Q4

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```
\verb|click| = \texttt{data.frame} \\ (\texttt{sales} = \texttt{c}(260.3, 286.1, 279.4, 410.8, 438.2, 315.3, 565.1, 570.0, 426.1, 315.0, 403.6, 220.5, 343.2, 315.0, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6, 403.6
```

(a) How much variation is left unexplained by the intercept model? (this will be called the null deviance)

```
deviance(lm(sales ~ 1, click))
## [1] 598253
```

(b) How much variation is explained by adding ad to the intercept model?

```
deviance(lm(sales ~ 1, click)) - deviance(lm(sales ~ ad, click))
## [1] 463451
```

(c) How much additional variation is explained by adding reps to a model that already has ad in it?

```
deviance(lm(sales ~ ad, click)) - deviance(lm(sales ~ ad + reps, click))
## [1] 59327.45
```

(d) How much additional variation is explained by adding eff to a model that already has ad and reps in it?

```
deviance(lm(sales ~ ad + reps, click)) - deviance(lm(sales ~ ad + reps + eff, click))
## [1] 4430.622
```

(e) How much variation is unexplained by a model having all three predictors?

71043.94

(f) How much less variation is explained if we drop ad from a model with all three predictors in it?

```
deviance(lm(sales ~ reps + eff, click)) - deviance(lm(sales ~ ad + reps + eff, click))
## [1] 44295.35
```

(g) Compute R2 for the three-predictor model "by hand" using only the numbers you have found above. Confirm your answer by having R compute it.

```
fit = lm(sales ~ ad + reps + eff, click)
summary(fit)
```

```
##
## lm(formula = sales ~ ad + reps + eff, data = click)
## Residuals:
      Min 1Q Median 3Q
                                    Max
## -87.407 -25.384 -6.546 26.937 76.693
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 31.150 34.175 0.911
                                          0.368
               12.968
                          2.737 4.738 3.34e-05 ***
## ad
## reps
               41.246
                          7.280 5.666 1.95e-06 ***
                                          0.143
## eff
              11.524
                          7.691 1.498
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 44.42 on 36 degrees of freedom
## Multiple R-squared: 0.8812, Adjusted R-squared: 0.8714
## F-statistic: 89.05 on 3 and 36 DF, p-value: < 2.2e-16
```

```
(598253 - 71043.94) / 598253
```

[1] 0.8812477

(h) Compute adjusted R2 by hand and confirm it.

```
1 - ((1 - 0.8812477) * 39 / 36)
```

[1] 0.8713517

(i) Compute the F statistic for the overall test of significance by hand.

```
((598253 - 71043.94) / 3) / (71043.94 / 36)
```

[1] 89.05065

(j) Compute the F statistic to test H0: B1 = 0 by hand.

```
44295.35 / (71043.94 / 36)
```

[1] 22.44572