

#flo #inclass

1 | probability

given a sample space, a **probability map** P is a function from subsets of Ω to $[0,1]$ where $P(\Omega) = 1$
 can imagine a bunch of disjoint sets, A_1, A_2, A_3 , ect. then the prob

$$P(\bigcup_{i=1}^{\infty} A_i) = \sum_{i=1}^{\infty} P(A_i)$$

where all A_j are disjoint.

note: Ω and the empty set are disjoint $P(A^c)$ means a complement, or every outcome not in A , is just $1 - P(A)$.

1.1 | inclusion / exclusion

overlapping sets, A and B counting formula, $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ #extract

if we have three, $P(a \cup b \cup c) = P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) + P(A \cap B \cap C)$
 demotmot's problem? de montmort.

$A_i = i^{th}$ card has the number i on it $P(\text{winning}) = P(A_1 \cup A_2 \cup \dots \cup A_n) = \sum P(A_i) - \sum P(A_i \cap A_j) + \sum P(A_i \cap A_j \cap A_k) \dots ??$ goes to $1 - 1/e$

this is called a derangement > In combinatorial mathematics, a derangement is a permutation of the elements of a set, such that no element appears in its original position. In other words, a derangement is a permutation that has no fixed points. -wiki

1.2 | independence

if we flip a coin and then roll a die, $P(2H) = P(H) P(2) = 1/2 * 1/6 = 1/12$

2 events A and B are independent if $P(a \cap B) = P(A) * P(B)$