}{400} \left(\sqrt{3}x - y\right)^2 - \frac{1}{400} \left(\sqrt{3}y - x\right)^2 + 10 \tag{2}$$

We will first convert the above function into rectangular bounds to take the area of.

$$x = 30\cos(t) \tag{3}$$

$$\Rightarrow \frac{x}{30} = \cos(t) \tag{4}$$

$$\Rightarrow t = \arccos\left(\frac{x}{30}\right) \tag{5}$$

Supplying this back to the original expression for y:

$$y = 20\sin\left(\arccos\left(\frac{x}{30}\right)\right) \tag{6}$$

$$=20\sqrt{1-\left(\frac{x}{30}\right)^2}\tag{7}$$

Therefore, the actual integral:

$$\int_{-30}^{30} \int_{-20\sqrt{1-\left(\frac{x}{30}\right)^2}}^{20\sqrt{1-\left(\frac{x}{30}\right)^2}} 1dy \, dx \tag{8}$$

We will endeavor now to use technology.

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var("x y")

f(x,y) = 1

f.integrate(y, -20*sqrt(1-(x/30)^2), 20*sqrt(1-(x/30)^2)).integrate(x, -30,30)
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It appears that the area of the floor is 600π .

We can do this something for the function of the roof. We will first figure correction factor dA, then take the integral as prescribed.

$$dA = \sqrt{1 + \left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2} \tag{9}$$

At this point, we realize that the actual function will turn to be much too complicated to integrate by hand at this moment; therefore, we will create the expression digitally.