

# **Vector Intermediate Language (VIL)**

**Gas-Efficient Vector VM as a Smart-Contract in Rust / Stylus (WASM)**

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December 1, 2025

# 1 Introduction: The VM<sup>2</sup> Architecture

The Vector — Language (VIL) Virtual Machine represents a modern approach to deploying complex mathematical and financial logic onto the Arbitrum ecosystem using Rust / Stylus.

This architecture is a VM<sup>2</sup>—a Virtual Machine (VIL) running as a smart contract within Virtual Machine (WASM, hosted by Arbitrum node).

## 1.1 Motivation: Gas Efficiency through On-Chain Vector Operations

The primary innovation of VIL is the substantial gas savings realized by relocating complex vector algebra directly into the smart contract's state and execution context.

In traditional EVM smart contract systems, performing vector operations often requires:

1. Loading raw data from storage (SLOAD).
2. Storing raw data into storage (SSTORE).
3. (De)Serializing structured data (e.g. `Vec<u128>`) between contract calls.
4. Passing large data arrays as call data, incurring significant calldata gas costs.
5. Executing memory-intensive loops in the EVM, which is highly gas-inefficient for array processing.

**VIL eliminates these bottlenecks:**

- **Zero Serialization Overhead:** Vector data, stored as a pure binary blob (`Vec<Amount>`; where `Amount` is `u128` wrapper type), is loaded directly into the VIL execution environment within the same smart contract. All vector operations (addition, subtraction, multiplication, etc.) happen purely within the VIL execution context, **avoiding expensive EVM-based serialization and ABI encoding/decoding between logic steps.**
- **Optimal Data Flow:** Data is loaded **once** from a single storage slot (SLOAD), processed entirely, and stored back once (SSTORE), maximizing efficiency within the WASM environment.
- **WASM Optimization:** By executing the core logic via a simple, specialized instruction set (VIL), the underlying WASM runtime can execute vector mathematics far more efficiently than general-purpose EVM bytecode.

## 2 Development Workflow with the `devil!()` Proc Macro

Writing raw instruction bytes and operands for any VM is tedious and error-prone. The `devil!()` procedural macro simplifies VIL program creation by allowing developers to embed native VIL assembly code directly within Rust functions.

### 2.1 Macro Functionality

The `devil!()` macro transpiles the human-readable VIL assembly language into an efficient, executable bytecode array (`Vec<u8>`). This allows for:

- **Readability:** Programs are easy to audit and maintain.
- **Type Safety:** The underlying Rust environment ensures correct operand types (e.g., `u128` storage IDs, registry names) are used.
- **Concise Syntax:** Eliminates the need for manual byte array construction.

### 2.2 Usage Example

The following snippet demonstrates how a complex sequence of data retrieval and vector operations is expressed concisely using the macro:

```
use devil_macros::devil;

pub fn execute_buy_order(...) -> Vec<u8> {
    devil! {
        LDV          asset_weights_id      // Load from Blockchain (SLOAD)
        STR          _Weights              // Store into registry
        // ...

        LDR          _CappedIndexQuantity  // Load from registry
        LDM          _Weights              // Move from registry
        MUL          1                     // Multiply
        // ...

        LDM          _AssetQuantities      // Move from registry
        STV          executed_asset_quantities_id // Store into Blockchain (SSTORE)
    }
}
```

### 3 VIL Instruction Set Reference

The VIL instruction set is designed around the concept of a stack machine operating on two primary data types: **Scalar** (Amount) and **Vector** (Vec<Amount>), and additionally **Labels** (Vec<u128>), which enable *Join* operations (e.g. JADD, JUPD, JFLT). The instructions manipulate the stack and the internal registry (R0...Rn).

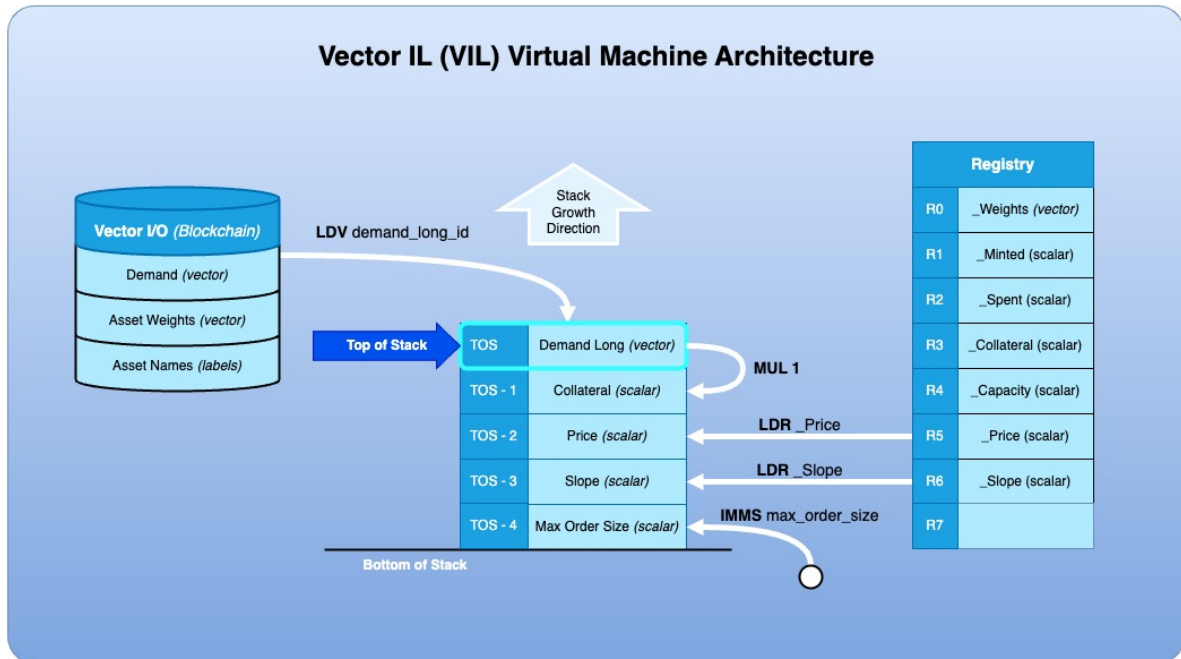


Figure 1: Conceptual VIL VM Stack and Data Flow.

### Instruction Set Quick Reference

Quick listing of instructions.

Table 1: VIL — Set Summary

Mnemonic	Brief Description
LDL	Load Labels object from VIO by ID. Pushes on TOS..
LDV	Load Vector object from VIO by ID. Pushes on TOS..
LDD	Load Duplicate (copy) of stack operand at $[T - pos]$ . Pushes on TOS..
LDR	Load value from Registry (R0-Rn). Pushes on TOS..
LDM	Load value moving it out of Registry (R0-Rn). Value is removed from registry. Pushes on TOS..
STL	Store Labels object into VIO. Consumes TOS..
STV	Store Vector object into VIO. Consumes TOS..
STR	Store into Registry (R0-Rn). Consumes TOS..
PKV	Pack 'count' values from stack into a new Vector. Consumes 'count' operands from TOS, and replaces them with Vector..

Table 1 – Continued from previous page

Mnemonic	Brief Description
PKL	Pack 'count' values from stack into a new Labels object. Consumes 'count' operands from TOS, and replaces them with Labels..
UNPK	Unpack a Vector/Labels object onto the stack. Consumes TOS, and replaces with its components..
VPUSH	Push a scalar onto the Vector (TOS). In-place updates Vector on TOS, appending new component at the end..
VPOP	Pop a scalar from the Vector (TOS). In-place updates Vector on TOS, removing last component..
T	Transpose 'count' vectors on stack $[V1, V2] \rightarrow [T1, T2]$ . In-place updates 'count' operands from TOS by performing transform..
LUNION	Union of two Labels operands (TOS and T-pos). Pushes on TOS..
LPUSH	Push a label value onto the Labels object (TOS). In-place updates Labels on TOS, appending new component at the end..
LPOP	Pop a label value from the Labels object (TOS). In-place updates Labels on TOS, removing last component..
JUPD	Update using Labels. Expands vector at $[TOS - pos\_B]$ using labels at $[TOS - lab\_B]$ to match labels of TOS at $[TOS - lab\_A]$ . In-place updates TOS. Consumes TOS..
JADD	Add using Labels. Expands vector at $[TOS - pos\_B]$ using labels at $[TOS - lab\_B]$ to match labels of TOS at $[TOS - lab\_A]$ . In-place updates TOS. Consumes TOS..
JFLT	Filter using Labels. Expands vector at $[TOS - 1]$ using labels at $[T - lab\_B]$ to match labels of TOS at $[T - lab\_A]$ . In-place updates TOS. Does not consume other operands..
ADD	Add TOS by operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
SUB	Subtract TOS by operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
SSB	Saturating subtract TOS by operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
MUL	Multiply TOS by operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
DIV	Divide TOS by operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
SQRT	Square root of TOS (scalar or component-wise vector). Works with vectors and scalars. In-place updates operand on TOS..
MIN	Min between TOS and operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
MAX	Max between TOS and operand at $[T - pos]$ . Works with vectors and scalars. In-place updates operand on TOS. Does not consume the other operand..
VSUM	Sum of all vector components. Pushes on TOS. Does not consume the operand..
VMIN	Minimum value found within vector components. Pushes on TOS. Does not consume the operand..
VMAX	Maximum value found within vector components. Pushes on TOS. Does not consume the operand..

Table 1 – Continued from previous page

<b>Mnemonic</b>	<b>Brief Description</b>
IMMS	Push immediate Scalar value on stack.
IMML	Push immediate Label value on stack.
ZEROS	Create Vector of zeros matching length of Labels at $[T - pos]$ . Pushes on TOS. Does not consume the operand..
ONES	Create Vector of ones matching length of Labels at $[T - pos]$ . Pushes on TOS. Does not consume the operand..
POPn	Pop 'n' values from the stack.
SWAP	Swap TOS with operand at $[T - n]$ .
B	Call sub-routine stored as Labels at 'prg_id', supplying 'N' inputs and taking 'M' outputs from stack. 'N' inputs are consumed from stack. 'M' outputs are moved from sub-routine's TOS to caller's TOS..
FOLD	Fold (iterate) over vector/label operands. Same as 'B' except sub-routine is called repeatedly over components of Vector at TOS..

## 3.1 Data Loading & Stack Access (Opcode 10..15)

### 3.1.1 LDL — Load Labels from Storage

Load (`Labels`) object by *ID* from *Vector I/O (VIO)*.

#### Notice

This is relatively gas-expensive operation as it will load binary blob from *Blockchain* using underlying (`SLOAD`) operation.

#### Operands

- `labels_id`: `u128` – An *ID* of the *Labels* object (*vector storage slot*).

#### Stack Args

- (*no stack args*).

#### Return

- `[TOS]`: `Labels` – *Labels* object loaded from vector storage.

#### Usage Example

```
LDL    asset_names_id
```

Load *Labels* with 'asset\_names\_id' ID from vector storage.

### 3.1.2 LDV — Load Vector from Storage

Load (`Vector`) object by *ID* from *Vector I/O (VIO)*.

#### Notice

This is relatively gas-expensive operation as it will load binary blob from *Blockchain* using underlying (`SLOAD`) operation.

#### Operands

- `labels_id`: `u128` – An *ID* of the *Vector* object (*vector storage slot*).

#### Stack Args

- (*no stack args*).

#### Return

- `[TOS]`: `Vector` – *Vector* object loaded from vector storage.

#### Usage Example

```
LDV    asset_weights_id
```

Load *Vector* with 'asset\_weights\_id' ID from vector storage.



### 3.1.3 LDD — Load Duplicate from Stack

Load duplicate (copy) of stack operand at  $T - pos$ .

#### Notice

This is mildly gas-expensive operation, much less gas-expensive than load from vector storage, but still it requires cloning of a vector.

#### Operands

- $pos$ : `u8` – Stack position relative to TOS from where we want to duplicate an operand.

#### Stack Args

- $[TOS - pos]$  – Source operand to be cloned.

#### Return

- $[TOS]$  – Duplicate of the operand at  $TOS - pos$ .

#### Usage Example

```
LDD    3
```

Create a duplicate of the operand three levels deep on the stack.

### 3.1.4 LDR — Load Duplicate from Registry

Load duplicate (copy) from registry `reg`.

#### Notice

This is mildly gas-expensive operation, much less gas-expensive than load from vector storage, but still it requires cloning of a vector.

#### Operands

- `reg: u8` – Register number `0..num_registry`.

#### Stack Args

- *(no stack args)*.

#### Return

- `[TOS]` – Duplicate of the registry `reg`.

#### Usage Example

```
LDR    _AssetWeights
```

Create a duplicate of the register allocated for `_AssetWeights`.

The `_AssetWeights` is a convenience label we associate with some register when we use `devil!()` macro.

### 3.1.5 LDM — Load Moving from Register

Load value moving it out of registry `reg`.

#### Notice

This is highly gas-effective operation, as operand is moved from register onto stack without copying.

#### Operands

- `reg: u8` – Register number `0..num_registry`.

#### Stack Args

- *(no stack args)*.

#### Return

- `[TOS]` – Value moved out of the registry `reg`.

#### Usage Example

```
LDM    _MarketAssetPrices
```

Move `_MarketAssetPrices` value out of register, and place it on stack.

The `_MarketAssetPrices` is a convenience label we associate with some register when we use `devil!()` macro.

## 3.2 Data Storage & Register Access (Opcode 20..23)

### 3.2.1 STL — Store Labels into Storage

Store (Labels) object by *ID* into *Vector I/O (VIO)*.

#### Notice

This is relatively gas-expensive operation as it will store binary blob into *Blockchain* using underlying (SSTORE) operation.

#### Operands

- labels\_id: u128 – An *ID* of the *Labels* object (*vector storage slot*).

#### Stack Args

- [TOS] – Operand on stack to be moved into vector storage labels\_id.

#### Return

- (*stack shifted by one level*).

#### Usage Example

```
STL      market_asset_names_id
```

Pop value from stack [TOS] and store it into vector storage with 'market\_asset\_names' ID.

### 3.2.2 STV — Store Vector into Storage

Store (Vector) object by *ID* into *Vector I/O (VIO)*.

#### Notice

This is relatively gas-expensive operation as it will store binary blob into *Blockchain* using underlying (SSTORE) operation.

#### Operands

- `vector_id`: u128 – An *ID* of the *Vector* object (*vector storage slot*).

#### Stack Args

- [TOS] – Operand on stack to be moved into vector storage `vector_id`.

#### Return

- (*stack shifted by one level*).

#### Usage Example

```
STV      market_asset_prices
```

Pop value from stack [TOS] and store it into vector storage with 'market\_asset\_prices' ID.

### 3.2.3 STR — Store Moving into Registry

Move value from stack and store it into registry `reg`.

#### Notice

This is highly gas-effective operation, as operand is moved from stack into register without copying.

#### Operands

- `reg: u8` – Register number `0..num_registry`.

#### Stack Args

- `[TOS]` – Operand on stack to be moved into registry `reg`.

#### Return

- *(stack shifted by one level).*

#### Usage Example

```
STR    _AssetWeights
```

Pop value from stack `[TOS]` and store it in register allocated for `_AssetWeights`.

### 3.3 Data Structure Manipulation (Opcode 30..35)

#### 3.3.1 PKV — Pack Scalar values into Vector

Pack *count* *Scalar* type values from stack into a new *Vector*.

##### Operands

- *count*: *u8* – Number of stack levels starting from *[TOS]* that we want to pack into *Vector*.

##### Stack Args

- *[TOS]*: *Scalar* – Operand on stack to be packed as last element of resulting *Vector*.

...

- *[TOS - count]*: *Scalar* – Operand on stack to be packed as first element of resulting *Vector*.

##### Return

- *[TOS]* – *Vector* constructed from stack operands *[TOS - count]*, ..., *[TOS]*
- (*stack shifted by 'count' levels*).

##### Usage Example

```
LDR    _Capacity
LDR    _Price
LDR    _Slope
PKV    3
```

Load three values from registry: *\_Capacity*, *\_Price*, *\_Slope*, and then pack them into single *Vector*: *[\_Capacity, \_Price, \_Slope]*.

### 3.3.2 PKL — Pack Label values into Labels object

Pack *count* *Label* type values from stack into a new *Labels*.

#### Operands

- *count*: *u8* – Number of stack levels starting from *[TOS]* that we want to pack into *Labels*.

#### Stack Args

- *[TOS]*: *Label* – Operand on stack to be packed as last element of resulting *Labels*.
- ...
- *[TOS - count]*: *Label* – Operand on stack to be packed as first element of resulting *Labels*.

#### Return

- *[TOS]* – *Labels* constructed from stack operands *[TOS - count]*, ..., *[TOS]*
- (*stack shifted by 'count' levels*).

#### Usage Example

```
IMML    btc_label
IMML    eth_label
IMML    xrp_label
PKL     3
```

Load three *Label* constants: *btc\_label*, *eth\_label*, *xrp\_label*, and then pack them into single *Labels*: [*btc\_label*, *eth\_label*, *xrp\_label*].



### 3.3.3 UNPK — Unpack values from Vector / Labels

Unpack a *Vector / Labels* object onto the stack.

#### Operands

- (no operands)

#### Stack Args

- [TOS]: *Vector|Labels* – An object to be unpacked onto stack *Vector / Labels*: `[[0], ..., [count - 1]]`.

#### Return

- [TOS]: *Scalar|Label* – Component unpacked as last from *Vector / Labels*.
- ...
- [TOS - count]: *Scalar|Label* – Component unpacked as first from *Vector / Labels*.
  - (stack shifted by one level).

#### Usage Example

```
LDV    index_quote_id
UNPK
```

Load a *Vector* from vector storage with 'index\_quote\_id' ID, and unpack its components onto stack. Given that 'index\_quote\_id' points to a vector, the component of which are: [capacity, price, slope], the resulting stack will have structure: [(previous stack state) ..., capacity, price, slope], where the value of 'slope' will be on [TOS].

### 3.3.4 VPUSH — Push Scalar onto Vector

Pushes a scalar onto the *Vector*.

#### Notice

This is gas-efficient in-place operation, as it updates a *Vector* on [TOS], appending new component at the end.

#### Operands

- `scalar`: `Scalar` – Constant *Scalar* value to be pushed onto *Vector* at [TOS].

#### Stack Args

- [TOS]: `Vector[0..len]` – A *Vector* of length 'len'.

#### Return

- [TOS]: `Vector[0..len + 1]` – Resulting *Vector* of length  $len + 1$ .

#### Usage Example

```
LDV    weights_id
VPUSH  10.0
```

Load from storage a vector with 'weights\_id' ID, and push scalar constant 10.0 to the end of it.

**Note** This does not modify the vector in-storage, and only its on-stack copy is modified. To store this modified vector back into storage separate `STV` instruction is required.

### 3.3.5 VPOP — Pop Scalar from Vector

Pop a scalar from the *Vector*.

#### Notice

This is gas-efficient in-place operation, as it updates a *Vector* on [TOS], removing its last component.

#### Operands

- (no operands)

#### Stack Args

- [TOS]: `Vector[0..len]` – A *Vector* of length 'len'.

#### Return

- [TOS]: `Vector[0..len - 1]` – Resulting *Vector* of length  $len - 1$ .

#### Usage Example

```
LDV    weights_id
VPOP
```

Load from storage a vector with 'weights\_id' ID, and pop last element from the end of it.

**Note** This does not modify the vector in-storage, and only its on-stack copy is modified. To store this modified vector back into storage separate *STV* instruction is required.

### 3.3.6 T — Transpose Vectors on Stack

Perform matrix transposition of  $M$  vectors on the stack, each of length  $N$ .

$$\begin{pmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,N} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,N} \\ \vdots & \vdots & \ddots & \vdots \\ a_{M,1} & a_{M,2} & \cdots & a_{M,N} \end{pmatrix}^T \Rightarrow \begin{pmatrix} a_{1,1} & a_{2,1} & \cdots & a_{M,1} \\ a_{1,2} & a_{2,2} & \cdots & a_{M,2} \\ \vdots & \vdots & \ddots & \vdots \\ a_{1,N} & a_{2,N} & \cdots & a_{M,N} \end{pmatrix}$$

#### Notice

This is gas-efficient in-place operation, which updates  $M$  vectors on the stack.

#### Operands

- `count`: `u8` – Number of vectors on the stack to transpose together.

#### Stack Args

- `[TOS]`: `Vector` – A *Vector* of length '`len`'.
- ...
- `[TOS - count]`: `Vector` – A *Vector* of length '`len`'.

#### Return

- `[TOS]`: `Vector` – A *Vector* of length '`count`'.
- ...
- `[TOS - len]`: `Vector` – A *Vector* of length '`count`'.

#### Usage Example

```
LDV    index_a_quote_id
LDV    index_b_quote_id
LDV    index_c_quote_id
T      3
```

Load from vector storage three vectors with IDs:

```
index_a_quote_id, index_b_quote_id, index_c_quote_id,
```

and then transpose them into vectors:

```
[index_a_capacity, index_b_capacity, index_c_capacity],  
[index_a_price, index_b_price, index_c_price],  
[index_a_slope, index_b_slope, index_c_slope],
```

or simply:

```
capacities, prices, slopes.
```

## 3.4 Labels Manipulation (Opcode 40..46)

### 3.4.1 LUNION — Union of Lables

Union of two operands of *Labels* type.

#### Notice

This is gas-efficient in-place operation of complexity  $O(N + M)$ .

#### Operands

- `pos: u8`: Position on stack of the other *Labels* object relative to `[TOS]`.

#### Stack Args

- `[TOS]`: *Labels* – The *Labels* object to be extended.
- `[TOS - pos]`: *Labels* – The *Labels* objects containing additional labels.

#### Return

- `[TOS]` – Resulting *Labels* object containig original and additional labels.

#### Usage Example

```
LDL      asset_weights
LDL      market_asset_weights
LUNION    1
```

Load two objects of type *Labels* from storage with IDs: `asset_weights` and `market_asset_weights`, and then modify last labels on `[TOS]` `market_asset_weights` by adding labels from `[TOS - 1]` stack level `asset_weights`. Resulting labels will contain all original labels from `market_asset_weights` and new labels from `asset_weights`.

### 3.4.2 LPUSH — Push Label onto Labels

Pushes a *Label* onto the *Labels*.

#### Notice

This is gas-efficient in-place operation, as it updates a *Labels* on [TOS], appending new component at the end.

#### Operands

- `label`: *Label* – Constant *Label* to be pushed onto *Labels* at [TOS].

#### Stack Args

- [TOS]: `Labels[0..len]` – A *Labels* of length '`len`'.

#### Return

- [TOS]: `Labels[0..len + 1]` – Resulting *Labels* of length `len + 1`.

#### Usage Example

```
LDL    asset_names_id
LPUSH  eth_label
```

Load from storage the labels with 'asset\_names\_id' ID, and push label constant 'eth\_label' to the end of it.

**Note** This does not modify the labels in-storage, and only its on-stack copy is modified. To store this modified labels back into storage separate STL instruction is required.

### 3.4.3 LPOP — Pop Label from Labels

Pop a label from the *Labels*.

#### Notice

This is gas-efficient in-place operation, as it updates a *Labels* on [TOS], removing its last component.

#### Operands

- (no operands)

#### Stack Args

- [TOS]: *Labels*[0..*len*] – A *Labels* of length '*len*'.

#### Return

- [TOS]: *Labels*[0..*len* - 1] – Resulting *Labels* of length *len* - 1.

#### Usage Example

```
LDL    asset_names_id
VPOP
```

Load from storage the labels with 'asset\_names\_id' ID, and pop a label from the end of it.

**Note** This does not modify the labels in-storage, and only its on-stack copy is modified. To store this modified labels back into storage separate STL instruction is required.



### 3.4.4 JUPD — Update (Replace) by Joining on Labels

Update *Vector* on top of the stack ([TOS]) by replacing its selected components with values from another vector on stack at [TOS - pos\_B] joining on *Labels*.

#### Notice

This is an efficient operation of complexity  $O(N)$  (for contiguous overlaps) or  $O(N \times \log M)$  (for overlaps with gaps).

#### Operands

- pos\_B: u8 – Stack position of *VectorB* relative to [TOS].
- lab\_A: u8 – Stack position of *LabelsA* relative to [TOS].
- lab\_B: u8 – Stack position of *LabelsB* relative to [TOS].

#### Stack Args

- [TOS: Vector] – Vector A
- [TOS - pos\_B: Vector] – Vector B
- [TOS - lab\_A: Labels] – Labels A
- [TOS - lab\_B: Labels] – Labels B

#### Return

- [TOS: Vector]: – *VectorA* updated by replacing values from *VectorB* mapping them through projection of *LabelsB* onto *LabelsA*.

#### Usage Example

```
JUPD    2    4    5
```

Update vector on stack at [TOS] by replacing its selected components with components of a vector at [TOS - 2], using labels at [TOS - 4] for vector at [TOS], and using labels at [TOS - 5] for vector at [TOS - 2], where labels overlap.

### 3.4.5 JADD — Add by Joining on Labels

Add two *Vectors* joining on *Labels*. Expands vector at [TOS - pos\_B] using labels at [TOS - lab\_B] to match labels of vector at TOS located on stack at [TOS - lab\_A].

#### Notice

This is an efficient operation of complexity  $O(N)$  (for contiguous overlaps) or  $O(N \times \log M)$  (for overlaps with gaps).

#### Operands

- pos\_B: u8 – Stack position of *VectorB* relative to [TOS].
- lab\_A: u8 – Stack position of *LabelsA* relative to [TOS].
- lab\_B: u8 – Stack position of *LabelsB* relative to [TOS].

#### Stack Args

- [TOS: Vector] – *VectorA*
- [TOS - pos\_B: Vector] – *VectorB*
- [TOS - lab\_A: Labels] – *LabelsA*
- [TOS - lab\_B: Labels] – *LabelsB*

#### Return

- [TOS: Vector]: – *VectorA* updated by adding values from *VectorB* mapping them through projection of *LabelsB* onto *LabelsA*.

#### Usage Example

```
JADD    2    4    5
```

Add to vector on stack at [TOS] selected components of a vector at [TOS - 2], using labels at [TOS - 4] for vector at [TOS], and using labels at [TOS - 5] for vector at [TOS - 2], where labels overlap.

### 3.4.6 JFLT — Filter by Joining on Labels

Filter vector on stack at [TOS] retaining only components corresponding to labels at [TOS - lab\_B] using labels at [TOS - lab\_A] for vector at [TOS], and where labels overlap.

#### Notice

This is an efficient operation of complexity  $O(N)$  (for contiguous overlaps) or  $O(N \times \log M)$  (for overlaps with gaps).

#### Operands

- lab\_A: u8 – Stack position of *LabelsA* relative to [TOS].
- lab\_B: u8 – Stack position of *LabelsB* relative to [TOS].

#### Stack Args

- [TOS: Vector] – *VectorA*
- [TOS - lab\_A: Labels] – *LabelsA*
- [TOS - lab\_B: Labels] – *LabelsB*

#### Return

- [TOS: Vector]: – *VectorA* filtered by retaining components through projection of *LabelsB* onto *LabelsA*.

#### Usage Example

```
JFLT    4    5
```

Filter vector on stack at [TOS] retaining only components corresponding to labels at [TOS - 5] using labels at [TOS - 4] for vector at [TOS], and where labels overlap.

## 3.5 Arithmetic & Core Math (Opcode 50..55)

### 3.5.1 ADD — Addition

Add operand at [TOS] to operand at [TOS - pos].

$$[TOS] \leftarrow [TOS] + [TOS - pos]$$

#### Notes

- Works with vectors and scalars.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with addition.
- [TOS - pos: Vector|Scalar] – Second operand of addition.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

```
IMMS    3.0
IMMS    5.0
ADD     1
```

Add 3.0 to 5.0, and replace 5.0 with result of the addition (8.0).

### 3.5.2 SUB — Subtraction

Subtract from operand at [TOS] an operand at [TOS - pos].

#### Notes

- Works with vectors and scalars.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with subtraction.
- [TOS - pos: Vector|Scalar] – Second operand of subtraction.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

```
IMMS    3.0
IMMS    5.0
SUB     1
```

Subtract 3.0 from 5.0, and replace 5.0 with result of the subtraction (2.0).

### 3.5.3 SSB — Saturating Subtraction

Subtract from operand at `[TOS]` an operand at `[TOS - pos]` saturating to 0.

$$[TOS] \leftarrow \max([TOS] - [TOS - pos], 0)$$

#### Notes

- Works with vectors and scalars.
- In-place updates operand on `[TOS]`.
- Does not consume the other operand.

#### Operands

- `pos`: `u8` – Stack position relative to `[TOS]`.

#### Stack Args

- `[TOS: Vector|Scalar]` – Operand to be updated in-place, with saturating subtraction.
- `[TOS - pos: Vector|Scalar]` – Second operand of saturating subtraction.

#### Return

- `[TOS]` – Updated first operand.

#### Usage Example

IMMS	5.0
IMMS	3.0
SSB	1

Subtract 5.0 from 3.0 saturating at 0.0, and replace 3.0 with result of the saturating subtraction (0.0).

### 3.5.4 MUL — Multiplication

Multiply operand at [TOS] by operand at [TOS - pos].

$$[TOS] \leftarrow [TOS] \odot [TOS - pos]$$

#### Notes

- Works with vectors and scalars.
- Multiplication of two vectors is performed component-wise.
- Multiplication of vector by scalar is possible, but not scalar by vector as it is an in-place operation.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with multiplication.
- [TOS - pos: Vector|Scalar] – Second operand of multiplication.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

```
IMMS    3.0
IMMS    5.0
MUL     1
```

Multiply 3.0 by 5.0, and replace 5.0 with result of the multiplication (15.0).

### 3.5.5 DIV — Division

Divide operand at [TOS] by operand at [TOS - pos].

$$[TOS] \leftarrow \frac{[TOS]}{[TOS - pos]}$$

#### Notes

- Works with vectors and scalars.
- Division of two vectors is performed component-wise.
- Division of vector by scalar is possible, but not scalar by vector as it is an in-place operation.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with division.
- [TOS - pos: Vector|Scalar] – Second operand of division.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

```
IMMS    3.0
IMMS    15.0
DIV      1
```

Divide 15.0 by 3.0, and replace 15.0 with result of the multiplication (3.0).



### 3.5.6 Sqrt — Square Root

Take square root of [TOS].

$$[TOS] \leftarrow \sqrt{[TOS]}$$

#### Note

- Works with vectors and scalars.
- Square root of two vector is performed component-wise.
- In-place updates operand on TOS.

#### Notice

This operation is implemented using *Babylonian method* of  $O(\log k)$  complexity where  $k$  is number of bits. Since it is fixed point 128-bit number, this is constant  $O(1)$ .

#### Operands

- (no operands)

#### Stack Args

- [TOS: Vector|Scalar] – Operand of square root.

#### Return

- [TOS] – Result of square root.

#### Usage Example

```
IMMS    4.0
SQRT
```

Take square root of 4.0, and replace 4.0 with the result (2.0).

## 3.6 Logic & Comparison (Opcode 60..61)

### 3.6.1 MIN — Minimum

Take minimum between operand at [TOS] and operand at [TOS - pos].

$$[TOS] \leftarrow \min([TOS], [TOS - pos])$$

#### Notes

- Works with vectors and scalars.
- Minimum of two vectors is performed component-wise.
- Minimum of vector by scalar is possible, but not scalar by vector as it is an in-place operation.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with minimum.
- [TOS - pos: Vector|Scalar] – Second operand of minimum.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

IMMS	3.0
IMMS	5.0
MIN	1

Take minimum of 5.0 and 3.0, and replace 5.0 with result of the minimum (3.0).

### 3.6.2 MAX — Maximum

Take maximum between operand at [TOS] and operand at [TOS - pos].

$$[TOS] \leftarrow \max([TOS], [TOS - pos])$$

#### Notes

- Works with vectors and scalars.
- Maximum of two vectors is performed component-wise.
- Maximum of vector by scalar is possible, but not scalar by vector as it is an in-place operation.
- In-place updates operand on [TOS].
- Does not consume the other operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- [TOS: Vector|Scalar] – Operand to be updated in-place, with maximum.
- [TOS - pos: Vector|Scalar] – Second operand of maximum.

#### Return

- [TOS] – Updated first operand.

#### Usage Example

IMMS	3.0
IMMS	5.0
MAX	1

Take minimum of 5.0 and 3.0, and replace 5.0 with result of the minimum (5.0).

## 3.7 Vector Aggregation (Opcode 70..72)

### 3.7.1 `VSUM` — Sum of Vector components

Sum of all vector components. Pushes on TOS. Does not consume the operand.

#### Operands

- (no operands)

#### Stack Args

- `stack args = [TOS : Vector]: Input`

#### Return

- `result = [TOS : Scalar]: Output`

#### Usage Example

`VSUM`

### 3.7.2 VMIN — Minimum component of a Vector

Minimum value found within vector components. Pushes on TOS. Does not consume the operand.

#### Operands

- (no operands)

#### Stack Args

- `stack args = [TOS : Vector]: Input`

#### Return

- `result = [TOS : Scalar]: Output`

#### Usage Example

VMIN

### 3.7.3 VMAX — Maximum component of a Vector

Maximum value found within vector components. Pushes on TOS. Does not consume the operand.

#### Operands

- (no operands)

#### Stack Args

- `stack args = [TOS : Vector]: Input`

#### Return

- `result = [TOS : Scalar]: Output`

#### Usage Example

VMAX

## 3.8 Immediate Values & Vector Creation (Opcode 80..83)

### 3.8.1 IMMS — Push Scalar on Stack

Push immediate Scalar value on stack

#### Operands

- value: Scalar – Constant *Scalar* value to be pushed on stack.

#### Stack Args

- no stack args: Input

#### Return

- result =  $[TOS : Scalar]$ : Output

#### Usage Example

```
IMMS <immediate (scalar)>
```

### 3.8.2 IMML — Push Label on Stack

Push immediate Label value on stack

#### Operands

- value: Label – Constant *Label* value to be pushed on stack.

#### Stack Args

- no stack args: Input

#### Return

- result =  $[TOS : Label]$ : Output

#### Usage Example

```
IMML <immediate (label)>
```



### 3.8.3 ZEROS — Zero Vector

Create Vector of zeros matching length of Labels at  $[T - pos]$ . Pushes on TOS. Does not consume the operand.

#### Operands

- `pos: u8` – Stack position relative to `[TOS]`.

#### Stack Args

- `stack args = [TOS - pos : Vector|Labels]: Input`

#### Return

- `result = [TOS : Vector]: Output`

#### Usage Example

```
ZEROS pos
```

### 3.8.4 ONES — Unit Vector

Create Vector of ones matching length of Labels at  $[T - pos]$ . Pushes on TOS. Does not consume the operand.

#### Operands

- pos: u8 – Stack position relative to [TOS].

#### Stack Args

- stack args =  $[TOS - pos : Vector|Labels]$ : Input

#### Return

- result =  $[TOS : Vector]$ : Output

#### Usage Example

```
ONES pos
```

## 3.9 Stack Control & Program Flow (Opcode 90..94)

### 3.9.1 POPN — Pop levels from Stack

Pop 'n' values from the stack

#### Operands

- `count`: `u8` – Number of levels to pop.

#### Stack Args

- `stack args` =  $[B..., TOS - count, ..., TOS]$ : Input

#### Return

- `result` =  $[B...]$ : Output

#### Usage Example

```
POPN <count>
```

### 3.9.2 SWAP — Swap levels on Stack

Swap TOS with operand at  $[T - n]$

#### Operands

- `pos: u8` – Stack position relative to `[TOS]`.

#### Stack Args

- `stack args =  $[TOS - pos : 'A, TOS : 'B]$` : Input

#### Return

- `result =  $[TOS - pos : 'B, TOS : 'A]$` : Output

#### Usage Example

```
SWAP pos
```

### 3.9.3 B — Branch into stored procedure

Call sub-routine stored as *Code* at 'prg\_id', supplying 'N' inputs and taking 'M' outputs from stack.

The 'N' inputs are consumed from stack. 'M' outputs are moved from sub-routine's [TOS] to caller's [TOS].

#### Operands

- prg\_id: `u128` – An *ID* of the stored procedure *Code* object in vector storage.
- N: `u8` – Number of arguments to move from our stack to stack of the stored procedure before its execution.
- M: `u8` – Number of returned values to move back from stack of the stored procedure after its execution.
- R: `u8` – Number of registers to allocate for stored procedure before its execution.

#### Stack Args

- [TOS] – Last argument
- [...]
- [TOS - N] – First argument

#### Return

- [TOS] – Last returned value
- [...]
- [TOS - M] – First returned value

#### Usage Example

```
B    prg_id  N    M    R
```

### 3.9.4 FOLD — Apply stored procedure to all components

Fold (iterate) over vector/label operands.

The behaviour of the operation is the same as B except sub-routine is called repeatedly over components of Vector at [TOS].

#### Notice

This is gas-efficient method of innovation of stored procedure multiple times for batch of items.

#### Operands

- `prg_id`: `u128` – An *ID* of the stored procedure *Code* object in vector storage.
- `N`: `u8` – Number of arguments to move from our stack to stack of the stored procedure before its execution.
- `M`: `u8` – Number of returned values to move back from stack of the stored procedure after its execution.
- `R`: `u8` – Number of registers to allocate for stored procedure before its execution.

#### Stack Args

- `[TOS]`: `Vector|Labels` – Iterable object of type *Vector* or *Labels*.
- `[TOS - 1]` – Last argument
- `[...]`
- `[TOS - N - 1]` – First argument

#### Return

- `[TOS]` – Last returned value
- `[...]`
- `[TOS - M]` – First returned value

#### Usage Example

```
FOLD    prg_id N    M    R
```