

Digital Image Processing

Experiment#1	Introduction to MATLAB Digital Image Processing Toolbox. To get familiar with some simple commands related to reading and displaying images using MATLAB.
Experiment#2	To get familiar with commands related to writing images on disk. To get familiar with image classes and conversion between image classes.
Experiment#3	To get familiar with matrix manipulation commands. To use matrix manipulation commands for rotating and compressing images.
Experiment#4	To get familiar with basic intensity transformation functions. To get familiar with M-file programming.
Experiment#5	To get familiar with histogram processing of images.
Experiment#6	To get familiar with histogram matching, local histogram processing and filtering.
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Experiment#1: Introduction to MATLAB Digital Image Processing Toolbox.

To get familiar with some simple commands related to reading and displaying images using MATLAB.

1. Experiment Text

- i. Digital Image Representation
- ii. Reading Images in MATLAB
- iii. Displaying Images

2. Lab Exercise

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Experiment Text

1. Digital Image Representation

A digital image may be defined as a two dimensional function $f(x, y)$, where x and y are spatial co-ordinates and the value of f at any value of x and y is called the intensity of image at that point. An image when captured may be continuous with respect to x and y co-ordinates and also in intensity. Converting such image to digital form means, that the co-ordinates as well as intensity is digitized. Digitizing the co-ordinates is called sampling, while digitizing intensity is called quantization. When co-ordinates x and y and intensity values of f are all finite, discrete quantities, the image is called digital image. In this lab we will use MATLAB for digital image processing. MATLAB has a special toolbox for dealing with images known as Image Processing Toolbox.

Let us suppose an image $f(x, y)$ is sampled such that it has M rows and N columns. We say that this image is of size $M \times N$ where x and y can take positive integer values. Although normally the values of x and y start from $(0,0)$ but in MATLAB they always start from $(1,1)$ since MATLAB cannot have zero index. The first value in the parenthesis i.e. x represents row while the second value y represents column e.g. notation $(1,2)$ is used to signify the second sample along the first row. One another difference is that MATLAB image processing toolbox uses the notation (r, c) instead of (x, y) where r and c represent row and column respectively. A typical digital image is shown in Figure 1.

$$f = \begin{bmatrix} f(1, 1) & f(1, 2) & \dots & f(1, N) \\ f(2, 1) & f(2, 2) & \dots & f(2, N) \\ \vdots & \vdots & \ddots & \vdots \\ \vdots & \vdots & \ddots & \vdots \\ f(M, 1) & f(M, 2) & \dots & f(M, N) \end{bmatrix}$$

A digital image is represented as a matrix in MATLAB. A typical image matrix in MAT-LAB is shown below.

2. Reading Images in MATLAB

Images are read in MATLAB using command

```
>> imread('filename')
```

where 'filename' is full name of an image file including extension. e.g.

```
>> f = imread('cameraman.tif');
```

reads the content of image 'cameraman.tif' in variable f. The above command reads an image from the current directory of the MATLAB. The path of the current directory of MATLAB is normally shown on top of command Window. Figure 2 shows different sections of a MATLAB window.

```
f=imread('cameraman.tif')
```

```
130 127 130 127 126 125 126 135 129 121 122 122 130 132 128 123 132 131  
. . .  
117 133 130 113
```

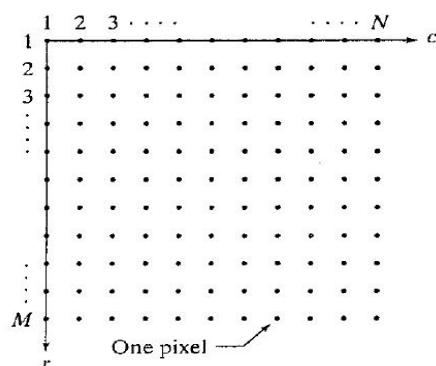


Figure 1: A typical digital image

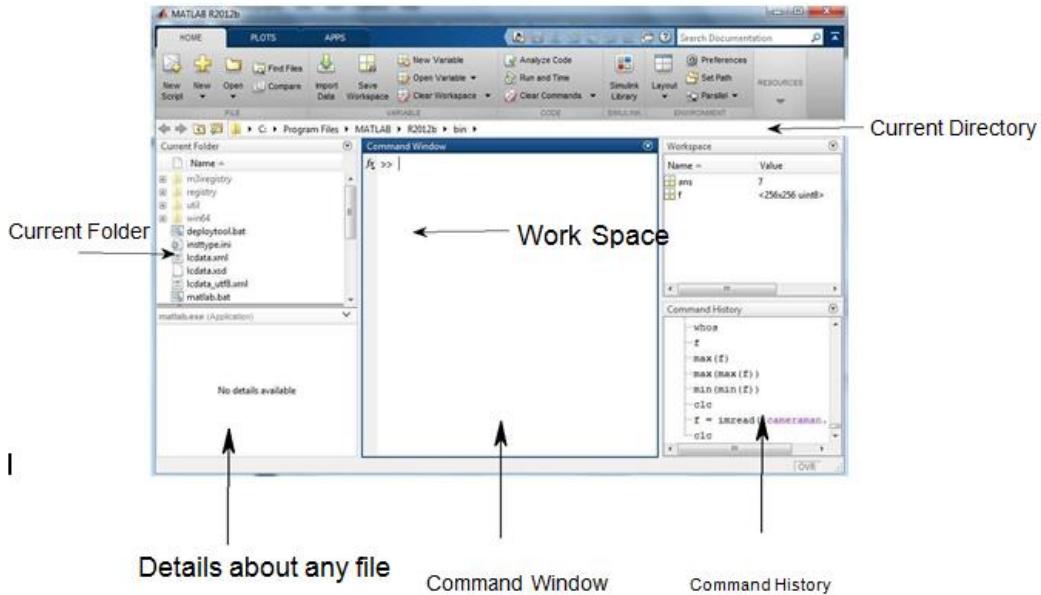


Figure 2: MATLAB Window

If you want to read file from a specific directory then you need to give the full path of that directory with 'filename' e.g. the following command reads an image from D: drive from folder named as images.

```
>> f = imread ('D:\images\cameraman.tif');
```

```
t=imread('E:\ImageProcessing\cameraman.tif')
```

```
124 118 119 119 126 126 120 123 118 111 120 116 118 116 113 108 117 120
.
.
.
137 153 150 133
```

The size of the image can be read using the following command.

```
>> size(f)
```

```
>> size_of_image_f=size(f)
```

```
size_of_image_f=
```

```
256 256
```

This command gives you the number of rows and columns of the image. You can also use the following command

```
>> [M N ] = size(f)
```

where the number of rows and columns will be saved in M and N respectively.

```
>>[M N]=size(f)
```

```
>> [M N]=size(f)
```

```
M =
```

```
 256
```

```
N =
```

```
 256
```

```
>> [M N R]=size(f)
```

```
M =
```

```
 256
```

```
N =
```

```
 256
```

```
R =
```

```
 1
```

The function whos can be used to get additional information about an image. For instance

```
>> whos
```

will give you details about f e.g. it will tell you the size, number of bytes taken and class of the image.

```
>> whos
```

Name	Size	Bytes	Class	Attributes
M	1x1	8	double	
N	1x1	8	double	
R	1x1	8	double	
ans	1x256	256	uint8	
f	256x256	65536	uint8	
g	256x256	65536	uint8	
size_of_image_f	1x2	16	double	
t	256x256	65536	uint8	

```
>> whos f
```

Name	Size	Bytes	Class	Attributes
f	256x256	65536	uint8	

3 Displaying Images

Images are shown in MATLAB by using command imshow e.g.

```
>> imshow(f)
```

will display the image read in variable f.

```
>>imshow(f);
```



The command

```
>> imshow(f, [low high])
```

displays all the pixels as black which are less than or equal to low and all values as white which are greater than or equal to high. All the values in between are displayed as intermediate intensity values using the default number of levels.

```
>> imshow(f,[0 255])
```



```
>> imshow(f,[50 255])
```



```
>> imshow(f,[150 255])
```



```
>> imshow(f,[0 230])
```



```
>> imshow(f,[0 150])
```

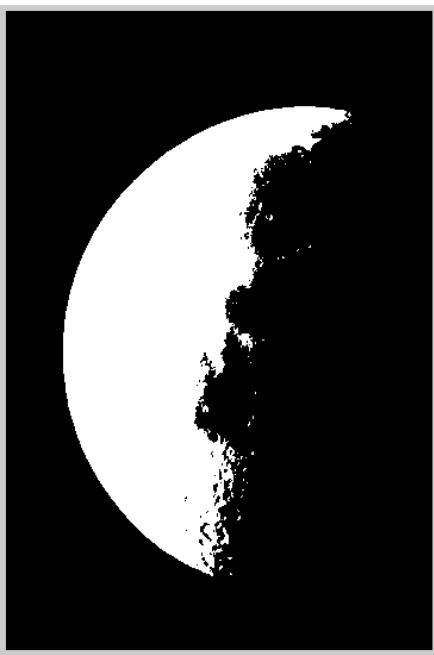


```
>> imshow(f,[50 150])
```



If you want to show images in separate figures, the command **figure** can be used. e.g. the following commands display two images in separate figure. If you have more than two figures you can use the command **figure** again.

```
>> figure  
imshow('moon.tif')  
figure  
f=imread('moon.tif');  
imshow(f,[127,128])
```



```
>> min(f)
min(min(f))
ans =
Columns 1 through 18
64 66 63 64 63 62 61 63 61 61 62 62 63 64 62 63 63 62
.....
Columns 253 through 256
26 27 21 24
ans =
7
>> max(f)
max(max(f))
ans =
Columns 1 through 18
166 168 166 169 169 174 188 187 181 194 204 173 170 203 196 175 193 178
.....
Columns 253 through 256
177 173 172 170
```

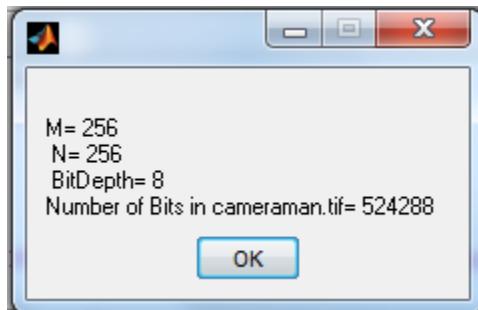
```
ans =
```

```
253
```

EXERCISE QUESTIONS

Q1 : Calculate the number of bits required to represent one intensity level in image 'cameraman.tif'. (Hint: The total size of an image in bits is $M \times N \times k$ where k represents the number of bits required for one intensity level.)

```
f=imread('cameraman.tif');
info=imfinfo('cameraman.tif');
k=info.BitDepth;
[M N]=size(f);
total_imbits=M*N*k;
output=sprintf('M= %d \n N= %d \n BitDepth= %d \n Number of Bits in cameraman.tif=%d',M,N,k,total_imbits);
msgbox(output);
```



```
clc
```

```
f=imread('cameraman.tif');
```

```
[m n]=size(f)
```

```
whos f
```

```
bit_depth=8*((m*n)/65536)
```

```
tot_bits=m*n*bit_depth
```

```
m =
```

```
256
```

```
n =
```

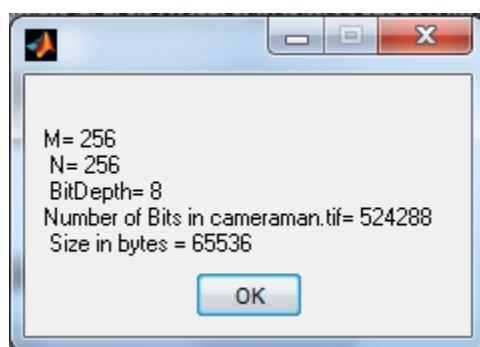
```
256
```

Name	Size	Bytes	Class	Attributes
f	256x256	65536	uint8	
bit_depth =				
8				
tot_bits =				
524288				

Q2 : Now recalculate the size of image in bytes from k. Does this result tally with the result given by whos?

(Hint: Size in bytes = $(M \times N \times k)/8$)

```
>> f=imread('cameraman.tif');
info=imfinfo('cameraman.tif');
k=info.BitDepth;
[M N]=size(f);
total_imbits=M*N*k;
size_in_bytes=total_imbits/8;
output=sprintf('M= %d \n N= %d \n BitDepth= %d \nNumber of Bits in cameraman.tif= %d \n Size in bytes =
%d ',M,N,k,total_imbits,size_in_bytes);
msgbox(output);
```



```
>> f=imread('cameraman.tif');
[m n]=size(f)
whos f
bit_depth=8*((m*n)/65536)
tot_bits=m*n*bit_depth;
tot_bytes=tot_bits/8
```

```

whos f
tot_bytes =
65536
Name      Size      Bytes      Class   Attributes
f         256x256    65536     uint8

```

Q3 : Find the minimum and maximum intensity value used in image 'cameraman.tif'. (Hint: The intensity values are stored in 'f', and minimum and maximum values can be found using MATLAB built in commands min and max.

```

>> f=imread('cameraman.tif');
minimum_values=min(f);
mini=min(min(f))
maxi=max(max(f))
mini =
7
maxi =
253

```

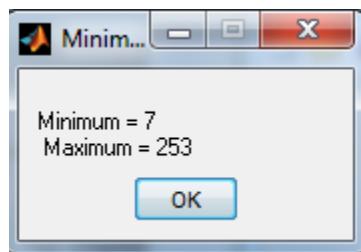
Q4 : Now use some value of low and high in command imshow(f, [low high]) based on the minimum and maximum value found in Q3. You can show many images with different values of low and high on same figure using command subplot. Use different values of low and high and see the changes in the image.

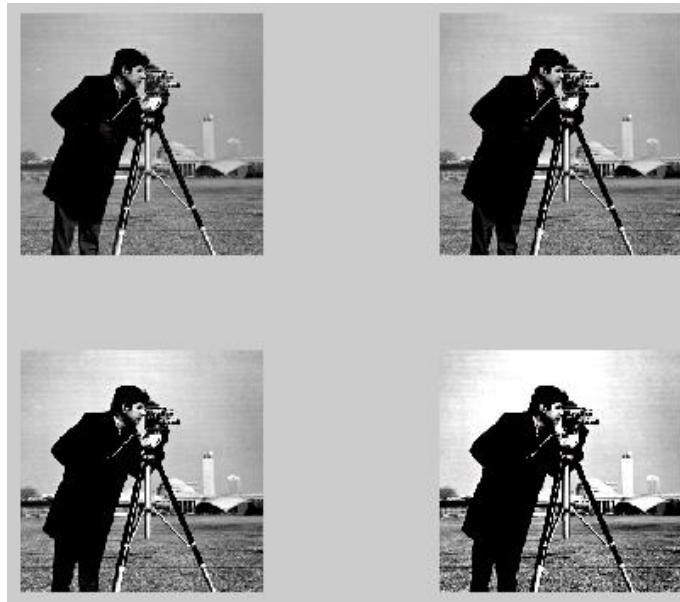
```

>> f=imread('cameraman.tif');
subplot(1,2,1)
imshow(f);
minimum_values=min(f);
mini=min(min(f))
maxi=max(max(f))
subplot(1,2,2);
imshow(f,[mini maxi])
h=sprintf('Minimum = %d \n Maximum = %d ', mini,maxi);
msgbox(h,'Minimum/Maximum Value')
figure
subplot(2,2,1);

```

```
imshow(f,[20 235])
subplot(2,2,2);
imshow(f,[40 215])
subplot(2,2,3);
imshow(f,[60 195])
subplot(2,2,4);
imshow(f,[80 175])
mini =
    7
maxi =
    253
```





Experiment#2: To get familiar with commands related to writing images on disk. To get familiar with image classes and conversion between image classes.

1. Experiment Text

- i. Writing Images
- ii. Image Classes
- iii. Image Types
- iv. Conversion Between Classes

2. Lab Exercise

3. Exercise Questions

EXPERIMENT TEXT

1 Writing Images

Images can be written to disk using command `imwrite(f,'filename')` e.g.

```
>> imwrite(f,'cameraman1.tif')
```

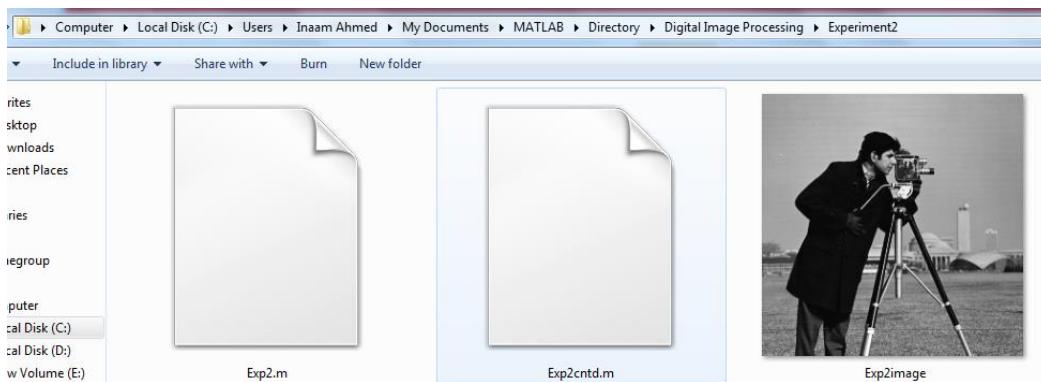
will save the contents of variable `f` in the form of an image named `cameraman1.tif'. The variable `f` should have contents of a valid image. (Hint: You can use command `f = imread()` to load contents of an image into `f`).

```
>> f=imread('cameraman.tif');
```



```
imshow(f)
```

```
imwrite(f,'Exp2image.tif');
```

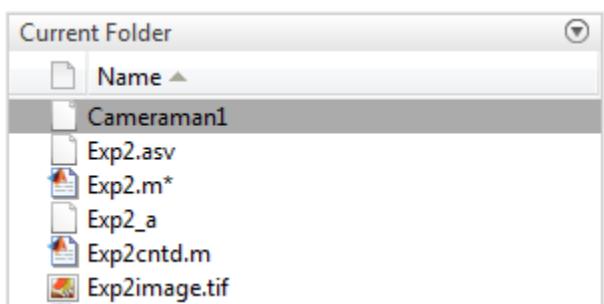


In the command shown above 'filename' should have a recognized file format extension. Alternatively, the desired format can be specified explicitly with a third input argument. e.g.

```
>> imwrite(f,'cameraman1','tif')
```

saves the contents of f in .tif format in file named **cameraman1**.

```
imwrite(f,'Cameraman1','tif');
```



If 'filename' contains no path information, **imwrite** will save the image in the current directory. If you want to save the image in another directory, you need to give full path with 'filename'. e.g. the following

command will save the image in drive D.

```
>> imwrite(f,'D:\cameraman1.tif')  
imwrite(f,'E:\ImageProcessing\Exp2image.tif');
```



To see the detailed information of an image, the command `imfinfo filename` can be used where `filename` is the name of the image stored on the disk. e.g. the following command will give detailed information about image `cameraman.tif`

```
>> imfinfo cameraman.tif  
>> struct=imfinfo('cameraman.tif')  
struct =  
Filename: [1x67 char]  
FileModDate: '04-Dec-2000 13:57:54'  
FileSize: 65240  
Format: 'tif'  
FormatVersion: []  
Width: 256
```

```
Height: 256
BitDepth: 8
ColorType: 'grayscale'
.
.
.
ImageDescription: [1x112 char]
```

The information fields displayed by `imfinfo` can be captured into a so-called structure variable that can be used for subsequent computations. Using the preceding image as an example, and letting `K` denote the structure variable, we use the syntax

```
>> K = imfinfo('cameraman.tif');
```

to store into variable `K` all the information generated by command `imfinfo`. The information generated by `imfinfo` is appended to the structure variable by means of fields, separated from `K` by a dot. For example, the image height and width are now stored in structure fields `K.Height` and `K.Width` which can be accessed using the following command.

```
>> K.Height
```

```
>> struct.Format
```

```
struct.Offset
```

```
struct.BitDepth
```

```
ans =
```

```
tif
```

```
ans =
```

```
64872
```

```
ans =
```

```
8
```

2 Image Classes

Although we work with integer coordinates, the intensities of pixels are not restricted to be integers in MATLAB. Figure 1 lists the various classes supported by MATLAB and the Image Processing Toolbox for representing pixel values. Classes **uint8** and **logical** are used extensively in image processing, and they are the usual classes encountered when reading images from image file formats such as TIFF or JPEG. These classes

use 1 byte to represent each pixel. Some scientific data sources, such as medical imagery, require more dynamic range than is provided by uint8, so the **uint16** and **int16** classes are used often for such data. These classes use 2 bytes for each array element. The classes double and single are used for computationally intensive operations such as the Fourier transform. The int8, uint32, and int32 classes, although supported by the toolbox, are not used commonly for image processing. There are quite a few images available in the MATLAB toolbox. A list is given in Figure 2.

Name	Description
double	Double-precision, floating-point numbers in the approximate range $\pm 10^{308}$ (8 bytes per element).
single	Single-precision floating-point numbers with values in the approximate range $\pm 10^{38}$ (4 bytes per element).
uint8	Unsigned 8-bit integers in the range [0, 255] (1 byte per element).
uint16	Unsigned 16-bit integers in the range [0, 65535] (2 bytes per element).
uint32	Unsigned 32-bit integers in the range [0, 4294967295] (4 bytes per element).
int8	Signed 8-bit integers in the range [-128, 127] (1 byte per element).
int16	Signed 16-bit integers in the range [-32768, 32767] (2 bytes per element).
int32	Signed 32-bit integers in the range [-2147483648, 2147483647] (4 bytes per element).
char	Characters (2 bytes per element).
logical	Values are 0 or 1 (1 byte per element).

Figure 1: Classes used for Images in MATLAB

3 Image Types

MATLAB toolbox supports four types of images Gray-scale, Binary, Indexed and RGB. Most monochrome image processing operations are carried out using binary or gray-scale images, so our initial focus is on these two image types.

3.1 Gray-scale Images

A gray-scale image is a data matrix whose values represent shades of gray. When the elements of a gray-scale image are of class uint8 or uint16, they have integer values in the range [0, 255] or [0, 65535], respectively. If the image is of class double or single, the values are floating-point numbers. Values of double and single gray-scale images normally are scaled in the range [0, 1], although other ranges can be used.

3.2 Binary Images

Binary images have a very specific meaning in MATLAB. A binary image is a logical array of 0s and 1s. Thus,

an array of 0s and 1s whose values are of data class, say, uint8, is not considered a binary image in MATLAB. A numeric array is converted to binary using function logical. Thus, if A is a numeric array consisting of 0s and 1s, we create a logical array B using the statement

```
AT3_1m4_01.tif      AT3_1m4_02.tif
AT3_1m4_03.tif      AT3_1m4_04.tif
AT3_1m4_05.tif      AT3_1m4_06.tif
AT3_1m4_07.tif      AT3_1m4_08.tif
AT3_1m4_09.tif      AT3_1m4_10.tif
    autumn.tif          bag.png
    blobs.png           board.tif
cameraman.tif        canoe.tif
    cell.tif            circbw.tif
    circles.png         circlesBrightDark.png
    circuit.tif         coins.png
coloredChips.png     concordaerial.png
concordorthophoto.png   eight.tif
    fabric.png          football.jpg
    forest.tif          gantrycrane.png
    glass.png           greens.jpg
hestain.png           kids.tif
liftingbody.png       logo.tif
    m83.tif             mandi.tif
    moon.tif            mri.tif
office_1.jpg          office_2.jpg
office_3.jpg          office_4.jpg
office_5.jpg          office_6.jpg
onion.png             paper1.tif
pears.png              peppers.png
pillsetc.png          pout.tif
rice.png               saturn.png
shadow.tif            snowflakes.png
spine.tif              tape.png
testpat1.png          text.png
tire.tif               tissue.png
trees.tif              westconcordaerial.png
westconcordorthophoto.png
```

B = logical (A)

```
cameraman=imread('cameraman.tif');
```

```
b=logical(cameraman)
```

```
1 1 1 1 1 1 1 1 1 1 1 1 1 1
```

```
.
```

```
.
```

```
.
```

```
1 1 1 1 1 1 1 1 1 1 1 1 1
```

If A contains elements other than 0s and 1s, the logical function converts all nonzero quantities to logical 1s and all entries with value 0 to logical 0s. Using relational and logical operators also results in logical arrays. To test if an array is of class logical we use the islogical function : islogical(C) If C is a logical array, this function returns a 1. Otherwise it returns a 0.

```
>> islogical(b)
```

```
ans =
```

```
1
```

```
>> whos b
```

Name	Size	Bytes	Class	Attributes
b	256x256	65536	logical	

An image is characterized by both a class and a type. For instance, a statement discussing a “uint8 gray-scale image” is simply referring to a gray-scale (type) image whose pixels are of class uint8 [1].

4 Conversion Between Classes

Converting images from one class to another is a common operation. When converting between classes, keep in mind the value ranges of the classes being converted (See Figure 1).

The general syntax for class conversion is

$$B = \text{class_name}(A)$$

where class name is one of the names in the first column of Figure 1. For example, suppose that A is an array of class uint8. A double-precision array, B, is generated by the command $B = \text{double}(A)$.

```
>> cameraman=imread('cameraman.tif');
```

```
>> whos cameraman
```

Name	Size	Bytes	Class	Attributes
cameraman	256x256	65536	uint8	

```

>> b=double(cameraman);
>> whos b
Name      Size            Bytes  Class       Attributes
b         256x256        524288  double

```

If C is an array of class double in which all values are in the range [0, 255] (but possibly containing fractional values), it can be converted to an uint8 array with the command D = uint8(C). If an array of class double has any values outside the range [0, 255] and it is converted to class uint8 in the manner just described, MATLAB converts to 0 all values that are less than 0, and converts to 255 all values that are greater than 255. Numbers in between are rounded to the nearest integer. Thus, proper scaling of a double array so that its elements are in the range [0, 255] is necessary before converting it to uint8.

```

>> u=1000*rand(3,3)
u =
  529.4502  260.7776  998.9270
  931.9208  453.7062  502.2118
  332.4853  1.2837   80.8436

```

Name	Size	Bytes	Class	Attributes
u	3x3	72	double	

```

>> un=uint8(u)
un =
  255  255  255
  255  255  255
  255  1    81

```

Converting any of the numeric data classes to logical creates an array with logical 1s in locations where the input array has nonzero values, and logical 0s in places where the input array contains 0s.

```

>> u=1000*rand(3,3)
u1=u-min(min(u))-1
l=logical(u)
u =
  334.2572  42.4156  241.4016
  914.4002  400.0491  296.6317

```

```
590.3546 872.6598 470.5874
```

```
u1 =
```

```
290.8416 -1.0000 197.9860  
870.9846 356.6335 253.2161  
546.9390 829.2442 427.1718
```

```
l =
```

```
1 1 1  
1 1 1  
1 1 1
```

The toolbox provides specific functions that perform the scaling and other book keeping necessary to convert images from one class to another. The functions are given in Figure 3.

Name	Converts Input to:	Valid Input Image Data Classes
im2uint8	uint8	logical,uint8,uint16,int16,single, and double
im2uint16	uint16	logical,uint8,uint16,int16,single, and double
im2double	double	logical,uint8,uint16,int16,single, and double
im2single	single	logical,uint8,uint16,int16,single, and double
mat2gray	double in the range [0,1]	logical,uint8,int8,uint16,int16, uint32,int32,single, and double
im2bw	logical	uint8,uint16,int16,single, and double

Figure 3: Conversion functions between different classes

Function im2uint8, for example, creates a unit8 image after detecting the data class of the input and performing all the necessary scaling for the toolbox to **recognize the data as valid image data**. For example, consider the following image f of class double, which could be the result of an intermediate computation:

```
>> f=[-0.5 0.5;0.75 1.5]
```

```
f =
```

```
-0.5000 0.5000  
0.7500 1.5000
```

```
>> whos f
```

Name	Size	Bytes	Class	Attributes
f	2x2	32	double	

Performing the conversion

```
>> g=double(f)

g =
-0.5000  0.5000
 0.7500  1.5000

>> whos g
  Name    Size         Bytes Class Attributes
  g        2x2          32  double

>> g1= im2double(f)

g1 =
-0.5000  0.5000
 0.7500  1.5000

>> whos g1
  Name    Size         Bytes Class Attributes
  g1       2x2          32  double

>> h=uint8(f)

h =
  0   1
  1   2

>> whos h
  Name    Size         Bytes Class
  h        2x2           4      uint8

>> h=im2uint8(f)

h =
  0   128
 191  255

>> h2=uint8(round(f*255))

h2 =
  0   128
 191  255

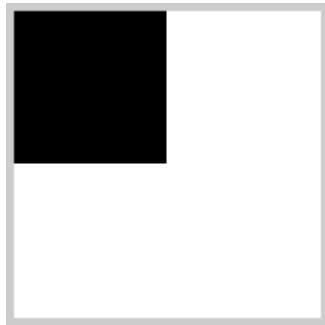
>> j= [-0.5 50; 255 755]
```

```
j =  
-0.5000 50.0000  
255.0000 755.0000
```

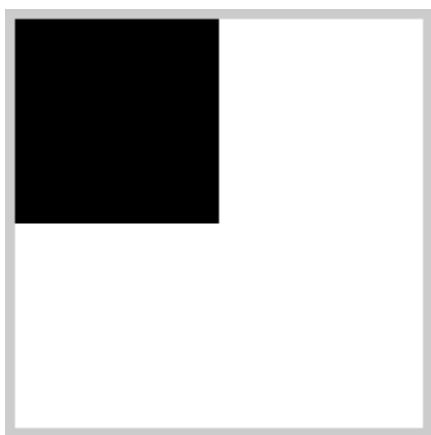
Name	Size	Bytes	Class
------	------	-------	-------

j	2x2	32	double
---	-----	----	--------

```
imshow(j,'InitialMagnification',1500)
```

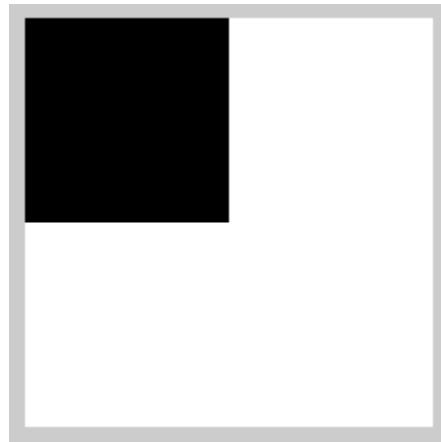


```
>> d= double (j)  
d =  
-0.5000 50.0000  
255.0000 755.0000  
>> imshow(d,'InitialMagnification',2000)
```



```
>> doub=im2double(j)  
doub =  
-0.5000 50.0000
```

```
255.0000 755.0000
```



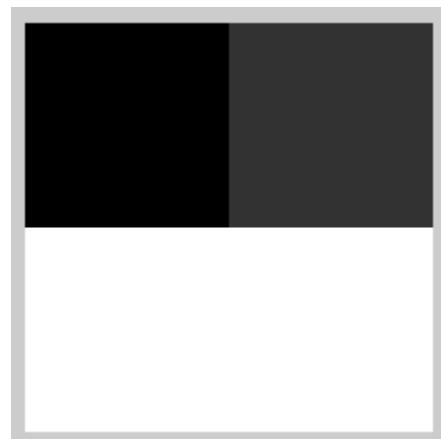
From which we see that function `im2uint8` sets to 0 all values in the input that are less than 0, sets to 255 all values in the input that are greater than 1, and multiplies all other values by 255. Rounding the results of the multiplication to the nearest integer completes the conversion.

```
>> ui=uint8(j)
```

```
ui =
```

```
0 50
```

```
255 255
```



```
>> j= [-0.5 50; 255 755]
```

```
j =
```

```
-0.5000 50.0000
```

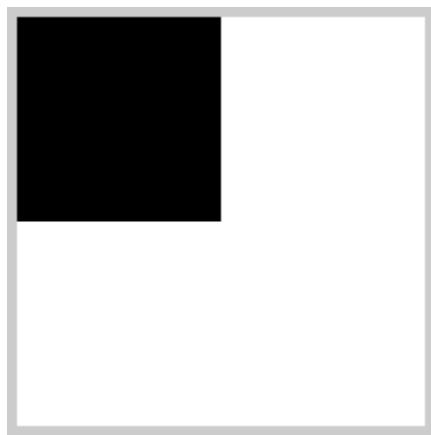
```
255.0000 755.0000
```

```
>> uint =im2uint8(j)
```

```
uint =
```

0 255

255 255



As an illustration, consider the following example

```
>> h = uint8([25 50; 128 200]);
```

```
>> g = im2double(h)
```

```
g =
```

```
0.0980 0.1961
```

```
0.4706 0.7843
```

from which we infer that the conversion when the input is of class uint8 is done simply by dividing each value of the input array by 255. If the input is of class uint16 the division is by 65535.

```
>> h=uint8 ([25 50;128 200])
```

```
h =
```

```
25 50
```

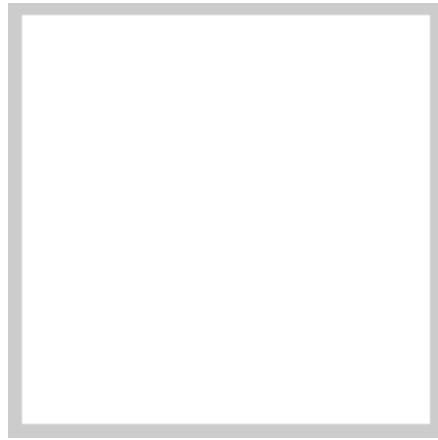
```
128 200
```

```
>> g1=double(h)
```

```
g1 =
```

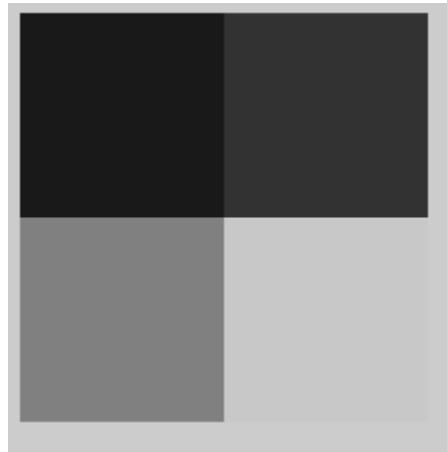
```
25 50
```

```
128 200
```



g2 =

```
0.0980  0.1961  
0.5020  0.7843
```



Function `im2double` converts an input to class double. If the input is of class `uint8`, `uint16`, or `logical`, function `im2double` converts it to class double with values in the range [0, 1]. If the input is of class `single`, or is already of class double, `im2double` returns an array that is of class double, but is numerically equal to the input. For example, if an array of class double results from computations that yield values outside the range [0, 1], inputting this array into `im2double` will have no effect. Function `mat2gray` can be used to convert an array of any of the classes to a double array with values in the range [0, 1].

Toolbox function `mat2gray` converts an image of any of the classes to an array of class double scaled to the range [0, 1]. The calling syntax is

```
g = mat2gray(A, [Amin, Amax])
```

where image g has values in the range 0 (black) to 1 (white). The specified parameters, Amin and Amax, are such that values less than Amin in A become 0 in g, and values greater than Amax in A correspond to 1 in g. Sets the values of Amin and Amax to the actual minimum and maximum values in A

```
>> f= [-0.5 50;345 90]
```

```
f =
```

```
-0.5000 50.0000  
345.0000 90.0000
```

```
>> whos f
```

Name	Size	Bytes	Class
f	2x2	32	double

```
>> g1=double (f)
```

```
g1 =
```

```
-0.5000 50.0000  
345.0000 90.0000
```

```
>> whos g1
```

Name	Size	Bytes	Class	Attributes
g1	2x2	32	double	

```
>> g2=im2double (f)
```

```
g2 =
```

```
-0.5000 50.0000  
345.0000 90.0000
```

```
>> whos g2
```

Name	Size	Bytes	Class	Attributes
g2	2x2	32	double	

```
>> g3=mat2gray (f)
```

```
g3 =
```

```
0 0.1462
```

```
1.0000 0.2619
```

```
>> whos g3
```

Name	Size	Bytes	Class	Attributes
g3	2x2	32	double	

```
>> g4=mat2gray(f,[50 90])
```

```
g4 =
```

0	0
1	1

```
>> whos g4
```

Name	Size	Bytes	Class	Attributes
g4	2x2	32	double	

```
>> f=[-0.5 50;345 90]
```

```
f =
```

-0.5000	50.0000
345.0000	90.0000

```
>> g=f-min(f(:))
```

```
g =
```

0	50.5000
345.5000	90.5000

```
>> g=g/max(g(:))
```

```
g =
```

0	0.1462
1.0000	0.2619

```
>> whos g
```

Name	Size	Bytes	Class	Attributes
g	2x2	32	double	

```
>> mat2gray(f) % g and ans are same here
```

```
ans =
```

```
0    0.1462  
1.0000  0.2619
```

The syntax

```
g = mat2gray(A)
```

The second syntax of mat2gray is a very useful tool because it scales the entire range of values in the input to the range [0, 1], independently of the class of the input, thus eliminating clipping.

Function im2double fails to create valid image data [0 --- 1] when input is in double and single in that case function mat2gray() is used.

```
>> f=uint8([-0.5 50;345 90])
```

```
f =
```

```
0 50  
255 90
```

```
>> whos f
```

Name	Size	Bytes	Class	Attributes
f	2x2	4	uint8	

```
>> g1=double(f)
```

```
g1 =
```

```
0 50  
255 90
```

```
>> whos g1
```

Name	Size	Bytes	Class	Attributes
g1	2x2	32	double	

```
>> g2=im2double(f)
```

```
g2 =
```

```
0 0.1961  
1.0000 0.3529
```

```
>> whos g2
  Name      Size      Bytes  Class  Attributes
  g2        2x2        32    double
```

```
>> g3=mat2gray(f)
```

```
g3 =
  0    0.1961
  1.0000  0.3529
```

```
>> whos g3
```

```
  Name      Size      Bytes  Class  Attributes
  g3        2x2        32    double
```

```
>> g4=mat2gray(f,[50 90])
```

```
g4 =
  0    0
  1    1
```

```
>> whos g4
```

```
  Name      Size      Bytes  Class  Attributes
  g4        2x2        32    double
```

```
>> g=f-min(f(:))
```

```
g =
  0  50
 255  90
```

```
>> g=g/max(g(:))
```

```
g =
  0  0
 1  0
```

```
>> whos g
Name      Size      Bytes  Class    Attributes
g         2x2        4     uint8
```

```
>> s=mat2gray(f)
```

```
s =
0    0.1961
1.0000  0.3529
```

Finally, we consider conversion to class logical. (Recall that the Image Processing Tool-box treats logical matrices as binary images.) Function logical converts an input array to a logical array. In the process, nonzero elements in the input are converted to 1s, and 0s are converted to 0s in the output. An alternative conversion procedure that often is more useful is to use a relational operator, such as `>`, with a threshold value. For example, the syntax

$$g = f > t$$

Produces a logical matrix containing 1s wherever the elements of f are greater than t and 0s elsewhere

Toolbox function `im2bw` performs this thresholding operation in a way that automatically scales the specified threshold in different ways, depending on the class of the input image. The syntax is

$$\text{im2bw}(f, T)$$

Values specified for the threshold T must be in the range $[0, 1]$, regardless of the class of the input. The function automatically scales the threshold value according to the input image class. For example, if f is `uint8` and T is 0.4, then `im2bw` thresholds the pixels in f by comparing them to $255 * 0.4 = 102$.

```
>> f = uint8 ([ 25 50; 128 200])
```

```
f =
25  50
128 200
>> s = im2double(f)
```

```
s =
0.0980  0.1961
0.5020  0.7843
```

```

>> s = mat2gray(f)
s =
    0         0.1429
    0.5886    1.0000
>> g = f>150

g =
    0   0
    0   1

>> whos g
  Name      Size            Bytes    Class       Attributes
  g            2x2              4    logical

>> g = im2bw(f,0.5)

g =
    0   0
    1   1

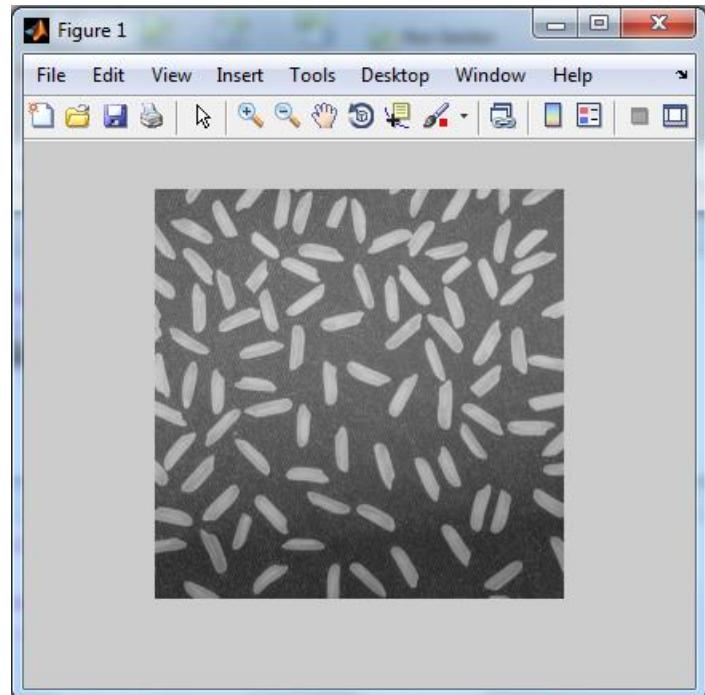
```

LAB EXERCISE

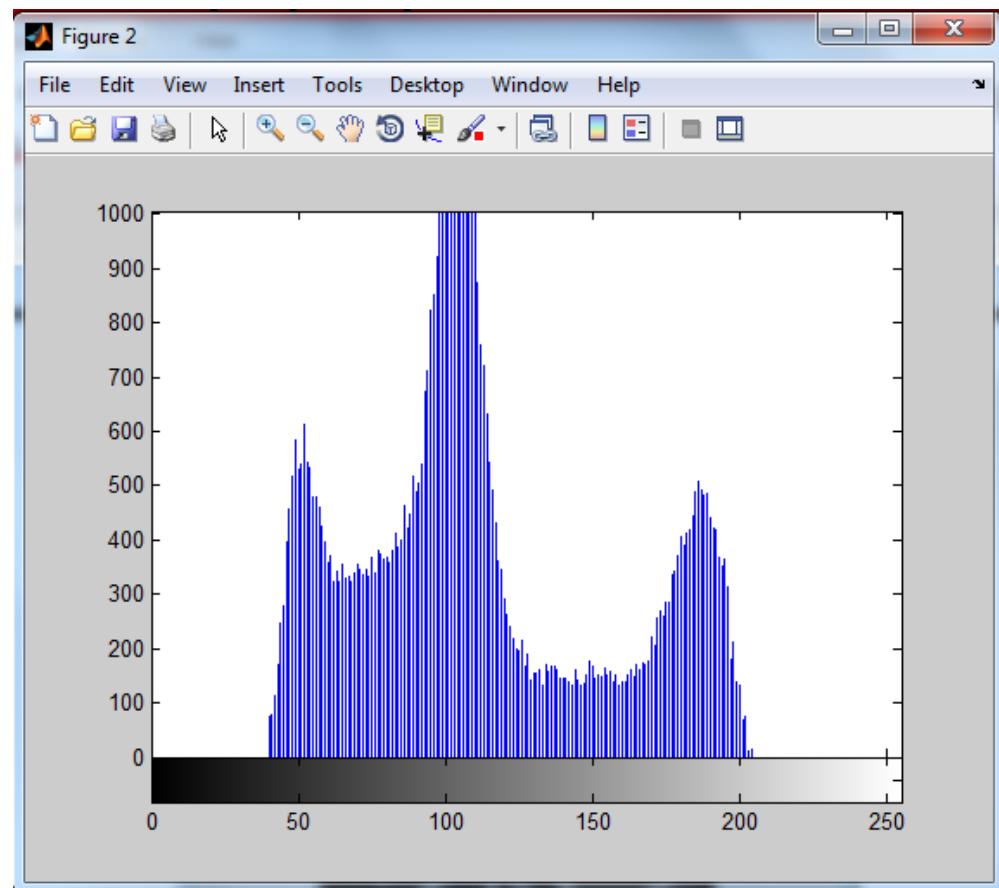
```

y=imread('rice.png');
figure
imshow(y);

```

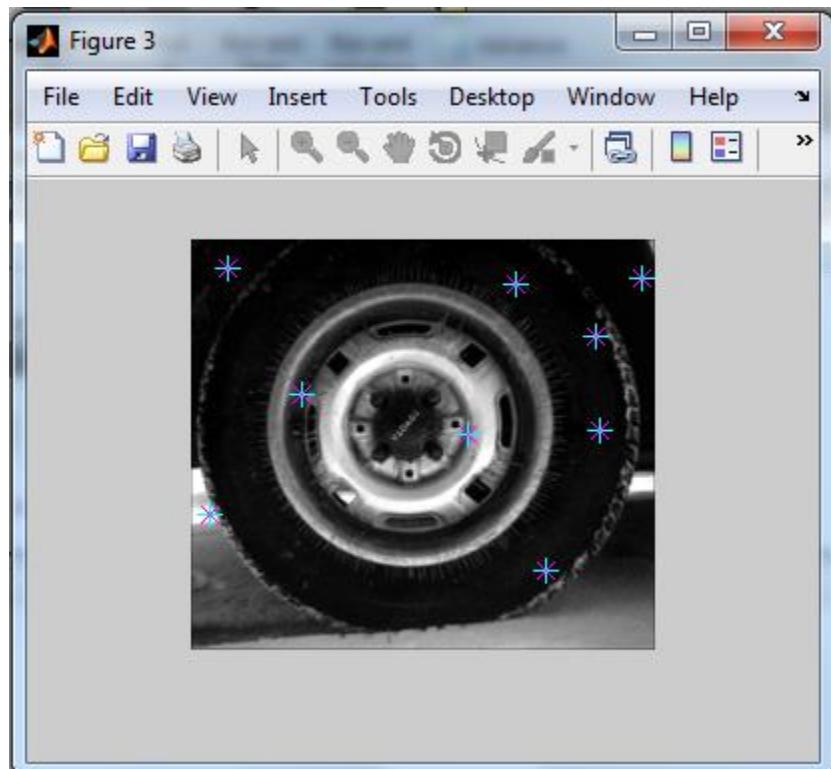


```
figure  
imhist(y);
```



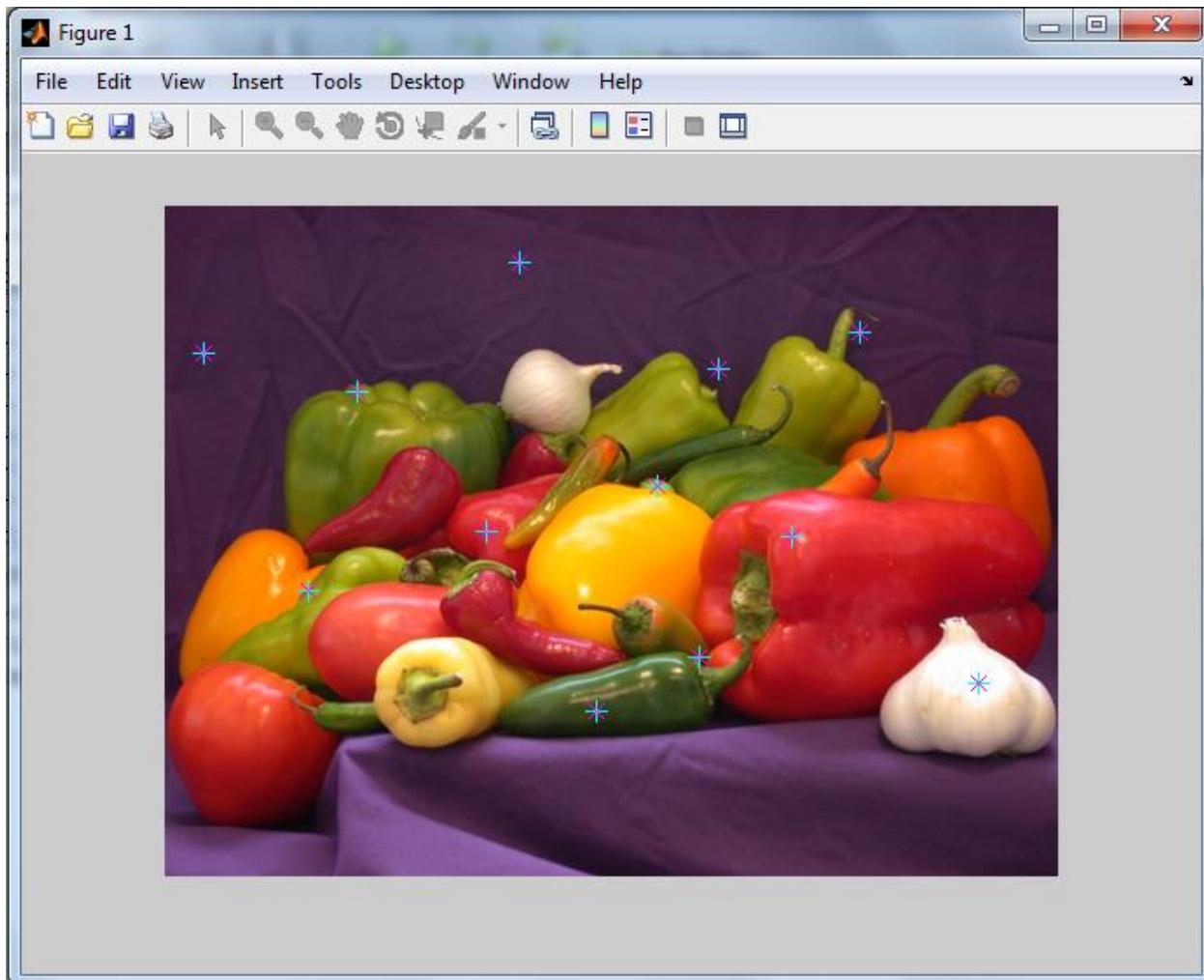
```
>> mean=mean2(y)
```

```
mean =  
111.2468  
>> std=std2(y)  
std =  
42.4935  
>> corellation_of_y_f=corr2(y,f)  
corellation_of_y_f =  
0.0968  
>> tire=imread('tire.tif');  
figure  
impixel(tire)
```



```
ans =  
24 24 24  
86 86 86  
13 13 13  
1 1 1  
6 6 6
```

```
1   1   1  
255 255 255  
8   8   8  
7   7   7  
>> tire=imread('peppers.png');  
figure  
impixel(tire)
```



```
ans =  
131 127 8  
214 51 51  
249 66 58  
83 49 7  
50 62 32  
138 140 5
```

195 182 90

71 40 65

67 36 67

75 47 76

66 35 62

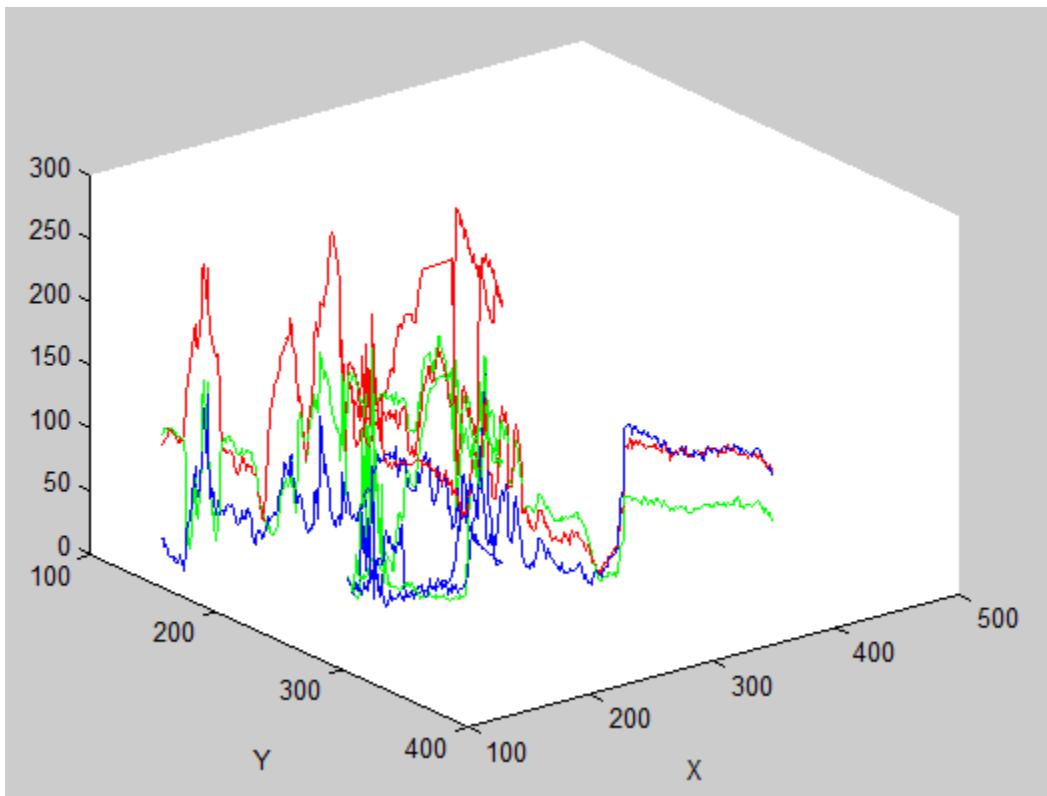
254 254 254

70 40 71

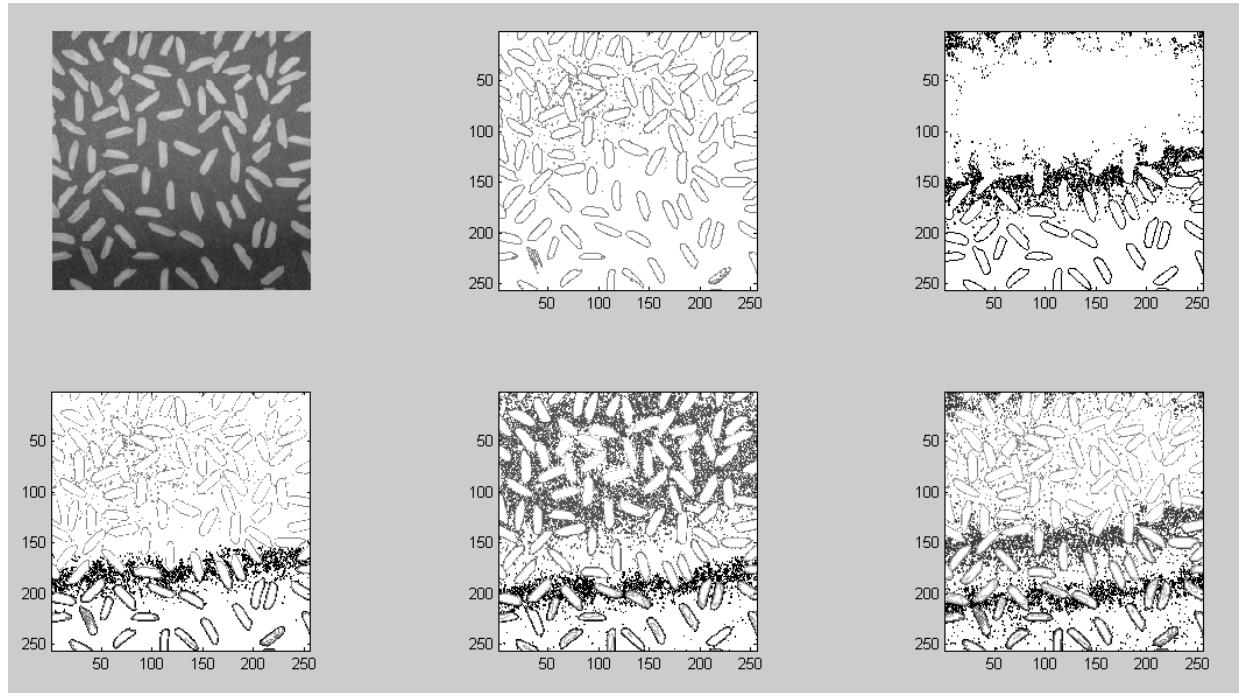
>>imshow('peppers.png')

Improfile





```
>> I=imread('rice.png')
subplot(2,3,1)
imshow(I)
subplot(2,3,2)
imcontour(I,1)
subplot(2,3,3)
imcontour(I,2)
subplot(2,3,4)
imcontour(I,3)
subplot(2,3,5)
imcontour(I,4)
subplot(2,3,6)
imcontour(I,5)
```



```

>> cameraman=imread('cameraman.tif');
b=logical(cameraman);
disp('B is logical or not : ');
islogical(b)
B is logical or not :
ans =
1
>>whos cameraman
>> whos cameraman
  Name      Size      Bytes Class Attributes
cameraman  256x256      65536  uint8
imshow(cameraman)
>> g=[-0.5 0.5;0.75 1.5]
y=im2uint8(g)
s=im2uint16(g)
g =
-0.5000  0.5000
 0.7500  1.5000
y =

```

```
0    128
191   255
s =
0          32768
49151      65535
c=double(cameraman)/65535;
imshow(c)
```



```
>> f=imread('cameraman.tif');
subplot(1,2,1);
imshow(f)
f=f+20;
imwrite(f,'E:\ImageProcessing\ecameraman.tif');
imwrite(f,'E:\ImageProcessing\ecameraman1','jpeg');
imwrite(f,'E:\ImageProcessing\ecameraman2','png');
imwrite(f,'E:\ImageProcessing\ecameraman3','gif');
imwrite(f,'E:\ImageProcessing\ecameraman4','bmp');
```



cameraman



ecameraman



ecameraman1



ecameraman2



ecameraman3



ecameraman3



ecameraman4



Exp2image

E:\ImageProcessing

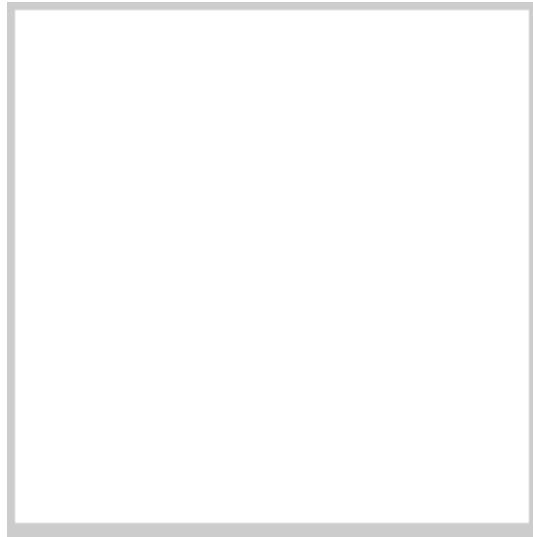
```
>> h=imfinfo('cameraman.tif');
g=sprintf('height =%d ',h.Height)
msgbox(g);
g =
height =256
```



```
>> figure
```

```
log=logical(f);
```

```
imshow(log);
```



```
>> figure
```

```
log=logical(f);
```

```
imshow(log);
```

```
>> d=im2double(f);
```

```
title('Tool Box Functions')
```

```
subplot(1,3,1)
```

```
imshow(d)
```

```
xlabel('double')
```

```
>> figure
```

```
d=im2double(f);
```

```
title('Tool Box Functions')
```

```
subplot(1,3,1)
```

```
imshow(d)
```

```
xlabel('double')
```

```
g=im2uint16(d);
```

```
subplot(1,3,2)
```

```
imshow(g)
```

```
xlabel('uint16')
```

```
l=im2single(d);
```

```
subplot(1,3,3)
```

```

imshow(I)
xlabel('single')
whos

```

Name	Size	Bytes	Class	Attributes
I	256x256	65536	uint8	
.....				
std	1x1	8	double	



EXERCISE QUESTIONS

Q1 : Read any image of class uint8 from MATLAB built in images. Convert it to double using the command given above and show it using imshow. Do you see any difference in the original image and the image converted to double? Why there is a difference?

```

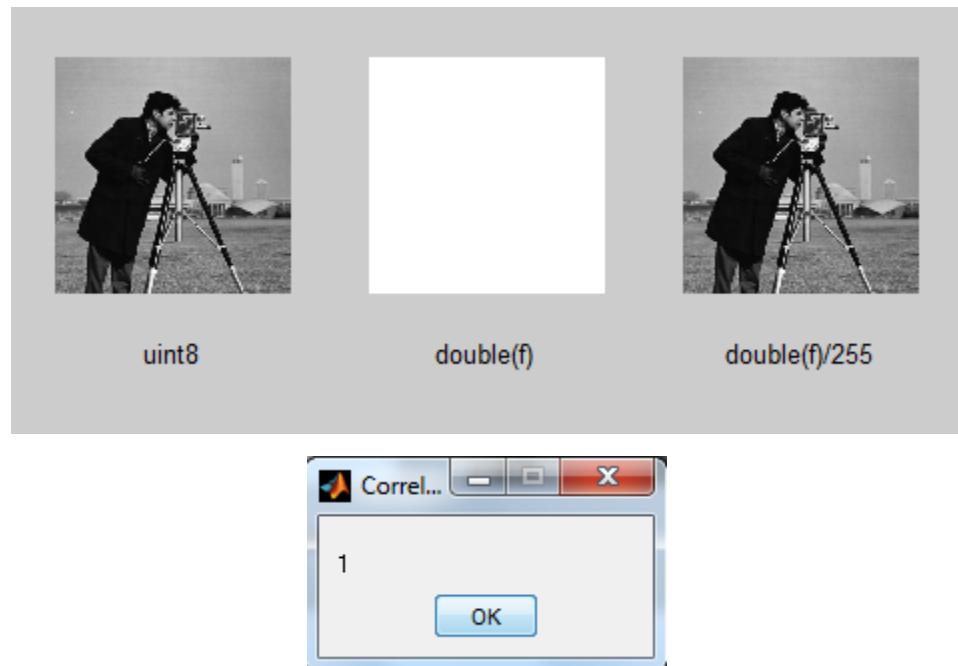
f=imread('cameraman.tif');
whos f
subplot(1,3,1)
imshow(f)
xlabel('uint8')
d=double(f)
d(1:10)
f(1:10)
subplot(1,3,2)
imshow(d)

```

```

xlabel('double(f)')
d=d/255;
subplot(1,3,3)
imshow(d)
xlabel('double(f)/255')
d(1:10)
f(1:10)
msgbox(num2str(corr2(f,d)), 'Correlation');

```



Q2 : Convert the above matrix h into type double using im2double and using mat2gray. Do you see any difference in the output? How does the function mat2gray scale the values in between maximum and minimum values of matrix h?

h =

$$\begin{matrix} 0 & 50 \\ 128 & 255 \end{matrix}$$

g =

$$\begin{matrix} 0 & 0.1961 \\ 0.5020 & 1.0000 \end{matrix}$$

c =

$$\begin{matrix} 0 & 40 \end{matrix}$$

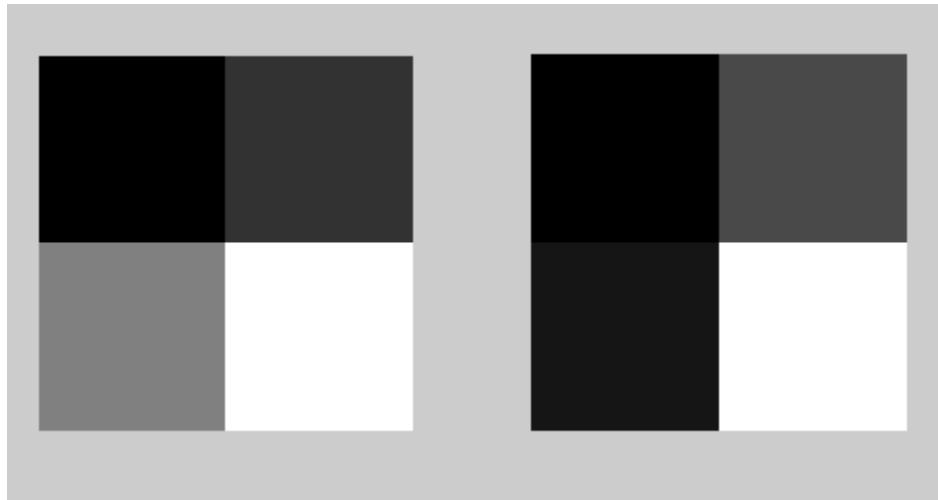
```
12 140
```

```
q =
```

```
0 0.2857
```

```
0.0857 1.0000
```

Name	Size	Bytes	Class	Attributes
I	256x256	65536	uint8	
.....				
y	2x2	4	uint8	



Q3 : Let us suppose we wish to convert the following small, double image ($h = [1 \ 2 ; 3 \ 4]$;) to binary such that values 1 and 2 become 0 and the other two values become 1. Use atleast two methods to convert it into binary. (Hint: convert the values of f between 0 and 1 before converting it to binary). After converting it into logical (binary) image convert it to uint8. Now convert this uint8 image to double without changing the values.

```
>> h=[1 2;3 4]
```

```
h =
```

```
1 2
```

```
3 4
```

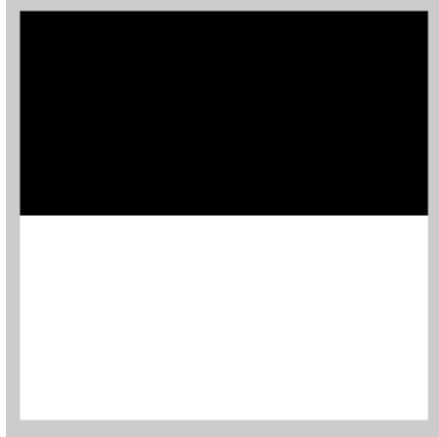
```
>> l=h>2
```

```
l =
```

```
0 0
```

```
1 1
```

```
>> imshow(l,'InitialMagnification',2000)
```



```
>> h
```

```
h =
```

```
1 2
```

```
3 4
```

```
>> v=uint8(h)
```

```
v =
```

```
1 2
```

```
3 4
```

```
>> fun2=im2bw(v,0.0098)
```

```
fun2 =
```

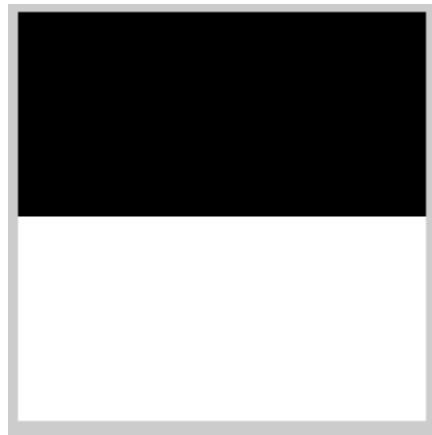
```
0 0
```

```
1 1  
>> fun2=im2bw(v,2.5/255)
```

```
fun2 =
```

```
0 0  
1 1
```

```
>> imshow(fun2,'InitialMagnification',2000)
```



```
>> h = [ 1 2 ; 3 4]
```

```
h =
```

```
1 2  
3 4
```

```
>> g = im2bw(h,0.6) %fails
```

```
g =
```

```
1 1  
1 1
```

```
>> g = im2bw(h,0.1) % fails
```

```
g =
```

```
1 1
```

```
1 1
```

```
>> g = im2bw(h,0) %fails
```

```
g =
```

```
1 1
```

```
1 1
```

```
>> s = im2double(h) %fails
```

```
s =
```

```
1 2
```

```
3 4
```

```
>> s = mat2gray(h) %agreed
```

```
s =
```

```
0 0.3333
```

```
0.6667 1.0000
```

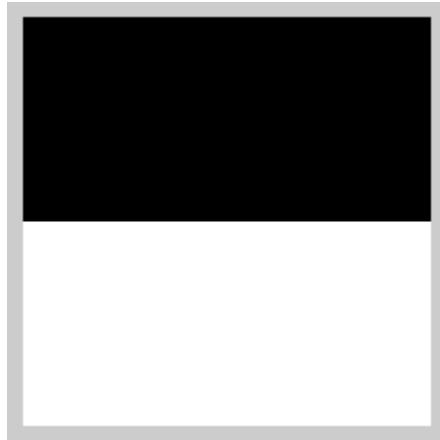
```
>> g = im2bw(s,0.4)
```

```
g =
```

```
0 0
```

```
1 1
```

```
>> imshow(g,'InitialMagnification',2000)
```



Experiment#3: To get familiar with matrix manipulation commands. To use matrix manipulation commands for rotating and compressing images.

- 1. Experiment Text**
 - i. **Array Indexing**
 - Vector Indexing**
 - Matrix Indexing**
- 2. Lab Exercise**
- 3. Exercise Questions**

EXPERIMENT TEXT

1 Array Indexing

1.1 Vector Indexing

An array of dimension 1xN is called a row vector. The elements of such a vector can be accessed using a single index value (also called a subscript). Thus, v(1) is the first element of vector v, v(2) is its second element, and so forth. Vectors can be formed in MATLAB by enclosing the elements, separated by spaces or commas, within square brackets. For example,

```
>> v = [1 3 5 7 9]
```

will generate a vector V and V(2) gives the second element of vector V. A row vector is converted to a column vector (and vice versa) using the transpose operator ('). e.g. the following command will store transpose of V in W.

```
>> w = v'
```

```
>> v=[1 3 5 7 9]
```

```
v =
```

```
1 3 5 7 9
```

```
>> v(1)
```

```
ans =
```

```
1  
>> v(5)
```

```
ans =
```

```
9
```

```
>> w=v'
```

```
w =
```

```
1  
3  
5  
7  
9
```

To access blocks of elements, we use MATLAB's colon notation. For example, to access the second through four elements of v we write v(2:4). To access all the elements from third to last we write v(3:END).

```
>> v(2:4)
```

```
ans =
```

```
3 5 7  
>> v(2:end)
```

```
ans =
```

```
3 5 7 9  
>> v([1 4 5])
```

```
ans =
```

```
1 7 9
```

```
>> v([1 4 9]) % Error
```

```
Index exceeds matrix dimensions.
```

1.2 Indexing Matrices

Matrices can be represented conveniently in MATLAB as a sequence of row vectors enclosed by square brackets and separated by semicolons. For example

```
>> A = [1 2 3; 4 5 6; 7 8 9]
```

Will create matrix A

```
>> a=[1 2 3;4 5 6;7 8 9]
```

```
a =
```

```
1 2 3  
4 5 6  
7 8 9
```

To extract the element in the second row, third column of matrix A, we write A(2,3).

```
>> a=[1 2 3;4 5 6;7 8 9]
```

a =

1	2	3
4	5	6
7	8	9

```
>> a(2,3)
```

ans =

6

A submatrix of A can be extracted by specifying a vector of values for both the row and the column indices. For example, the following statement extracts the submatrix of A containing rows 1 and 2 and columns 1, 2, and 3:

```
>> T2 = A([1 2], [1 2 3])
```

```
>> T1=a([1 2],[1 2 3])
```

T1 =

1	2	3
4	5	6

The preceding statement could be written also as T2 = A(1:2, 1:3).

```
>> T2=a (1:2,1:3)
```

T2 =

1	2	3
4	5	6

A colon in the row index position is shorthand notation for selecting all rows. e.g. the following command will select third column and all rows.

```
>> T2 = A (:,3)
```

```
>> T2=a (:,3)
```

T2 =

```
3  
6  
9
```

Similarly this statement will extract the second row.

```
>> T2 = A (2,:)
```

```
>> T3=a(2,:)
```

```
T3 =
```

```
4 5 6
```

The keyword END, when it appears in the row index position, is shorthand notation for the last row. When END appears in the column index position, it indicates the last column. For example, the following statement finds the element in the last row and last column of A:

```
>> T2 = A (END,END)  
>> t=a (end,end)
```

```
t =
```

```
9
```

and the following statement gives the last row as first row and first row as second row.

```
>> T2 = A([END 1],:)
```

```
>> T2=a([end 1],:)
```

```
T2 =
```

```
7 8 9  
1 2 3
```

```
>> T4=a(end,:)
```

```
T4 =
```

```
7 8 9  
>> T5=a(:,end)
```

```
T5 =
```

```
3  
6
```

9
>> T6=a([end 1],:)

T6 =

7 8 9
1 2 3

>> T6=a([end 1],:)

T6 =

7 8 9
1 2 3

>> T8=a([end 1],1)

T8 =

7
1

>> T9=a(:,[1 end])

T9 =

1 3
4 6
7 9

>> T9=a(:,[2 end])

T9 =

2 3
5 6
8 9

>> T10=a(:,[end 2])

T10 =

3 2
6 5
9 8

>> a

a =

1 2 3
4 5 6
7 8 9

```
>> rot90(a)
```

```
ans =
```

3	6	9
2	5	8
1	4	7

```
>> rot90(a,2)
```

```
ans =
```

9	8	7
6	5	4
3	2	1

```
>> rot90(a,4)
```

```
ans =
```

1	2	3
4	5	6
7	8	9

An image can be cropped by selecting only a few rows and columns. e.g. the following command $S = F(50:200,50:200)$ can crop the cameraman.tif image. How should we select the row and column number for cropping? (Hint: See the total number of rows and columns of the image).

```
>> I=imread('cameraman.tif');
```

```
c =
```

```
174 172 176 175 177 180 178 179 180 178 179 176 175 179 174 176 176 178
```

```
.
```

```
.
```

```
.
```

```
139 139 149 142 135 125 128
```

```
>> I=imread('cameraman.tif');
J=imcrop(I,[44.5 35.5 167 159]);
imshow(J)
```



```
c=I(50:200,50:200)
```

```
imshow(c)
```



```
>> a
```

```
a =
```

```
1 2 3  
4 5 6  
7 8 9
```

```
>> B=flipud(a)
```

```
B =
```

```
7 8 9  
4 5 6  
1 2 3
```

```
>> a
```

```
a =
```

```
1 2 3  
4 5 6  
7 8 9
```

```
>> C=flipdim(a,1)
```

```
C =
```

```
7 8 9  
4 5 6  
1 2 3
```

```
>> a
```

```
a =
```

```
1 2 3
```

```

4   5   6
7   8   9
>> D=flipdim(a,2)
D =
3   2   1
6   5   4
9   8   7

```

An image can be compressed by skipping some of the rows and columns in the original image (It will degrade the original image though). The following command makes the size of an image 1/4 by skipping every second row and column.

```

>> fs = f(1:2:END, 1:2:END);
>> f=imread('cameraman.tif');
comp=f(1:2:end,1:2:end);
subplot(1,2,1)
imshow(f)
xlabel('Original')
subplot(1,2,2)
imshow(comp)
xlabel('Compressed By f(1:2:end,1:2:end) ')

```



```

>> f=imread('cameraman.tif');
comp=f(1:5:end,1:5:end);

```

```
subplot(1,2,1)  
imshow(f)  
xlabel('Original')  
subplot(1,2,2)  
imshow(comp)  
xlabel('Compressed By f(1:5:end,1:5:end) ')
```



LAB EXERCISE

CROPPING

```
>> I=imread('cameraman.tif');  
J=imcrop(I,[44.5 35.5 167 159]);  
imshow(J)
```



```
c=I(50:200,50:200)  
imshow(c)
```



QUESTIONS:

Q1: What do the command `v(1:2:END)` and `v(END:-2:1)` do? Now use these commands to create a vector W which have same elements as V but in reverse order.

```
>> v=[1 3 5 7 9]
```

```
v =
```

```
1 3 5 7 9
```

```
>> v (1:1:end)
```

```
ans =
```

```
1 3 5 7 9
```

```
>> v (1:2:end)
```

```
ans =
```

```
1 5 9
```

```
>> v (1:3:end)
```

```
ans =
```

```
1 7
```

```
>> v (1:4:end)
```

```
ans =
```

```
1 9
```

```
>> v (1:5:end)
```

```
ans =
```

```
1
```

```
>> v (1:6:end)
```

```
ans =
```

```
1
```

```
>> v(1:-1:end)
```

```
ans =  
Empty matrix: 1-by-0
```

```
>> v(1:-4:end)
```

```
ans =  
Empty matrix: 1-by-0
```

```
>> v(end:1:1)
```

```
ans =  
Empty matrix: 1-by-0
```

```
>> v(end:-1:1)
```

```
ans =  
9 7 5 3 1
```

```
>> v(end:-2:1)
```

```
ans =  
9 5 1
```

```
>> v(end:-3:1)
```

```
ans =  
9 3
```

```
>> v(end:-4:1)
```

```
ans =  
9 1
```

```
>> v(end:-5:1)
```

```
ans =  
9
```

b)

```
>> w=v(end:-1:1)
```

```
w =
```

```
9 7 5 3 1
```

Q2 : Create a 5x5 matrix A with any elements. Now make another matrix B from A such that the first and last rows of A and B are exchanged, similarly the second and second last rows are also exchanged. (Hint use END to access last row and then move backwards).

```
>> v=sort(magic(5))
```

```
v =
```

```
4 5 1 2 3
```

```
10   6   7   8   9  
11   12  13  14  15  
17   18  19  20  16  
23   24  25  21  22
```

```
>> w=v([end:-1:1],:)
```

```
w =  
23   24  25  21  22  
17   18  19  20  16  
11   12  13  14  15  
10   6   7   8   9  
4    5   1   2   3
```

```
v =  
4    5   1   2   3  
10   6   7   8   9  
11   12  13  14  15  
17   18  19  20  16  
23   24  25  21  22
```

```
>> w1=v(:,[end :-1:1])
```

```
w1 =  
3    2   1   5   4  
9    8   7   6   10  
15   14  13  12  11  
16   20  19  18  17  
22   21  25  24  23
```

```
>> flipud(v) %flip up to down
```

```
ans =
```

```
23   24  25  21  22
```

```
17 18 19 20 16  
11 12 13 14 15  
10  6   7   8   9  
 4   5   1   2   3
```

```
>> fliplr(v) %flip right left
```

```
ans =
```

```
 3   2   1   5   4  
 9   8   7   6   10  
15  14  13  12  11  
16  20  19  18  17  
22  21  25  24  23
```

```
>> flipdim(v,1)
```

```
ans =
```

```
 23  24  25  21  22  
 17  18  19  20  16  
 11  12  13  14  15  
 10  6   7   8   9  
  4   5   1   2   3
```

```
>> flipdim(v,2)
```

```
ans =
```

```
 3   2   1   5   4  
 9   8   7   6   10  
15  14  13  12  11  
16  20  19  18  17  
22  21  25  24  23
```

Q3 : Read the cameraman.tif image from MATLAB (this image is in the form of a matrix) and use the same procedure used in **Q2** to exchange the rows. Now show both images (original and exchanged on the same graph. What does the exchanged image show?

```
>> a=imread('cameraman.tif');  
b=a([end:-1:1],:);  
c=a(:,[end:-1:1]);  
subplot(1,3,1)
```

```

imshow(a)
xlabel('original')
subplot(1,3,2)
imshow(b)
xlabel('Exchanged Row wise')
subplot(1,3,3)
imshow(c)
xlabel('Exchanged Column wise')

```



Q4 : Use subplot to show four images on a figure. The first image should be the actual cameraman.tif image. The second image should be the 90 degree clockwise (CW) rotation of first one. The third image should be the 90 degree CW rotation of second one and the last image should be 90 degree CW rotation of third image.

```
>> y=imread('cameraman.tif');
```

```
title('Using Matrix Indexing')
```

```
subplot(2,2,1)
```

```
imshow(y)
```

```
xlabel('original')
```

```
rot=y(end:-1:1,:);
```

```
rot1=rot';
```

```
subplot(2,2,2)
```

```
imshow(rot1);
```

```
xlabel('1st Rotate')
```

```
rot=rot1(end:-1:1,:);
```

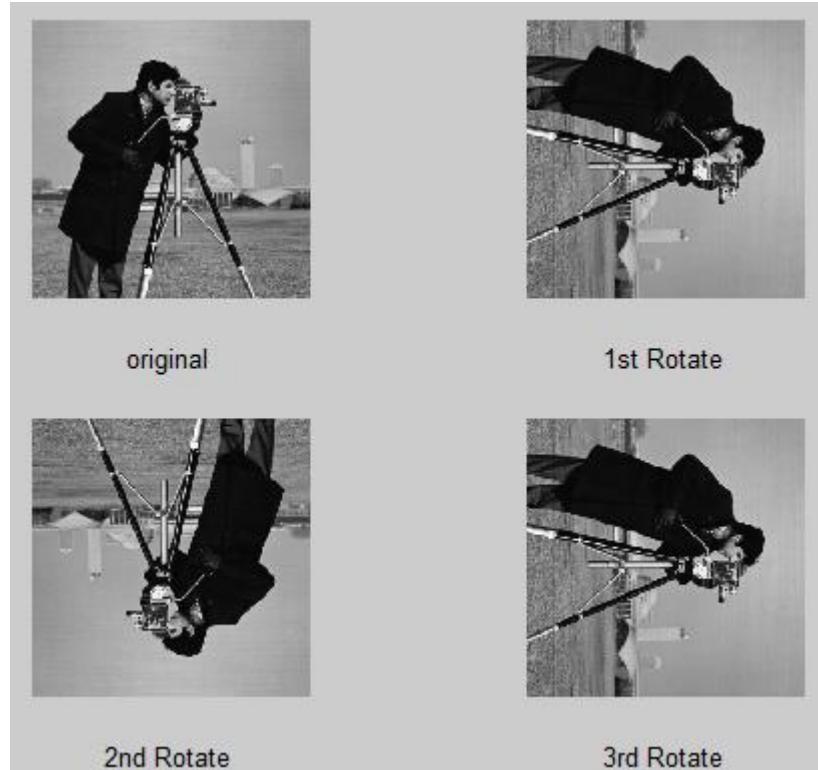
```
rot2=rot';
```

```
subplot(2,2,3)
```

```

imshow(rot2);
xlabel('2nd Rotate')
rot=rot2(end:-1:1,:);
rot3=rot';
subplot(2,2,4)
imshow(rot1);
xlabel('3rd Rotate')

```



Using rot90 function

```

clc
a=rot90(y,-1);
b=rot90(y,-2);
c=rot90(y,-3);
d=rot90(y,-4);
figure('name','rot90 function');
subplot(2,2,1);
imshow(a);
title('rot90 function');
xlabel('k=1');

```

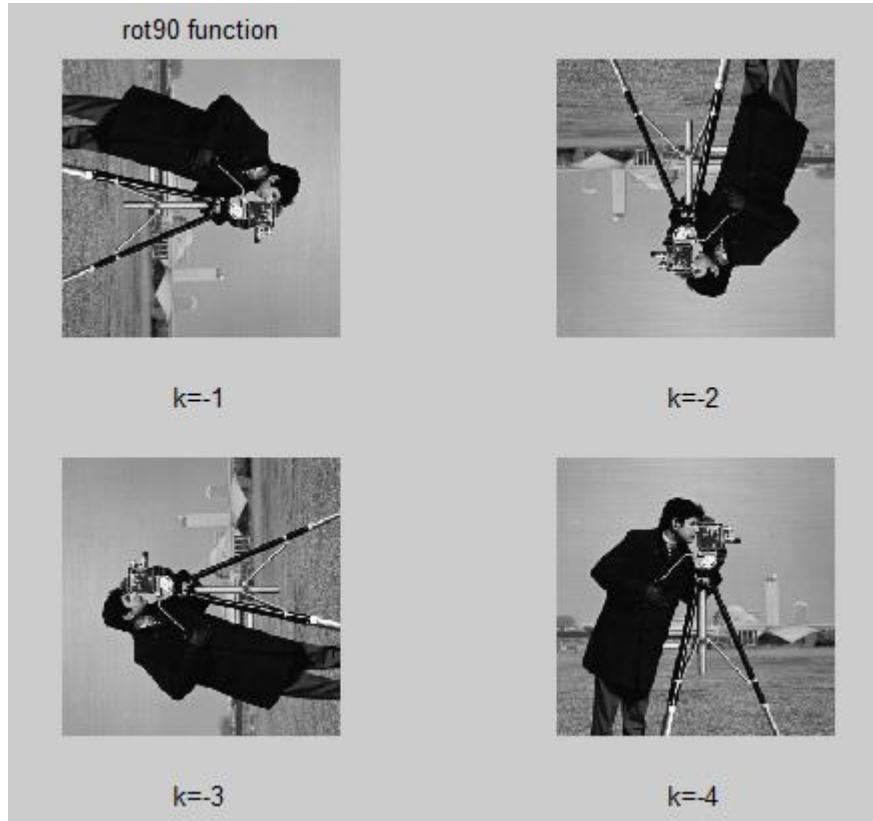
```

subplot(2,2,2);
imshow(b);
xlabel('k=2');

subplot(2,2,3);
imshow(c);
xlabel('k=3');

subplot(2,2,4);
imshow(d);
xlabel('k=4');

```



Q5: Compare the size of F_S with F . Plot both the images using subplot. Do you see much degradation? Now create two more images with increments of 5 and 10 instead of 2 and plot all four images (Original, with increment of 2, 5, 10) on same figure using subplot.

```

clc
y=imread('cameraman.tif');
title('Using Matrix Indexing')

```

```
subplot(2,2,1)
imshow(y);
xlabel('original')
ylabel('No Compression');
fs2=y(1:2:end,1:2:end);
subplot(2,2,2)
imshow(fs2)
x=sprintf(num2str(size(fs2)));
xlabel(x)
ylabel('y(1:2:end,1:2:end)');
fs5=y(1:5:end,1:5:end);
subplot(2,2,3)
imshow(fs5)
x=sprintf(num2str(size(fs5)));
xlabel(x)
ylabel('y(1:5:end,1:5:end)')
fs10=y(1:10:end,1:10:end);
subplot(2,2,4)
imshow(fs10)
x=sprintf(num2str(size(fs10)));
xlabel(x)
ylabel('y(1:10:end,1:10:end)')
```

No Compression



original

$y(1:5:\text{end},1:5:\text{end})$



52 52

$y(1:2:\text{end},1:2:\text{end})$



128 128

$y(1:10:\text{end},1:10:\text{end})$



26 26

Experiment#4: To get familiar with basic intensity transformation functions and to get familiar with M-file programming.

- 1. Experiment Text**
 - i. Intensity Transformation**
 - ii. M-Files**
- 2. Lab Exercise**
- 3. Exercise Questions**

1 Intensity Transformation

1.1 Background

The term spatial domain refers to the image plane and any spatial operation refers to directly manipulating the pixels of an image. There are two important categories of spatial domain processing, intensity transformation and spatial filtering. The spatial processes are denoted by the expression

$$g(x, y) = T[f(x, y)] \quad (1)$$

where $f(x, y)$ is the input image, $g(x, y)$ is the output image and T is an operator applied on f over a specific neighborhood defined around (x, y) . If the neighborhood is a matrix of size 1×1 then it is called intensity transformation otherwise spatial filtering.

1.2 Intensity Transformation

The intensity transformation can be denoted as

$$s = T(r) \quad (2)$$

where r is the intensity of the input image, s is the intensity of the output image and T is the operation performed on the input image.

1.2.1 Power Law transformation

Function `imadjust` is the basic tool for transforming grey scale images. It has the syntax

```
>> g = imadjust(f, [low-in high-in], [low-out high-out], gamma)
```

This function maps the intensity values of image f to new values in g such that the values in between `low-in` and `high-in` map to values `low-out` and `high-out`. Values below `low-in` map to `low-out` and those above `high-in` map to `high-out`. The value of `gamma` decides how would the intensities be mapped (Refer to class lectures

for more details about **gamma**).

The input image can be of class uint8, uint16 or double and the output image will have the same class as input. All the inputs to **imadjust** (except **f** and **gamma**) are specified between 0 and 1, regardless of class of **f**. If class of **f** is uint8, **imadjust** multiplies the supplied values with 255 to get the actual values to use. Using empty matrix ([]) for [low-in high-in] and low-out high-out will result in default values [0 1]. If **gamma** is omitted then it is gets default value of 1. The following command can be used to take negative of an image.

```
>> g = imadjust(f, [0 1] [1 0], 1)
```

Now read image blobs.png and take its negative using **imadjust** (Remember to change class of image before applying **imadjust**).

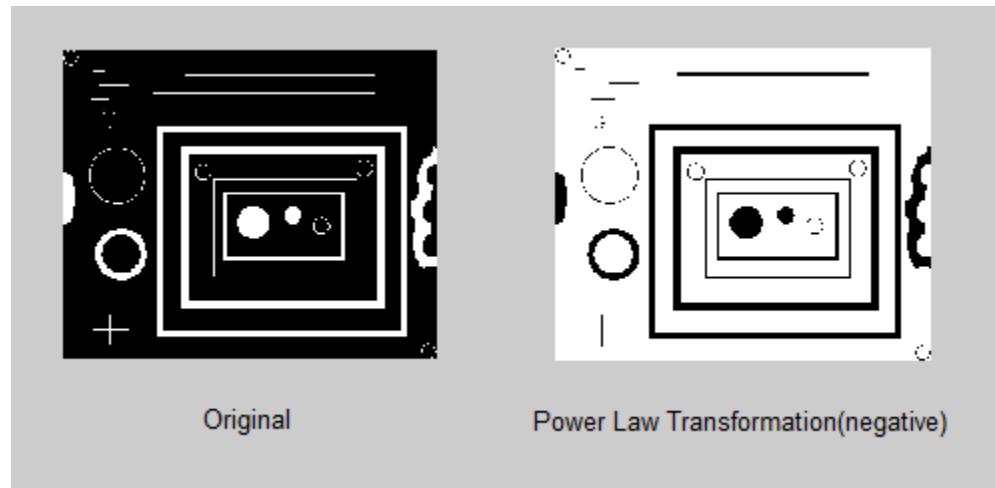
```
clc  
i=imread('blobs.png');  
whos i  
f=im2uint8(i);  
whos f  
powerlaw=imadjust(f,[0 1],[1 0],1);  
figure('Name','Power Law Transformation')  
subplot(1,2,1)  
imshow(f);  
xlabel('Original')  
subplot(1,2,2)  
imshow(powerlaw);  
xlabel('Power Law Transformation(negative)')
```

Name	Size	Bytes	Class	Attributes
------	------	-------	-------	------------

i	272x329	89488	logical	
---	---------	-------	---------	--

Name	Size	Bytes	Class	Attributes
------	------	-------	-------	------------

f	272x329	89488	uint8	
---	---------	-------	-------	--



Now read another image `spine.tif` and plot both image and its negative on same figure. Which image shows the object more clear? Why?

```

clc
i=imread('spine.tif');
whos i
g= imadjust(i, [0 1], [1 0] ,1);
h=imadjust(g, [0.5 1], [0 1] ,1);
subplot(1,3,1)
imshow(i)
xlabel('original')
subplot(1,3,2)
imshow(g)
xlabel('complement')
subplot(1,3,3)
imshow(h)
x=sprintf('imadjust(g,[0.5 1] [0 1],1)')
xlabel(x)

```

Name	Size	Bytes	Class	Attributes
------	------	-------	-------	------------

i	367x490	179830	uint8	
---	---------	--------	-------	--



The negative of an image can also be taken using the command

```
>> g = imcomplement(f)
```

Now take complement of `spine.tif` and save it in `g`. Now apply the command,

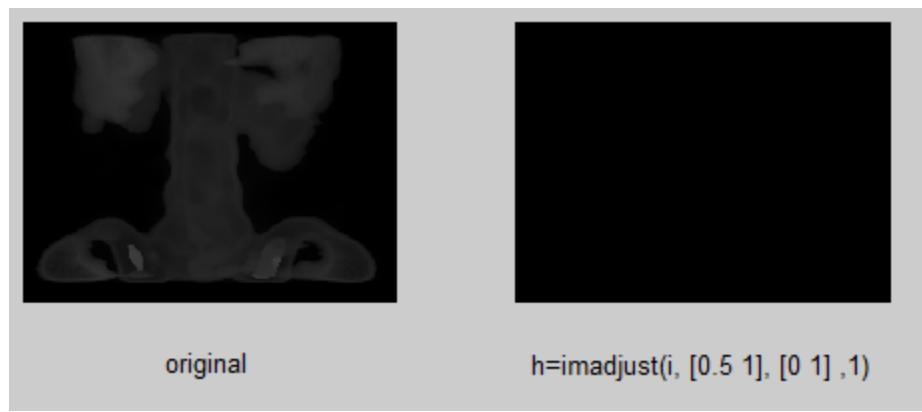
```
clc  
i=imread('spine.tif');  
g=imcomplement(i);  
h=imadjust(i, [0 1], [1 0] ,1);  
subplot(1,3,1)  
imshow(i)  
xlabel('original')  
subplot(1,3,2)  
imshow(g)  
xlabel('imcomplement(i)')  
subplot(1,3,3)  
imshow(h)  
x=sprintf('imadjust(g, [0 1], [1 0] ,1)')  
xlabel(x)
```



```

>> h = imadjust(g, [0.5 1] [0 1], 1)
clc
i=imread('spine.tif');
whos i
h=imadjust(i, [0.5 1], [0 1] ,1);
subplot(1,2,1)
imshow(i)
xlabel('original')
subplot(1,2,2)
imshow(h)
xlabel(' h=imadjust(i, [0.5 1], [0 1] ,1) ')

```



Can you see that your object has become more prominent now? This command expands the grey scale region between 0.5 and 1 to 0 and 1. Now what if you change the positions of scaling, e.g. if you execute the command,

```
>> h = imadjust(g, [0 1] [0.5 1], 1)
```

What do you see now? Is the new image washed out? Why?

```
clc  
i=imread('spine.tif');  
whos i  
h=imadjust(i, [0 1], [0.5 1] ,1);  
subplot(1,2,1)  
imshow(i)  
xlabel('original')  
subplot(1,2,2)  
imshow(h)  
 xlabel(' h=imadjust(i, [0 1], [0.5 1] ,1) ')
```



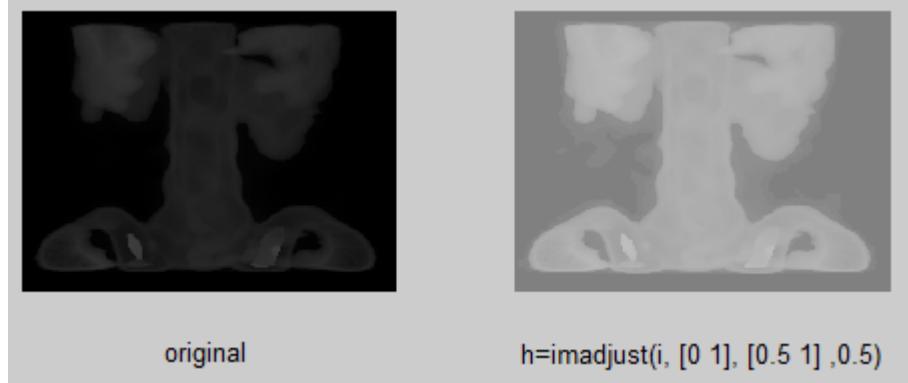
The image can be also be made more brighter or darker by changing the value of `gamma`. A value of `gamma` greater than one compresses the lower end of intensities (makes the image more darker) while a value less than one makes the stretches the lower end of intensities (makes the image more brighter).

```
clc  
i=imread('spine.tif');  
whos i  
h=imadjust(i, [0 1], [0.5 1] ,0.5);
```

```

subplot(1,2,1)
imshow(i)
xlabel('original')
subplot(1,2,2)
imshow(h)
xlabel(' h=imadjust(i, [0 1], [0.5 1] ,0.5 ) ')

```



```

clc
i=imread('spine.tif');
whos i

h1=imadjust(i, [0 1], [0.5 1] ,0.5);
h2=imadjust(i, [0 1], [0.5 1] ,0.9);
h3=imadjust(i, [0 1], [0.5 1] ,1.5);
h4=imadjust(i, [0 1], [0.5 1] ,1.9);

imshow(i)
xlabel('original')
figure
subplot(2,2,1)
imshow(h1)
xlabel(' h1=imadjust(i, [0 1], [0.5 1] ,0.5 ) ')


```

```

subplot(2,2,2)
imshow(h2)

```

```
xlabel(' h2=imadjust(i, [0 1], [0.5 1] ,0.9 ) ')
```

```
subplot(2,2,3)
```

```
imshow(h3)
```

```
xlabel(' h3=imadjust(i, [0 1], [0.5 1] ,1.5 ) ')
```

```
subplot(2,2,4)
```

```
imshow(h4)
```

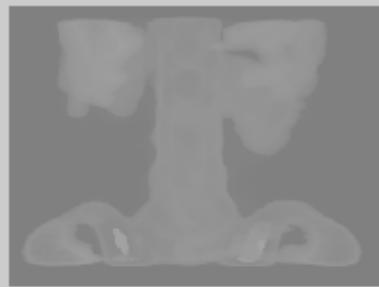
```
xlabel(' h4=imadjust(i, [0 1], [0.5 1] ,1.9 ) ')
```



original



h1=imadjust(i, [0 1], [0.5 1] ,0.5)



h2=imadjust(i, [0 1], [0.5 1] ,0.9)



h3=imadjust(i, [0 1], [0.5 1] ,1.5)



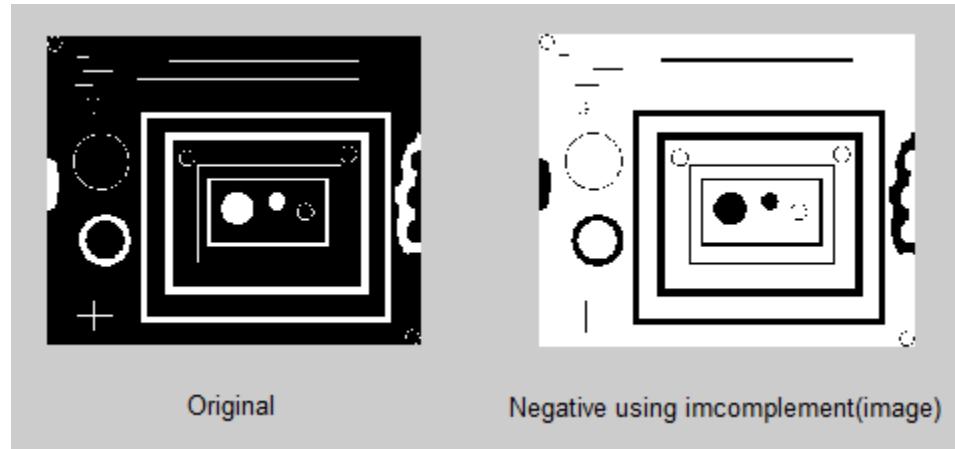
h4=imadjust(i, [0 1], [0.5 1] ,1.9)

clc

```

i=imread('blobs.png');
neg=imcomplement(i);
subplot(1,2,1)
imshow(i);
xlabel('Original')
subplot(1,2,2)
imshow(neg);
xlabel('Negative using imcomplement(image)')

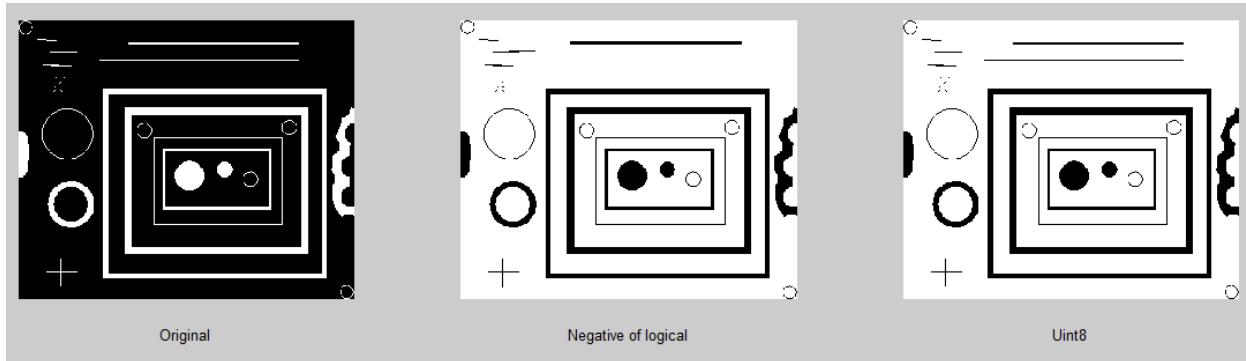
```



```

clc
i=imread('blobs.png');
f=im2uint8(i);
neg=imcomplement(i);
neg_con=imcomplement(f);
subplot(1,3,1)
imshow(i);
xlabel('Original')
subplot(1,3,2)
imshow(neg);
xlabel('Negative of logical')
subplot(1,3,3)
imshow(neg_con)
xlabel('Uint8')

```



1.2.2 Logarithmic Transformations

Logarithmic transformations are implemented using the expression

```
>> g = c * log (1 + double (f))
```

The shape of the logarithmic curve is similar to the `gamma < 1` curve, however, the shape of `gamma` curve is variable while the shape of logarithmic curve is fixed. While dealing with logarithmic transformation, it is always desirable to bring the resulting compressed values back to the original range. For 8 bits, the easiest way to do in MATLAB is to use this expression

```
>> gs = im2uint8(mat2gray(g))
```

Where `g` is the logarithmic image. The function `mat2gray` converts the image to range [0,1] while function `im2uint8` converts it to range [0,255].

```
clc
clear
i=imread('spine.tif');
g=imcomplement(i);
c=input('Enter C = ');
lg=c*log(1+double(i));
subplot(2,2,1)
imshow(i)
xlabel('original')
subplot(2,2,2)
imshow(g)
xlabel('Negative')
subplot(2,2,3)
imshow(lg)
```

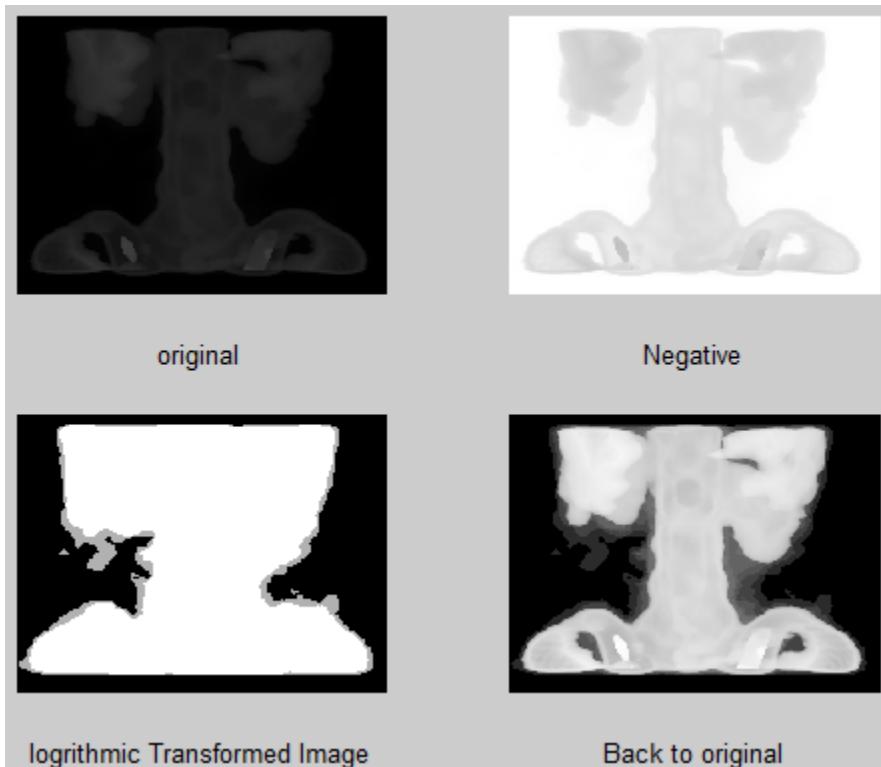
```

xlabel('logarithmic Transformed Image')
gs=im2uint8(mat2gray(lg));
subplot(2,2,4)
imshow(gs)
xlabel('Back to original')
whos

```

Enter C = 1

Name	Size	Bytes	Class	Attributes
c	1x1	8	double	
g	367x490	179830	uint8	
gs	367x490	179830	uint8	
i	367x490	179830	uint8	
lg	367x490	1438640	double	



2 M-Files

There are two types of M-files in MATLAB, script files and function files. Script files simply execute a series of MATLAB statements while function files can accept arguments and can produce one or more outputs. M-files can be

created by right clicking on current folder section and selecting 'new file' and then selecting function or script file.

As mentioned earlier script files will have a sequence of commands which can be execute by either typing the name of script file at command prompt or by using the 'Run' button at top of M-file.

Function files have a function definition line at the start of M -file which has the following syntax

Function [a, b] = function_name(c, d)

Where **c** and **d** are the inputs to the file while **a** & **b** are the output of the file. The function name and filename should always be same.

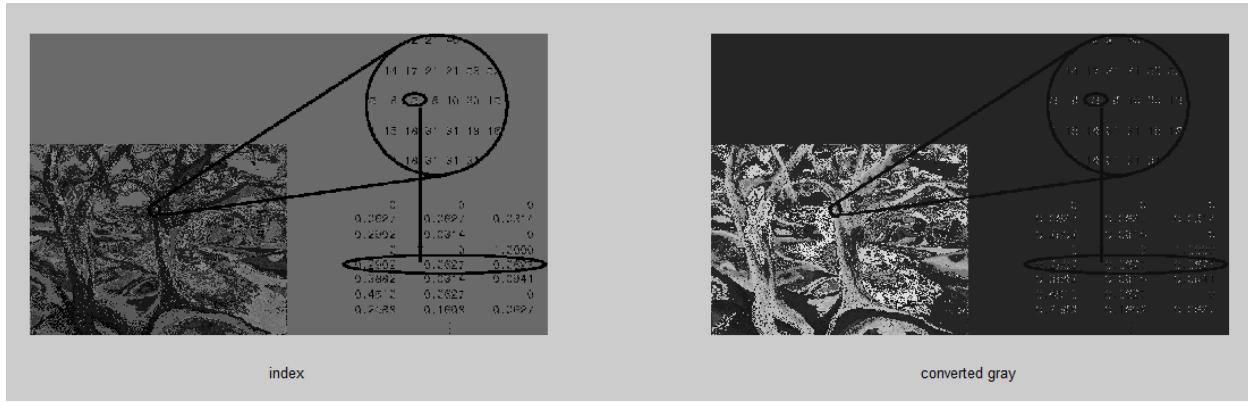
MATLAB EXERCISE

Color Conversion

Index to Gray

Y=ind2gray(x,map), ‘map’ is gray scale map

```
clc  
clear  
x=imread('chimage9.tif');  
imfinfo('chimage9.tif')  
y=ind2gray(x,colormap);  
imwrite(y,'chimage9y.tif')  
imfinfo('chimage9y.tif')  
subplot(1,2,1)  
imshow(x)  
xlabel('index')  
subplot(1,2,2)  
imshow(y);  
xlabel('converted gray')
```



Gray to Index

[y map]=gray2index(x,level)

```

clc
clear
x=imread('cameraman.tif');
imfinfo('cameraman.tif')
y=gray2ind(x,128);
imwrite(y,'cameramany.tif')
imfinfo('cameramany.tif')
subplot(1,2,1)
imshow(x)
xlabel('Gray')
subplot(1,2,2)
imshow(y);
xlabel('converted indexed')
```



RGB to grayscale

Y=rgb2gray(x)

```
clc  
clear  
x=imread('peppers.png');  
imfinfo('peppers.png')  
y=rgb2gray(x);  
imwrite(y,'peppersy.png')  
imfinfo('peppersy.png')  
subplot(1,2,1)  
imshow(x)  
xlabel('RGB')  
subplot(1,2,2)  
imshow(y);  
xlabel('converted Gray')
```



RGB to Index

```
[y map]=rgb2ind(x)
```

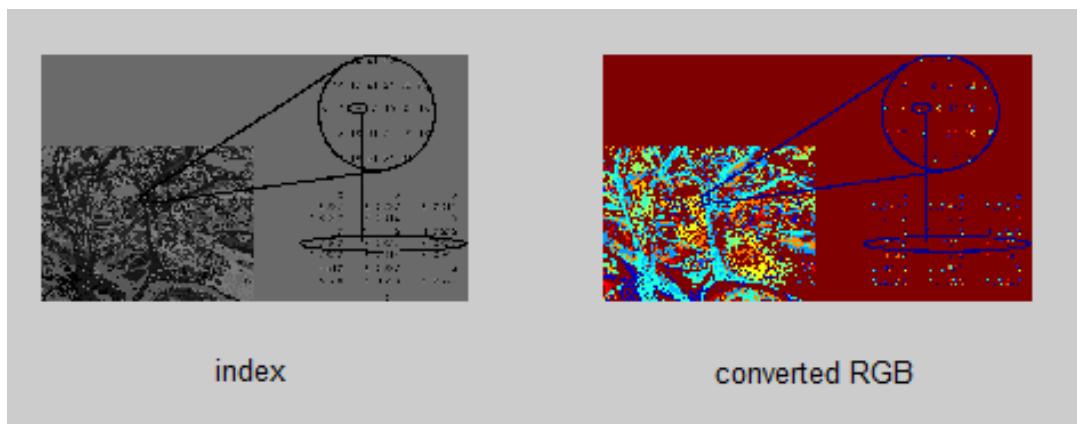
```
clc  
clear  
x=imread('peppers.png');  
imfinfo('peppers.png')  
[y,map]=rgb2ind(x,128);  
imwrite(y,'peppersy.png')  
imfinfo('peppersy.png')  
subplot(1,2,1)  
imshow(x)  
xlabel('RGB')  
subplot(1,2,2)  
imshow(y);  
xlabel('converted Index')
```



Index to RGB

Y=ind2rgb(x)

```
clc
clear
x=imread('chimage9.tif');
imfinfo('chimage9.tif')
y=ind2rgb(x,colormap);
imwrite(y,'chimage9y.tif')
imfinfo('chimage9y.tif')
subplot(1,2,1)
imshow(x)
xlabel('index')
subplot(1,2,2)
imshow(y);
xlabel('converted RGB')
```



Gray to BW

X=im2bw(x,map,level) , level is threshold value always b/w [0,1] regardless of class of input

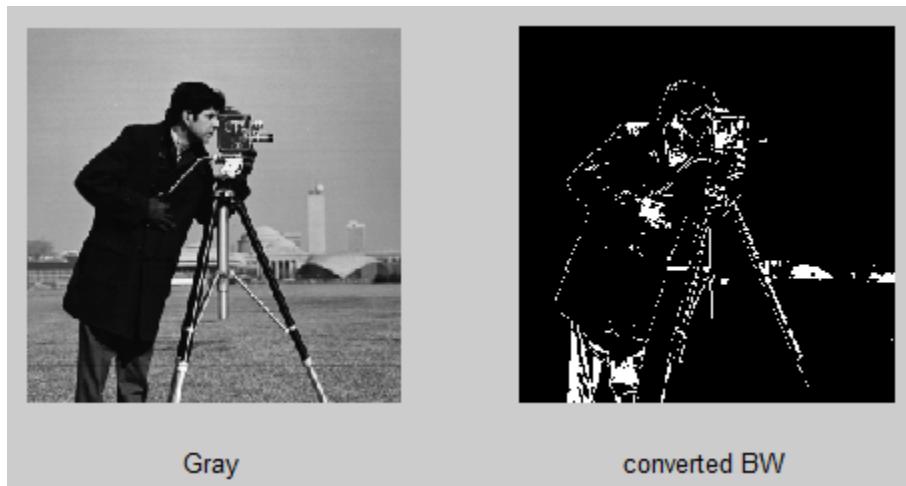
(0 – black 1—white) Even if class in uint16 in this case each threshold value is multiplied by 255 65535.

Threshold in different ways depends on the class of image, if it is 0.5 the pixel value lies in midway to black and white.

Uint8 → 0-255

Uint16 → 0-65535

```
clc  
clear  
x=imread('cameraman.tif');  
imfinfo('cameraman.tif')  
y=im2bw(x,colormap,0.5);  
imwrite(y,'cameramany.tif')  
imfinfo('cameramany.tif')  
subplot(1,2,1)  
imshow(x)  
xlabel('Gray')  
subplot(1,2,2)  
imshow(y);  
xlabel('converted BW')
```



Im2bw(f,t) , if f belongs to uint8 class and t=0.4 in this case im2bw threshold the pixel in f by comparing them to

$$255 \times 0.4 = 102$$

```

clc
clear
x=imread('cameraman.tif');
imfinfo('cameraman.tif')
y=im2bw(x,0.5);
imwrite(y,'cameramany.tif')
imfinfo('cameramany.tif')
subplot(1,2,1)
imshow(x)
xlabel('Gray')
subplot(1,2,2)
imshow(y);
xlabel('converted BW')

```

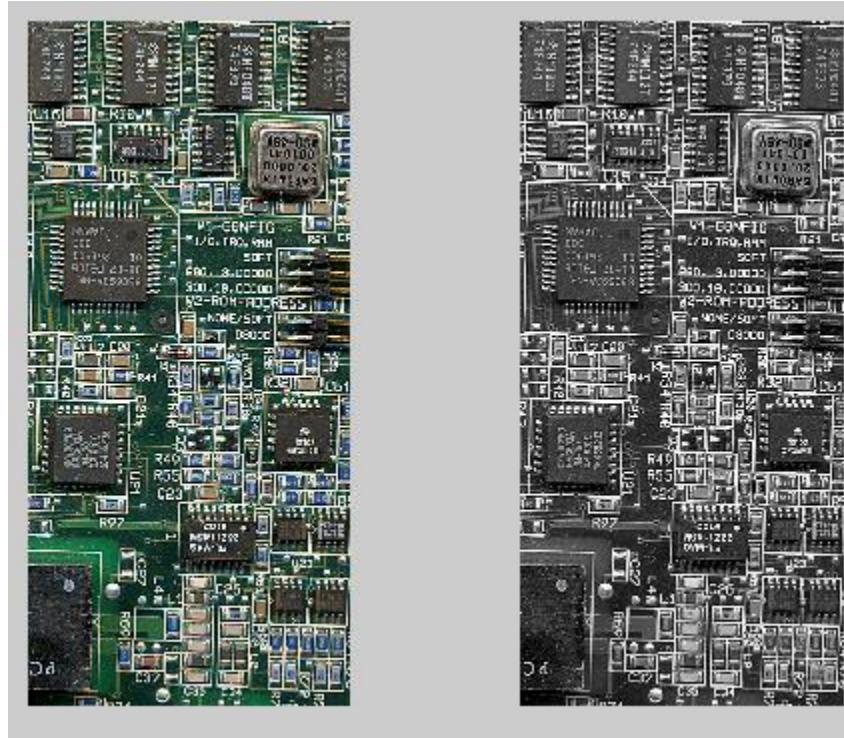


Example:

```

i=imread('board.tif');
j=rgb2gray(i);
subplot(1,2,1)
imshow(i)
subplot(1,2,2)
imshow(j)

```



Intensity Transformation

%without converting image type

EXERCISE QUESTIONS:

Q1 : Read image spine.tif, take its compliment and save in g. Now apply imadjust on this image with different values of gamma and show all the figures on the same plot. Also show the value of gamma on top of each figure.

(Hint: Use command title to show value of gamma on top of figure. You can use \gamma to show the symbol γ in MATLAB.).

```
clc
i=imread('spine.tif');
g=imcomplement(i);
subplot(2,3,1)
imshow(i)
title('original')
subplot(2,3,2)
imshow(g)
title('complement')
```

```

a=imadjust(g, [0 1], [0 1] ,0.5);
subplot(2,3,3)
imshow(a)
x=sprintf('gamma=0.5')
title(x)

b=imadjust(g, [0 1], [0 1] ,0.1);
subplot(2,3,4)
imshow(b)
title('gamma=0.1')

c=imadjust(g, [0 1], [0 1] ,1.5);
subplot(2,3,5)
imshow(c)
title('gamma=1.5')

d=imadjust(g, [0 1], [0 1] ,2.5);
subplot(2,3,6)
imshow(d)
title('gamma=2.5')

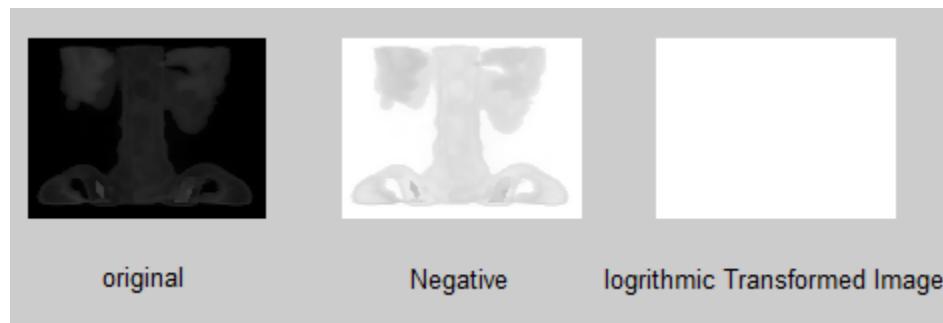
```



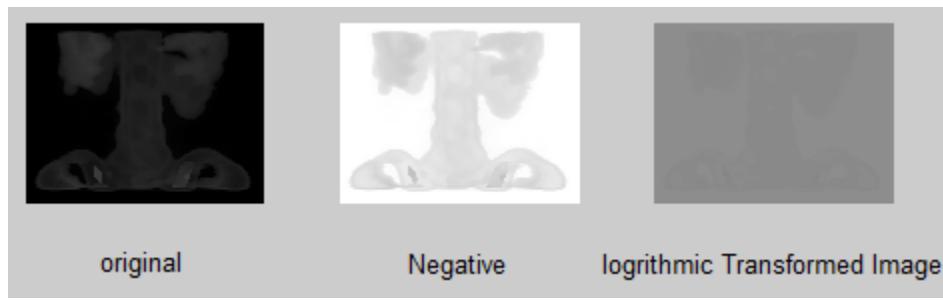
Q2 : Read image spine.tif, take its compliment and save in g. Now apply logarithmic transform on g and show both original and transformed image on same figure.

```
clc  
i=imread('spine.tif');  
g=imcomplement(i);  
c=input('Enter C = ')  
lg=c*log(1+double(g));  
subplot(1,3,1)  
imshow(i)  
xlabel('original')  
subplot(1,3,2)  
imshow(g)  
xlabel('Negative')  
subplot(1,3,3)  
imshow(lg)  
xlabel('logarithmic Transformed Image')
```

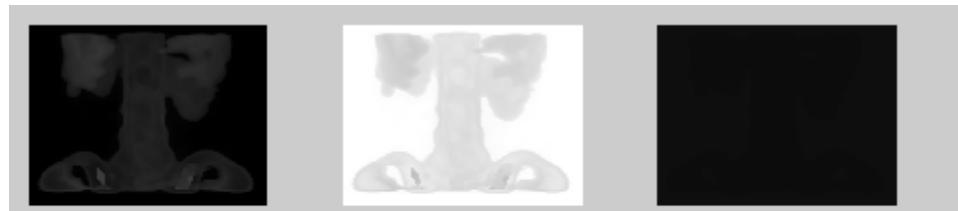
C=1



C=0.1



C=0.01

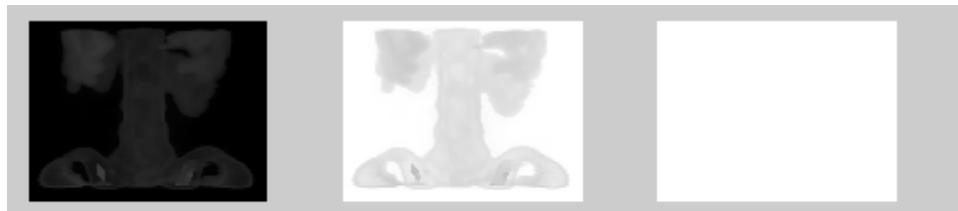


original

Negative

logarithmic Transformed Image

C=0.9



original

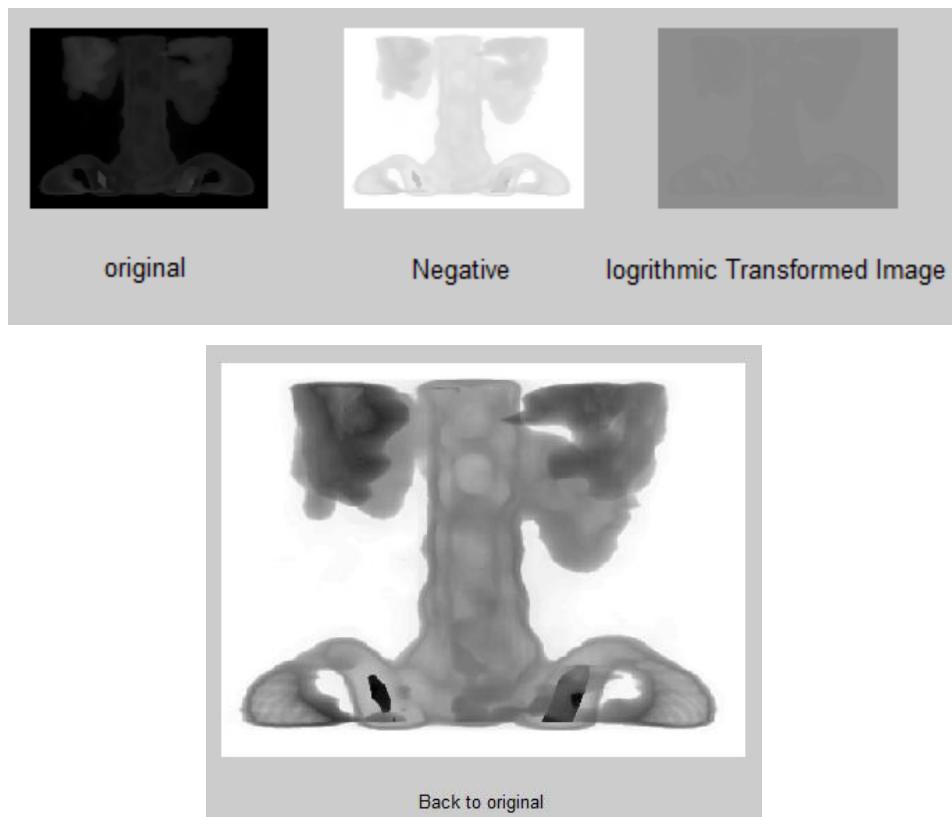
Negative

logarithmic Transformed Image

Returning to original Image

```
clc  
  
i=imread('spine.tif');  
g=imcomplement(i);  
c=input('Enter C = ')  
lg=c*log(1+double(g));  
subplot(1,3,1)  
imshow(i)  
xlabel('original')  
subplot(1,3,2)  
imshow(g)  
xlabel('Negative')  
subplot(1,3,3)  
imshow(lg)  
xlabel('logarithmic Transformed Image')  
gs=im2uint8(mat2gray(lg))  
  
figure  
imshow(gs)  
xlabel('Back to original')
```

C=0.1

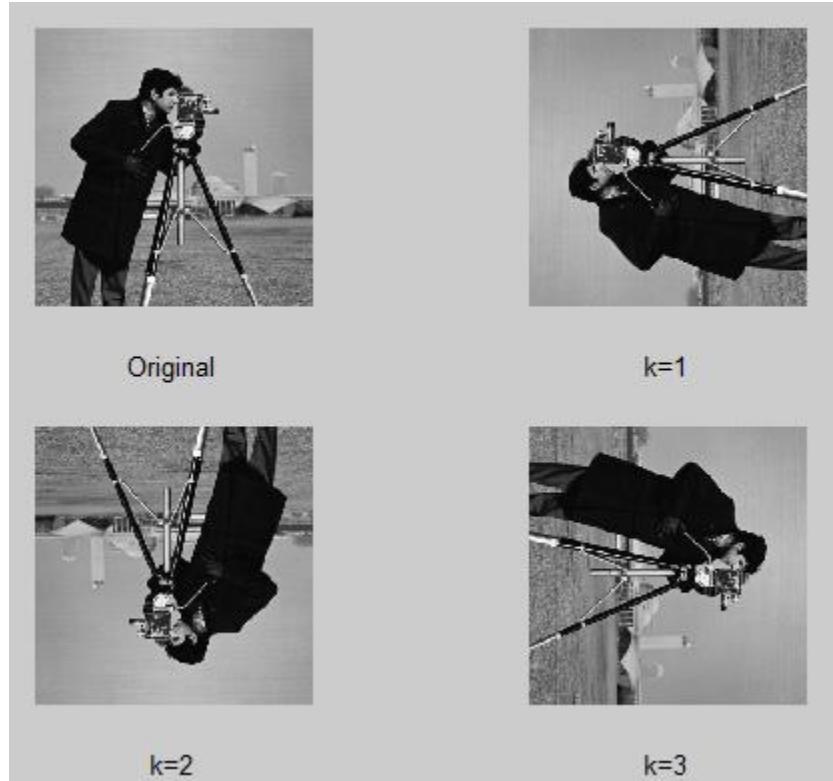


Q3: Create a Script M-file named 'Rotation.m'. Now write a code in this file which should ask the user to give name of an image file and should show four images on a single figure where the first image should be original image and other images should be 90 degree rotated compared to previous images (Hint: Use command 'input' to get input from user).

```
clc  
x=input('Enter Name of Image','s');  
i=imread (x)  
a=rot90 (i,1);  
b=rot90 (i,2);  
c=rot90 (i,3);  
figure('name','Rotation function Ouput');  
subplot(2,2,1);  
imshow(i);  
xlabel('Original');  
subplot(2,2,2);
```

```
imshow(a);
xlabel('k=1');
subplot(2,2,3);
imshow(b);
xlabel('k=2');
subplot(2,2,4);
imshow(c);
xlabel('k=3');
```

Enter Name of Image: cameraman.tif



Q4 : Now create another Script file 'gammatransform.m' which takes image from user as input and plots four images on one figure for different values of gamma. It should also write the value of gamma on top of each image.

```
clc
x=input('Enter Name of Image : ','s');
i=imread(x);
```

```
subplot(2,2,1)
imshow(i)
title('original')

a=imadjust(i, [0 1], [0 1] ,0.1);
subplot(2,2,2)
imshow(a)
x=sprintf('gamma=0.1')
title(x)

b=imadjust(i, [0 1], [0 1] ,0.9);
subplot(2,2,3)
imshow(b)
x=sprintf('gamma=0.9')
title(x)

c=imadjust(i, [0 1], [0 1] ,2.5);
subplot(2,2,4)
imshow(c)
title('gamma=2.5')
```

Enter Name of Image : cameraman.tif



Q5 : Create a Function M-file (give any name) which should accept image file as input argument and should convert the image into binary and logarithmic and return both images as output.

Function:

```
function [ bin logarithmic bin_logarithmic ] = Q5( image )
bin=im2bw(image,0.5);
logarithmic=1*log(1+double(image));
bin_logarithmic=1*log(1+double(bin));
end
```

```
i=imread('cameraman.tif');
[bin logarithmic bin_logarithmic]=Q5(i);
```

```
subplot(2,2,1)
imshow(i)
xlabel('Original')
subplot(2,2,2)
```

```

imshow(bin)
xlabel('Binary im2bw(image,0.5)')
subplot(2,2,3)
imshow(logarithmic)
xlabel('Log Transform c=1')
subplot(2,2,4)
imshow(bin_logarithmic)
xlabel('Log Transform of Binary Image')

```



Q6 : Create a Function m-file which accepts an image as input, compresses it 16 times, displays the original and compressed image on a single figure and also returns compressed image as output.

Function M File

```

function [ comp ] = Q6( image )
subplot(1,2,1)
imshow(image)
x=sprintf(num2str(size(image)));
 xlabel(x)

```

```
comp=image(1:16:end,1:16:end);
subplot(1,2,2)
imshow(comp)
x=sprintf(num2str(size(comp)));
xlabel(x)
end
>> i=imread('cameraman.tif');
>> [compressed]=Q6(i);
```



256 256



16 16

Experiment#5: To get familiar with histogram processing of images.

- 1. Experiment Text**
 - i. Histogram Processing**
- 2. Lab Exercise**
- 3. Exercise Questions**

EXPERIMENT TEXT

1 Histogram Processing

1.1 Background

The histogram of a digital image with L possible intensity levels is a discrete function written as

$$h(r_k) = n_k$$

Where r_k is the kth intensity level and n_k is the number of pixels in the image with intensity levels r_k . The value of L for uint8 image is 256, 65536 for uint16 image and 1 for a double image. If we divide all the elements of $h(r_k)$ with total number of pixels in an image we get a normalized histogram. i.e.

$$\begin{aligned} p(r_k) &= \frac{h(r_k)}{MN} \\ &= \frac{n_k}{MN} \end{aligned}$$

Where we recognize that $p(r_k)$ is the probability of occurrence of intensity level r_k .

1.2 Image Histogram

The core function that deals with image histograms in MATLAB is `imhist`, which has the following syntax.

$$h = \text{imhist}(f, b)$$

Where h is the histogram, f is the input image and b is the number of bins used in histogram. Using `imhist(f,b)` without h will plot the histogram of image f. The default value of b is 256. A bin is subdivision of intensity

scales e.g. if for `uint8` image you use $b = 2$, then the intensity scale is subdivided into two ranges; 0 to 127 and 128 to 255. The resulting histogram will have two values, $h(1)$ equal to number of pixels in the range [0,127] and $h(2)$ equal to the number of pixels in the range [128,255].

```
clc  
b=1;  
f=imread('cameraman.tif');  
h=imhist(f,b);  
subplot(2,2,1)  
imhist(f,b); %without h plotting the histogram otherwise save histogram into h and don't plot it  
b=2;  
f=imread('cameraman.tif');  
h=imhist(f,b)  
subplot(2,2,2)  
imhist(f,b);  
b=3;  
f=imread('cameraman.tif');  
h=imhist(f,b)  
subplot(2,2,3)  
imhist(f,b);  
b=4;  
f=imread('cameraman.tif');  
h=imhist(f,b)  
subplot(2,2,4)  
imhist(f,b);
```

Output

$h =$

26477

39059

$h =$

16032

48331

1173

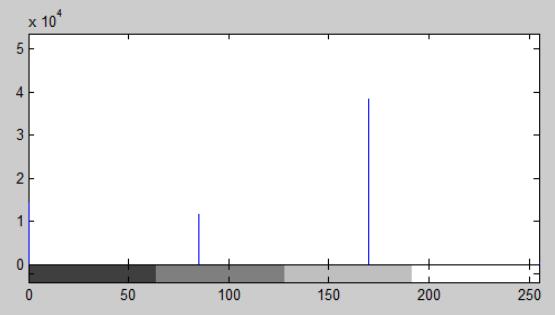
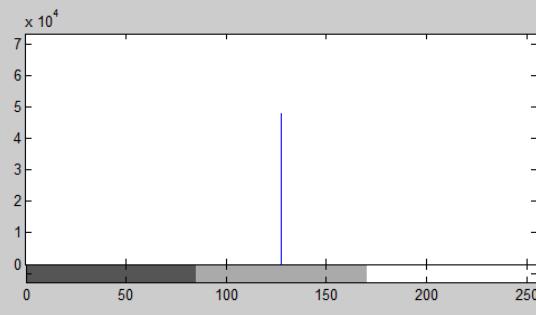
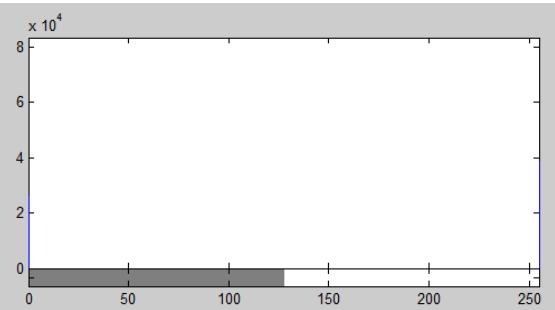
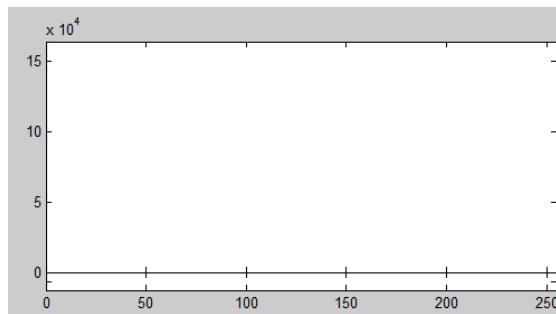
$h =$

14538

11939

38531

528



An image can be normalized by using the expression

$$h1 = imhist(f, b)/numel(f)$$

where `numel(f)` gives the number of elements in an image.

```
clc  
f=imread('cameraman.tif');  
numel(f)  
imhist(f)/numel(f)
```

ans =

65536

ans =

0
0
0
0
0
0
0

0.0001

0.0065

0.0225

.

.

.

.

.

.

0.0000

```
0
```

```
0
```

Histograms can also be plotted using some other commands e.g. histograms can be plotted using bar graphs. For this purpose we can use the function

```
bar(horz, v, width)
```

where v is a row vector with actual points that need to be plotted, horz contains the increments of the horizontal scale and width is a number between 0 and 1. If horz is omitted, horizontal axis is divided from 0 to length(v). When width is 1, the bars touch, when it is 0 then bars are just vertical lines. The default value of width is 0.8. The following commands show histogram using bar graph with increments of 10.

```
clc
```

```
f=imread('cameraman.tif');
```

```
f1= imhist(f);
```

```
h=f1(1:50)
```

```
subplot(2,3,1)
```

```
bar(h); % default value of width is 0.8
```

```
x=sprintf('bar(h) default value of width is 0.8');
```

```
xlabel(x)
```

```
pause
```

```
subplot(2,3,2)
```

```
bar(h,0)
```

```
x=sprintf('bar(h,0)');
```

```
xlabel(x)
```

```
pause
```

```
subplot(2,3,3)
```

```
bar(h,0.1)
```

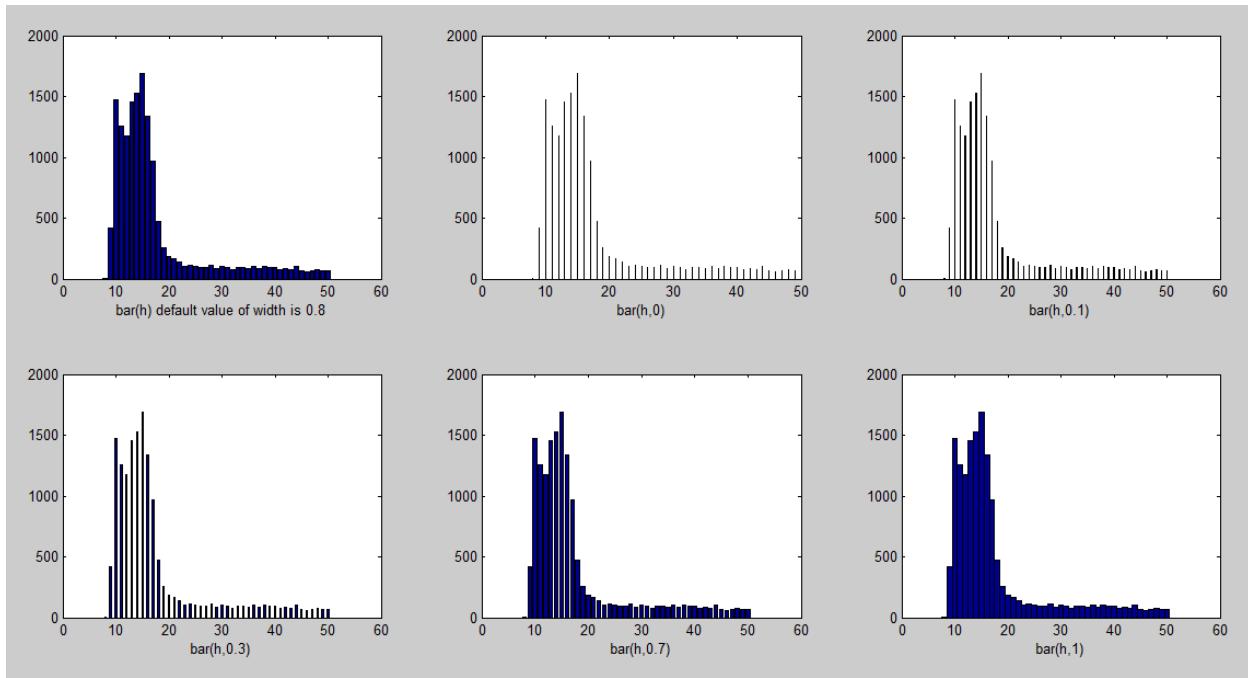
```
x=sprintf('bar(h,0.1)');
```

```
xlabel(x)

pause
subplot(2,3,4)
bar(h,0.3)
x=sprintf('bar(h,0.3)');
xlabel(x)
```

```
pause
subplot(2,3,5)
bar(h,0.7)
x=sprintf('bar(h,0.7)');
xlabel(x)
```

```
pause
subplot(2,3,6)
bar(h,1)
x=sprintf('bar(h,1)');
xlabel(x)
```

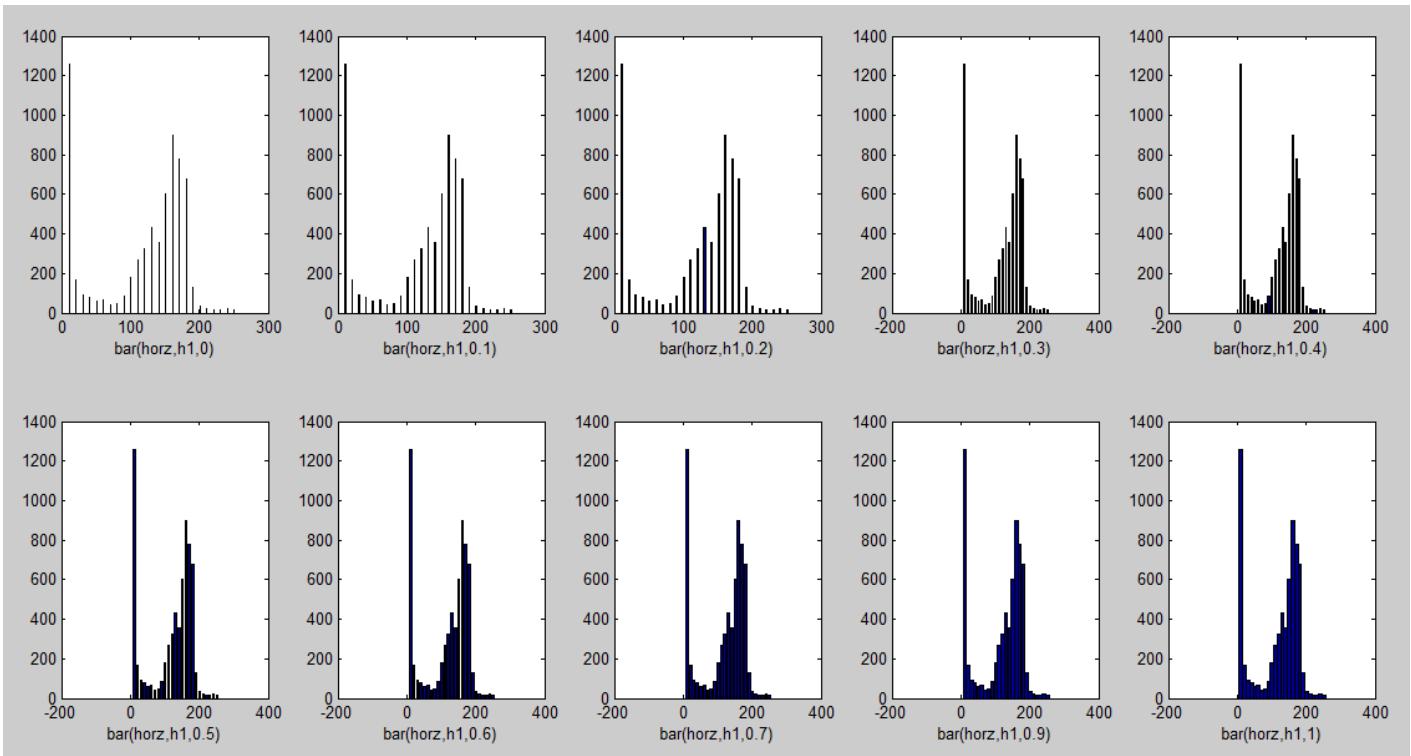


```

h = imhist(f)
h1 = h(1:10:256)
horz = 1:10:256
subplot(2,5,1)
bar(horz,h1,0)
x=sprintf('bar(horz,h1,0)')
xlabel(x)
subplot(2,5,2)
bar(horz,h1,0.1)
x=sprintf('bar(horz,h1,0.1)')
xlabel(x)
subplot(2,5,3)
bar(horz,h1,0.2)
x=sprintf('bar(horz,h1,0.2)')
xlabel(x)
subplot(2,5,4)
bar(horz,h1,0.3)
x=sprintf('bar(horz,h1,0.3)')

```

```
xlabel(x)
subplot(2,5,5)
bar(horz,h1,0.4)
x=sprintf('bar(horz,h1,0.4)')
xlabel(x)
subplot(2,5,6)
bar(horz,h1,0.5)
x=sprintf('bar(horz,h1,0.5)')
xlabel(x)
subplot(2,5,7)
bar(horz,h1,0.6)
x=sprintf('bar(horz,h1,0.6)')
xlabel(x)
subplot(2,5,8)
bar(horz,h1,0.7)
x=sprintf('bar(horz,h1,0.7)')
xlabel(x)
subplot(2,5,9)
bar(horz,h1,0.9)
x=sprintf('bar(horz,h1,0.9)')
xlabel(x)
subplot(2,5,10)
bar(horz,h1,1)
x=sprintf('bar(horz,h1,1)')
xlabel(x)
```



where the command `axis` is used to set the range of x and y axis. You can change values of horz and width to see what effect it would have on the image.

```

h = imhist(f)
h1 = h(1:10:256)
horz = 1:10:256
subplot(2,5,1)
bar(horz,h1,0)
axis ([ 0 300 0 1400]);
x=sprintf('bar(horz,h1,0)')
xlabel(x)
subplot(2,5,2)
bar(horz,h1,0.1)
axis ([ 0 300 0 1400]);
x=sprintf('bar(horz,h1,0.1)')
xlabel(x)
subplot(2,5,3)
bar(horz,h1,0.2)
axis ([ 0 300 0 1400]);

```

```
x=sprintf('bar(horz,h1,0.2)')

xlabel(x)

subplot(2,5,4)

bar(horz,h1,0.3)

axis ([ 0 300 0 1400]);

x=sprintf('bar(horz,h1,0.3)')

xlabel(x)

subplot(2,5,5)

bar(horz,h1,0.4)

axis ([ 0 300 0 1400]);

x=sprintf('bar(horz,h1,0.4)')

xlabel(x)

subplot(2,5,6)

bar(horz,h1,0.5)

axis ([ 0 300 0 1400]);

x=sprintf('bar(horz,h1,0.5)')

xlabel(x)

subplot(2,5,7)

bar(horz,h1,0.6)

axis ([ 0 300 0 1400]);

x=sprintf('bar(horz,h1,0.6)')

xlabel(x)

subplot(2,5,8)

bar(horz,h1,0.7)

axis ([ 0 300 0 1400]);

x=sprintf('bar(horz,h1,0.7)')

xlabel(x)

subplot(2,5,9)

bar(horz,h1,0.9)

axis ([ 0 300 0 1400]);

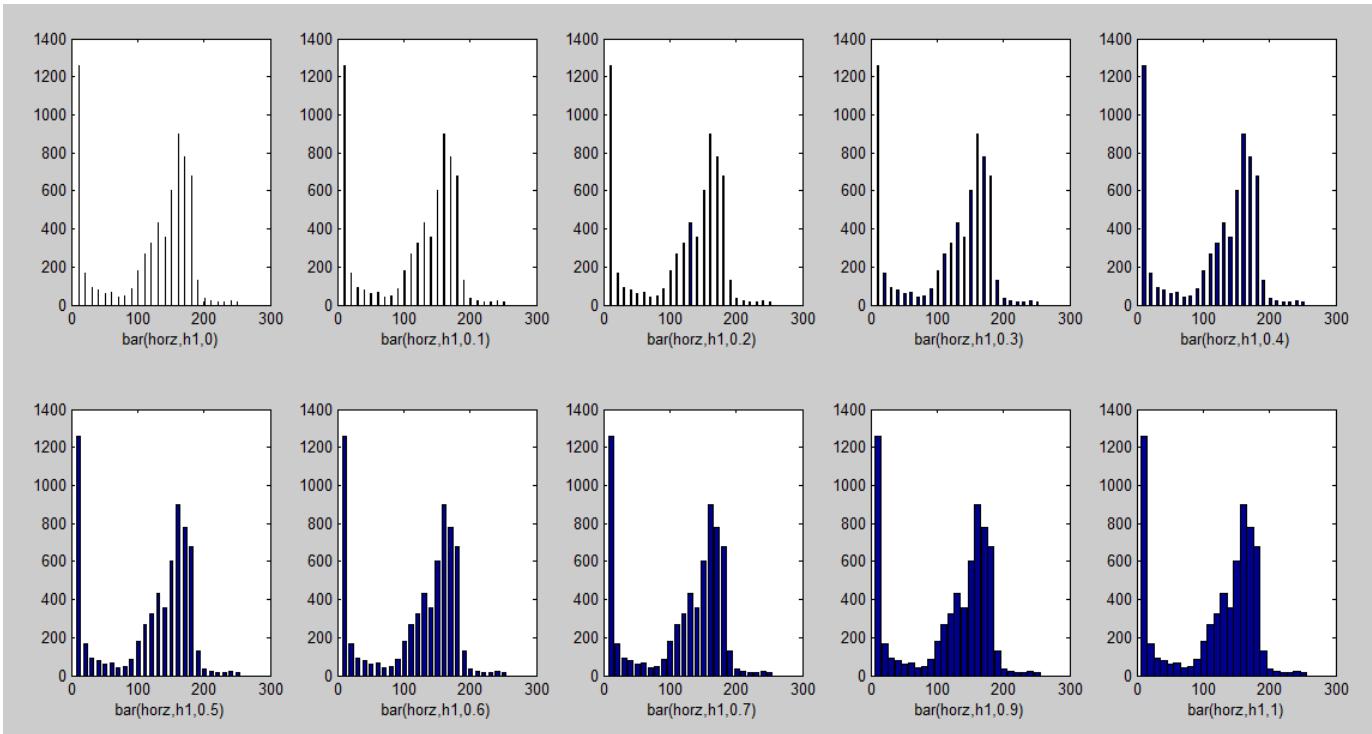
x=sprintf('bar(horz,h1,0.9)')

xlabel(x)
```

```

subplot(2,5,10)
bar(horz,h1,1)
axis ([ 0 300 0 1400]);
x=sprintf('bar(horz,h1,1)')
xlabel(x)

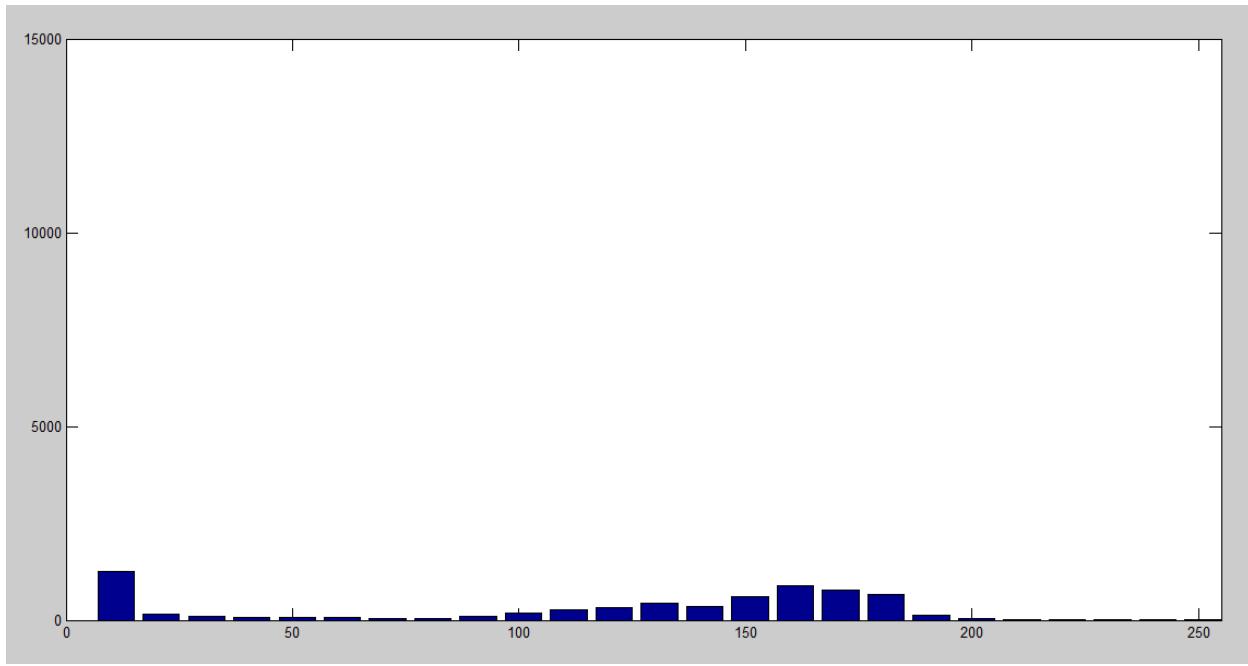
```



```

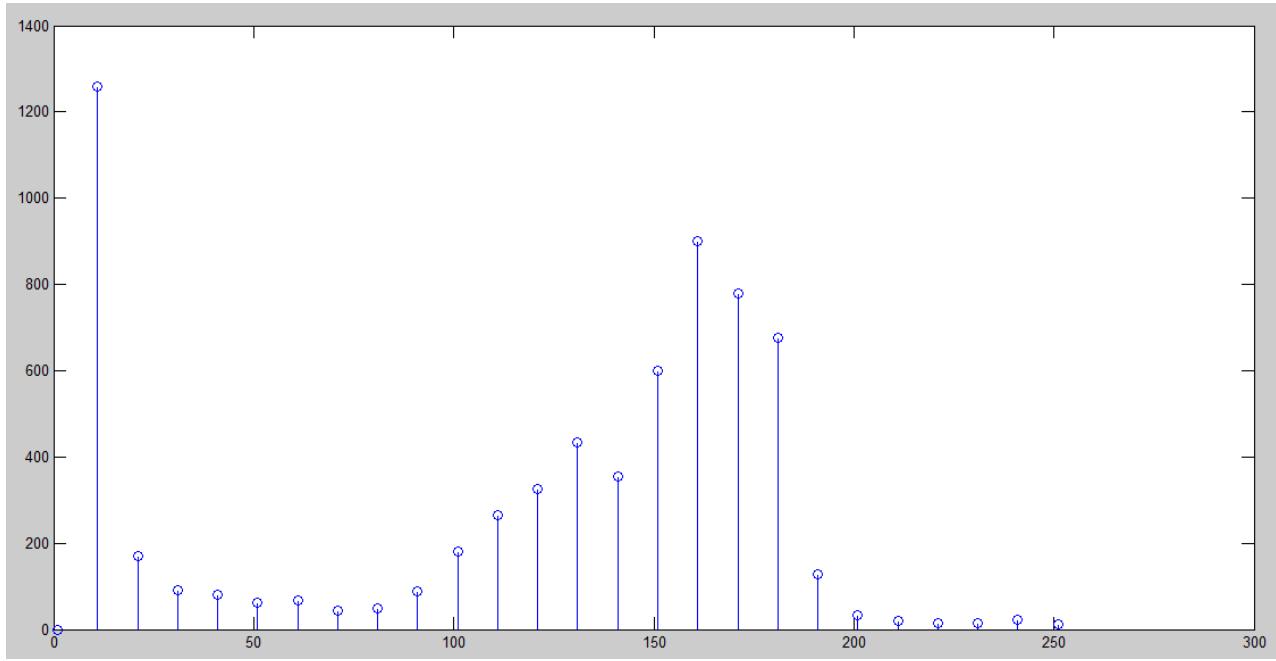
h = imhist(f)
h1 = h(1:10:256)
horz = 1:10:256
bar(horz,h1)
axis ([ 0 255 0 15000]);

```



Another way to show histogram is using **stem** function which has similar syntax as **bar** but does not have **width** parameter.

```
clc  
h = imhist(f)  
h1 = h(1:10:256)  
horz = 1:10:256  
stem(horz,h1)  
axis ([ 0 300 0 1400]);
```



1.3 Histogram Equalization

Histogram equalization is a process to increase the contrast of an image by changing the histogram of an image such that the histogram of new image covers a wide range of intensity levels. Suppose that we have an image with intensity levels between $[0, L-1]$ and let $p_r(r)$ be its probability density function. Suppose we perform the following transformation to obtain an output image

$$s = T(r) = \int_0^r p_r(w) dw$$

It can be shown (refer to lectures) that using this transformation function generates an image whose intensity levels are equally likely. The net result is an image with increased dynamic range, which will have a high contrast. For discrete quantities we deal with summations and the above transform can be written as

$$\begin{aligned}
 s_k &= T(r_k) \\
 &= \sum_{j=1}^k p_r(r_j) \\
 &= \sum_{j=1}^k n_j / MN
 \end{aligned} \tag{1}$$

where s_k is the intensity value in the output image corresponding to r_k intensity in the input image.

Histogram equalization is performed in MATLAB using the function **histeq** which has the syntax

```
>> g = histeq(f,nlev);
```

where f is the input image and nlev is the number of intensity level for the output image. For equation 1, the number of output intensity levels (nlev) should be equal to the input intensity levels. The default value of nlev is 64.

```
%g=histeq(f,nlev)
```

```
clc
```

```
f=imread('cameraman.tif');
```

```
i=f(100:110,100:110)
```

```
j=imhist(i);
```

```
bar(j)
```

```
xlabel('Input Image Histogram')
```

```
figure
```

```
j=histeq(i,2);
```

```
subplot(4,2,1)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,2)')
```

```
xlabel(l)
```

```
j=histeq(i,4);
```

```
subplot(4,2,2)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,4)')
```

```
xlabel(l)
```

```
j=histeq(i,8);
```

```
subplot(4,2,3)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,8)')
```

```
xlabel(l)
```

```
j=histeq(i,16);
```

```
subplot(4,2,4)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,16)')
```

```
xlabel(l)
```

```
j=histeq(i,32);
```

```
subplot(4,2,5)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,32)')
```

```
xlabel(l)
```

```
j=histeq(i,64);
```

```
subplot(4,2,6)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,64)')
```

```
xlabel(l)
```

```
j=histeq(i,128);
```

```
subplot(4,2,7)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,128)')
```

```
xlabel(l)
```

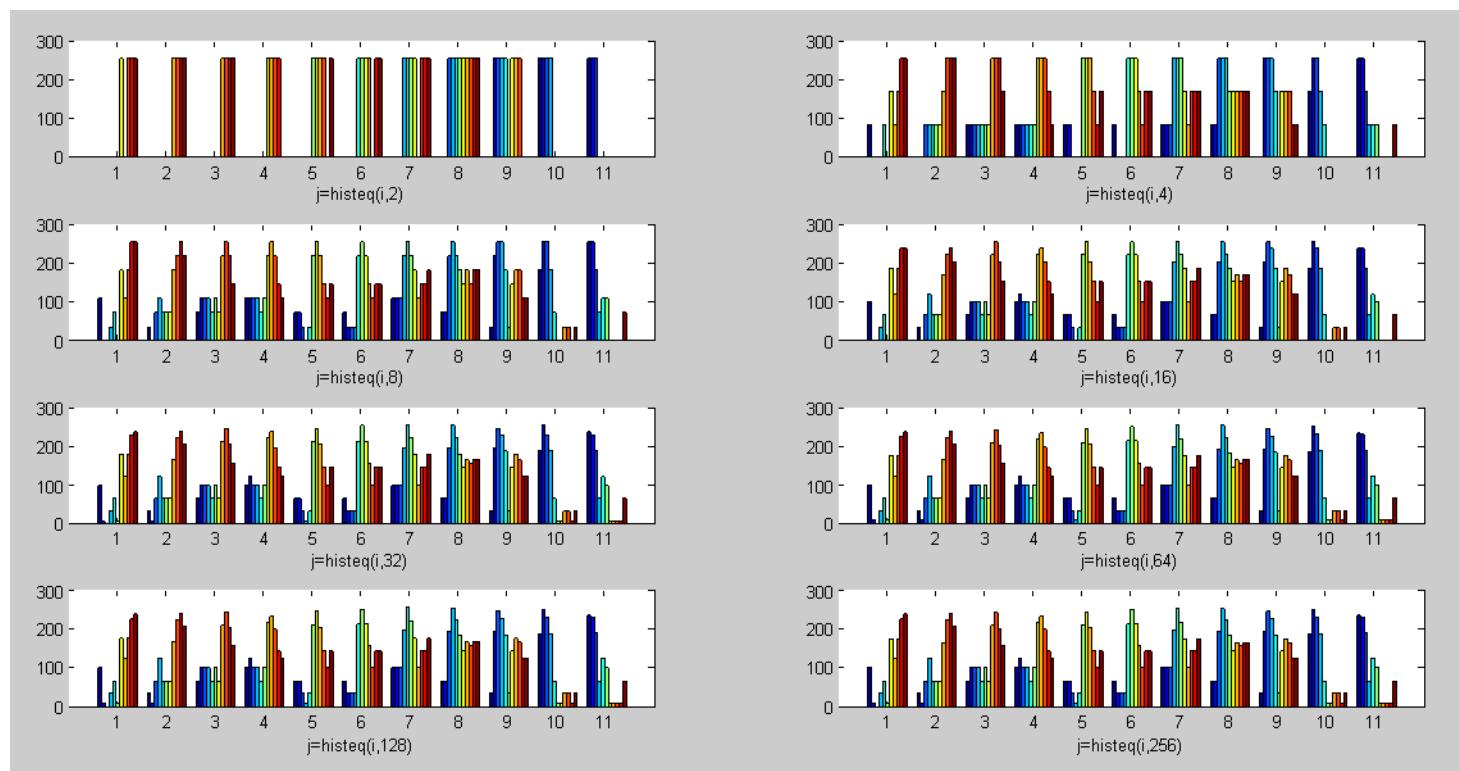
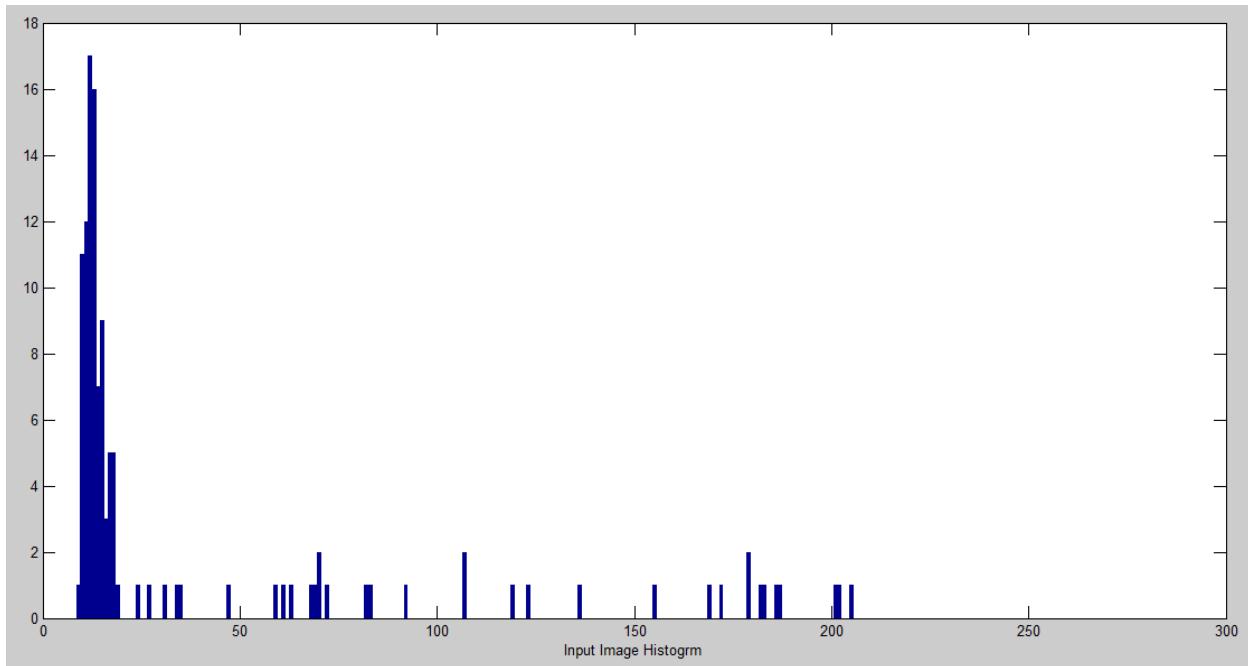
```
j=histeq(i,256);
```

```
subplot(4,2,8)
```

```
bar(j,1)
```

```
l=sprintf('j=histeq(i,256)')
```

```
xlabel(l)
```



```

clc
i=imread('cameraman.tif');
figure
imshow(i)

```

```
xlabel('Input Image')
```

```
figure
```

```
j=histeq(i,2);
```

```
subplot(2,4,1)
```

```
imshow(j)
```

```
l=sprintf('j=histeq(i,2)')
```

```
xlabel(l)
```

```
j=histeq(i,4);
```

```
subplot(2,4,2)
```

```
imshow(j)
```

```
l=sprintf('j=histeq(i,4)')
```

```
xlabel(l)
```

```
j=histeq(i,8);
```

```
subplot(2,4,3)
```

```
imshow(j)
```

```
l=sprintf('j=histeq(i,8)')
```

```
xlabel(l)
```

```
j=histeq(i,16);
```

```
subplot(2,4,4)
```

```
imshow(j)
```

```
l=sprintf('j=histeq(i,16)')
```

```
xlabel(l)
```

```
j=histeq(i,32);
```

```
subplot(2,4,5)
```

```
imshow(j)
```

```
l=sprintf('j=histeq(i,32)')
```

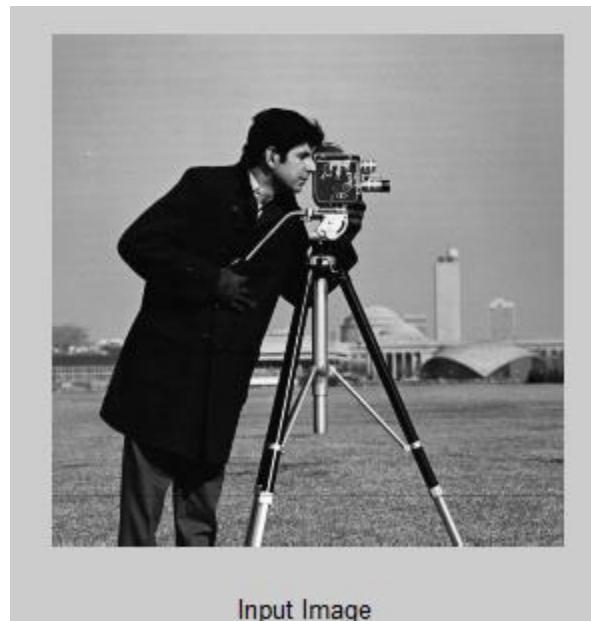
```
xlabel(l)
```

```
j=histeq(i,64);
```

```
subplot(2,4,6)
imshow(j)
l=sprintf('j=histeq(i,64)')
xlabel(l)
```

```
j=histeq(i,128);
subplot(2,4,7)
imshow(j)
l=sprintf('j=histeq(i,128)')
xlabel(l)
```

```
j=histeq(i,256);
subplot(2,4,8)
imshow(j)
l=sprintf('j=histeq(i,256)')
xlabel(l)
```



Input Image



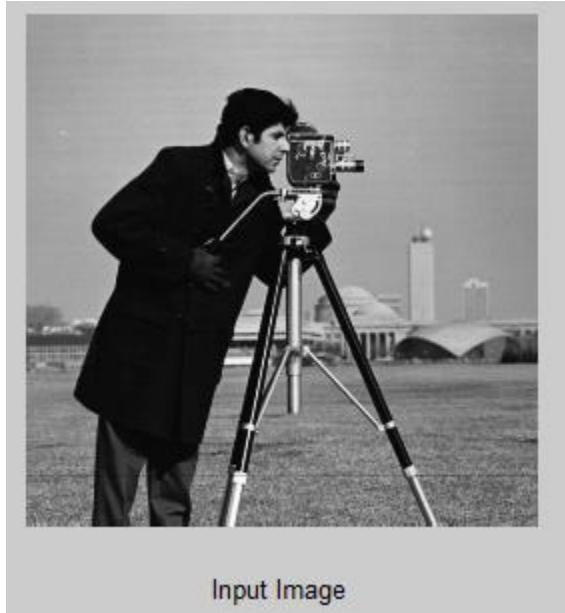
As explained earlier that the transformation function ($T(r)$) for making a high contrast image is simply the sum of normalised histogram values. The transformation function can be obtained using the MATLAB cumsum function. e.g.

```
>> hnorm = imhist(f)./numel(f);
>> cdf = cumsum(hnorm);
```

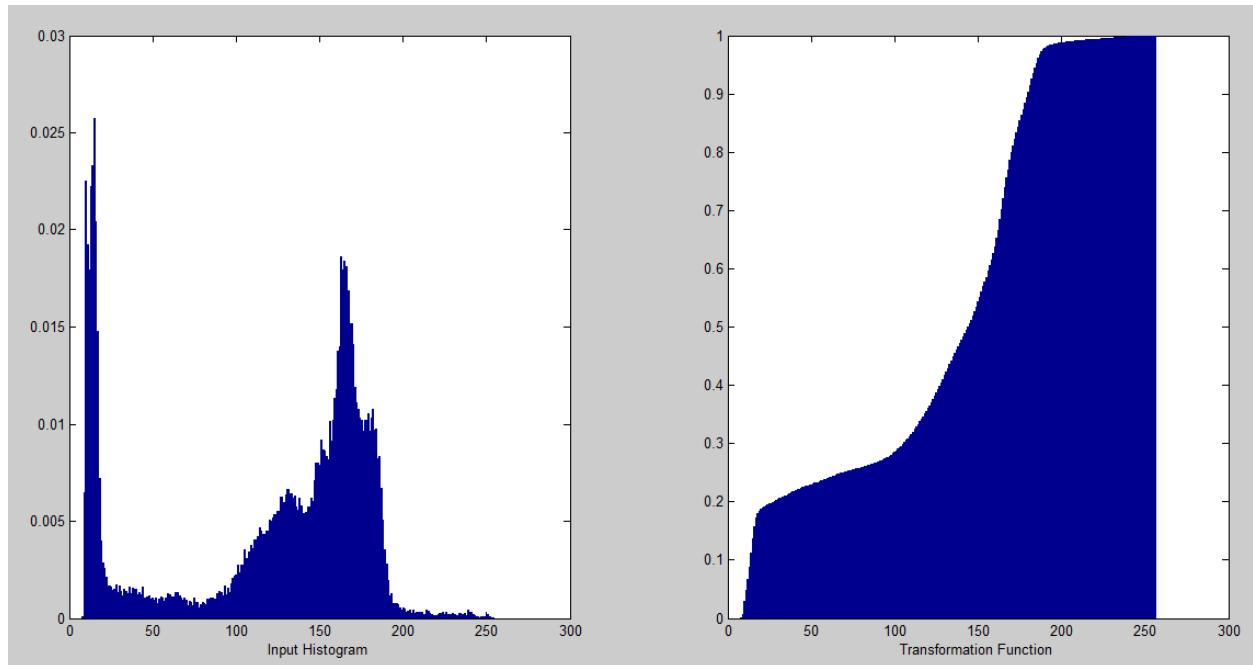
where cdf is the transformation function.

```
clc
i=imread('cameraman.tif');
figure
imshow(i)
xlabel('Input Image')
figure
subplot(1,2,1)
tr=imhist(i)./numel(i);
bar(tr)
xlabel('Input Histogram')
subplot(1,2,2)
```

```
im_cdf=cumsum(tr);
bar(im_cdf)
xlabel('Transformation Function')
```



Input Image



LAB EXERCISE

EXERCISE QUESTIONS

Q1 : Read image cameraman.tif, show the image, show its histogram using imhist and its normalised histogram using bar. All the images should be on one figure and you should use a script file.

```
clc
```

```
f=imread('cameraman.tif');
```

```
he=histeq(f);
```

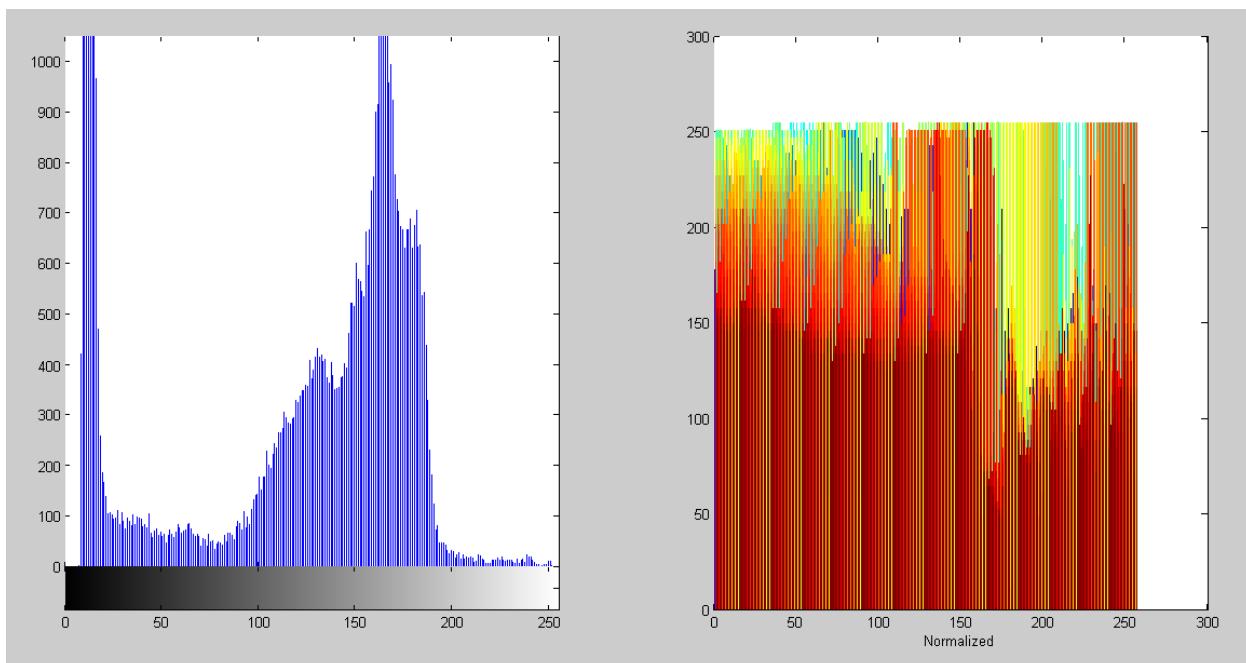
```
subplot(1,2,1)
```

```
imhist(f)
```

```
subplot(1,2,2)
```

```
bar(he)
```

```
xlabel('Normalized')
```



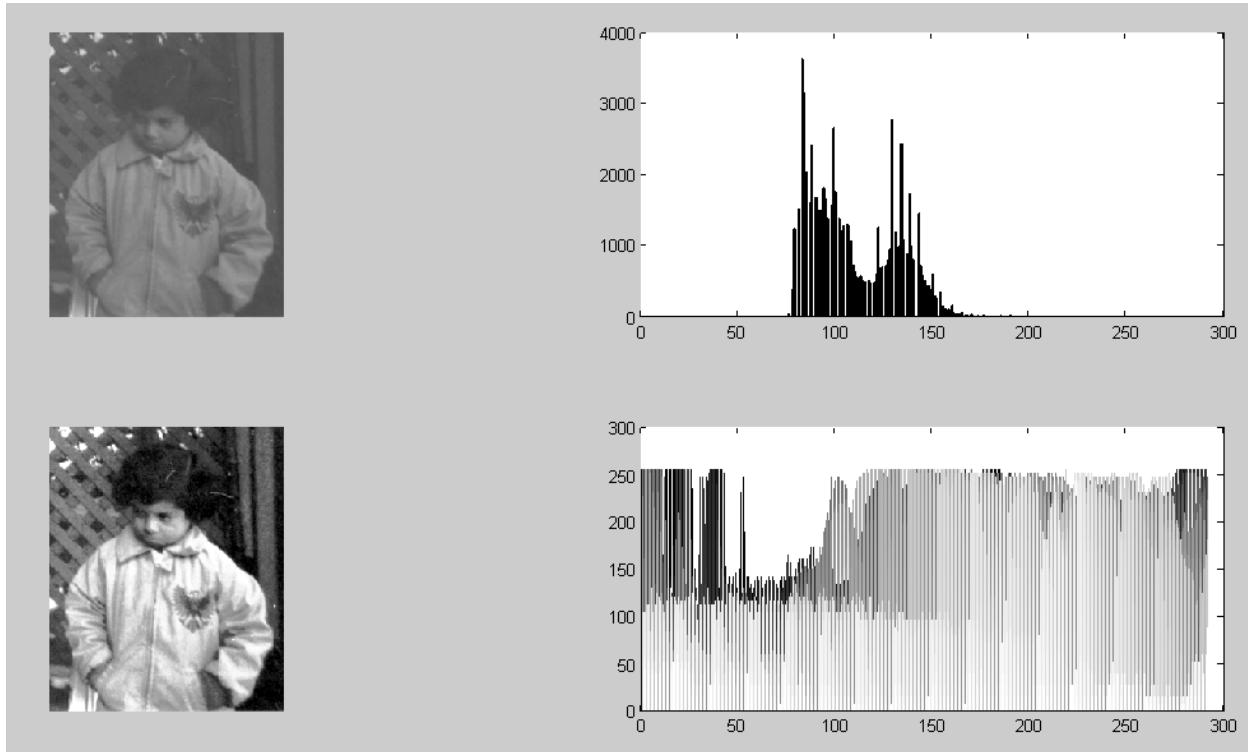
Q2 : Read image pout.tif, show the image, its histogram, equalized image and equalized histogram, all on one figure using a script file. Now repeat the above steps for another image circuit.tif.

```
clc
```

```
f=imread('pout.tif');
```

```
histogram=imhist(f);
```

```
eq=histeq(f);
subplot(2,2,1)
imshow(f)
subplot(2,2,2)
bar(histogram)
subplot(2,2,3)
imshow(eq)
subplot(2,2,4)
bar(eq)
```

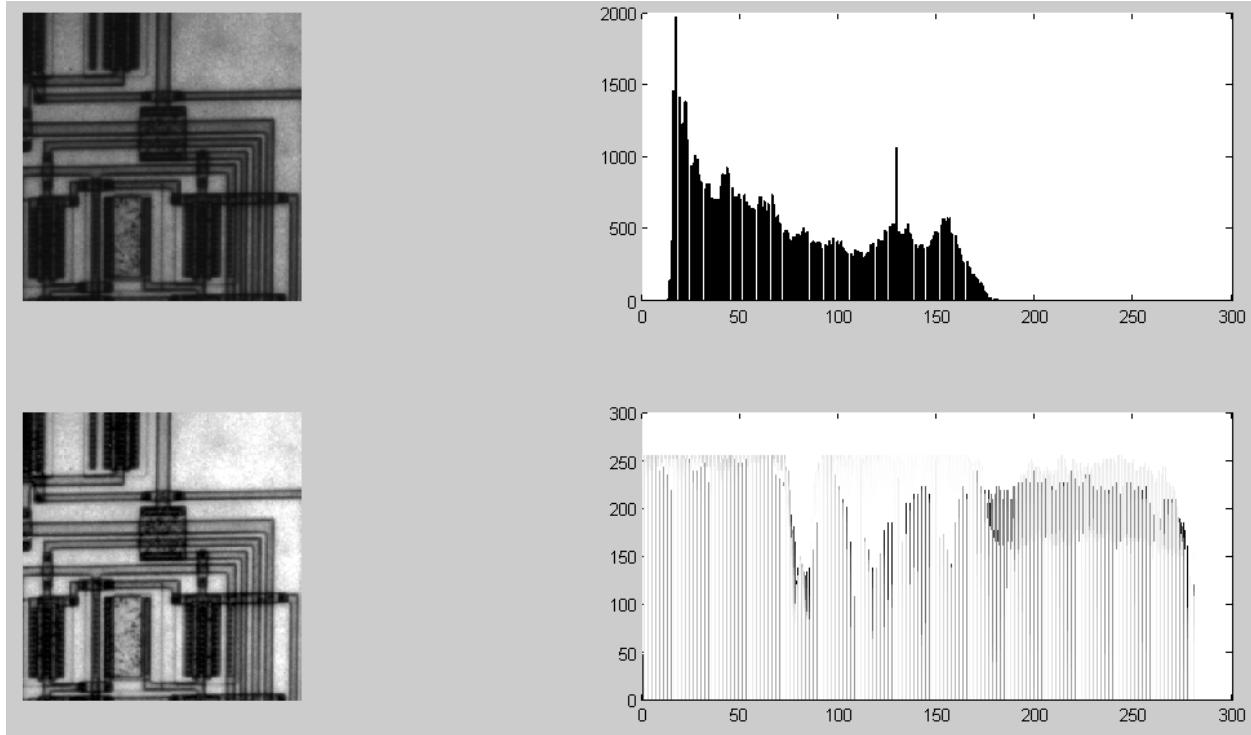


```
clc
f=imread('circuit.tif');
histogram=imhist(f);
eq=histeq(f);
subplot(2,2,1)
imshow(f)
subplot(2,2,2)
bar(histogram)
```

```

subplot(2,2,3)
imshow(eq)
subplot(2,2,4)
bar(eq)

```



Q3 : For Q2 and for image pout.tif show its histogram, the transformation function and histogram of transformed image on one figure.

```

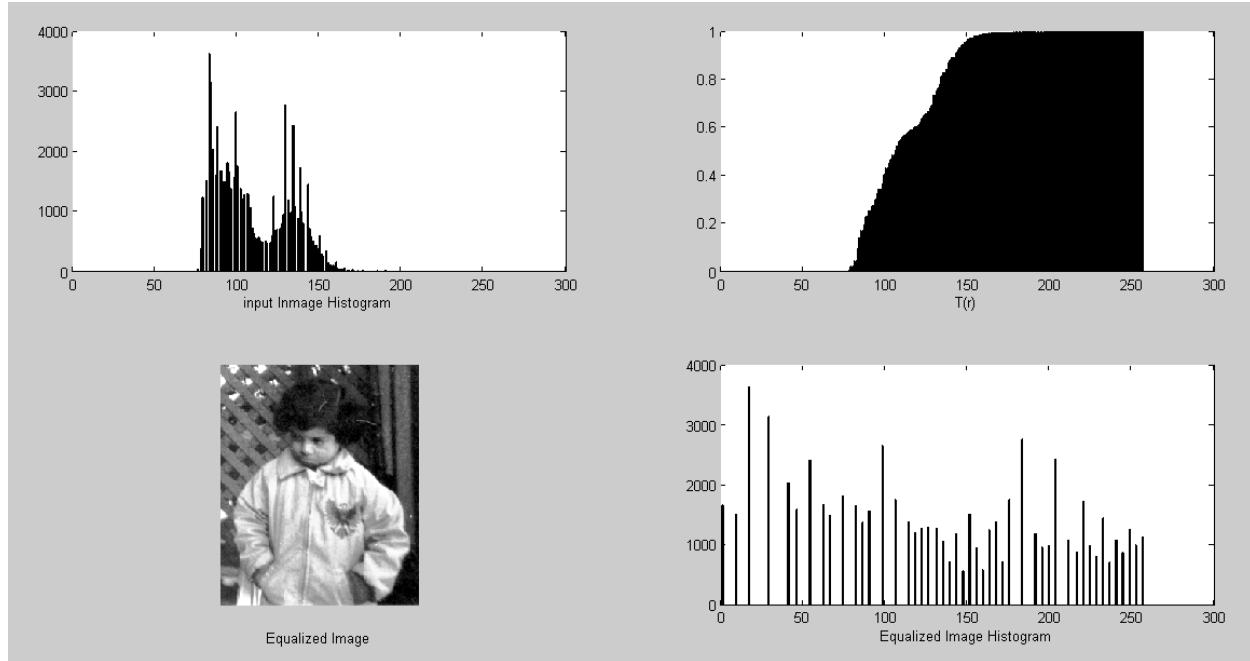
clc
f=imread('pout.tif');
subplot(2,2,1)
bar(imhist(f))
xlabel('input Inmage Histogram')
nor=imhist(f)/numel(f);
tr=cumsum(nor);
subplot(2,2,2)
bar(tr)
xlabel('T(r)')
subplot(2,2,3)

```

```

x=histeq(f);
imshow(x)
xlabel('Equalized Image')
subplot(2,2,4)
bar(imhist(x));
xlabel('Equalized Image Histogram')

```



Q4 : For image pout.tif use cdf to convert it into high contrast image without using histeq. Now compare your result with histeq result. (Hint : Use for loop to map input intensities to output intensities and consult example 3.5 of your lecture notes).

```

clc
f=imread('pout.tif');
nor=imhist(f)./numel(f)
cdf=cumsum(nor);
stem(cdf);
xlabel('T(r)')
h=histeq(f,256);
figure
subplot(2,1,1)

```

```

bar(h)

xlabel('Histogram using histeq()');

for i=1:256

    x(round(cdf(i))+1) =nor(i);

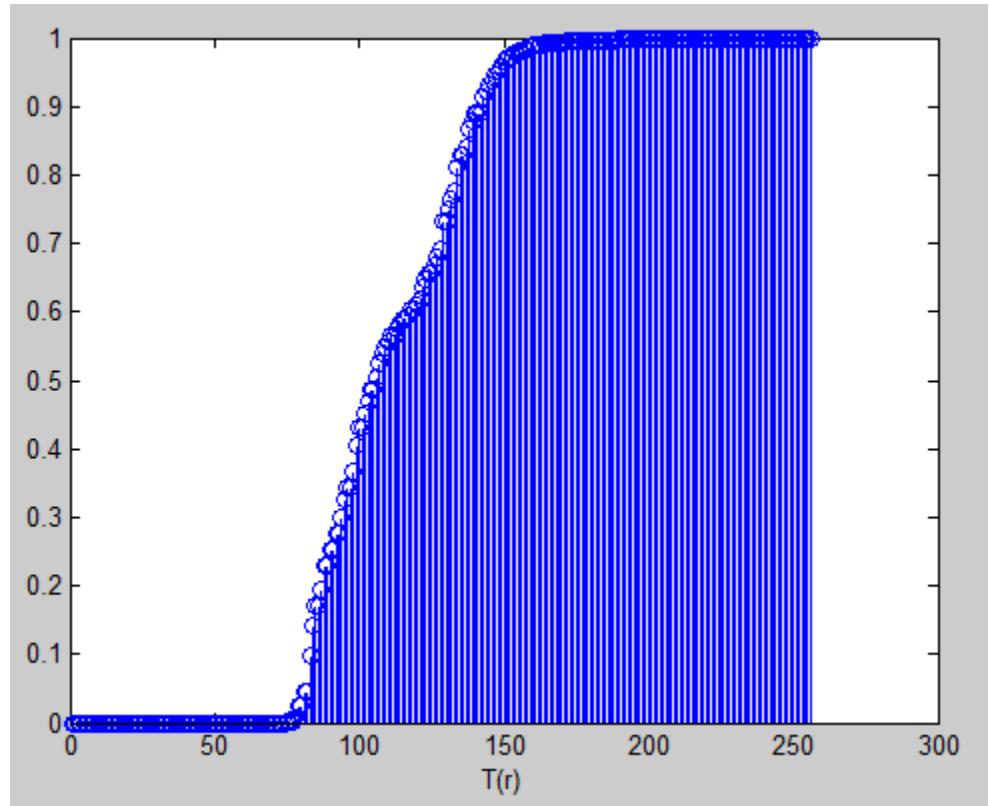
end

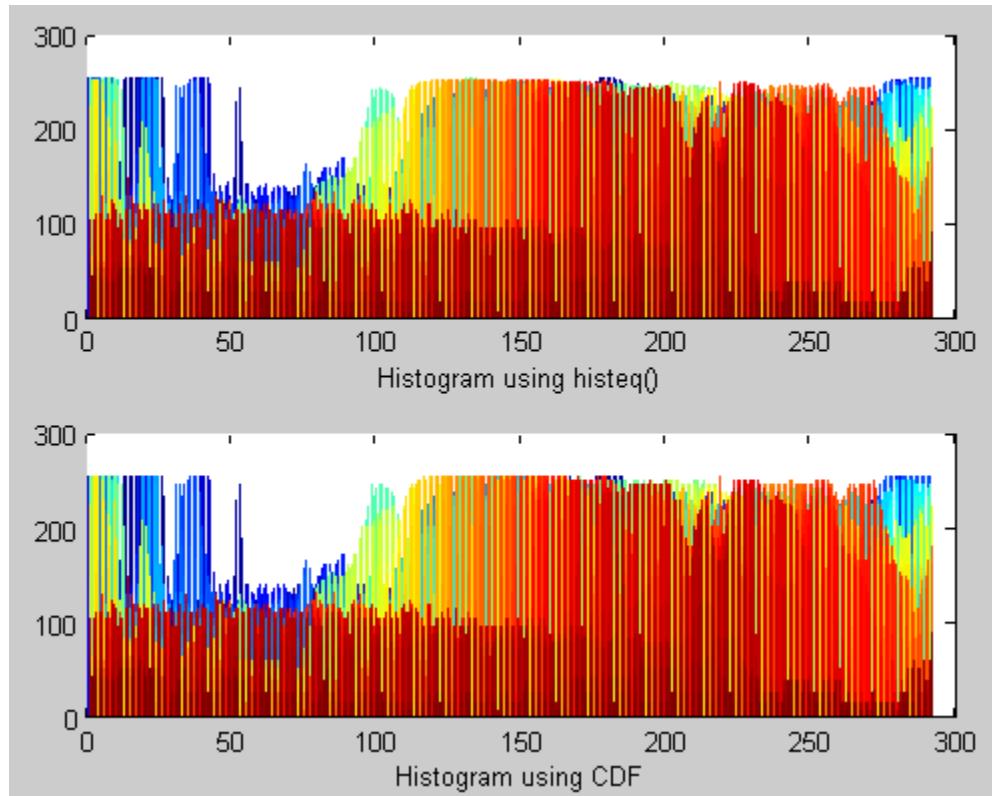
subplot(2,1,2)

bar(x)

xlabel('Histogram using CDF');

```





Experiment#6: To get familiar with histogram matching, local histogram processing and filtering.

- 1. Experiment Text**
 - i. Histogram Matching
 - ii. Local Histogram Processing
 - iii. Spatial Filtering
- 2. Lab Exercise**
- 3. Exercise Questions**

EXPERIMENT TEXT:

1 Histogram Matching

1.1 Background

Histogram equalization produces a transformation function that is adaptive in the sense that it is based on the histogram of the given image. It produces enhancement by spreading the intensities of the input image over a wider range of the intensity scale. We will show in the next section that this does not always lead to successful result. In some applications we want to specify the shape of the histogram that we wish the output image to have. The method used to generate an image that has a specified histogram is called histogram matching.

Histogram matching can be done using histogram equalisation. Suppose r is the intensity of the input image and z is the intensity of the output image. Let probability density functions of the input and output image be $p_r(r)$ and $p_z(z)$. We know for histogram equalization

$$s = T(r) = \int_0^r p_r(w)dw$$

where s has uniform probability density function. Let us define a variable z with the property

$$H(z) = \int_0^z p_z(w)dw = s$$

where z is the intensity of the histogram matched image and $p_z(z)$ is its histogram. From the preceding two equations it follows that

$$z = H^{-1}(s) = H^{-1}[T(r)]$$

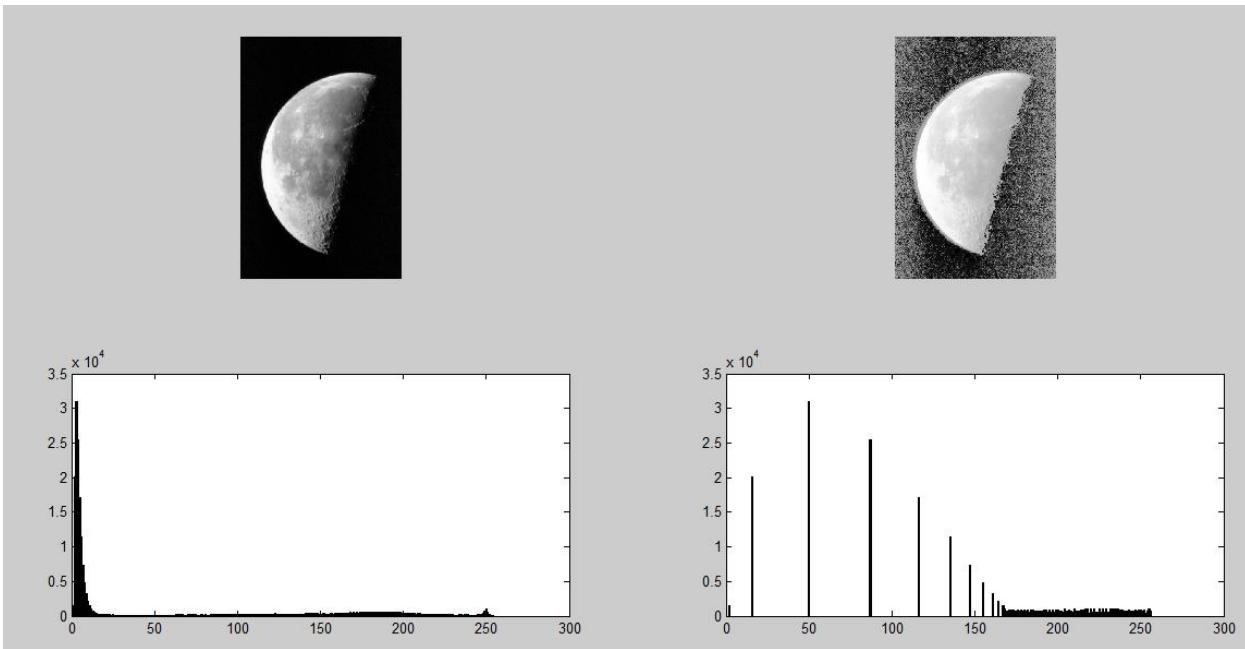
So we can use the preceding equation to find the transformed level z . The toolbox uses the following syntax to implement histogram matching

```
g = histeq(f, hspec);
```

where f is the input image, $hspec$ is the specified histogram (a row vector of intensity values) and g is the output image whose histogram matches the specified histogram, $hspec$.

Read the image `moon.tif` in variable f . Now create a histogram equalised image g from f (Refer to Experiment 5 for histogram equalised image). Now show both, original and histogram equalised image on the same figure. The figure will show you that the histogram equalization did not produce a very good result (enhancement) in this case. The reason for this can be seen by studying the histograms of both the images. Now plot image f , its histogram, image g and its histogram, all on one figure . You will see that most of the intensity levels are shifted to the upper half of the grey scale, giving the image a washed out appearance. The cause of this shift is the large concentration of dark intensities in the original image.

```
f=imread('moon.tif');
g=histeq(f,256);
fh=imhist(f);
gh=imhist(g);
subplot(2,2,1)
imshow(f)
subplot(2,2,2)
imshow(g)
subplot(2,2,3)
bar(fh)
subplot(2,2,4)
bar(gh)
```



The solution to this problem is histogram matching, with the desired histogram having lesser concentration of intensity levels on the lower end of the gray scale and maintaining the general shape of the original histogram. Unfortunately, there is no straight forward method in MATLAB for histogram matching. The user has to develop his own function files to specify what kind of histogram user wants output image to have and it is beyond undergraduate level. But there is another solution to this problem and it is local histogram processing.

2 Local Histogram Processing

Local histogram processing can be used when we want to enhance the contrast of small areas of an image. We saw in the previous section that the global histogram method failed to produce good results when enhancement was needed in small areas. The syntax for local histogram processing in MATLAB is

```
g = adapthisteq(f, param1, val1, param2, val2, ...)
```

Now apply the following function on image `moon.tif` and plot both the original and modified image on the same plot.

```
>> g = adapthisteq(f);
```

Do you see the improvement in the new image. Now get another image by using the following command and

plot all three images on same figure.

clc

```
f=imread('moon.tif');
```

```
subplot(1,3,1)
```

```
imshow(f)
```

```
xlabel('input image')
```

```
g=histeq(f,256);
```

```
subplot(1,3,2)
```

```
imshow(g)
```

```
xlabel('histogram equalization')
```

```
gl=adapthisteq(f);
```

```
subplot(1,3,3)
```

```
imshow(gl)
```

```
xlabel('local histogram processing')
```



input image



histogram equalization



local histogram processing

```
>> g = adapthisteq(f,'NumTiles',[25 25]);
```

clc

```
gl=adaphisteq(f,'NumTiles',[25 25]);
```

```
subplot(2,3,1)
```

```
imshow(gl)
```

```
xlabel('NumTiles [25 25]')
```

```
gl=adaphisteq(f,'NumTiles',[50 50]);
```

```
subplot(2,3,2)
```

```
imshow(gl)
```

```
xlabel('NumTiles [50 50]')
```

```
gl=adaphisteq(f,'NumTiles',[100 100]);
```

```
subplot(2,3,3)
```

```
imshow(gl)
```

```
xlabel('NumTiles [100 100]')
```

```
gl=adaphisteq(f,'NumTiles',[150 150]);
```

```
subplot(2,3,4)
```

```
imshow(gl)
```

```
xlabel('NumTiles [150 150]')
```

```
gl=adaphisteq(f,'NumTiles',[200 200]);
```

```
subplot(2,3,5)
```

```
imshow(gl)
```

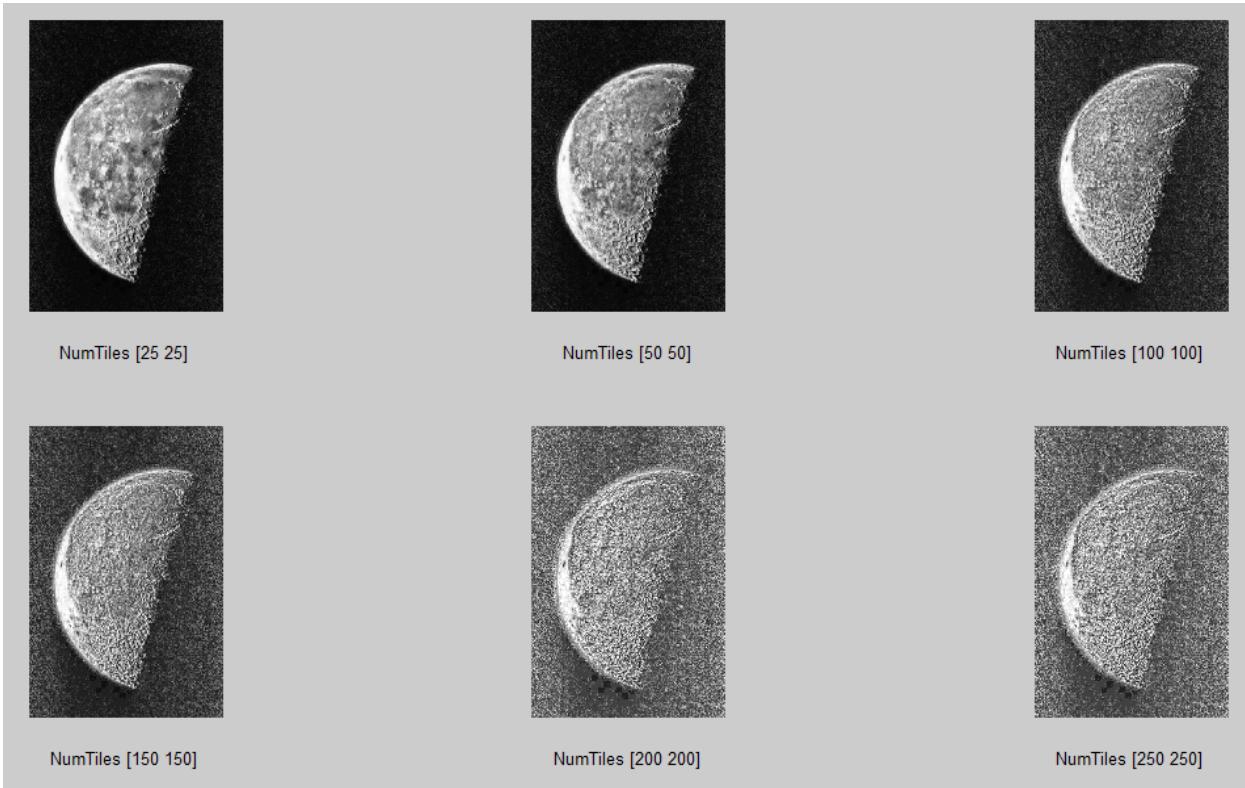
```
xlabel('NumTiles [200 200]')
```

```
gl=adaphisteq(f,'NumTiles',[250 250]);
```

```
subplot(2,3,6)
```

```
imshow(gl)
```

```
xlabel('NumTiles [250 250]')
```



Now get another image by using the following command and plot all four images on same figure.

```
>> g = adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.02);
```

```
clc
gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.1);
subplot(2,3,1)
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.1')
```

```
gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.2);
subplot(2,3,2)
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.2')
```

```
gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.3);
subplot(2,3,3)
```

```
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.3')

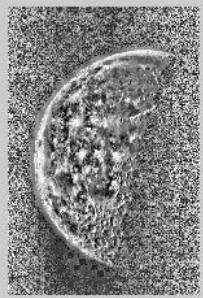
gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.4);
subplot(2,3,4)
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.4')

gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.5);
subplot(2,3,5)
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.5')

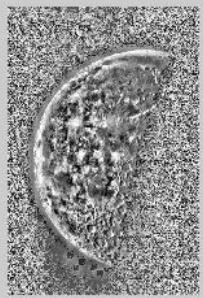
gl=adapthisteq(f,'NumTiles',[25 25],'ClipLimit',0.6);
subplot(2,3,6)
imshow(gl)
xlabel('NumTiles [25 25] ClipLimit 0.6')
```



NumTiles [25 25] ClipLimit 0.1



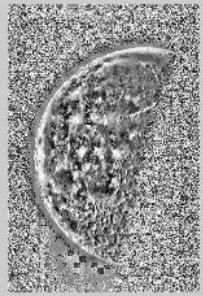
NumTiles [25 25] ClipLimit 0.2



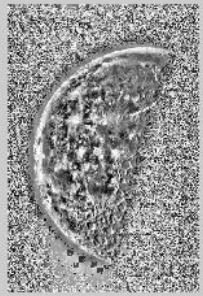
NumTiles [25 25] ClipLimit 0.3



NumTiles [25 25] ClipLimit 0.4



NumTiles [25 25] ClipLimit 0.5



NumTiles [25 25] ClipLimit 0.6

You can see that the contrast improves as we add more parameters. You can explore other parameters by typing **help adapthisteq** on the command prompt.

'NumTiles'	Two-element vector of positive integers specifying the number of tiles by row and column, [M N]. Both M and N must be at least 2. The total number of tiles is equal to M*N. Default: [8 8]
'ClipLimit'	Real scalar in the range [0 1] that specifies a contrast enhancement limit. Higher numbers result in more contrast. Default: 0.01
'NBins'	Positive integer scalar specifying the number of bins for the histogram used in building a contrast enhancing transformation. Higher values result in greater dynamic range at the cost of slower processing speed. Default: 256
'Range'	String specifying the range of the output image data. 'original' — Range is limited to the range of the original image, [min(I(:)) max(I(:))]. 'full' — Full range of the output image class is used. For example, for uint8 data, range is [0 255]. Default: 'full'
'Distribution'	String specifying the desired histogram shape for the image tiles. 'uniform' — Flat histogram 'rayleigh' — Bell-shaped histogram 'exponential' — Curved histogram Default: 'uniform'
'Alpha'	Nonnegative real scalar specifying a distribution parameter.

Default: 0.4

Note: Only used when 'Distribution' is set to either 'rayleigh' or 'exponential'.

3 Spatial Filtering

Spatial filtering follows the following steps:

- 1) Defining a centre point (x,y)
- 2) Performing an operation that involves only the pixels in predefined neighbourhood
- 3) Letting the result of that operation be response of the process at that point
- 4) Repeating the process for every point in the image.

The process of moving the center creates new neighborhood, one for each pixel in the input image. The two terms used for this process are neighborhood operation and spatial filtering.

3.1 Linear Filtering

If the computations performed on the neighborhood of a pixel are linear, it is called linear filtering. The linear operations of interest in this experiment are limited to multiplying each pixel in the neighborhood with a weight and summing the result to obtain the response at point (x,y). The weights are arranged in the form of a matrix also called as **filter, mask, kernel, template or window**. The filtering process consists of simply moving the center of the filter mask w, from point to point in the image f (x, y). At each point (x,y), the response of the filter at that point is the sum of the products of the filter weights and the corresponding neighborhood pixels in the area spanned by the filter mask.

There are two closely related concepts with linear filtering, correlation and convolution. Correlation is the process of moving the filter mask over the image and calculating sum of products at each location as described previously. The mechanics of convolution are exactly the same as correlation except that the filter is first rotated by 180 degree.

The toolbox implements the linear filtering using the following function

```
g = imfilter(f, w, filteringmode, boundaryoptions, sizeoptions);
```

Where f is the input image, w is the filtering mask and g is the filtered result. Filtering mode is used to specify whether to do correlation ('corr') or convolution ('conv'). The boundary option is about how to pad the boundary of image ('replicate','circular','symmetric',P) while filtering and the size option is used either to save the full output image (padded)('full') or after truncating the padded values ('same').

A popular application of linear filtering is blurring which can be achieved using averaging filter. Averaging can be achieved from correlation where after taking sum of products we can divide the result by number of elements of mask. It can also be achieved by having a mask such that each element of the mask is equal to 1/(number of elements of mask).

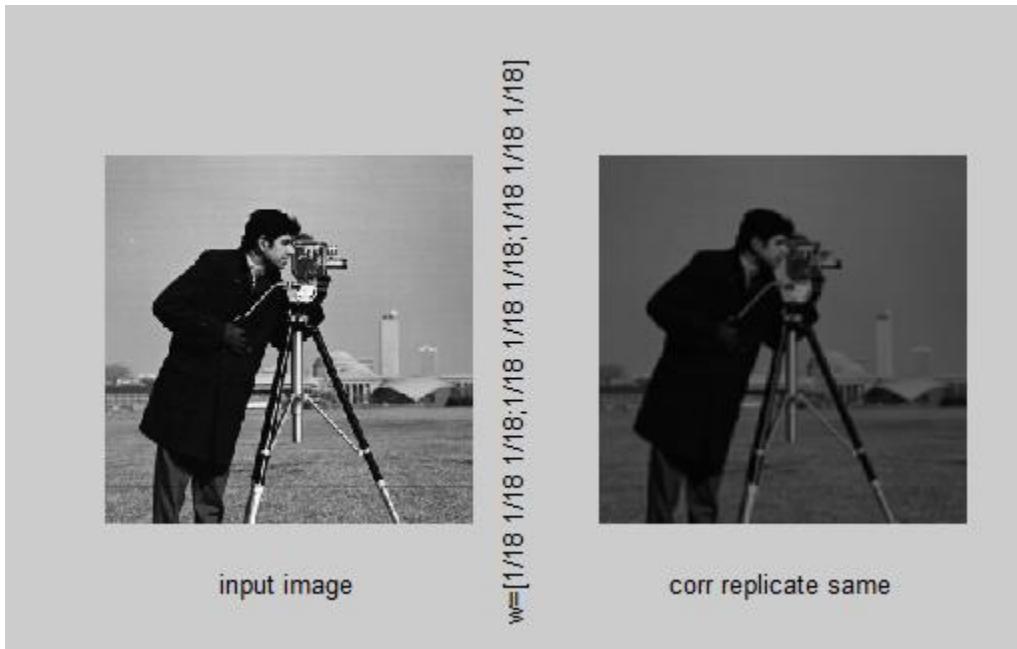
```
clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr','replicate','same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr replicate same');
```



```

clc
f=imread('cameraman.tif');
w=[1/18 1/18 1/18;1/18 1/18 1/18;1/18 1/18 1/18];
g=imfilter(f,w,'corr','replicate','same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr replicate same');
ylabel('w=[1/18 1/18 1/18;1/18 1/18 1/18;1/18 1/18 1/18]');

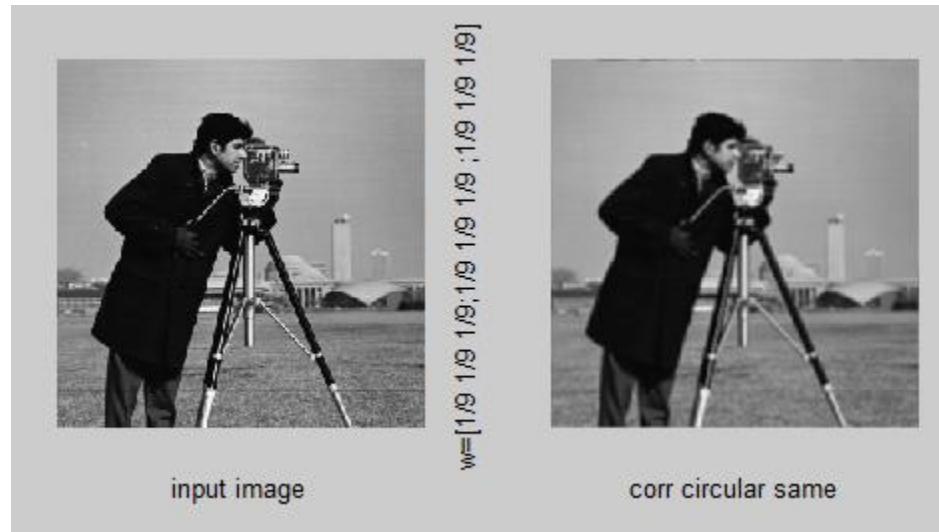
```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr','circular','same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr circular same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



clc

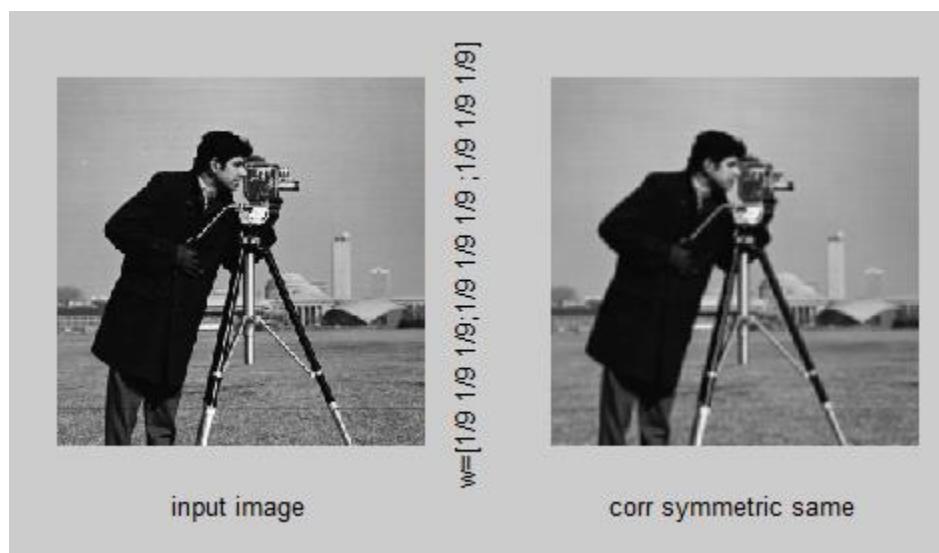
```
f=imread('cameraman.tif');

w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr','symmetric','same');

subplot(1,2,1)
imshow(f)
xlabel('input image')

subplot(1,2,2)
imshow(g)
xlabel('corr symmetric same');

ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')
```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr', [0],'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr [0] same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



```

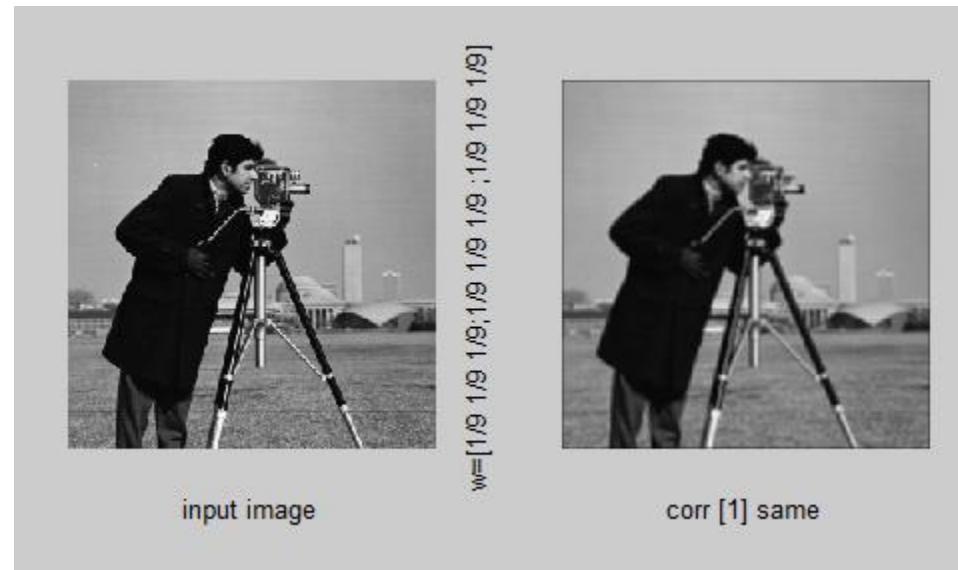
clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr', [1],'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)

```

```

imshow(g)
xlabel('corr [1] same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr', [128],'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr [128] same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



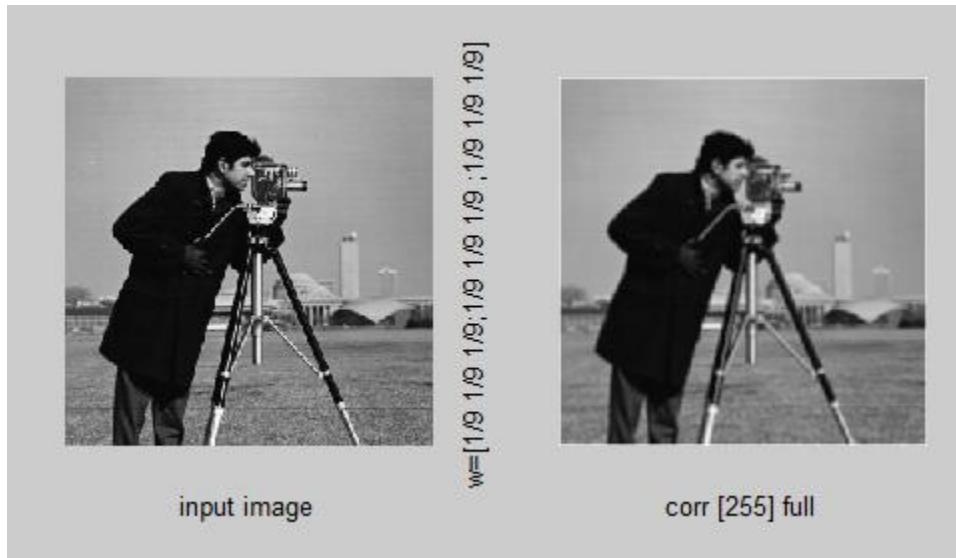
```
clc  
f=imread('cameraman.tif');  
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];  
g=imfilter(f,w,'corr', [255],'same');  
subplot(1,2,1)  
imshow(f)  
xlabel('input image')  
subplot(1,2,2)  
imshow(g)  
xlabel('corr [255] same');  
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9]')
```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr', [255], 'full');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr [255] full');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



```
clc
```

```
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'corr', [0],'full');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('corr [0] full');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')
```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'conv', 'replicate' , 'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('conv replicate same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

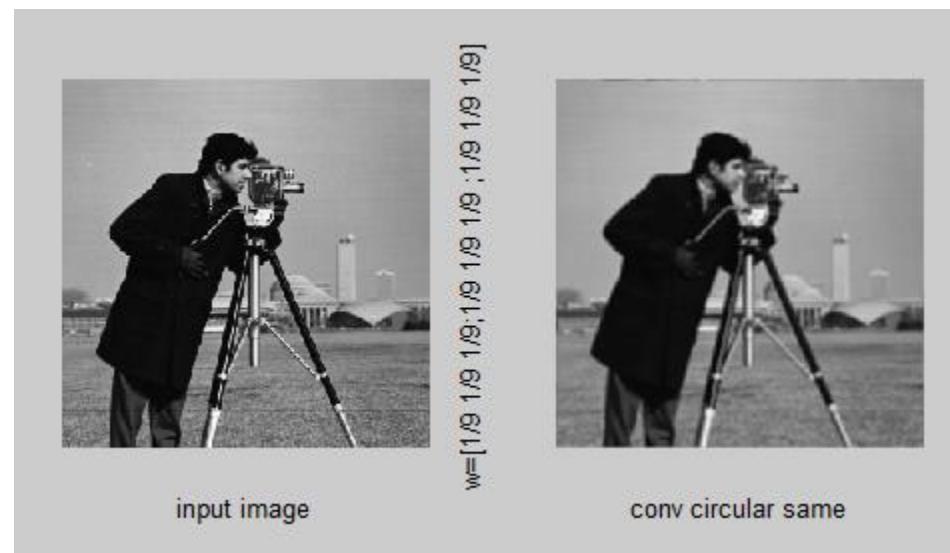
```



```

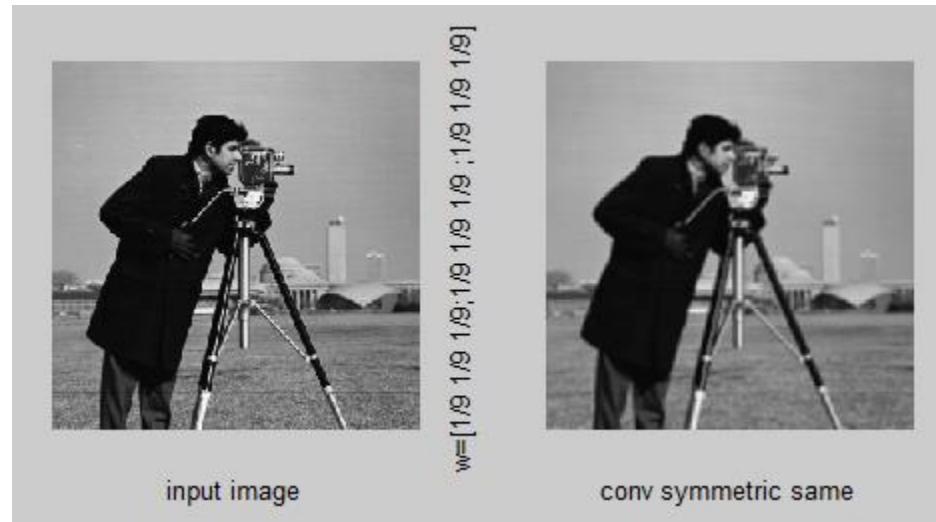
clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'conv', 'circular' , 'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('conv circular same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



```
clc
```

```
f=imread('cameraman.tif');  
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];  
g=imfilter(f,w,'conv', 'symmetric' , 'same');  
subplot(1,2,1)  
imshow(f)  
xlabel('input image')  
subplot(1,2,2)  
imshow(g)  
xlabel('conv symmetric same');  
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')
```



```

clc
f=imread('cameraman.tif');
w=[1/9 1/9 1/9;1/9 1/9 1/9;1/9 1/9 1/9];
g=imfilter(f,w,'conv', [0] , 'same');
subplot(1,2,1)
imshow(f)
xlabel('input image')
subplot(1,2,2)
imshow(g)
xlabel('conv [0] same');
ylabel('w=[1/9 1/9 1/9;1/9 1/9 1/9 ;1/9 1/9 1/9]')

```



clc

```

f=imread('cameraman.tif');

w=[1/25 1/25 1/25 1/25 1/25;1/25 1/25 1/25 1/25 1/25;1/25 1/25 1/25 1/25 1/25];

g=imfilter(f,w,'conv', [0] , 'same');

subplot(1,2,1)

imshow(g)

xlabel('conv [0] same')

h=imfilter(f,w,'corr',[0],'same')

subplot(1,2,2)

imshow(h)

xlabel('corr [0] same');

ylabel('[1/25 1/25 1/25 1/25 1/25;1/25 1/25 1/25 1/25 1/25;1/25 1/25 1/25 1/25 1/25]')

```



conv [0] same



corr [0] same

EXERCISE QUESTIONS

Q1 Make a matrix of size 5x5 such that only the center pixel is 1 and all other values are zero. Now make a filter of size 3x3 with values from 1 to 9 (as discussed during lecture). Now use MATLAB filtering function to do convolution and correlation. Also explore the parameter size options. Do the results match with theory?

clc

```

I=zeros(5);

siz=size(I);

```

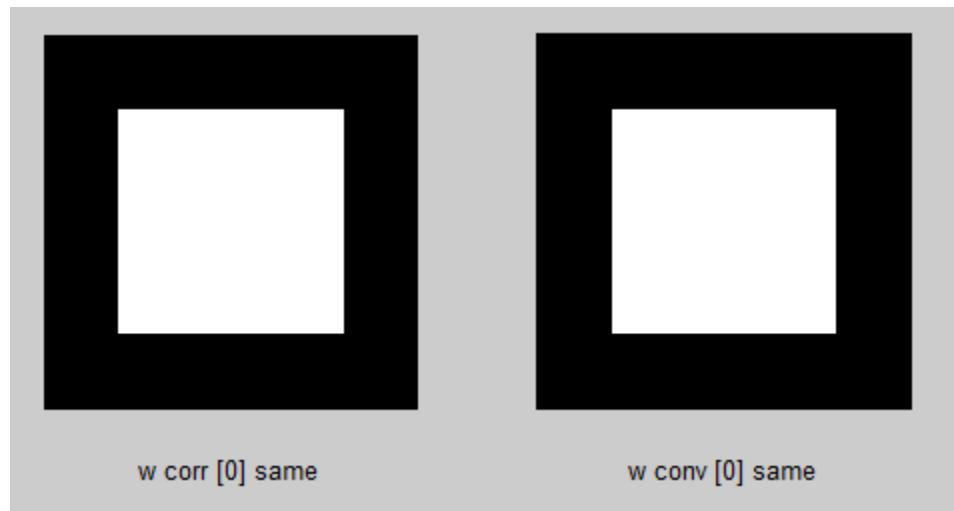
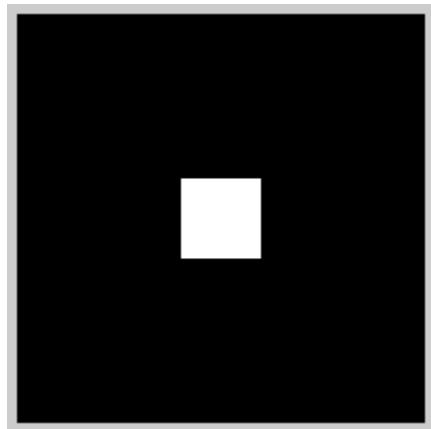
```

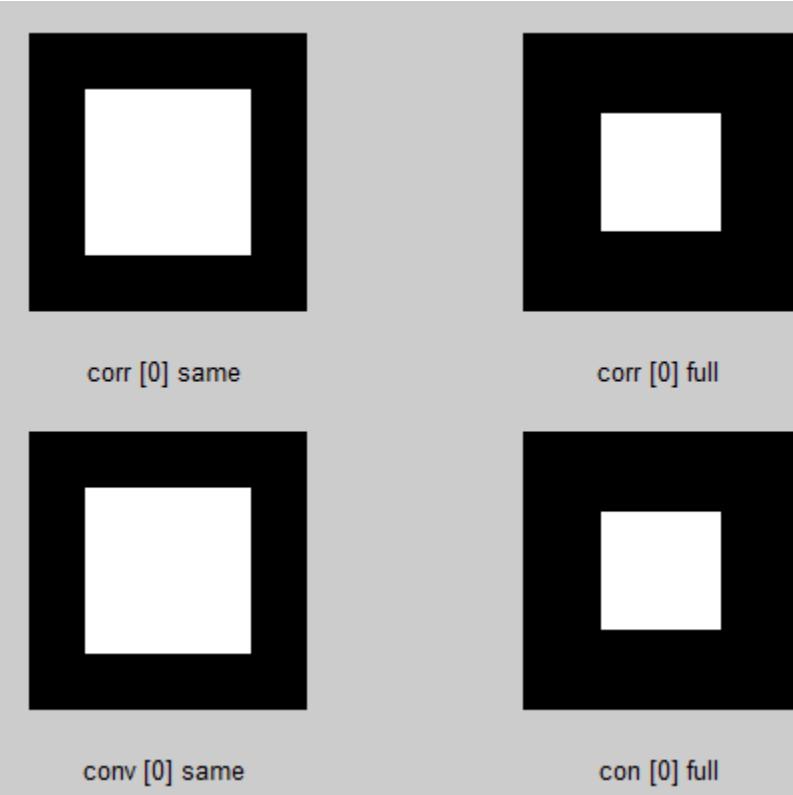
for i=1:siz(1)
    for j=1:siz(2)
        if (i==(siz(1)+1)/2 & j==(siz(2)+1)/2 )
            img(i,j)=1;
        else
            img(i,j)=0;
        end
    end
end
im_size=size(img);
imshow(img, 'InitialMagnification', 800);
w=[1 2 3;4 5 6; 7 8 9];
g=imfilter(img,w,'corr',[0],'same');
figure
subplot(1,2,1)
imshow(g)
xlabel('w corr [0] same')
h=imfilter(img,w,'conv',[0],'same');
subplot(1,2,2)
imshow(h)
xlabel('w conv [0] same')

figure
subplot(2,2,1)
gs=imfilter(img,w,'corr',[0],'same');
imshow(gs)
xlabel('corr [0] same')
subplot(2,2,2)
gf=imfilter(img,w,'corr',[0],'full');
imshow(gf)
xlabel('corr [0] full')
subplot(2,2,3)

```

```
hs=imfilter(img,w,'conv',[0],'same');  
imshow(hs)  
xlabel('conv [0] same')  
subplot(2,2,4)  
hf=imfilter(img,w,'conv',[0],'full')  
imshow(hf)  
xlabel('con [0] full')
```





Q2 Create an images f of size 512×512 such that if this image is divided into four squares, the first and last square should be black while second and third squares should be white (Hint: use MATLAB built in functions zeros and ones to create the image). Now Create an averaging mask w of size 31×31 (Hint: Create a matrix of ones of size 31×31 . Now divide it by 31^2). Apply the MATLAB filtering operation on the image with different value s of boundary options. Plot all the images on the same figure. What difference do you see with different values of boundary option?

```

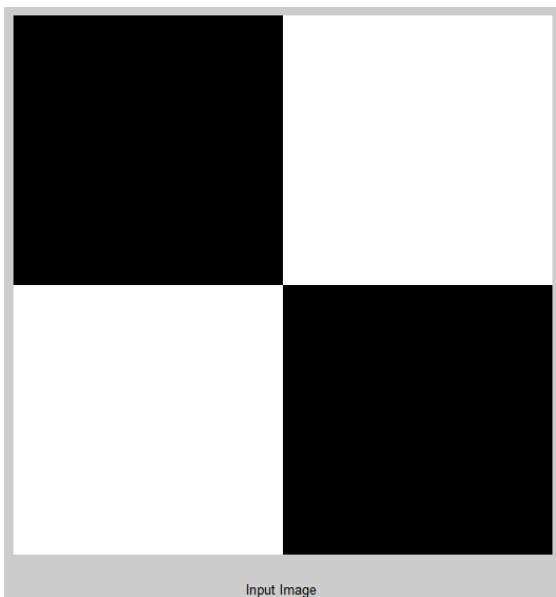
clc
x=512/2
img=[zeros(x,x),ones(x,x);ones(x,x),zeros(x,x)];
imshow(img);
xlabel('Input Image')
w=(ones(31,31))./((31)^2);
figure
subplot(2,2,1)
g1=imfilter(img,w,'corr','circular','same');
imshow(g1)
xlabel('corr circular same')

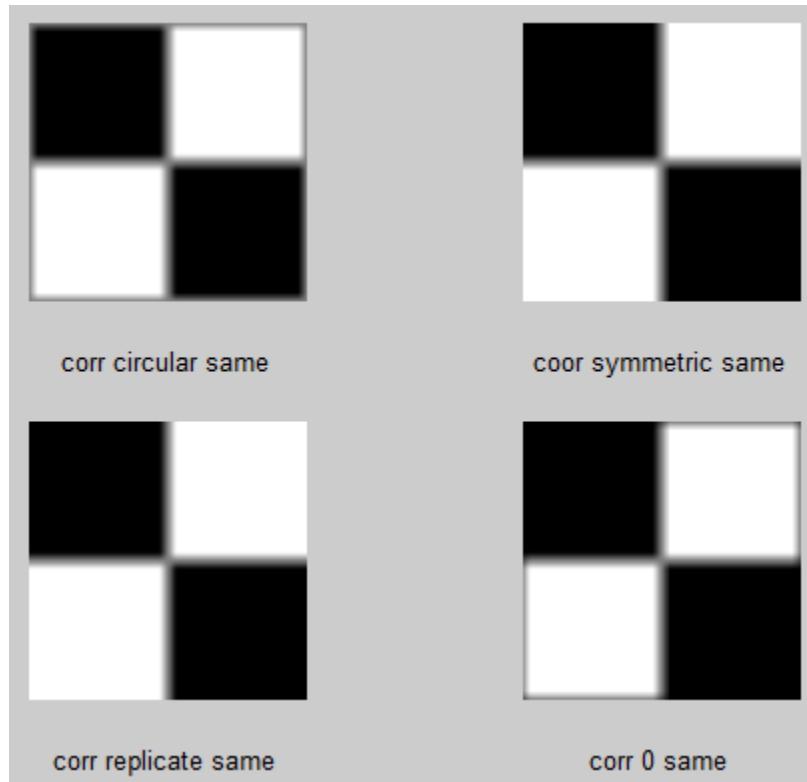
```

```
subplot(2,2,2)
g2=imfilter(img,w,'corr','symmetric','same');
imshow(g2)
xlabel('coor symmetric same')
```

```
subplot(2,2,3)
g3=imfilter(img,w,'corr','replicate','same');
imshow(g3)
xlabel('corr replicate same')
```

```
subplot(2,2,4)
g4=imfilter(img,w,'corr',0,'same');
imshow(g4)
xlabel('corr 0 same')
```





Q3 Now read image `moon.tif` and `cameraman.tif`. Make an averaging filter of size 11×11 . Apply this filter on both the images and show all four images on same figure. Are the new images blurred?

```

clc
f=imread('cameraman.tif');
i=imread('moon.tif');
w=ones(11,11) / (11)^2;

gf=imfilter(f,w,'corr','replicate','same');
gi=imfilter(i,w,'corr','replicate','same');

subplot(2,2,1)
imshow(f)
xlabel('input')

subplot(2,2,2)
imshow(gf)
xlabel('corr replicate same')

```

```
subplot(2,2,3)
```

```
imshow(i)
```

```
xlabel('input')
```

```
subplot(2,2,4)
```

```
imshow(gi)
```

```
xlabel('corr replicate same')
```



input



corr replicate same



input



corr replicate same

Experiment#7: To get familiar with Linear and Non-Linear Filtering

- 1. Experiment Text**
 - i. Spatial Filtering**
- 2. Lab Exercise**
- 3. Exercise Questions**

1 Spatial Filtering

In the previous experiment we implemented the filtering operation by manually specifying our filter. MATLAB toolbox supports a number of predefined 2-D linear spatial filters, obtained by using function `fspecial`, which generates a filter mask `w`, using the syntax

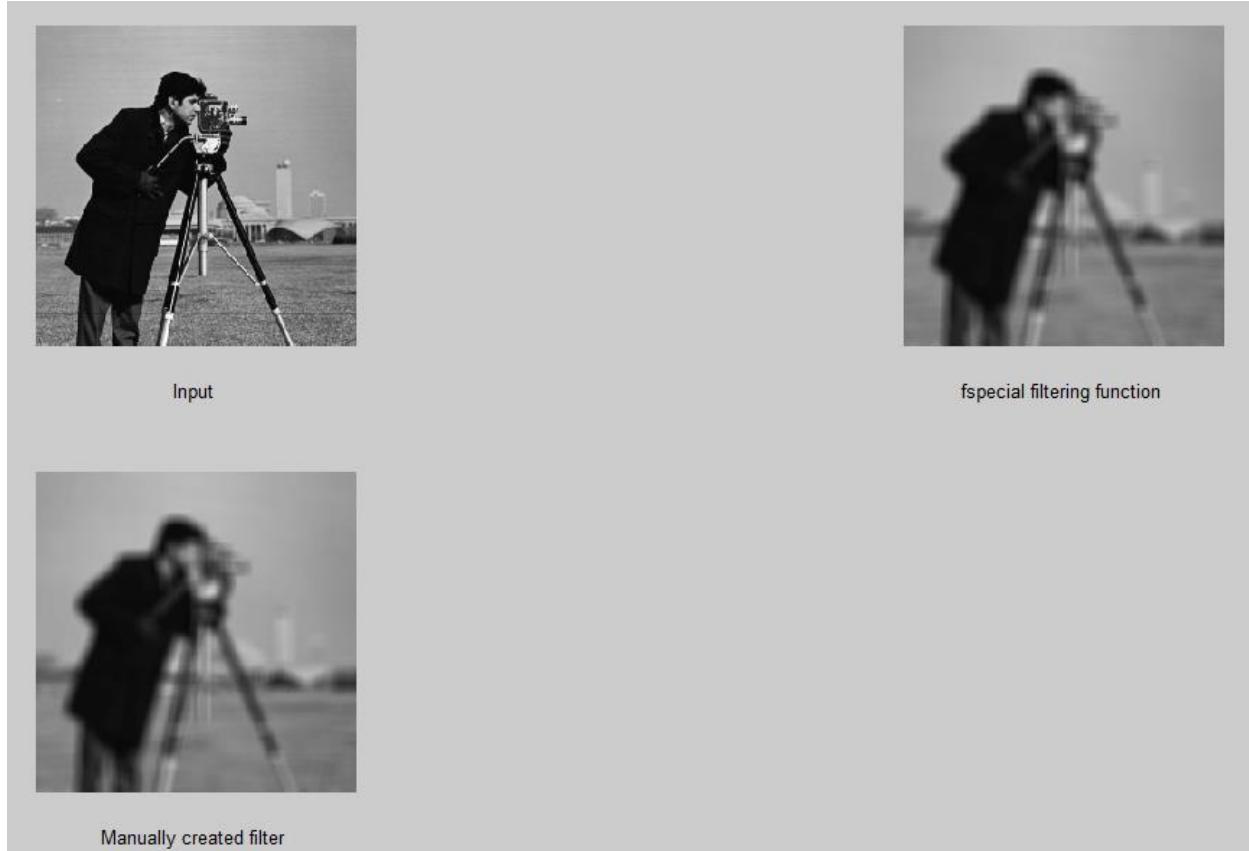
$$w = \text{fspecial}('type', \text{parameters})$$

where '`type`' specifies the filter type, and parameters further define the specified filter. The spatial filters supported by `fspecial` are given in Figure 1.

Read an image `cameraman.tif` (`f`) and create an averaging filter (`w`) of size 11×11 using `fspecial`. Create a blurred image (`g`) using this filter. Now create another filter `w1` of size 11×11 manually (as did in last experiment) and apply it on `f` to get a new image (`g1`). Plot `f`, `g` and `g1` on the same figure. Do you see any difference between `g` and `g1`?

```
clc
f=imread('cameraman.tif');
w=fspecial('average',[11 11]);
g=imfilter(f,w,'corr','replicate','same');
w1=ones(11,11)/ 11^2;
g1=imfilter(f,w1,'corr','replicate','same');
subplot(2,2,1)
imshow(f)
xlabel('Input')
subplot(2,2,2)
imshow(g)
xlabel('fspecial filtering function')
subplot(2,2,3)
```

```
imshow(g1)
 xlabel('Manually created filter')
```



An image can be sharpened using a Laplacian filter. The syntax for using a Laplacian filter is

$$w = fspecial('laplacian', \alpha)$$

which creates a Laplacian filter of size 3x3? The shape of the filter determined by α whose values are between [0, 1] with a default value of 0.5. The filter is created using value of α by following formula.

$$\begin{bmatrix} \frac{\alpha}{1+\alpha} & \frac{1-\alpha}{1+\alpha} & \frac{\alpha}{1+\alpha} \\ \frac{1-\alpha}{1+\alpha} & \frac{-4}{1+\alpha} & \frac{1-\alpha}{1+\alpha} \\ \frac{\alpha}{1+\alpha} & \frac{1-\alpha}{1+\alpha} & \frac{\alpha}{1+\alpha} \end{bmatrix}$$

```
clc
imread('cameraman.tif');
w=fspecial('laplacian',0);
```

```

f0=imfilter(f,w,'corr','replicate','same');
imshow(f0)
xlabel('0')
figure
f1=imfilter(f,fspecial('laplacian',0.1),'corr','replicate','same');
f2=imfilter(f,fspecial('laplacian',0.2),'corr','replicate','same');
f3=imfilter(f,fspecial('laplacian',0.3),'corr','replicate','same');
f4=imfilter(f,fspecial('laplacian',0.4),'corr','replicate','same');
f5=imfilter(f,fspecial('laplacian',0.5),'corr','replicate','same');
f6=imfilter(f,fspecial('laplacian',0.6),'corr','replicate','same');
f7=imfilter(f,fspecial('laplacian',0.7),'corr','replicate','same');
f8=imfilter(f,fspecial('laplacian',0.8),'corr','replicate','same');
f9=imfilter(f,fspecial('laplacian',0.9),'corr','replicate','same');
f10=imfilter(f,fspecial('laplacian',1),'corr','replicate','same');
subplot(2,5,1)
imshow(f1)
xlabel('0.1')
subplot(2,5,2)
imshow(f2)
xlabel('0.2')
subplot(2,5,3)
imshow(f3)
xlabel('0.3')
subplot(2,5,4)
imshow(f4)
xlabel('0.4')
subplot(2,5,5)
imshow(f5)
xlabel('0.5')
subplot(2,5,6)
imshow(f6)
xlabel('0.6')

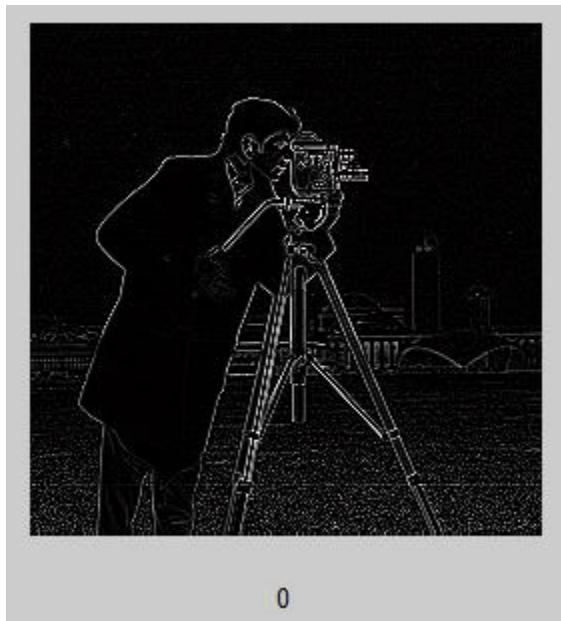
```

```
subplot(2,5,7)
imshow(f7)
xlabel('0.7')

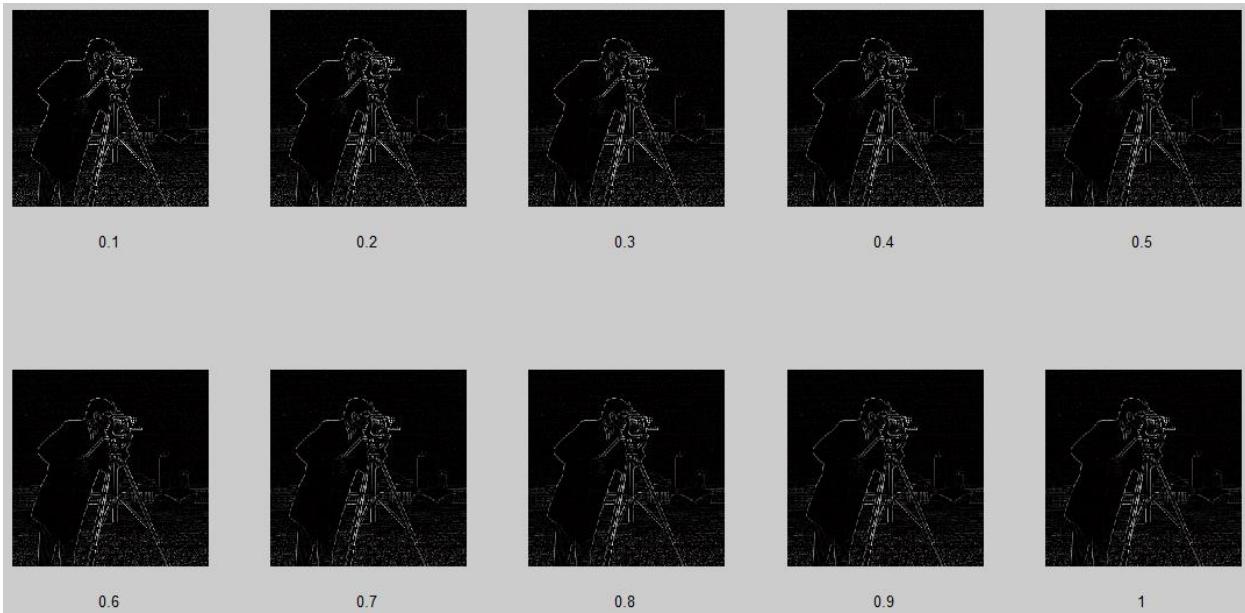
subplot(2,5,8)
imshow(f8)
xlabel('0.8')

subplot(2,5,9)
imshow(f9)
xlabel('0.9')

subplot(2,5,10)
imshow(f10)
xlabel('1')
```



0



Type	Syntax and Parameters
'average'	<code>fspecial('average', [r c])</code> . A rectangular averaging filter of size $r \times c$. The default is 3×3 . A single number instead of $[r c]$ specifies a square filter.
'disk'	<code>fspecial('disk', r)</code> . A circular averaging filter (within a square of size $2r + 1$) with radius r . The default radius is 5.
'gaussian'	<code>fspecial('gaussian', [r c], sig)</code> . A Gaussian lowpass filter of size $r \times c$ and standard deviation sig (positive). The defaults are 3×3 and 0.5. A single number instead of $[r c]$ specifies a square filter.
'laplacian'	<code>fspecial('laplacian', alpha)</code> . A 3×3 Laplacian filter whose shape is specified by $alpha$, a number in the range $[0, 1]$. The default value for $alpha$ is 0.5.
'log'	<code>fspecial('log', [r c], sig)</code> . Laplacian of a Gaussian (LoG) filter of size $r \times c$ and standard deviation sig (positive). The defaults are 5×5 and 0.5. A single number instead of $[r c]$ specifies a square filter.
'motion'	<code>fspecial('motion', len, theta)</code> . Outputs a filter that, when convolved with an image, approximates linear motion (of a camera with respect to the image) of len pixels. The direction of motion is $theta$, measured in degrees, counterclockwise from the horizontal. The defaults are 9 and 0, which represents a motion of 9 pixels in the horizontal direction.
'prewitt'	<code>fspecial('prewitt')</code> . Outputs a 3×3 Prewitt mask, wv , that approximates a vertical gradient. A mask for the horizontal gradient is obtained by transposing the result: $wh = wv'$.
'sobel'	<code>fspecial('sobel')</code> . Outputs a 3×3 Sobel mask, sv , that approximates a vertical gradient. A mask for the horizontal gradient is obtained by transposing the result: $sh = sv'$.
'unsharp'	<code>fspecial('unsharp', alpha)</code> . Outputs a 3×3 unsharp filter. Parameter $alpha$ controls the shape; it must be greater than 0 and less than or equal to 1.0; the default is 0.2.

Figure 1: Filter Types

1.1 Non Linear Filters

A commonly used tool for generating non linear spatial filters in MATLAB is to use function `ordfilt2` which generates order static filters. These are non linear filters whose response is based on ordering the pixels contained in image neighbourhood and then replacing the value of the centre pixel in the neighbourhood with the value determined by the ranking result. The values are arranged in ascending order in this filter. The syntax of the function is

$$g = \text{ordfilt2}(f, \text{order}, \text{domain})$$

```
clc  
clear  
x=imread('cameraman.tif')  
s=ones(11,11);  
g=ordfilt2(x,100,s)  
imshow(g)
```



This function creates a new image g by replacing each element of f by order'th element in the sorted set of neighbours specified by non zero elements in domain. Here domain is $m \times n$ mask of 1s and 0s which specify the pixel locations in the neighbourhood that are to be used. The pixels in the neighbourhood that correspond to 0s in the domain mask are not included in the computation e.g. to implement a min filter (first element/order 1/0th percentile), the syntax used is

$$g = \text{ordfilt2}(f, 1, \text{ones}(m, n));$$

```
clc  
clear  
x=imread('cameraman.tif')  
s=ones(3,3);  
g=ordfilt2(x,1,s)  
imshow(g)
```



In this example 1 denotes the first element in the ordered set of mn pixels and `ones(m, n)` creates a mxn matrix consisting of 1s, indicating that all the elements of neighbourhood are to be used. Similarly to implement a max filter, the syntax used is

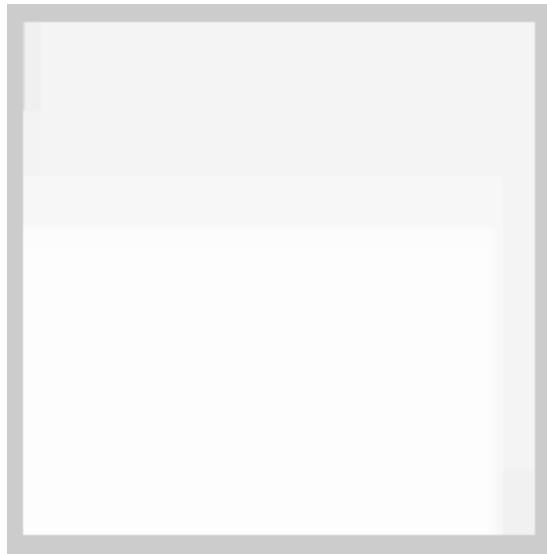
$$g = \text{ordfilt2}(f, m * n, \text{ones}(m, n));$$

```
clc  
clear  
x=imread('cameraman.tif')  
s=ones(3,3);  
[m n]=size(s);  
g=ordfilt2(x,m*n,s)  
imshow(g)
```



where $m*n$ specifies the last element (100th percentile) in ordering e.g. if you are using 3×3 neighbourhood then $m*n$ would mean $3*3$ i.e. the 9th element in the ordering.

```
clc  
clear  
x=imread('cameraman.tif')  
[m n]=size(x)  
s=ones(m,n);  
g=ordfilt2(x,m*n,s)  
imshow(g)
```

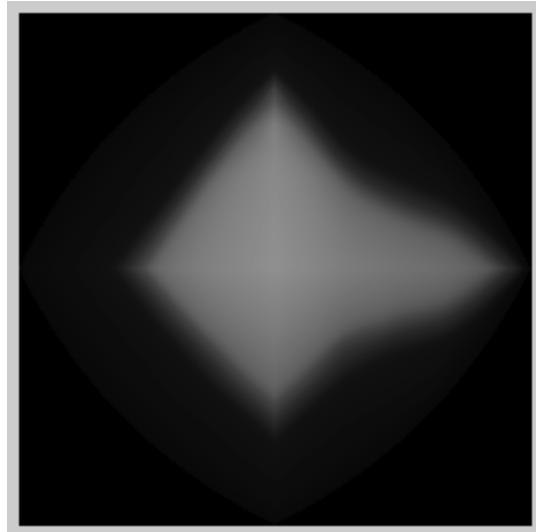


The best known order-static filter in image processing is the **median** filter which corresponds to 50th

percentile.

$$g = \text{ordfilt2}(f, \text{median}(1 : m * n), \text{ones}(m, n));$$

```
clc  
clear  
x=imread('cameraman.tif')  
[m n]=size(x)  
s=ones(m,n);  
md=round((median(1:m*n)))  
g=ordfilt2(x,md,s);  
imshow(g)
```



```
clc  
clear  
x=imread('cameraman.tif')  
[m n]=size(x)  
s=ones(15,15);  
md=round((median(1:m*n)))  
g=ordfilt2(x,md,s);  
imshow(g)
```



where `median(1 : m * n)` computes the median of the neighbourhood. Because of its special importance, the toolbox provides a special function just for median filter.

$$g = \text{medfilt2}(f, [m \ n], \text{padopt});$$

where the parameter `[m n]` defines the neighborhood over which `median` needs to be computed and `padopt` specifies the padding options. The default form of this function is

$$g = \text{medfilt2}(f);$$

which uses a 3x3 neighborhood and pads the borders with 0s?

`clc`

`clear`

```
x=imread('cameraman.tif')
```

```
g=medfilt2(x);
```

```
imshow(g)
```



```
clc  
clear  
x=imread('cameraman.tif')  
g=medfilt2(x,[5 5]);  
imshow(g)
```



Median filtering is widely used to remove salt and pepper noise e. Now we will see how median filtering performs for an image corrupted with salt & pepper noise. An image can be corrupted with salt & pepper noise by using function `imnoise` which has the following syntax

$$g = imnoise(f, 'salt & pepper', 0.2);$$

where the last value (0.2) controls the amount of noise added to the image. The value of last parameter is between 0 and 1 where a higher value means more noise.

```
clc
clear
i=imread('cameraman.tif');
g=imnoise(i,'salt & pepper',0.2);
g1=medfilt2(g);
subplot(1,3,1)
imshow(i)
xlabel('Input Image')
subplot(1,3,2)
imshow(g)
xlabel('Noisy Image')
subplot(1,3,3)
imshow(g1)
xlabel('Removed Noise')
```



Input Image



Noisy Image



Removed Noise

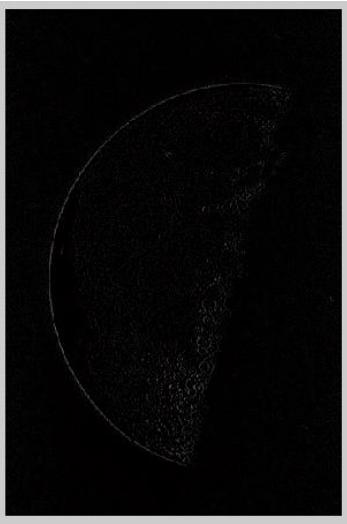
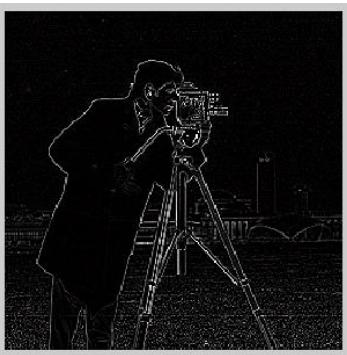
MATLAB EXERCISE

EXERCISE QUESTIONS

Q1 Make a script file. Now write the code to read image `moon.tif` and `cameraman.tif`. Make a Laplacian filter with $\alpha = 0$. Apply this filter on both the images to get derivative images . Now subtract the derivative images from original images to get sharpened images and show four images on two figures (one figure for `moon.tif` and `cameraman.tif` each). Each figure should have original and sharpened image. Do you see the sharpness?

```
clc  
clear  
f=imread('cameraman.tif');  
g=imread('moon.tif');  
w=fspecial('laplacian',0);  
g1=imfilter(g,w,'corr','replicate','same');  
f1=imfilter(f,w,'corr','replicate','same');  
f_sharp=f-f1;  
g_sharp=g-g1;  
figure  
subplot(1,3,1)  
imshow(f)  
subplot(1,3,2)  
imshow(f1)  
subplot(1,3,3)  
imshow(f_sharp)
```

```
figure  
subplot(1,3,1)  
imshow(g)  
subplot(1,3,2)  
imshow(g1)  
subplot(1,3,3)  
imshow(g_sharp)
```



Contradiction

f_sharp=f+f1;
g_sharp=g+g1; %Theory





Q2 Now create a Laplacian mask such that the values of mask are same as in last experiment but the signs are reversed. Now apply this mask on both images and get sharpened image (by addition). Show three images (original, with old mask, with new mask) on two figures (for both images). Do you see any improvement with new mask?

```

clc
clear
f=imread('cameraman.tif');
g=imread('moon.tif');
w1=fspecial('laplacian',0);
w2=-w1;
g1=imfilter(g,w1,'corr','replicate','same');
f1=imfilter(f,w1,'corr','replicate','same');
g2=imfilter(g,w2,'corr','replicate','same');
f2=imfilter(f,w2,'corr','replicate','same');
f_sharp=f+f2;
g_sharp=g+g2;
figure
subplot(1,4,1)
imshow(f)
xlabel('Input Image')
subplot(1,4,2)

```

```
imshow(f1)
xlabel('old mask')
subplot(1,4,3)
imshow(f2)
xlabel('new mask')
subplot(1,4,4)
imshow(f_sharp)
xlabel('sharpened')

figure
subplot(1,4,1)
imshow(g)
xlabel('original')
subplot(1,4,2)
imshow(g1)
xlabel('old mask')
subplot(1,4,3)
imshow(g2)
xlabel('new mask')
subplot(1,4,4)
imshow(g_sharp)
xlabel('sharpened')

w1 =
0   1   0
1  -4   1
0   1   0

w2 =
0  -1   0
-1   4  -1
0  -1   0
```



Q3 Now make two masks $w1 = [0 -1 0; -1 4 -1; 0 -1 0]$ and $w2 = [-1 -1 -1; -1 8 -1; -1 -1 -1]$. Now apply this mask on both images and show original and sharpened images for both masks (on one figure) and for both images (on different figures). Which mask is better?

clc

clear

```
f=imread('cameraman.tif');
g=imread('moon.tif');
w1=[0 -1 0 ; -1 4 -1 ; 0 -1 0];
w2=[-1 -1 -1 ; -1 8 -1; -1 -1 -1];
g1=imfilter(g,w1,'corr','replicate','same');
f1=imfilter(f,w1,'corr','replicate','same');
g2=imfilter(g,w2,'corr','replicate','same');
f2=imfilter(f,w2,'corr','replicate','same');
f_sharp=f+f2;
g_sharp=g+g2;
figure
subplot(1,4,1)
```

```
imshow(f)
xlabel('Input Image')
subplot(1,4,2)
imshow(f1)
xlabel('w1')
subplot(1,4,3)
imshow(f2)
xlabel('w2')
subplot(1,4,4)
imshow(f_sharp)
xlabel('sharpened')

figure
subplot(1,4,1)
imshow(g)
xlabel('original')
subplot(1,4,2)
imshow(g1)
xlabel('w1')
subplot(1,4,3)
imshow(g2)
xlabel('w2')
subplot(1,4,4)
imshow(g_sharp)
xlabel('sharpened')
```



Input Image



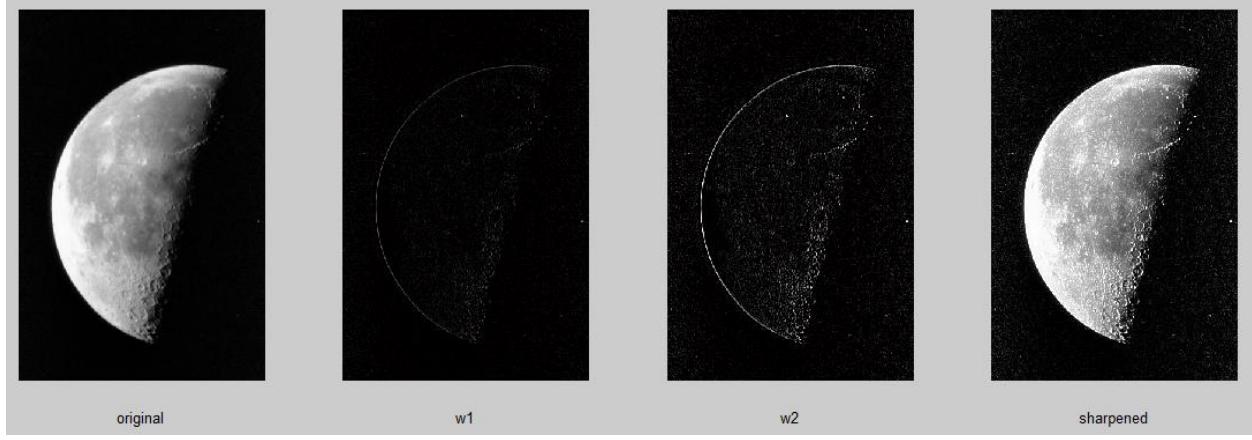
w1



w2



sharpened



An image can also be made sharp by using unsharp filtering. In unsharp filtering we create a mask by subtracting the blurred image from original and then we add that mask to the original image to get a sharpened image.

Q4 Read an image `eight.tif`. Now create a blurred image using average filtering. Subtract the blurred image from original to get mask. Now add this mask to original image to get sharp image. Now show both original and sharp image

`clc`

`clear`

```
f=imread('eight.tif');
```

```
w=ones(3,3)/3^2;
```

```
g=imfilter(f,w,'corr','replicate','same');
```

```
edge=f-g;
```

```
sharp=f+edge;
```

```
subplot(2,2,1)
```

```
imshow(f)
```

```
xlabel('input Image');
```

```
subplot(2,2,2)
```

```
imshow(g)
```

```
xlabel('blur');
```

```

subplot(2,2,3)
imshow(edge)
xlabel('edge mask');

subplot(2,2,4)
imshow(sharp)
xlabel('sharpened');

```



Q5 Read an image `eight.tif`. Add salt & pepper noise to this image. Now apply both averaging and median filtering on the noisy image. Show original, noisy , average filtered and median filtered images on one figure. Which filter performs better. (Note: You can use the `padopt as symmetric` in `medfilt2` to remove the noise from borders of image).

```

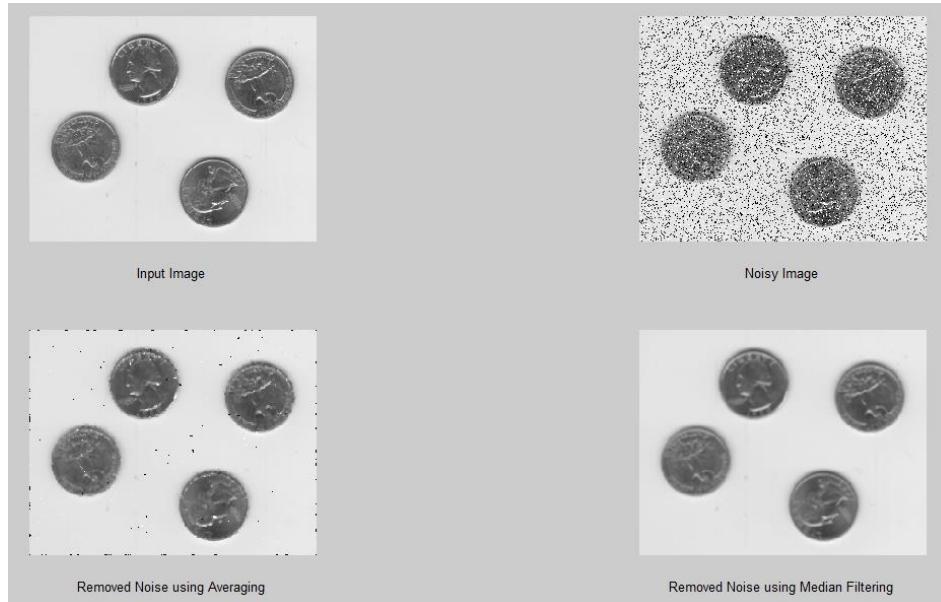
clc
clear
i=imread('eight.tif');
g=imnoise(i,'salt & pepper',0.2);
g1=medfilt2(g);
w=ones(3,3)/3^2;
g2=imfilter(i,w,'corr','symmetric','same')
subplot(2,2,1)
imshow(i)
xlabel('Input Image')
subplot(2,2,2)

```

```

imshow(g)
xlabel('Noisy Image')
subplot(2,2,3)
imshow(g1)
xlabel('Removed Noise using Averaging')
subplot(2,2,4)
imshow(g2)
xlabel('Removed Noise using Median Filtering')

```



**To get
morphological operations**

**Experiment#8:
familiar with**

- **Experiment Text**
 - i. **Morphological Image Processing**
 - ii. **Dilation and Erosion**
- **Lab Exercise**
- **Exercise Questions**

EXPERIMENT TEXT:

1 Morphological Image Processing

The word morphology commonly deals with branch of biology that deals with form and structure of animals and plants. For image processing the term mathematical morphology deals with extracting image components that are useful in description and representation of a region shape, boundary, skeleton etc. Morphological processes also deal with filtering, thinning and pruning.

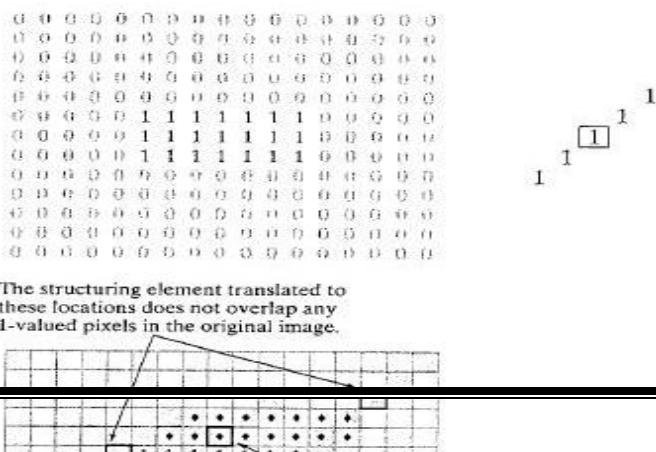
2 Dilation and Erosion

The operations dilation and erosion are fundamental to morphological image processing.

2.1 Dilation

Dilation is process that grows or thickens an object in an image. The specific manner and amount of thickness is controlled by structuring element (SE). Figure 1 shows an example of dilation. The top left part of the figure shows a simple binary image containing an object (object is represented by 1's).

The top right of figure shows a diagonal structuring element. SEs are normally represented as a combination of 1s and 0s in the form of a rectangle but sometimes we only show 1s if it is more convenient. Also the origin of the SE must also be specified and in the figure it is specified by a black outline. The middle part of the figure graphically depicts the dilation process as origin of SE moves through the image. The output image has 1 at each location of the origin such that the SE overlaps with atleast one 1-valued pixel of the input image.



Mathematically dilation is defined in terms of set operations. The dilation of image A by structuring element B is written as $A \oplus B$ and is defined as

$$A \oplus B = \{z | (\hat{B})_z \cap A \neq \phi\}$$

In words, dilation of A by B is the set of all SE origin locations where the reflected and translated B overlaps atleast some portion of A. Since the SE in this case is symmetric about its origin the reflection does not change its shape.

MATLAB built in function for dilation is `imdilate` and its syntax is

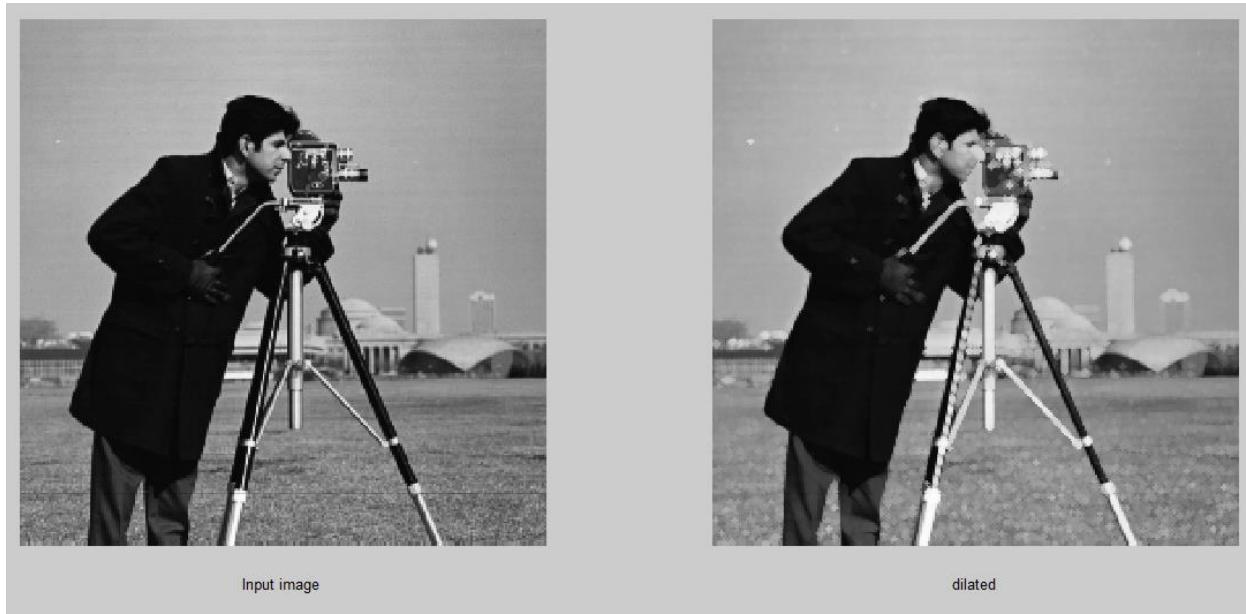
$$f1 = \text{imdilate}(f, B)$$

```
f=imread('cameraman.tif');
```

```

se=[0 1 0;1 1 1;0 1 0];
d=imdilate(f,se);
subplot(1,2,1)
imshow(f);
xlabel('Input image')
subplot(1,2,2)
imshow(d)
xlabel('dilated')

```



where f , $f1$ are input and output binary images while B is a structuring element.

MATLAB has a built in function **strel** for creating SEs. This function has a general syntax

$$se = \text{strel}(\text{shape}, \text{parameter});$$

where shape is a string specifying desired shape and parameters specify information about the shape. e.g. the shape could be diamond, disk, rectangle, square etc. More information about shapes and parameters can be found using help strel.

```

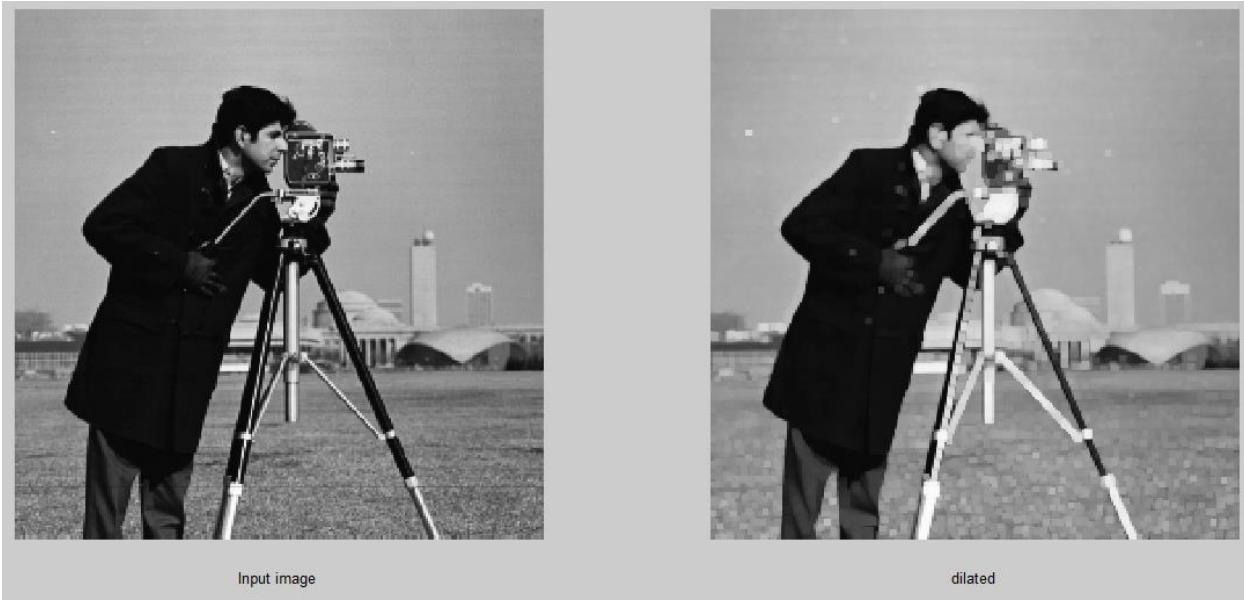
f=imread('cameraman.tif');
se=strel('rectangle',[3 3])
d=imdilate(f,se);
subplot(1,2,1)

```

```

imshow(f);
xlabel('Input image')
subplot(1,2,2)
imshow(d)
xlabel('dilated')

```



```

se1 = strel('square',11)    % 11-by-11 square
se2 = strel('line',10,45)   % line, length 10, angle 45 degrees
se3 = strel('disk',15)      % disk, radius 15
se4 = strel('ball',15,5)    % ball, radius 15, height 5

```

2.2 Erosion

Erosion shrinks or thins objects in an image. Figure 2 shows an example of erosion. In erosion, the output image has a value 1 if at each location of origin of structuring element, the elements of SE overlap with only 1-valued pixels of input image. The erosion of A by B denoted as $A \ominus B$ is defined as

$$A \ominus B = \{z | (B)_z \cap A^c \neq \emptyset\}$$

Erosion of A by B is the set of all structuring element origin locations where the translated B has no overlap with background of A i.e B completely fits within 1's of A. Erosion is performed by function `imerode`.

```

f=imread('cameraman.tif');
se=[0 1 0;1 1 1;0 1 0];
d=imerode(f,se);

```

```
subplot(1,2,1)  
imshow(f);  
xlabel('Input image')  
subplot(1,2,2)  
imshow(d)  
xlabel('Erosion')
```



```
f=imread('cameraman.tif');  
se=strel('rectangle',[3 3])  
d=imerode(f,se);  
subplot(1,2,1)  
imshow(f);  
xlabel('Input image')  
subplot(1,2,2)  
imshow(d)  
xlabel('Erosion')
```



Input image

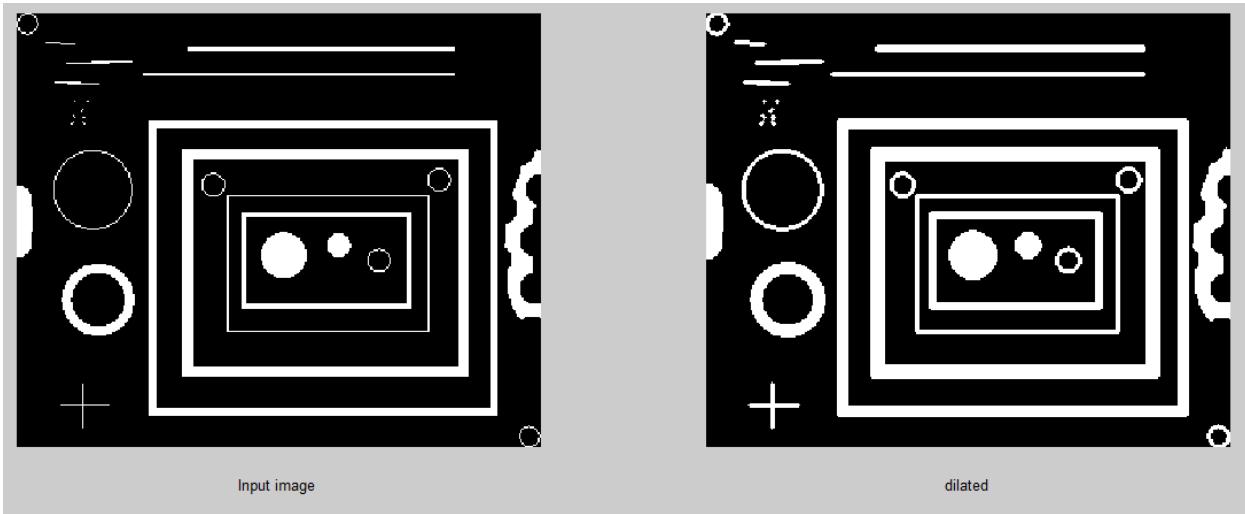


Erosion

EXERCISE QUESTIONS

Q1 Read an image blobs.png and apply dilation using structuring element $B = [0 \ 1 \ 0 ; 1 \ 1 \ 1 ; 0 \ 1 \ 0]$. Now show both original and dilated image on one figure. Do you see thickening in the new image?

```
clc  
clear  
f=imread('blobs.png');  
se=[0 1 0 ; 1 1 1 ; 0 1 0];  
d=imdilate(f,se);  
subplot(1,2,1)  
imshow(f);  
xlabel('Input image')  
subplot(1,2,2)  
imshow(d)  
xlabel('dilated')
```

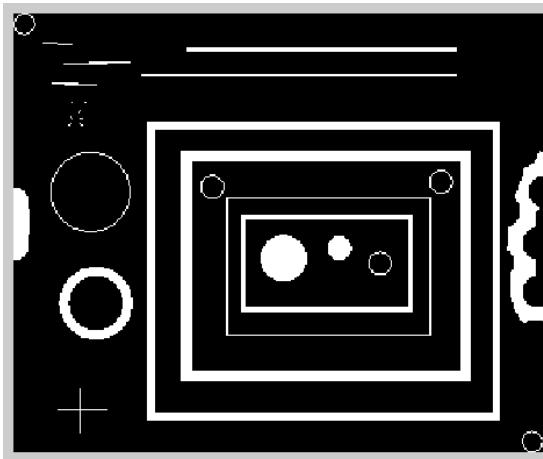


Q2 Read an image `blobs.png` and apply dilation using same structuring element as did in the last question but now SE should be defined using `strel`. (hint: use diamond shape). Now show both original and dilated image on one figure. You can change size of the structuring element to see the change in thickening.

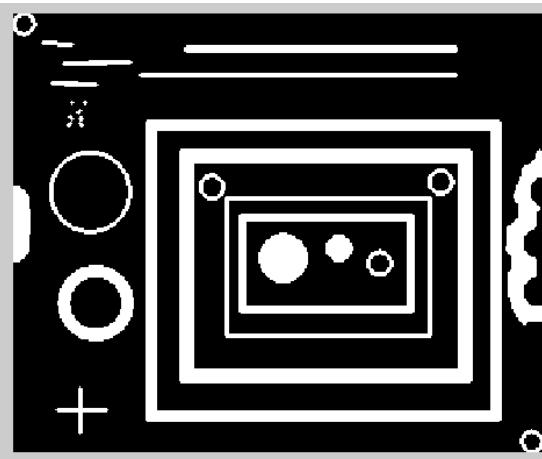
```

clc
clear
f=imread('blobs.png');
se=strel('diamond',1)
d=imdilate(f,se);
subplot(1,2,1)
imshow(f);
xlabel('Input image')
subplot(1,2,2)
imshow(d)
xlabel('dilated with R=1')

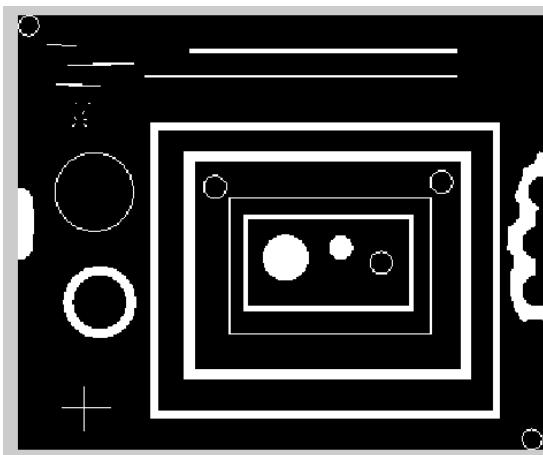
```



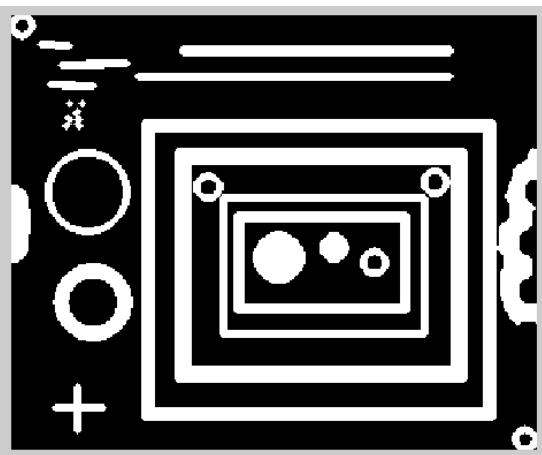
Input image



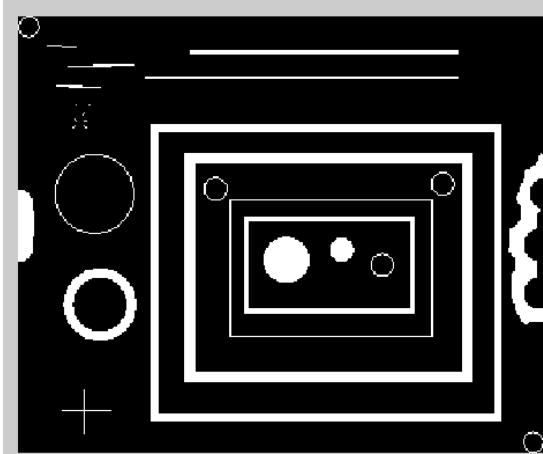
dilated with R=1



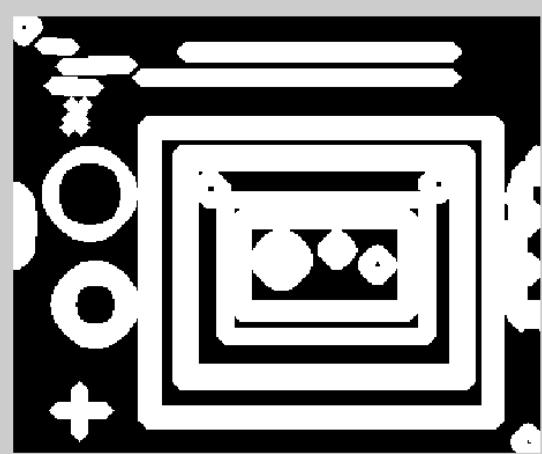
Input image



dilated with R=2



Input image



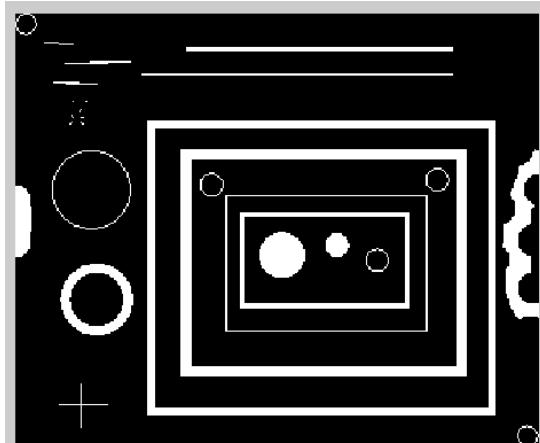
dilated with R=5

Q3 Read the image `blobs.png` and apply erosion using same structuring element as did in question 2. Now show both original and eroded image on one figure. What difference do you see? Now apply another SE on the same image but with a bigger size. Does increasing the size make a difference?

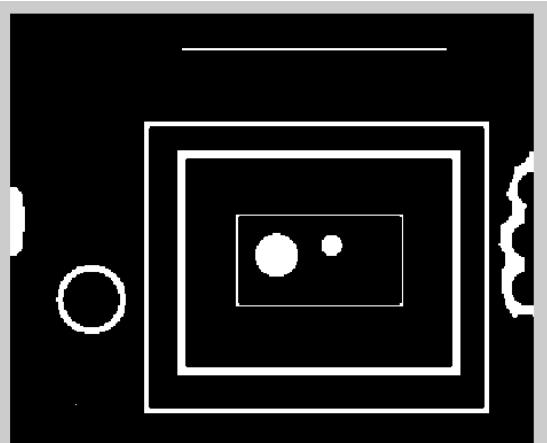
```

clc
clear
f=imread('blobs.png');
se=strel('diamond',1)
d=imerode(f,se);
subplot(1,2,1)
imshow(f);
xlabel('Input image')
subplot(1,2,2)
imshow(d)
xlabel('Erosion with R=1')

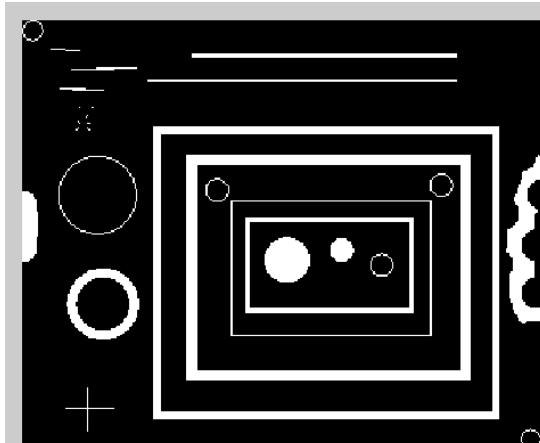
```



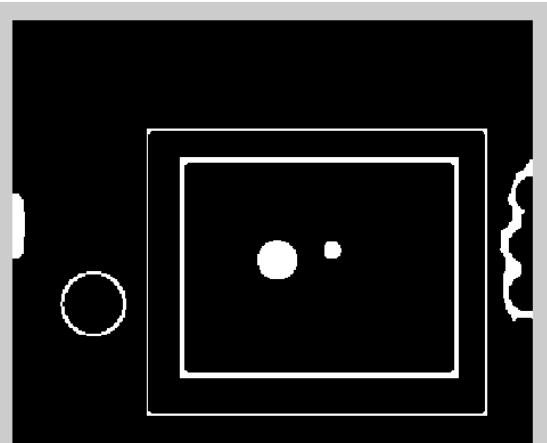
Input image



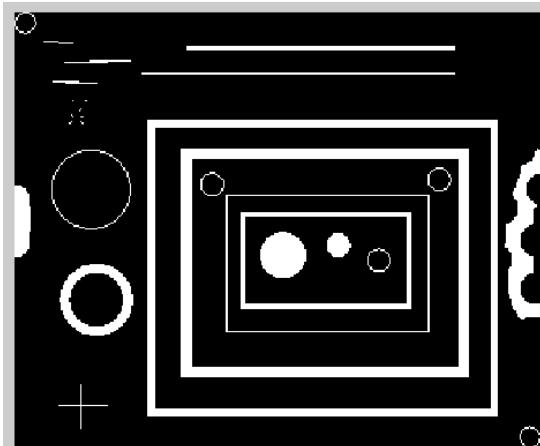
Erosion with R=1



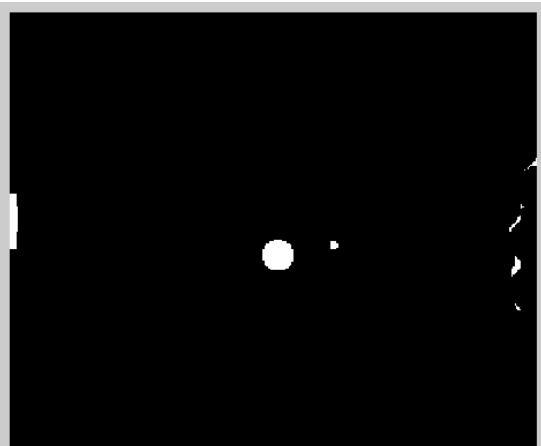
Input image



Erosion with R=2



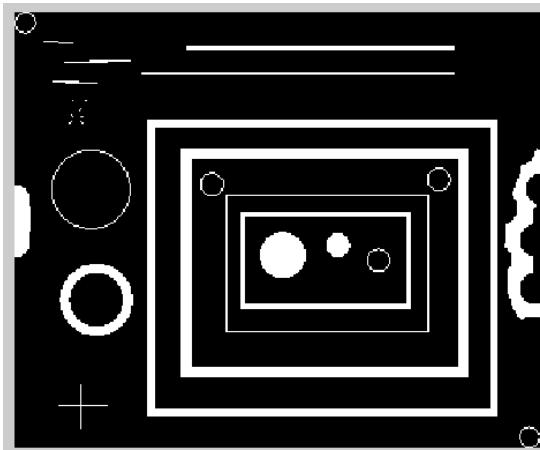
Input image



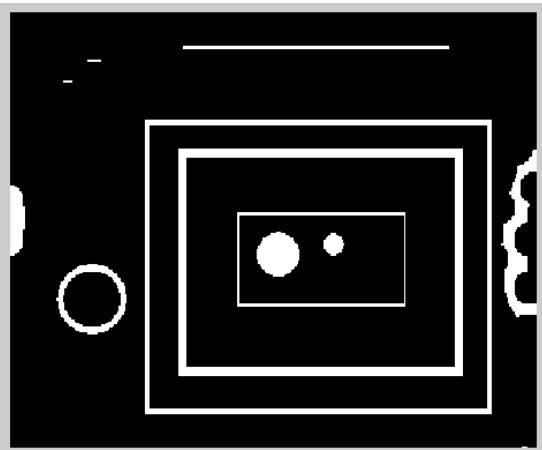
Erosion with R=5

Changing SE

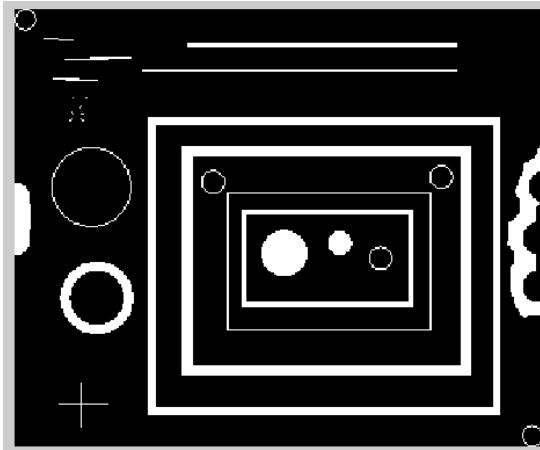
```
clc  
clear  
f=imread('blobs.png');  
se=strel('rectangle',[2 3])  
d=imerode(f,se);  
subplot(1,2,1)  
imshow(f);  
xlabel('Input image')  
subplot(1,2,2)  
imshow(d)  
xlabel('Erosion with Rectangle [2 3]')
```



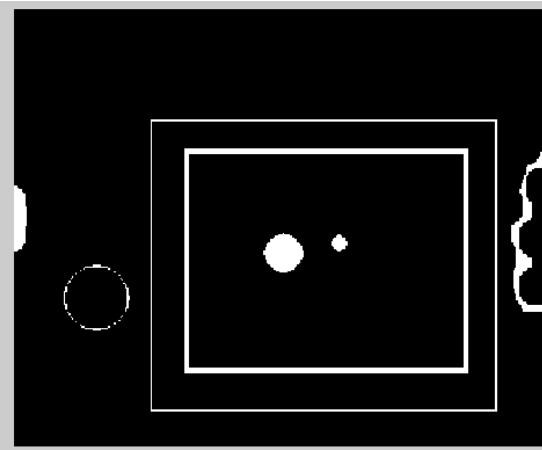
Input image



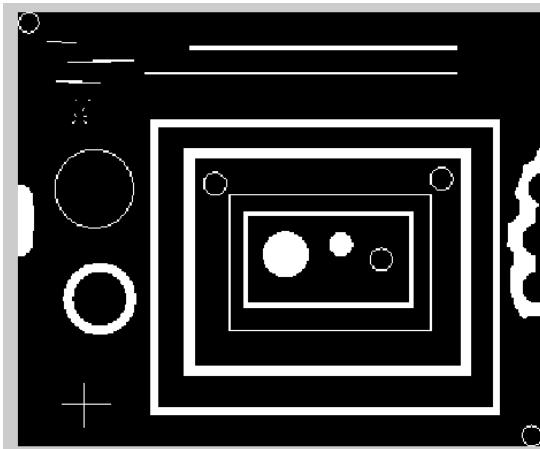
Erosion with Rectangle [2 3]



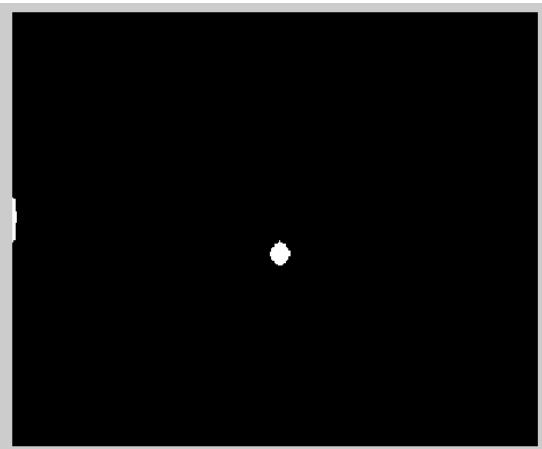
Input image



Erosion with Rectangle [5 5]



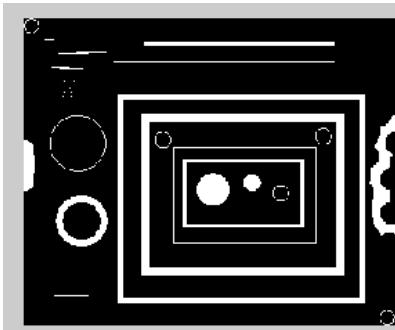
Input image



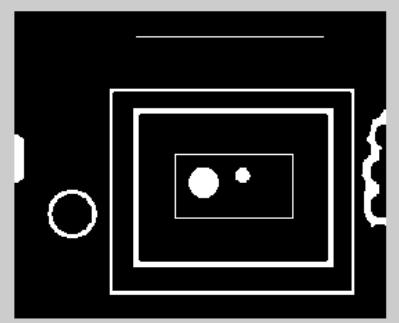
Erosion with Rectangle [10 15]

Q4 Read the image blobs.png and apply erosion and then dilation on the eroded image. Now show original, eroded and eroded+dilated image on one figure . What do you see?

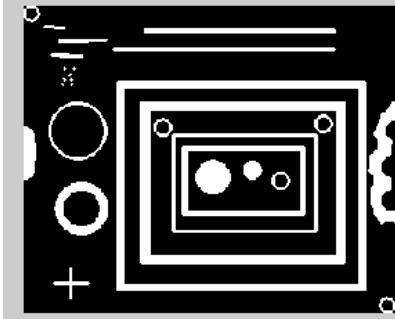
```
clc  
clear  
f=imread('blobs.png');  
se=strel('diamond',1)  
d=imerode(f,se);  
x=imdilate(f,se);  
y=imdilate(d,se);  
subplot(2,2,1)  
imshow(f);  
xlabel('Input image')  
subplot(2,2,2)  
imshow(d)  
xlabel('Erosion with Diamond R=1')  
subplot(2,2,3)  
imshow(x)  
xlabel('Dialation with Diamond R=1')  
subplot(2,2,4)  
imshow(y)  
xlabel('Dilation over Erosion')
```



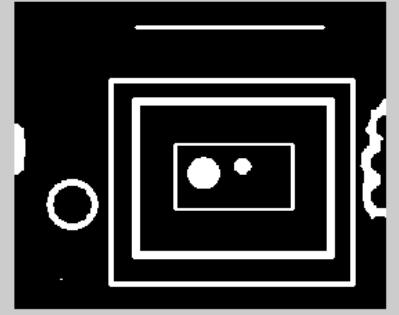
Input image



Erosion with Diamond R=1



Dilation with Diamond R=1



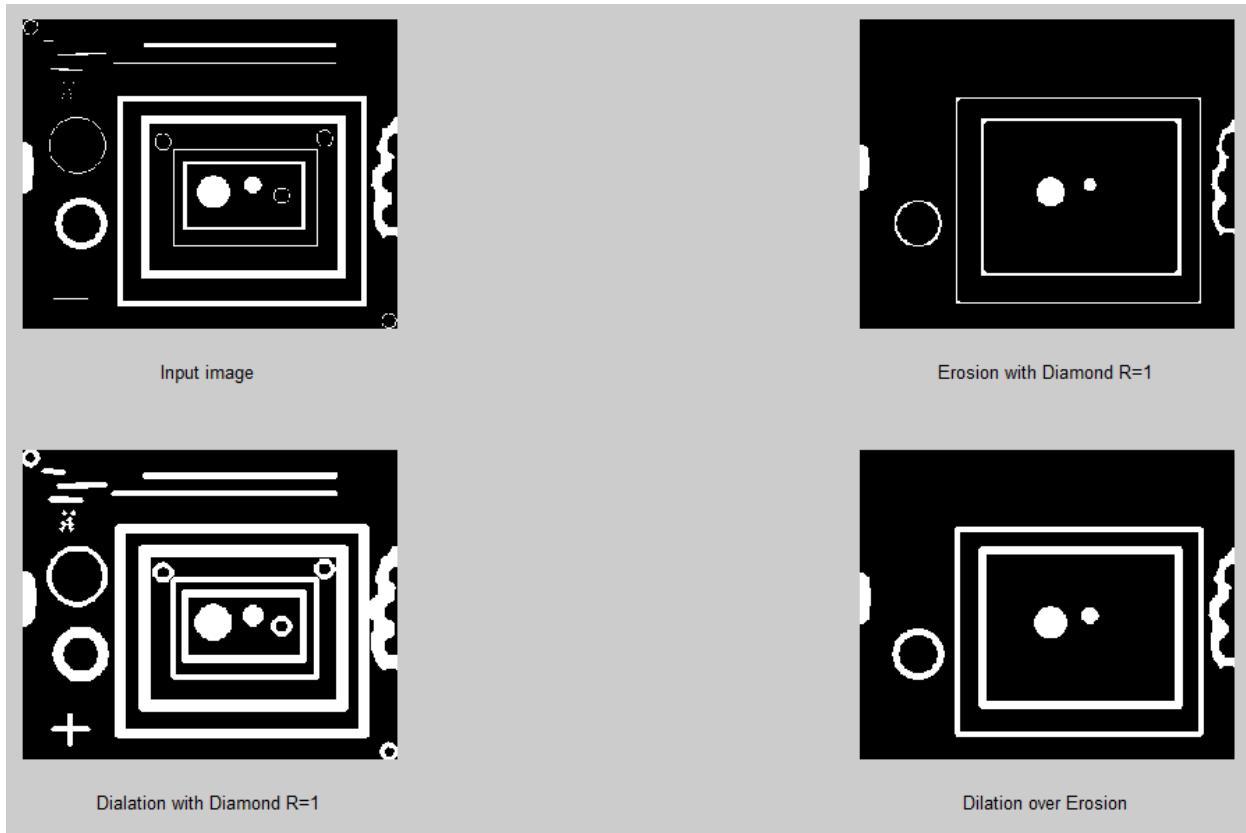
Dilation over Erosion

```
clc  
clear  
  
f=imread('blobs.png');  
se=strel('diamond',2)  
d=imerode(f,se);  
x=imdilate(f,se);  
y=imdilate(d,se);  
  
subplot(2,2,1)  
imshow(f);  
xlabel('Input image')  
  
subplot(2,2,2)  
imshow(d)  
xlabel('Erosion with Diamond R=1')  
  
subplot(2,2,3)  
imshow(x)  
xlabel('Dialation with Diamond R=1')  
  
subplot(2,2,4)
```

```

imshow(y)
xlabel('Dilation over Erosion')

```



MATLAB has a built in function for erosion followed by dilation (opening) and dilation followed by erosion (closing) by same SE. The built in function are imopen(f,B) and imclose(f,B)

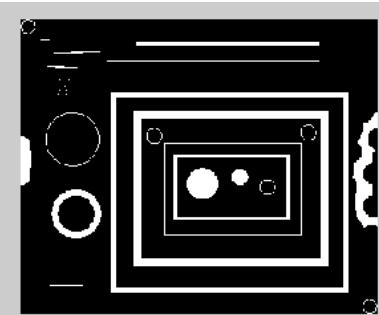
```
clc
```

```

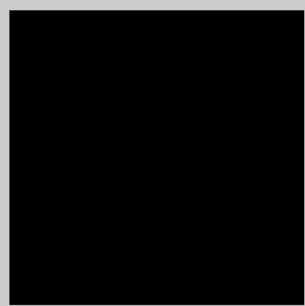
clear
f=imread('blobs.png');
se=strel('diamond',1)
subplot(2,2,1)
imshow(f);
xlabel('Input image')
o=imopen(f,se)
subplot(2,2,2)
imshow(o)
xlabel('Opening Diamond R=1')

```

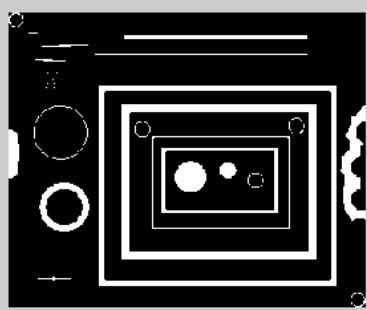
```
c=imclose(f,se)  
subplot(2,2,3)  
imshow(c)  
xlabel('Closing with Diamond R=1')
```



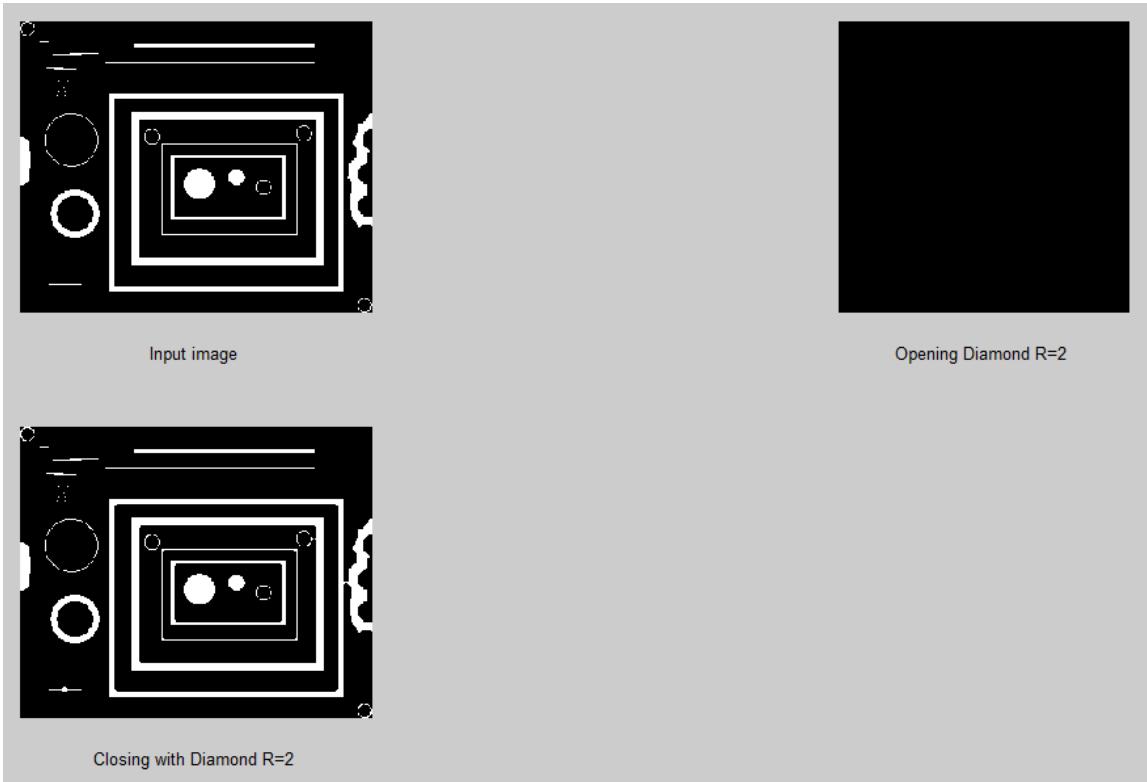
Input image



Opening Diamond R=1



Closing with Diamond R=1



Q5 Read the image blobs.png and apply erosion and then dilation on the eroded image. Now apply opening on original image. Now show original, eroded+dilated image and opened image on one figure. Are the last two images same?

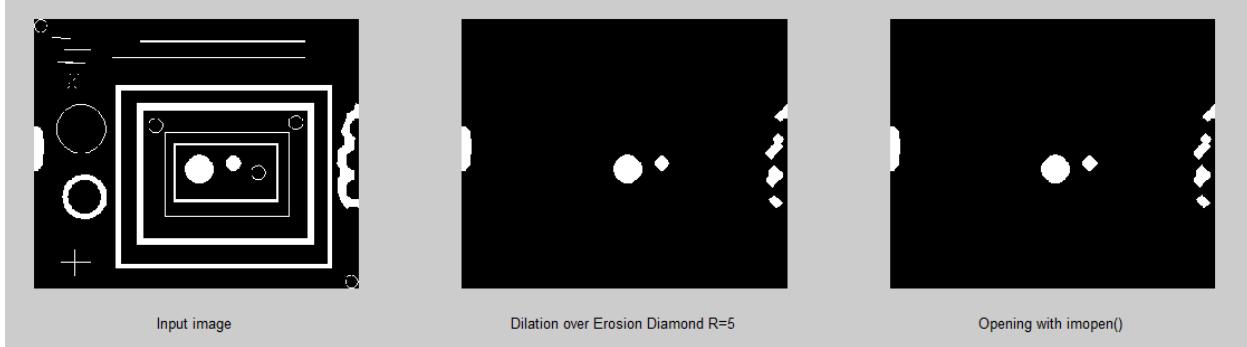
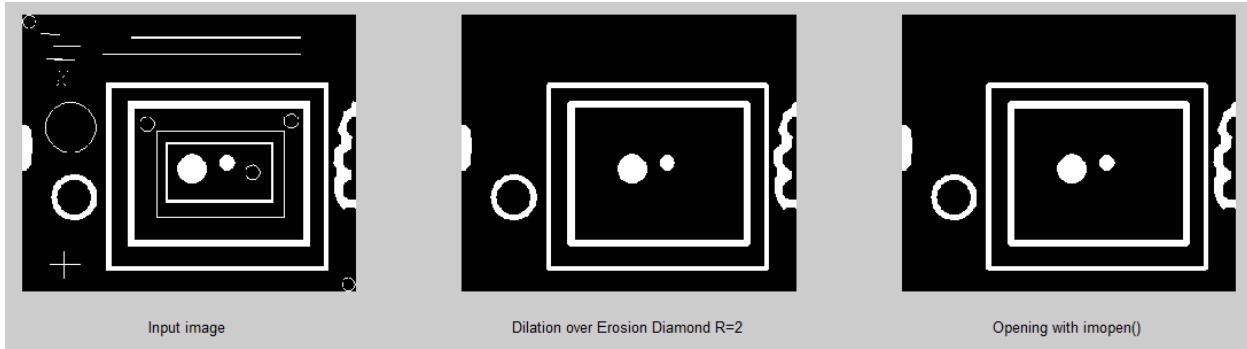
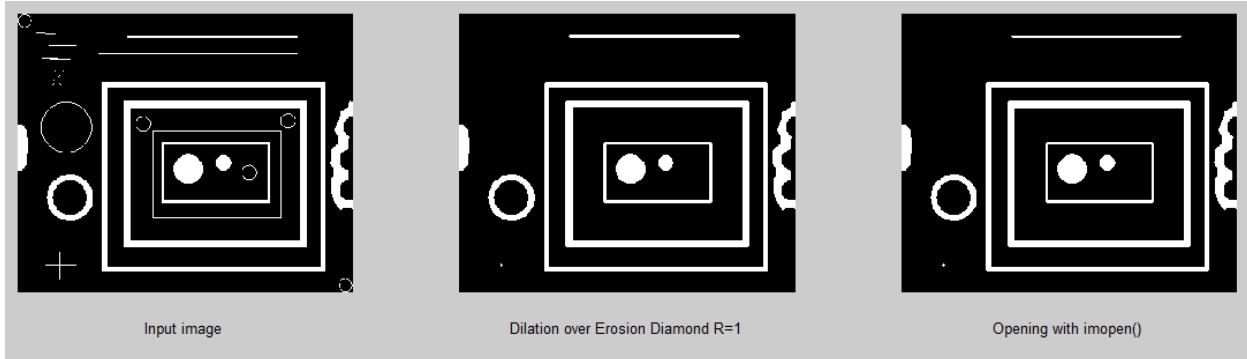
```

clc
clear
f=imread('blobs.png');
se=strel('diamond',1);
er=imerode(f,se);
di=imdilate(er,se);
op=imopen(f,se);
subplot(1,3,1)
imshow(f);
xlabel('Input image')
subplot(1,3,2)
imshow(di)
xlabel('Dilation over Erosion Diamond R=1')
subplot(1,3,3)

```

```
imshow(op)
```

```
xlabel('Opening with imopen()')
```



Now apply closing on original image and see what does it do. (Hint: Use a bigger SE for closing).

```
clc
```

```
clear
```

```
f=imread('blobs.png');
```

```
se=strel('diamond',1);
```

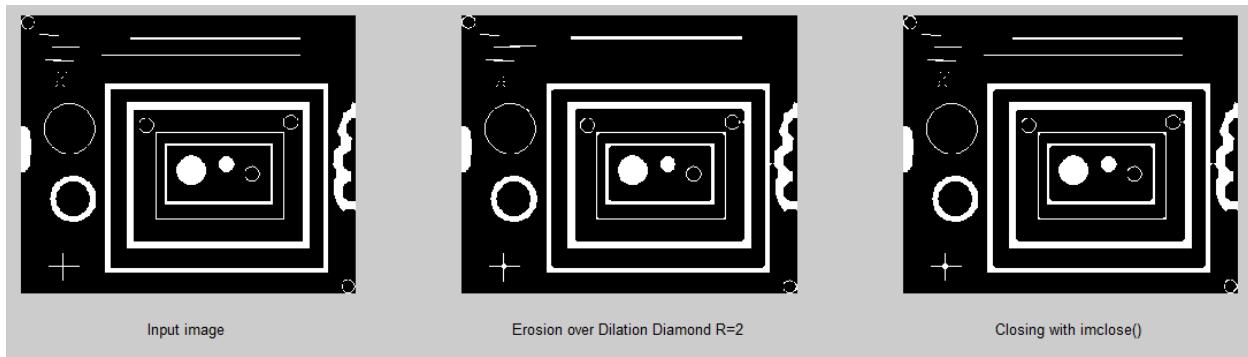
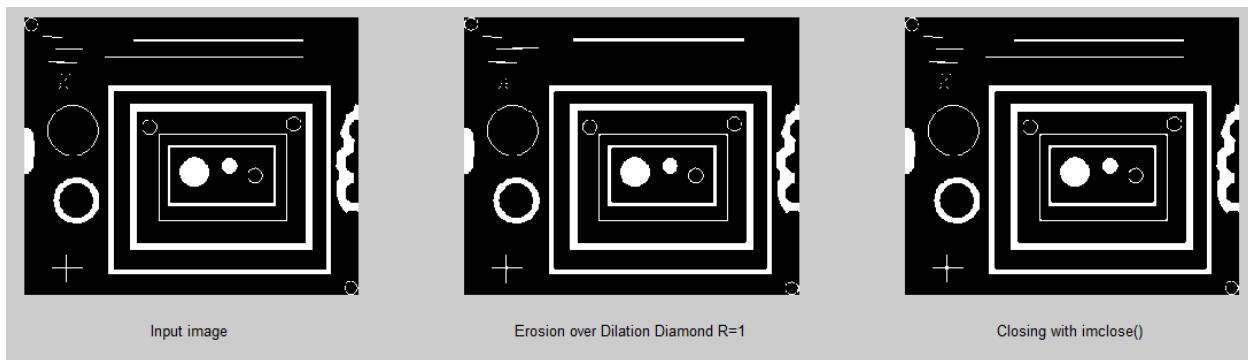
```
di=imdilate(f,se);
```

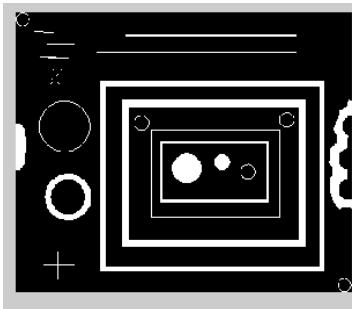
```
cl=imerode(di,se);
```

```

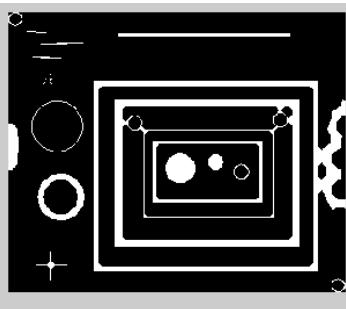
close=imclose(f,se);
subplot(1,3,1)
imshow(f);
xlabel('Input image')
subplot(1,3,2)
imshow(cl)
xlabel('Erosion over Dilation Diamond R=1')
subplot(1,3,3)
imshow(close)
xlabel('Closing with imclose()')

```

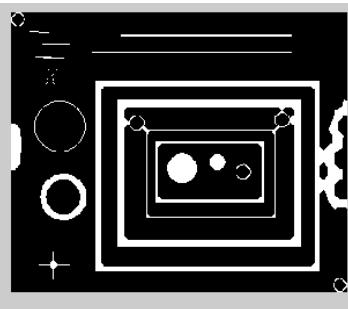




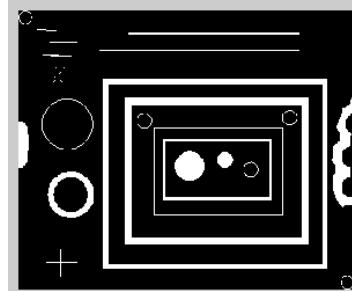
Input image



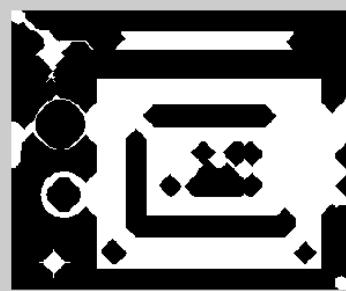
Erosion over Dilation Diamond R=3



Closing with imclose()



Input image



Erosion over Dilation Diamond R=10



Closing with imclose()

