

## G & H - Differentiation & Integration

<p>What are the derivatives of <math>\sin(kx)</math> and <math>\cos(kx)</math>?</p>	<table> <tr> <th data-bbox="591 394 1003 457"><math>f(x)</math></th><th data-bbox="1003 394 1417 457"><math>f'(x)</math></th></tr> <tr> <td data-bbox="591 457 1003 520"><math>\sin(kx)</math></td><td data-bbox="1003 457 1417 520"><math>k\cos(kx)</math></td></tr> <tr> <td data-bbox="591 520 1003 583"><math>\cos(kx)</math></td><td data-bbox="1003 520 1417 583"><math>-k\sin(kx)</math></td></tr> </table>	$f(x)$	$f'(x)$	$\sin(kx)$	$k\cos(kx)$	$\cos(kx)$	$-k\sin(kx)$
$f(x)$	$f'(x)$						
$\sin(kx)$	$k\cos(kx)$						
$\cos(kx)$	$-k\sin(kx)$						
<p>What does it mean when <math>f''(x) &lt; 0, = 0, &gt; 0</math>? And how do you find points of inflection?</p>	<ul style="list-style-type: none"> <li>• <math>f''(x) &gt; 0 \Rightarrow \text{concave} \Rightarrow \text{maximum point.}</math></li> <li>• <math>f''(x) = 0 \Rightarrow</math> <b>MAYBE</b> a point of inflection <b>YET</b> point of inflection <math>\Rightarrow f''(x) = 0.</math> <ul style="list-style-type: none"> <li>○ To make sure you have a point, check for a change in concavity either side of the point (if so, is a point of inflection) and consider points where the <math>f''(x)</math> is undefined.</li> </ul> </li> <li>• <math>f''(x) &lt; 0 \Rightarrow \text{convex} \Rightarrow \text{minimum point.}</math></li> </ul>						
<p>Using rectangles to integrate</p>	$\lim_{n \rightarrow \infty} \sum_{i=1}^n y_i \delta x = \int_a^b y \, dx$						