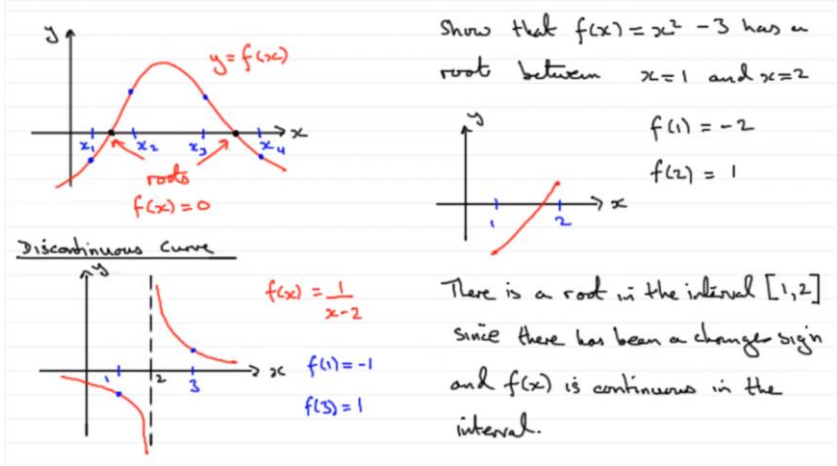
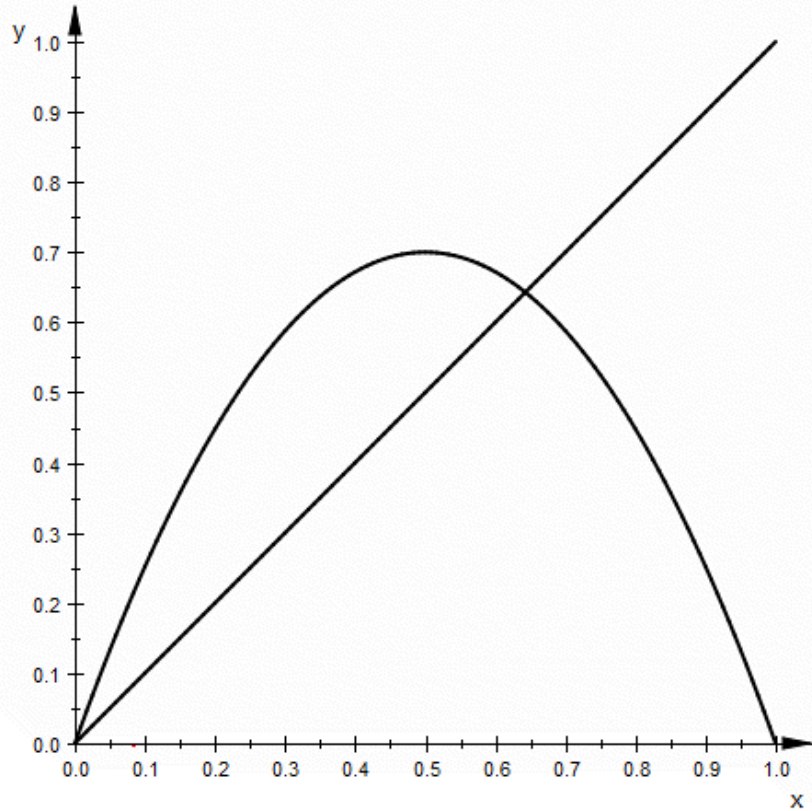


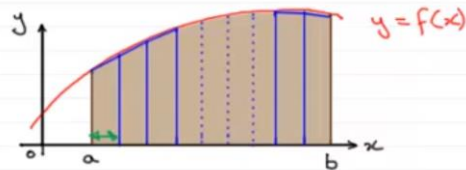
I - Numerical Methods

<p>How is change of sign used to find roots? And when does it not work / fail?</p>	<ul style="list-style-type: none"> Look for a change of sign between 2 points. Fails when... <ul style="list-style-type: none"> The interval was not narrow enough, captured an even number of roots (including repeated roots). The graph is discontinuous in the interval. <div data-bbox="586 596 1419 1058">  </div>
<p>When does an iteration converge? How can this be drawn?</p>	<p>Let $g(x)$ have a solution α</p> <div data-bbox="597 1142 1419 1268" style="background-color: #e0f0ff; padding: 10px;"> <p>Key point</p> <p>If $-1 < g'(x) < 1$ for all x in an interval which contains α and the starting value x_1, then $x_{n+1} = g(x_n)$ converges.</p> </div> <p>An animation of the cobweb is drawn below:</p>



This works since finding the point of intersection is the same as finding roots.

What is the trapezium rule?



$$\int_a^b f(x) dx = \text{Area}$$

$$\text{Area} = \frac{\text{width of strip}}{2} \left[\text{1st height} + 2(\text{sum of middle heights}) + \text{last height} \right]$$