1 | Groups

- · definition
 - closed

$$\star$$
 if $a,b \in S$ then $a+b \in S$

– has an identity \boldsymbol{e}

$$\star e + a = a + e = a$$

- each element has an inverse

$$\star -a + a = a + -a = e$$

- needs to be associative

*
$$(a+b) + c = a + (b+c)$$

· communitivity is nice but not required

$$-a+b=b+a$$

• Which number systems are groups under addition and multiplication?

| Number System | Multiplication | Addition |
|-----------------|----------------|-------------|
| Natural Numbers | No inverse | No identity |
| Whole Numbers | No inverse | No inverse |
| Integers | No inverse | Yes |
| Rationals | Yes* | Yes |
| Reals | Yes* | Yes |
| Complex Numbers | Yes* | Yes |

Zero doesn't have an inverse, so it usually gets dropped. For example, \mathbf{Q} is \mathbf{Q} w/o zero #todo-exr0n: rewrite in latex say \$\$

• SRC20200825135700.png \[$\begin{bmatrix} 8 & 2 \\ -2 & 0 \end{bmatrix}$ \]