

#flo #ret #ref #disorganized #incomplete #hw

1 | Les go.

- we need to figure out:
 - what is the curve of generation over a day
 - how does this curve shift over the seasons?
- our inputs
 - location
 - time of year (season)
- output
 - generation curve over a day

look into: Global Tilted Irradiance.

all we care about is the relative shape and how the relative shape changes! this is because the other stuff will be consistent, and we aren't recommending a solar system

1.0.1 | terms:

solar irradiance: power per unit area (W/m^2) integrated over time gives us: insolation (J/m^2) solar irradiance aka solar flux: power per unit area!

TSI: total solar irradiance. when the sun is perpendicular! over a square meter. this is just a constant

zenith angle: angle between sun's rays and vertical direction (of earth). "local normal to earth's surface" and sun rays (line between point on earth surface and sun)

declination angle: latitude of point directly under the sun at **noon** complement of solar zenith angle

subsolar point: point that is closest to the sun on a planet

hour angle h : defined as the longitude of the subsolar point relative to its position at noon. AKA how far it moves in an hour!

A cos zenith angle is the area of sunlight received per area on earth AKA how much sunlight area you're actually getting for an area on earth.

1.0.2 | helpful relations

spherical law of cosines!

$$\cos \delta = \sin \phi \sin \delta_0 + \cos \phi \cos \delta_0 \cos h_0$$

1.0.3 | Vars!

Assume circular orbit?

charge $Q = S_0 \left(\frac{R_0}{R_e} \right)^2 \cos \theta_s$ or $Q = \begin{cases} S_0 \frac{R_o^2}{R_E^2} \cos(\Theta) & \cos(\Theta) > 0 \\ 0 & \cos(\Theta) \leq 0 \end{cases}$ can be approximated as $Q \approx S_0 \cos \theta_s$

declination angle $\delta = -0.409 \cdot \cos \left(\frac{2\pi}{365} \cdot (d + 10) \right)$

spherical law of cosines $\cos(c) = \cos(a) \cos(b) + \sin(a) \sin(b) \cos(C)$ and derivation $C = h$ $c = \Theta$ $a = \frac{1}{2}\pi - \phi$ $b = \frac{1}{2}\pi - \delta$

to calculation of $\cos(\text{zenith})$ $\cos(\Theta) = \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \cos(h)$

substituting back in $Q = S_0 \left(\frac{R_0}{R_e} \right)^2 (\sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \cos(h))$

we can get the delta with $\delta = -0.409 \cdot \cos \left(\frac{2\pi}{365} \cdot (d + 10) \right)$ where 23.45deg in radians in 0.409

integrating over a day, h goes from pi to negative pi $\overline{Q}^{\text{day}} = -\frac{1}{2\pi} \int_{\pi}^{-\pi} Q dh$

$\frac{R_o^2}{R_E^2}$ is constant, so the integral becomes

$$\begin{aligned} \int_{\pi}^{-\pi} Q dh &= \int_{h_o}^{-h_o} Q dh \\ &= S_0 \frac{R_o^2}{R_E^2} \int_{h_o}^{-h_o} \cos(\Theta) dh \\ &= S_0 \frac{R_o^2}{R_E^2} [h \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h)]_{h=h_o}^{h=-h_o} \\ &= -2S_0 \frac{R_o^2}{R_E^2} [h_o \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h_o)] \end{aligned}$$

factoring in the $-1/2\pi$,

we get the:

final

$$\overline{Q}^{\text{day}} = \frac{S_0}{\pi} \frac{R_o^2}{R_e^2} [h_o \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h_o)]$$

$$\begin{aligned} \int_{\pi}^{-\pi} Q dh &= \int_{h_o}^{-h_o} Q dh \\ &= S_0 \frac{R_o^2}{R_E^2} \int_{h_o}^{-h_o} \cos(\Theta) dh \\ &= S_0 \frac{R_o^2}{R_E^2} [h \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h)]_{h=h_o}^{h=-h_o} \\ &= -2S_0 \frac{R_o^2}{R_E^2} [h_o \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h_o)] \end{aligned}$$

wiki: Let h_0 be the hour angle when Q becomes positive. This could occur at sunrise when $\Theta = \frac{1}{2}\pi$, or for h_0 as a solution of

$$\sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \cos(h_o) = 0$$

or

$$h_0 = \cos^{-1}(-\tan(\phi) \tan(\delta)) \text{ end wiki therefore, } h_0 = \cos^{-1}(-\tan(\phi) \tan(\delta))$$

theoretical daily average insolation at the top of the atmosphere as a function of latitude and time of year
Pasted image 20211110162119.png

Pasted image 20211110172859.png equator, summer solstice

θ_s

1.0.4 |Writing!

Assumption: the earth's orbit is circular Assumption: we are not using tracking PV arrays

- {JUSTIFICATION}
 - Given our assumption that the total generation over a year is equal to our total consumption over a year, all that needs to be determined is the distribution of this generation. We can then scale this distribution to match our yearly consumption.

We can model the solar irradiance, a measure of power per unit area, as a fraction of the Total Solar Irradiance (TSI). TSI is treated as a constant describing the mean solar irradiance at the mean position of earth as measured on a surface perpendicular to the sun's rays. However, due to the curvature of the earth's surface, the sun's rays are not always received at a perpendicular angle. The difference between these two angles – perpendicular and actual – is called the solar zenith angle, denoted θ_s . Formally, this is the angle between the zenith, defined as the local normal vector to the earth's surface, and the sun's rays. Frame 1.pdf {FIGURE THINGS}

Thus, we can express the solar irradiance as

$$Q = \begin{cases} S_0 \left(\frac{R_0}{R_E} \right)^2 \cos(\theta_s) & \cos(\theta_s) > 0 \\ 0 & \cos(\theta_s) \leq 0 \end{cases}$$

where R_E represents the distance between the earth and the sun, R_0 represents the mean distance between the earth and the sun, and S_0 represents the TSI. For our purposes, we can approximate the relatively trivial value of $\left(\frac{R_0}{R_E} \right)^2$ as 1.

Using the spherical law of cosines,

$$\cos(c) = \cos(a) \cos(b) + \sin(a) \sin(b) \cos(C)$$

the solar zenith angle can be calculated as a function of the latitude, declination angle, and the hour angle:

$$\cos(\theta_s) = \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \cos(h)$$

Here, ϕ represents the latitude, δ represents the declination angle, and h represents the hour angle. The declination angle varies seasonally due to the earth's axial tilt, reaching its maximum and minimum on the northern summer and winter solstices respectively. δ can be calculated as

$$\delta = -\gamma \cdot \cos\left(\frac{2\pi}{365} \cdot (d + 10)\right)$$

where γ represents the earth's axial tilt and d is number of days since the beginning of the year. The hour angle, h , represents how far the earth has turned since noon. Formally, it is defined as the difference in longitude between the point closest to the sun at noon to the point's current longitude. Graphing our equation for Q yields the following: irradiance_{day}graph.png /Graph of solar irradiance at the top of the atmosphere over a day at the equator during the northern summer solstice. Generated with values of $S_0 = 1.367 \text{ kW/m}^2$, $\gamma = 0.409$, $d = 172$, and $\phi = 0$. *

Integrating our equation over a day gives us

$$\begin{aligned}\overline{Q}^{\text{day}} &= -\frac{1}{2\pi} \int_{\pi}^{-\pi} Q \, dh \\ &= -\frac{1}{2\pi} S_0 \int_{\pi}^{-\pi} \cos(\theta_s) \, dh \\ &= \frac{S_0}{\pi} [h_0 \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(h_0)]\end{aligned}$$

where h_0 is defined as the hour angle at sunrise and sunset. h_0 can be calculated as

$$h_0 = \cos^{-1}(-\tan(\phi) \tan(\delta))$$

Graphing our equation for $\overline{Q}^{\text{day}}$ yields

contourgraph.png / A graph of latitude vs. day of the year vs. $\overline{Q}^{\text{day}}$. Generated with values of $S_0 = 1.367$ kW/m² and $\gamma = 0.409$. /

%%We can account for this change in angle based

Due to the earth being spherical,

We can model the solar irradiance, or power per unit area at a given instance, based on a

We can model the power per unit area received from the sun at a given instance, called solar irradiance,

We can model this generated power distribution over a day based on latitude and time of year.

%% Given our house attributes as inputs,

- We can model the generation function over a day as such