1. Keras - MLPs on MNIST

2. Import Libraries

In [1]:

```
1 | # if you keras is not using tensorflow as backend set "KERAS_BACKEND=tensorflow" use the
 2 from keras.utils import np_utils
   from keras.datasets import mnist
4 from keras.optimizers import Adam, RMSprop, SGD
 5 from keras.layers import Dropout
   from keras.layers import Dense, Activation
   from keras.layers.normalization import BatchNormalization
7
   from keras.models import Sequential
9 from keras.initializers import RandomNormal
10 from keras.wrappers.scikit learn import KerasClassifier
11 | from sklearn.model_selection import GridSearchCV
   import seaborn as sns
   import matplotlib.pyplot as plt
13
14 | import numpy as np
15 import time
```

Using TensorFlow backend.

3. Plot Function

In [2]:

```
1 | # https://gist.github.com/greydanus/f6eee59eaf1d90fcb3b534a25362cea4
   # https://stackoverflow.com/a/14434334
   # this function is used to update the plots for each epoch and error
4
   def plt_dynamic(x, vy, ty, ax, colors=['b']):
        ax.plot(x, vy, 'b', label="Validation Loss")
 5
 6
        ax.plot(x, ty, 'r', label="Train Loss")
 7
       plt.legend()
 8
       plt.grid()
9
        fig.canvas.draw()
10
11
```

4. Data

In [3]:

```
# the data, shuffled and split between train and test sets
   (X_train, y_train), (X_test, y_test) = mnist.load_data()
 4
   print("Number of training examples :", X_train.shape[0], "and each image is of shape ()
   print("Number of training examples :", X_test.shape[0], "and each image is of shape (%)
 5
 6
   # if you observe the input shape its 2 dimensional vector
 7
 8
   # for each image we have a (28*28) vector
9
   # we will convert the (28*28) vector into single dimensional vector of 1 * 784
10
11
   X_train = X_train.reshape(X_train.shape[0], X_train.shape[1]*X_train.shape[2])
   X_test = X_test.reshape(X_test.shape[0], X_test.shape[1]*X_test.shape[2])
12
13
14
   # after converting the input images from 3d to 2d vectors
15
    print("Number of training examples :", X_train.shape[0], "and each image is of shape ()
16
    print("Number of training examples :", X_test.shape[0], "and each image is of shape (%)
17
18
19
```

```
Number of training examples: 60000 and each image is of shape (28, 28)
Number of training examples: 10000 and each image is of shape (28, 28)
Number of training examples: 60000 and each image is of shape (784)
Number of training examples: 10000 and each image is of shape (784)
```

```
In [4]:
```

```
# An example data point
print(X_train[0]);
```

```
0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
         0
               0
                          0
                               0
                                     0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
                    0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                         0
                               0
                                     0
                                                           0
                                                                0
                                                                      0
                                                                                      0
                                                                                                 0
                    0
                                          0
                                                0
                                                     0
                                                                           0
                                                                                 0
                                                                                            0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                                0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                                                                                 0
    0
         0
               0
                    0
                         0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                3
                                                    18
                                                         18
                                                               18 126 136 175
                                                                                     26 166
                                                                                              255
 247 127
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                                0
                                                                           0
                                                                               30
                                                                                     36
                                                                                          94
                                                                                              154
                                                           0
                                                                      0
      253
                                  225
                                       172
                                                  242 195
                                                                      0
                                                                           0
                                                                                      0
                                                                                            0
 170
            253
                 253
                       253
                            253
                                            253
                                                               64
                                                                                 0
                                                                                                 0
                                  238
                                       253
                                             253
                                                  253
                                                        253
                                                             253
    0
         0
               0
                    0
                          0
                              49
                                                                   253
                                                                        253
                                                                              253
                                                                                   251
                                                                                          93
                                                                                                82
  82
        56
             39
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                           0
                                                                                 0
                                                                                     18
                                                                                         219
                                                                                              253
 253 253
            253 253
                       198
                            182
                                  247
                                       241
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
         0
               0
                    0
                                                                                      0
                                                                                          43
                                                                                              154
    0
                          0
                               0
                                     0
                                          0
                                              80
                                                  156
                                                        107
                                                             253
                                                                   253
                                                                        205
                                                                               11
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                                     a
    0
        14
               1
                 154
                       253
                              90
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                        139
                                                                              253
                                                                                   190
                                                                                            2
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                              11
                                  190
                                              70
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                       253
    0
         0
               0
                    0
                          0
                               0
                                     0
                                                0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                          35
                                                                                              241
                                          0
 225
                          0
                               0
                                                                0
                                                                      0
      160
            108
                    1
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                    81
                                                        240
                                                             253
                                                                   253 119
                                                                               25
                                                                                      0
                                                                                            0
                                                                                                 0
                          0
                               0
                                     0
                                                                                      0
    0
         0
               0
                    0
                                          0
                                                0
                                                                0
                                                                           0
                                                                                 0
                                                                                            0
                                                                                                 0
                                                     0
                                                           0
                                                                      0
    0
         0
             45
                 186
                      253 253
                                  150
                                         27
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
               0
                          0
                               0
                                                                                   252
                                                                                         253
    0
         0
                    0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                          16
                                                                               93
                                                                                              187
    0
         0
               0
                    0
                         0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                       249
                                            253
                                                  249
                                                         64
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                                                               46
    0
         0
               0
                          0
                               0
                                     0
                                                0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                   130 183
                                                                                              253
                    0
                                          0
                                                     0
 253
      207
               2
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
               0
                        39
                           148
                                  229
                                                        250
                                                                                      0
    0
         0
                    0
                                       253
                                             253
                                                  253
                                                             182
                                                                      0
                                                                           0
                                                                                 0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                                                0
                                                                    24 114
                                                                              221
                                                                                   253 253
                                          0
                                                0
                                                     0
                                                           0
                                                                                              253
 253
      201
             78
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                  253
                                                                2
    0
         0
             23
                   66 213
                            253
                                       253
                                             253
                                                  198
                                                         81
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                               0
                                     0
                                                0
                                                     0
                                                         18
                                                             171
                                                                   219
                                                                        253
                                                                              253
                                                                                   253
                                                                                         253
                                                                                              195
  80
         9
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
  55
      172
            226
                 253
                       253
                            253
                                  253
                                       244
                                             133
                                                    11
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    a
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                        136
                                                             253
                                                                   253
                                                                        253
                                                                              212
                                                                                   135
                                                                                         132
                                                                                                16
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                         0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
               0
                    0
                         0
                               0
                                     0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
                                          0
    0
         0
               0
                    0
                         0
                               0
                                     0
                                                0
                                                                                      0
                                                                                            0
                                                                                                 0
                                          0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
    0
         0
               0
                    0
                          0
                               0
                                     0
                                          0
                                                0
                                                     0
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                 0
                                                                                      0
                                                                                            0
                                                                                                 0
    0
         0
                          0
                               0
               0
                    0
                                     0
                                          0
                                                0
                                                     0]
```

5. Normalise the data

In [5]:

```
# if we observe the above matrix each cell is having a value between 0-255
   # before we move to apply machine learning algorithms lets try to normalize the data
   \# X \Rightarrow (X - Xmin)/(Xmax-Xmin) = X/255
 5
   X_{train} = X_{train}/255
 6
   X_{\text{test}} = X_{\text{test}}/255
7
   # example data point after normlizing
   print(X_train[0]);
0.21568627 0.6745098 0.88627451 0.99215686 0.99215686 0.99215686
0.99215686 0.95686275 0.52156863 0.04313725 0.
                                                              0.
            0.
                        0.
                                     0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.53333333 0.99215686
0.99215686 0.99215686 0.83137255 0.52941176 0.51764706 0.0627451
            0.
                        0.
                                     0.
                                                 0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
                                                 0.
            0.
                        0.
                                     0.
                                                              0.
0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
                        0.
0.
            0.
                                     0.
                                                 0.
                                                              0.
0.
            0.
                        0.
                                     0.
                                                 0.
                                                              0.
```

6. Encode Label

In [6]:

```
# here we are having a class number for each image
 2
   print("Class label of first image :", y_train[0])
 3
   # lets convert this into a 10 dimensional vector
4
 5
   # ex: consider an image is 5 convert it into 5 => [0, 0, 0, 0, 0, 1, 0, 0, 0]
   # this conversion needed for MLPs
 6
   Y_train = np_utils.to_categorical(y_train, 10)
8
9
   Y_test = np_utils.to_categorical(y_test, 10)
10
11
   print("After converting the output into a vector : ",Y train[0])
```

```
Class label of first image : 5
After converting the output into a vector : [0. 0. 0. 0. 0. 1. 0. 0. 0. 0.]
```

7. Model (MLP)

7.1 Parameters

In [7]:

```
1  output_dim = 10
2  input_dim = X_train.shape[1]
3  
4  batch_size = 128
5  nb_epoch = 10
6  
7
```

7.2.1 MLP (2 hidden layers) + Batch-Norm + Dropout + AdamOptimizer

In [8]:

```
1
 2
    model_1 = Sequential()
 3
 4
    model_1.add(Dense(512, activation='relu', input_shape=(input_dim,), kernel_initializer
 5
    model 1.add(BatchNormalization())
    model_1.add(Dropout(0.5))
 6
 7
    model_1.add(Dense(128, activation='relu', kernel_initializer='he_normal'))
 8
9
    model_1.add(BatchNormalization())
    model 1.add(Dropout(0.5))
10
11
    model 1.add(Dense(output dim, activation='softmax'))
12
13
14
   model_1.summary()
```

WARNING:tensorflow:From C:\Users\Byron\Applications\PythonMaster\lib\site-pa ckages\tensorflow\python\framework\op_def_library.py:263: colocate_with (fro m tensorflow.python.framework.ops) is deprecated and will be removed in a fu ture version.

Instructions for updating:

Colocations handled automatically by placer.

WARNING:tensorflow:From C:\Users\Byron\Applications\PythonMaster\lib\site-packages\keras\backend\tensorflow_backend.py:3445: calling dropout (from tensorflow.python.ops.nn_ops) with keep_prob is deprecated and will be removed in a future version.

Instructions for updating:

Please use `rate` instead of `keep_prob`. Rate should be set to `rate = 1 - keep_prob`.

Lavon (type)	O.,+ p.,+	Chana	Danam #
Layer (type)	Output	Snape	Param #
dense_1 (Dense)	(None,	512)	401920
batch_normalization_1 (Batch	(None,	512)	2048
dropout_1 (Dropout)	(None,	512)	0
dense_2 (Dense)	(None,	128)	65664
batch_normalization_2 (Batch	(None,	128)	512
dropout_2 (Dropout)	(None,	128)	0
dense_3 (Dense)	(None,	10)	1290

Total params: 471,434
Trainable params: 470,154
Non-trainable params: 1,280

localhost:8957/notebooks/Keras-Different-architecture.ipynb

In [9]:

```
model_1.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
    history = model_1.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose
```

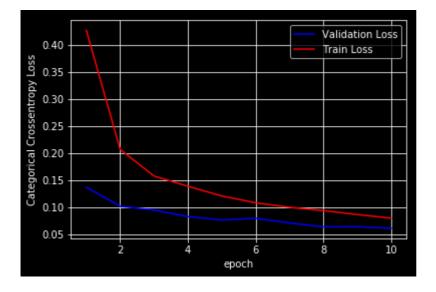
```
WARNING:tensorflow:From C:\Users\Byron\Applications\PythonMaster\lib\site-pa
ckages\tensorflow\python\ops\math ops.py:3066: to int32 (from tensorflow.pyt
hon.ops.math ops) is deprecated and will be removed in a future version.
Instructions for updating:
Use tf.cast instead.
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 8s 136us/step - loss: 0.4271
- acc: 0.8700 - val loss: 0.1373 - val acc: 0.9563
Epoch 2/10
60000/60000 [============= ] - 7s 124us/step - loss: 0.2069
- acc: 0.9383 - val_loss: 0.1020 - val_acc: 0.9682
Epoch 3/10
60000/60000 [============ ] - 7s 121us/step - loss: 0.1579
- acc: 0.9527 - val_loss: 0.0952 - val_acc: 0.9699
Epoch 4/10
60000/60000 [============= ] - 7s 120us/step - loss: 0.1390
- acc: 0.9589 - val_loss: 0.0831 - val_acc: 0.9735
Epoch 5/10
60000/60000 [============= ] - 7s 121us/step - loss: 0.1212
- acc: 0.9623 - val_loss: 0.0769 - val_acc: 0.9758
Epoch 6/10
60000/60000 [=============== ] - 7s 121us/step - loss: 0.1085
- acc: 0.9658 - val_loss: 0.0799 - val_acc: 0.9760
Epoch 7/10
60000/60000 [============= ] - 7s 122us/step - loss: 0.1002
- acc: 0.9689 - val_loss: 0.0713 - val_acc: 0.9779
Epoch 8/10
60000/60000 [============== ] - 7s 122us/step - loss: 0.0941
- acc: 0.9710 - val_loss: 0.0641 - val_acc: 0.9804
60000/60000 [============= ] - 7s 122us/step - loss: 0.0868
- acc: 0.9737 - val loss: 0.0645 - val acc: 0.9804
Epoch 10/10
60000/60000 [============= ] - 7s 124us/step - loss: 0.0802
- acc: 0.9746 - val_loss: 0.0614 - val_acc: 0.9819
```

In [10]:

```
score = model_1.evaluate(X_test, Y_test, verbose=0)
   print('Test score:', score[0])
 2
 3
   print('Test accuracy:', score[1])
4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
7
8
   # list of epoch numbers
9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
25
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.061443126168311574

Test accuracy: 0.9819

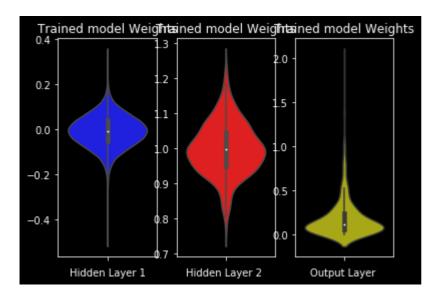


In [11]:

```
w_after = model_1.get_weights()
 2
 3
   h1_w = w_after[0].flatten().reshape(-1,1)
 4
   h2_w = w_after[2].flatten().reshape(-1,1)
 5
    out_w = w_after[4].flatten().reshape(-1,1)
 6
 7
 8
   fig = plt.figure()
    plt.title("Weight matrices after model trained")
9
10
   plt.subplot(1, 3, 1)
11
   plt.title("Trained model Weights")
    ax = sns.violinplot(y=h1 w,color='b')
12
    plt.xlabel('Hidden Layer 1')
13
14
15
   plt.subplot(1, 3, 2)
16
    plt.title("Trained model Weights")
17
    ax = sns.violinplot(y=h2_w, color='r')
18
    plt.xlabel('Hidden Layer 2 ')
19
20
    plt.subplot(1, 3, 3)
21
    plt.title("Trained model Weights")
22
    ax = sns.violinplot(y=out_w,color='y')
    plt.xlabel('Output Layer ')
23
24
    plt.show()
25
26
   del(model_1)
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



7.2.2 MLP (3 hidden layers) + Batch-Norm + Dropout + AdamOptimizer

In [12]:

```
1
 2
    model_2 = Sequential()
 3
    model_2.add(Dense(500, activation='relu', input_shape=(input_dim,), kernel_initializer
 4
    model_2.add(BatchNormalization())
 5
    model_2.add(Dropout(0.5))
 6
 7
    model_2.add(Dense(300, activation='relu', kernel_initializer='he_normal'))
 8
 9
    model_2.add(BatchNormalization())
    model_2.add(Dropout(0.5))
10
11
    model_2.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
12
    model_2.add(BatchNormalization())
13
    model_2.add(Dropout(0.5))
14
15
    model_2.add(Dense(output_dim, activation='softmax'))
16
17
18
    model_2.summary()
19
```

Layer (type)	Output	Shape	Param #
======================================	(None,	500)	392500
batch_normalization_3 (Batch	(None,	500)	2000
dropout_3 (Dropout)	(None,	500)	0
dense_5 (Dense)	(None,	300)	150300
batch_normalization_4 (Batch	(None,	300)	1200
dropout_4 (Dropout)	(None,	300)	0
dense_6 (Dense)	(None,	100)	30100
batch_normalization_5 (Batch	(None,	100)	400
dropout_5 (Dropout)	(None,	100)	0
dense_7 (Dense)	(None,	10)	1010

Trainable params: 577,510
Non-trainable params: 1,800

In [13]:

```
model_2.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
    history = model_2.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose
```

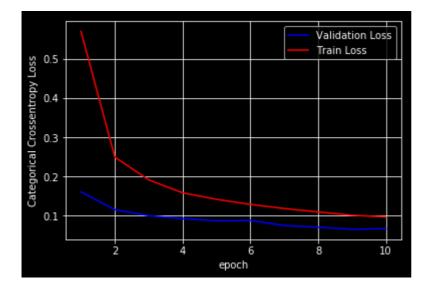
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 10s 162us/step - loss: 0.5704
- acc: 0.8269 - val_loss: 0.1611 - val_acc: 0.9505
60000/60000 [============ ] - 9s 146us/step - loss: 0.2497
- acc: 0.9281 - val_loss: 0.1158 - val_acc: 0.9645
Epoch 3/10
60000/60000 [============= ] - 9s 147us/step - loss: 0.1918
- acc: 0.9439 - val_loss: 0.1005 - val_acc: 0.9705
Epoch 4/10
- acc: 0.9531 - val_loss: 0.0930 - val_acc: 0.9725
Epoch 5/10
60000/60000 [============= ] - 9s 142us/step - loss: 0.1421
- acc: 0.9579 - val_loss: 0.0873 - val_acc: 0.9732
Epoch 6/10
60000/60000 [=============== ] - 8s 134us/step - loss: 0.1291
- acc: 0.9620 - val_loss: 0.0882 - val_acc: 0.9746
Epoch 7/10
60000/60000 [============= ] - 8s 134us/step - loss: 0.1187
- acc: 0.9644 - val_loss: 0.0754 - val_acc: 0.9783
Epoch 8/10
60000/60000 [============= ] - 8s 137us/step - loss: 0.1099
- acc: 0.9679 - val_loss: 0.0712 - val_acc: 0.9790
Epoch 9/10
60000/60000 [============= ] - 8s 137us/step - loss: 0.1017
- acc: 0.9699 - val_loss: 0.0657 - val_acc: 0.9809
Epoch 10/10
60000/60000 [============= ] - 8s 140us/step - loss: 0.0973
- acc: 0.9709 - val_loss: 0.0675 - val_acc: 0.9790
```

In [14]:

```
score = model_2.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
 2
 3
    print('Test accuracy:', score[1])
 4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
 7
 8
   # list of epoch numbers
 9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.06748124550754438

Test accuracy: 0.979

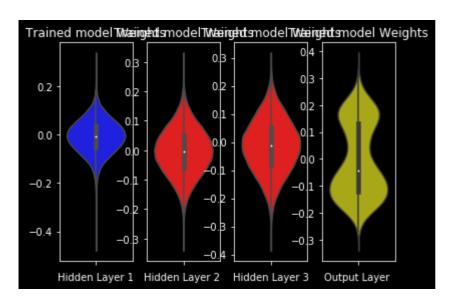


In [16]:

```
h1 w = w after[0].flatten().reshape(-1,1)
   h2_w = w_after[6].flatten().reshape(-1,1)
   h3_w = w_after[12].flatten().reshape(-1,1)
   out_w = w_after[18].flatten().reshape(-1,1)
 5
 6
 7
   fig = plt.figure()
   plt.title("Weight matrices after model trained")
 8
9
   plt.subplot(1, 4, 1)
   plt.title("Trained model Weights")
10
11
   ax = sns.violinplot(y=h1_w,color='b')
12
   plt.xlabel('Hidden Layer 1')
13
14
   plt.subplot(1, 4, 2)
   plt.title("Trained model Weights")
15
16
    ax = sns.violinplot(y=h2_w, color='r')
17
   plt.xlabel('Hidden Layer 2 ')
18
   plt.subplot(1, 4, 3)
19
   plt.title("Trained model Weights")
20
21
    ax = sns.violinplot(y=h3_w, color='r')
22
   plt.xlabel('Hidden Layer 3')
23
24
   plt.subplot(1, 4, 4)
25
   plt.title("Trained model Weights")
26
   ax = sns.violinplot(y=out_w,color='y')
27
    plt.xlabel('Output Layer ')
28
   plt.show()
29
30
   del(model_2)
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



7.2.3 MLP (25 hidden layers) + Batch-Norm + Dropout + AdamOptimizer

In [17]:

```
1
 2
   model_3 = Sequential()
 3
   model_3.add(Dense(200, activation='relu', input_shape=(input_dim,), kernel_initializer
 4
 5
   model 3.add(BatchNormalization())
 6
   model_3.add(Dropout(0.5))
 7
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 8
9
   model_3.add(BatchNormalization())
   model 3.add(Dropout(0.5))
10
11
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
12
13
   model_3.add(BatchNormalization())
14
   model_3.add(Dropout(0.5))
15
16
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
17
   model_3.add(BatchNormalization())
18
   model_3.add(Dropout(0.5))
19
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
20
21
   model_3.add(BatchNormalization())
22
   model_3.add(Dropout(0.5))
23
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
24
25
   model_3.add(BatchNormalization())
26
   model_3.add(Dropout(0.5))
27
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
28
29
   model 3.add(BatchNormalization())
   model_3.add(Dropout(0.5))
30
31
32
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
33
   model_3.add(BatchNormalization())
   model 3.add(Dropout(0.5))
34
35
36
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
37
   model 3.add(BatchNormalization())
38
   model_3.add(Dropout(0.5))
39
   model 3.add(Dense(100, activation='relu', kernel initializer='he normal'))
40
   model_3.add(BatchNormalization())
41
42
   model_3.add(Dropout(0.5))
43
44
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
45
   model_3.add(BatchNormalization())
46
   model 3.add(Dropout(0.5))
47
48
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
49
   model 3.add(BatchNormalization())
50
   model_3.add(Dropout(0.5))
51
   model 3.add(Dense(100, activation='relu', kernel initializer='he normal'))
52
53
   model 3.add(BatchNormalization())
   model 3.add(Dropout(0.5))
54
55
   model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
56
57
   model_3.add(BatchNormalization())
```

```
model 3.add(Dropout(0.5))
 58
 59
    model 3.add(Dense(100, activation='relu', kernel initializer='he normal'))
 60
    model 3.add(BatchNormalization())
 61
    model 3.add(Dropout(0.5))
 62
 63
 64
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 65
    model_3.add(BatchNormalization())
 66
    model 3.add(Dropout(0.5))
 67
    model 3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 68
 69
    model 3.add(BatchNormalization())
    model_3.add(Dropout(0.5))
70
 71
 72
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
    model 3.add(BatchNormalization())
 73
 74
    model_3.add(Dropout(0.5))
 75
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 76
 77
    model_3.add(BatchNormalization())
    model 3.add(Dropout(0.5))
78
 79
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 80
    model 3.add(BatchNormalization())
 81
    model_3.add(Dropout(0.5))
 82
 83
    model 3.add(Dense(100, activation='relu', kernel initializer='he normal'))
 84
 85
    model 3.add(BatchNormalization())
    model 3.add(Dropout(0.5))
 86
 87
    model 3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 88
 89
    model_3.add(BatchNormalization())
 90
    model 3.add(Dropout(0.5))
91
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 92
    model_3.add(BatchNormalization())
93
 94
    model_3.add(Dropout(0.5))
95
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
 96
    model 3.add(BatchNormalization())
97
    model 3.add(Dropout(0.5))
98
99
    model_3.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
100
    model 3.add(BatchNormalization())
101
    model 3.add(Dropout(0.5))
102
103
    model 3.add(Dense(output dim, activation='softmax'))
104
105
106
    model_3.summary()
107
108
```

Layer (type)	Output	Shape	Param #
dense_8 (Dense)	(None,	200)	157000
batch_normalization_6 (Batch	(None,	200)	800
dropout_6 (Dropout)	(None,	200)	0

dense_9 (Dense)	(None,	100)	20100
batch_normalization_7 (Batch	(None,	100)	400
dropout_7 (Dropout)	(None,	100)	0
dense_10 (Dense)	(None,	100)	10100
batch_normalization_8 (Batch	(None,	100)	400

In [18]:

```
model_3.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
history = model_3.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose)
```

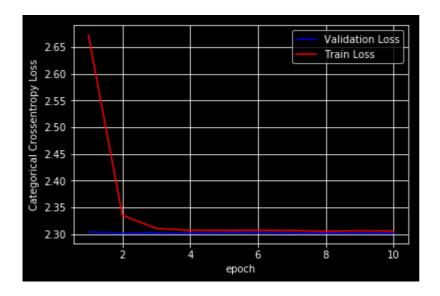
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 29s 477us/step - loss: 2.6718
- acc: 0.0996 - val_loss: 2.3042 - val_acc: 0.1135
Epoch 2/10
60000/60000 [=============== ] - 19s 318us/step - loss: 2.3356
- acc: 0.1038 - val_loss: 2.3017 - val_acc: 0.1135
Epoch 3/10
60000/60000 [============= ] - 19s 321us/step - loss: 2.3108
- acc: 0.1067 - val_loss: 2.3025 - val_acc: 0.1135
Epoch 4/10
60000/60000 [============ ] - 19s 321us/step - loss: 2.3074
- acc: 0.1067 - val_loss: 2.3019 - val_acc: 0.1135
Epoch 5/10
60000/60000 [============= ] - 19s 320us/step - loss: 2.3071
- acc: 0.1086 - val_loss: 2.3027 - val_acc: 0.1135
Epoch 6/10
60000/60000 [============ ] - 19s 320us/step - loss: 2.3073
- acc: 0.1057 - val_loss: 2.3031 - val_acc: 0.1135
Epoch 7/10
60000/60000 [============ ] - 19s 322us/step - loss: 2.3069
- acc: 0.1084 - val_loss: 2.3018 - val_acc: 0.1135
Epoch 8/10
60000/60000 [============= ] - 19s 324us/step - loss: 2.3055
- acc: 0.1082 - val_loss: 2.3021 - val_acc: 0.1135
60000/60000 [============= ] - 22s 369us/step - loss: 2.3064
- acc: 0.1053 - val_loss: 2.3022 - val_acc: 0.1135
Epoch 10/10
60000/60000 [================= ] - 20s 337us/step - loss: 2.3058
- acc: 0.1056 - val_loss: 2.3020 - val_acc: 0.1135
```

In [19]:

```
score = model_3.evaluate(X_test, Y_test, verbose=0)
   print('Test score:', score[0])
 2
   print('Test accuracy:', score[1])
4
   fig,ax = plt.subplots(1,1)
 5
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
 7
8
   # list of epoch numbers
9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
   ty = history.history['loss']
24
25
   plt_dynamic(x, vy, ty, ax)
26
27
   del(model_3)
```

Test score: 2.302019982147217

Test accuracy: 0.1135



7.2.4 MLP (4 hidden layers) + Batch-Norm + Dropout + AdamOptimizer

In [20]:

```
1
   model_4 = Sequential()
 2
   model_4.add(Dense(100, activation='relu', input_shape=(input_dim,), kernel_initializer
 3
 4
   model_4.add(BatchNormalization())
 5
   model 4.add(Dropout(0.5))
 6
 7
   model_4.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
   model_4.add(BatchNormalization())
 8
9
   model_4.add(Dropout(0.5))
10
   model_4.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
11
   model 4.add(BatchNormalization())
12
   model_4.add(Dropout(0.5))
13
14
   model_4.add(Dense(100, activation='relu', kernel_initializer='he_normal'))
15
16
   model 4.add(BatchNormalization())
   model_4.add(Dropout(0.5))
17
18
   model_4.add(Dense(output_dim, activation='softmax'))
19
20
21
   model_4.summary()
```

Layer (type)	Output	Shape	Param #
dense_34 (Dense)	(None,	100)	78500
batch_normalization_31 (Batc	(None,	100)	400
dropout_31 (Dropout)	(None,	100)	0
dense_35 (Dense)	(None,	100)	10100
batch_normalization_32 (Batc	(None,	100)	400
dropout_32 (Dropout)	(None,	100)	0
dense_36 (Dense)	(None,	100)	10100
batch_normalization_33 (Batc	(None,	100)	400
dropout_33 (Dropout)	(None,	100)	0
dense_37 (Dense)	(None,	100)	10100
batch_normalization_34 (Batc	(None,	100)	400
dropout_34 (Dropout)	(None,	100)	0
dense_38 (Dense)	(None,	10)	1010
Total params: 111,410 Trainable params: 110,610			

Non-trainable params: 800

In [21]:

```
model_4.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
    history = model_4.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose
```

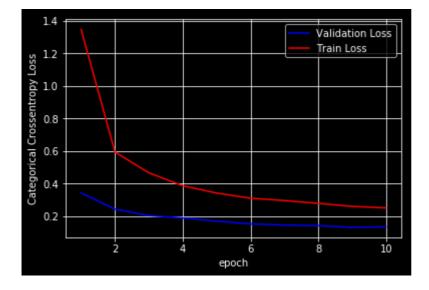
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 8s 132us/step - loss: 1.3473
- acc: 0.5643 - val_loss: 0.3420 - val_acc: 0.9041
60000/60000 [============= ] - 5s 81us/step - loss: 0.5937 -
acc: 0.8200 - val_loss: 0.2426 - val_acc: 0.9299
Epoch 3/10
60000/60000 [============= ] - 5s 82us/step - loss: 0.4655 -
acc: 0.8671 - val_loss: 0.2026 - val_acc: 0.9411
Epoch 4/10
60000/60000 [================ ] - 5s 77us/step - loss: 0.3861 -
acc: 0.8914 - val_loss: 0.1887 - val_acc: 0.9482
Epoch 5/10
60000/60000 [============ ] - 5s 77us/step - loss: 0.3411 -
acc: 0.9063 - val_loss: 0.1684 - val_acc: 0.9521
Epoch 6/10
acc: 0.9158 - val_loss: 0.1519 - val_acc: 0.9575
Epoch 7/10
60000/60000 [============= ] - 5s 78us/step - loss: 0.2953 -
acc: 0.9196 - val_loss: 0.1446 - val_acc: 0.9595
Epoch 8/10
60000/60000 [============= ] - 5s 80us/step - loss: 0.2778 -
acc: 0.9250 - val_loss: 0.1413 - val_acc: 0.9611
Epoch 9/10
60000/60000 [============= ] - 5s 78us/step - loss: 0.2596 -
acc: 0.9294 - val_loss: 0.1308 - val_acc: 0.9654
Epoch 10/10
60000/60000 [============ ] - 5s 79us/step - loss: 0.2502 -
acc: 0.9319 - val loss: 0.1341 - val_acc: 0.9650
```

In [22]:

```
score = model_4.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
 2
 3
    print('Test accuracy:', score[1])
 4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
 7
 8
   # list of epoch numbers
 9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
25
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.13409332928974182

Test accuracy: 0.965

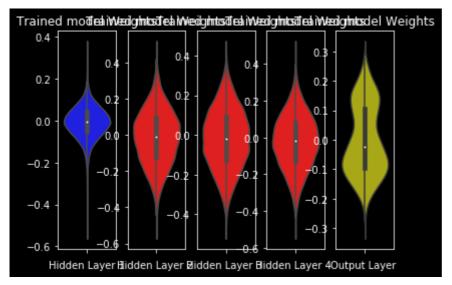


In [24]:

```
h1 w = w after[0].flatten().reshape(-1,1)
   h2_w = w_after[6].flatten().reshape(-1,1)
   h3_w = w_after[12].flatten().reshape(-1,1)
 4 \mid h4 w = w after[18].flatten().reshape(-1,1)
 5
    out_w = w_after[24].flatten().reshape(-1,1)
 6
 7
 8
   fig = plt.figure()
    plt.title("Weight matrices after model trained")
9
10
   plt.subplot(1, 5, 1)
   plt.title("Trained model Weights")
11
    ax = sns.violinplot(y=h1 w,color='b')
12
    plt.xlabel('Hidden Layer 1')
13
14
15
   plt.subplot(1, 5, 2)
16
    plt.title("Trained model Weights")
    ax = sns.violinplot(y=h2_w, color='r')
17
    plt.xlabel('Hidden Layer 2 ')
18
19
20
    plt.subplot(1, 5, 3)
21
    plt.title("Trained model Weights")
22
    ax = sns.violinplot(y=h3_w, color='r')
23
    plt.xlabel('Hidden Layer 3 ')
24
25
    plt.subplot(1, 5, 4)
26
   plt.title("Trained model Weights")
27
    ax = sns.violinplot(y=h4_w, color='r')
28
    plt.xlabel('Hidden Layer 4 ')
29
30
   plt.subplot(1, 5, 5)
    plt.title("Trained model Weights")
31
32
    ax = sns.violinplot(y=out_w,color='y')
33
   plt.xlabel('Output Layer ')
34
   plt.show()
35
36
   del(model 4)
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



7.2.5 MLP (1 hidden layer) + Batch-Norm + Dropout + AdamOptimizer

In [25]:

```
model_5 = Sequential()
model_5.add(Dense(1000, activation='relu', input_shape=(input_dim,), kernel_initialize
model_5.add(BatchNormalization())
model_5.add(Dropout(0.5))

model_5.add(Dense(output_dim, activation='softmax'))
model_5.summary()
```

Layer (type)	Output	Shape	Param #
dense_39 (Dense)	(None,	1000)	785000
batch_normalization_35 (Batc	(None,	1000)	4000
dropout_35 (Dropout)	(None,	1000)	0
dense_40 (Dense)	(None,	10)	10010

Total params: 799,010 Trainable params: 797,010 Non-trainable params: 2,000

localhost:8957/notebooks/Keras-Different-architecture.ipynb

In [26]:

```
model_5.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
history = model_5.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose
```

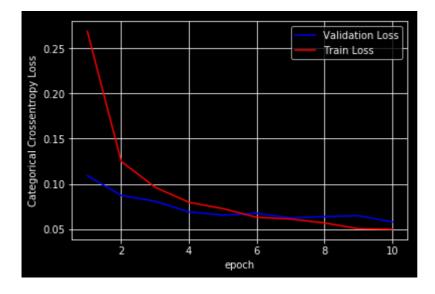
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============== ] - 12s 206us/step - loss: 0.2689
- acc: 0.9215 - val_loss: 0.1091 - val_acc: 0.9662
60000/60000 [============= ] - 10s 164us/step - loss: 0.1248
- acc: 0.9616 - val_loss: 0.0872 - val_acc: 0.9743
Epoch 3/10
60000/60000 [============= ] - 10s 165us/step - loss: 0.0962
- acc: 0.9700 - val_loss: 0.0806 - val_acc: 0.9748
Epoch 4/10
60000/60000 [================= ] - 10s 166us/step - loss: 0.0795
- acc: 0.9747 - val_loss: 0.0689 - val_acc: 0.9783
Epoch 5/10
60000/60000 [============= ] - 10s 169us/step - loss: 0.0725
- acc: 0.9763 - val_loss: 0.0653 - val_acc: 0.9806
Epoch 6/10
60000/60000 [================ ] - 10s 167us/step - loss: 0.0629
- acc: 0.9800 - val_loss: 0.0673 - val_acc: 0.9797
Epoch 7/10
60000/60000 [============= ] - 10s 172us/step - loss: 0.0610
- acc: 0.9798 - val_loss: 0.0622 - val_acc: 0.9808
Epoch 8/10
60000/60000 [============ ] - 10s 172us/step - loss: 0.0567
- acc: 0.9806 - val_loss: 0.0637 - val_acc: 0.9819
Epoch 9/10
60000/60000 [============== ] - 10s 175us/step - loss: 0.0503
- acc: 0.9831 - val_loss: 0.0647 - val_acc: 0.9816
Epoch 10/10
- acc: 0.9836 - val_loss: 0.0579 - val_acc: 0.9822
```

In [27]:

```
score = model_5.evaluate(X_test, Y_test, verbose=0)
   print('Test score:', score[0])
 2
 3
   print('Test accuracy:', score[1])
4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
7
8
   # list of epoch numbers
9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.05786827448041295

Test accuracy: 0.9822

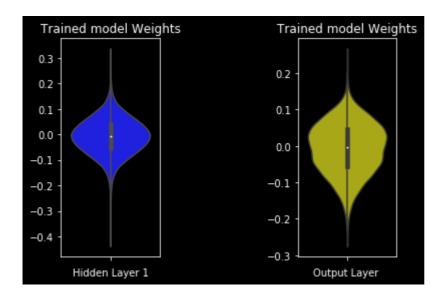


In [29]:

```
w_after = model_5.get_weights()
   h1_w = w_after[0].flatten().reshape(-1,1)
   out_w = w_after[6].flatten().reshape(-1,1)
 5
 6
   fig = plt.figure()
 7
   plt.title("Weight matrices after model trained")
8
   plt.subplot(1, 3, 1)
9
   plt.title("Trained model Weights")
   ax = sns.violinplot(y=h1 w,color='b')
10
11
   plt.xlabel('Hidden Layer 1')
12
13
   plt.subplot(1, 3, 3)
14
   plt.title("Trained model Weights")
   ax = sns.violinplot(y=out_w,color='y')
15
   plt.xlabel('Output Layer ')
16
17
   plt.show()
18
   del(model_5)
19
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



7.2.6 MLP (1 hidden layer) + Batch-Norm + Dropout (low) + AdamOptimizer

In [30]:

```
model_6 = Sequential()
model_6.add(Dense(300, activation='relu', input_shape=(input_dim,), kernel_initializer:
model_6.add(BatchNormalization())
model_6.add(Dropout(0.1))

model_6.add(Dense(output_dim, activation='softmax'))
model_6.summary()
```

Layer (type)	Output	Shape	Param #
dense_41 (Dense)	(None,	300)	235500
batch_normalization_36 (Batc	(None,	300)	1200
dropout_36 (Dropout)	(None,	300)	0
dense_42 (Dense)	(None,	10)	3010

Total params: 239,710 Trainable params: 239,110 Non-trainable params: 600

In [31]:

```
model_6.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
    history = model_6.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose
```

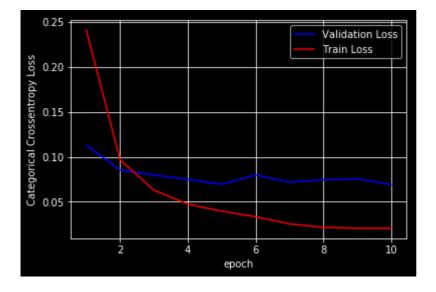
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 6s 98us/step - loss: 0.2407 -
acc: 0.9280 - val_loss: 0.1131 - val_acc: 0.9678
60000/60000 [============= ] - 4s 66us/step - loss: 0.0964 -
acc: 0.9715 - val_loss: 0.0853 - val_acc: 0.9743
Epoch 3/10
60000/60000 [============= ] - 4s 66us/step - loss: 0.0629 -
acc: 0.9813 - val_loss: 0.0797 - val_acc: 0.9759
Epoch 4/10
60000/60000 [=============== ] - 4s 66us/step - loss: 0.0474 -
acc: 0.9863 - val_loss: 0.0749 - val_acc: 0.9767
Epoch 5/10
60000/60000 [============= ] - 4s 66us/step - loss: 0.0396 -
acc: 0.9877 - val loss: 0.0695 - val acc: 0.9793
Epoch 6/10
60000/60000 [=============== ] - 4s 66us/step - loss: 0.0334 -
acc: 0.9897 - val_loss: 0.0798 - val_acc: 0.9771
Epoch 7/10
60000/60000 [============= ] - 4s 66us/step - loss: 0.0255 -
acc: 0.9922 - val_loss: 0.0719 - val_acc: 0.9782
Epoch 8/10
60000/60000 [============= ] - 4s 67us/step - loss: 0.0217 -
acc: 0.9933 - val_loss: 0.0746 - val_acc: 0.9768
Epoch 9/10
60000/60000 [============= ] - 4s 66us/step - loss: 0.0207 -
acc: 0.9934 - val_loss: 0.0754 - val_acc: 0.9790
Epoch 10/10
60000/60000 [============ ] - 4s 67us/step - loss: 0.0206 -
acc: 0.9934 - val loss: 0.0693 - val_acc: 0.9800
```

In [32]:

```
score = model_6.evaluate(X_test, Y_test, verbose=0)
   print('Test score:', score[0])
 2
 3
   print('Test accuracy:', score[1])
4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
7
8
   # list of epoch numbers
9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.06930483953608782

Test accuracy: 0.98

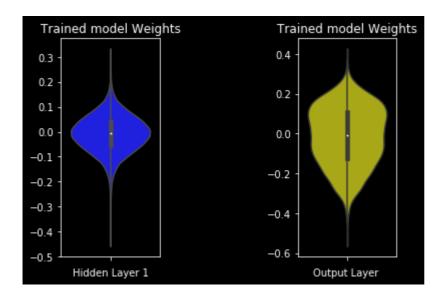


In [34]:

```
w_after = model_6.get_weights()
   h1_w = w_after[0].flatten().reshape(-1,1)
   out_w = w_after[6].flatten().reshape(-1,1)
 5
 6
   fig = plt.figure()
 7
   plt.title("Weight matrices after model trained")
8
   plt.subplot(1, 3, 1)
9
   plt.title("Trained model Weights")
   ax = sns.violinplot(y=h1 w,color='b')
10
11
   plt.xlabel('Hidden Layer 1')
12
13
   plt.subplot(1, 3, 3)
14
   plt.title("Trained model Weights")
   ax = sns.violinplot(y=out_w,color='y')
15
   plt.xlabel('Output Layer ')
16
17
   plt.show()
18
   del(model_6)
19
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



7.2.7 MLP (1 hidden layer) + Batch-Norm + Dropout (high) + AdamOptimizer

In [35]:

```
model_7 = Sequential()
model_7.add(Dense(300, activation='relu', input_shape=(input_dim,), kernel_initializer:
model_7.add(BatchNormalization())
model_7.add(Dropout(0.9))

model_7.add(Dense(output_dim, activation='softmax'))
model_7.summary()
```

Layer (type)	Output	Shape	Param #
dense_43 (Dense)	(None,	300)	235500
batch_normalization_37 (Batc	(None,	300)	1200
dropout_37 (Dropout)	(None,	300)	0
dense_44 (Dense)	(None,	10)	3010

Total params: 239,710 Trainable params: 239,110 Non-trainable params: 600

In [36]:

```
model_7.compile(optimizer='adam', loss='categorical_crossentropy', metrics=['accuracy'
history = model_7.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, verbose)
```

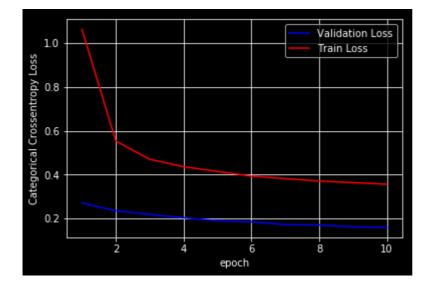
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============= ] - 6s 104us/step - loss: 1.0630
- acc: 0.7194 - val_loss: 0.2704 - val_acc: 0.9217
60000/60000 [============= ] - 4s 68us/step - loss: 0.5531 -
acc: 0.8324 - val_loss: 0.2353 - val_acc: 0.9301
Epoch 3/10
60000/60000 [============= ] - 4s 68us/step - loss: 0.4699 -
acc: 0.8575 - val_loss: 0.2184 - val_acc: 0.9344
Epoch 4/10
60000/60000 [================ ] - 4s 68us/step - loss: 0.4361 -
acc: 0.8693 - val_loss: 0.2031 - val_acc: 0.9395
Epoch 5/10
60000/60000 [============ ] - 4s 69us/step - loss: 0.4146 -
acc: 0.8765 - val_loss: 0.1903 - val_acc: 0.9399
Epoch 6/10
60000/60000 [=============== ] - 4s 69us/step - loss: 0.3932 -
acc: 0.8820 - val_loss: 0.1848 - val_acc: 0.9442
Epoch 7/10
60000/60000 [============= ] - 4s 69us/step - loss: 0.3817 -
acc: 0.8842 - val_loss: 0.1725 - val_acc: 0.9470
Epoch 8/10
60000/60000 [============= ] - 4s 70us/step - loss: 0.3709 -
acc: 0.8880 - val_loss: 0.1705 - val_acc: 0.9483
Epoch 9/10
60000/60000 [============ ] - 4s 69us/step - loss: 0.3637 -
acc: 0.8915 - val_loss: 0.1619 - val_acc: 0.9510
Epoch 10/10
60000/60000 [============ ] - 4s 69us/step - loss: 0.3562 -
acc: 0.8944 - val loss: 0.1598 - val_acc: 0.9525
```

In [37]:

```
score = model_7.evaluate(X_test, Y_test, verbose=0)
    print('Test score:', score[0])
 2
 3
    print('Test accuracy:', score[1])
 4
 5
   fig,ax = plt.subplots(1,1)
   ax.set_xlabel('epoch'); ax.set_ylabel('Categorical Crossentropy Loss')
 6
 7
 8
   # list of epoch numbers
 9
   x = list(range(1,nb_epoch+1))
10
11
   # print(history.history.keys())
   # dict_keys(['val_loss', 'val_acc', 'loss', 'acc'])
12
   # history = model_drop.fit(X_train, Y_train, batch_size=batch_size, epochs=nb_epoch, ve
13
14
   # we will get val_loss and val_acc only when you pass the paramter validation_data
15
16
   # val_loss : validation loss
   # val_acc : validation accuracy
17
18
   # loss : training loss
19
20
   # acc : train accuracy
   # for each key in histrory.histrory we will have a list of length equal to number of e
21
22
   vy = history.history['val_loss']
23
24
   ty = history.history['loss']
   plt_dynamic(x, vy, ty, ax)
```

Test score: 0.15979730788581073

Test accuracy: 0.9525

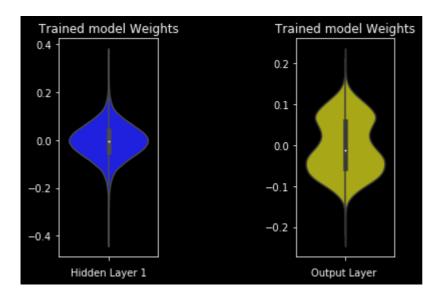


In [39]:

```
w_after = model_7.get_weights()
   h1_w = w_after[0].flatten().reshape(-1,1)
 2
    out_w = w_after[6].flatten().reshape(-1,1)
4
 5
 6
   fig = plt.figure()
    plt.title("Weight matrices after model trained")
 7
    plt.subplot(1, 3, 1)
8
    plt.title("Trained model Weights")
9
    ax = sns.violinplot(y=h1_w,color='b')
10
11
    plt.xlabel('Hidden Layer 1')
12
13
    plt.subplot(1, 3, 3)
    plt.title("Trained model Weights")
14
    ax = sns.violinplot(y=out_w,color='y')
15
    plt.xlabel('Output Layer ')
16
17
    plt.show()
18
   del(model_7)
19
```

C:\Users\Byron\Applications\PythonMaster\lib\site-packages\scipy\stats\stat s.py:1713: FutureWarning: Using a non-tuple sequence for multidimensional in dexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the fu ture this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval



Type *Markdown* and LaTeX: α^2

In [2]:

```
1
    import prettytable
 2
 3
   table = prettytable.PrettyTable()
   table.add_row(['Model','Parameters','Training loss','Validation loss','Accuracy','epoc
 4
   table.add_row(['2 HL,relu,adam,dropout,batch norm','471434','0.08','0.06','98','10'])
 5
   table.add_row(['3 HL,relu,adam,dropout,batch norm','577520','0.09','0.07','97','10'])
 7
    table.add_row(['25 HL,relu,adam,dropout,batch norm,100 neurons','420810','2.3','2.3','
   table.add_row(['4 HL,relu,adam,dropout,batch norm,100 neurons','111410','0.17','0.09',
 8
   table.add_row(['1 HL,relu,adam,dropout,batch norm,1000 neurons','799010','0.05','0.06'
 9
    table.add_row(['1 HL,relu,adam,batch norm,low dropout,300 neurons','239710','0.01','0.
10
    table.add_row(['1 HL,relu,adam,batch norm,high dropout,300 neurons','239710','0.36','0
11
12
13
   print(table)
```

+	eld
3 Field 4 Field 5 Field 6	
+	. – –
Model Parameters Traini	ing
2 HL,relu,adam,dropout,batch norm 471434 0	0.0
8 0.06 98 10 3 HL,relu,adam,dropout,batch norm 577520 0	0.0
9 0.07 97 10 25 HL,relu,adam,dropout,batch norm,100 neurons 420810 2	2.3
2.3 11 10 4 HL, relu, adam, dropout, batch norm, 100 neurons 111410 6	ð. 1
7 0.09 97 10	–
1 HL,relu,adam,dropout,batch norm,1000 neurons 799010 0	0.0
5 0.06 98 10	
1 HL,relu,adam,batch norm,low dropout,300 neurons 239710 6 1 0.06 98 10	0.0
	3.3
6 0.16 95 10	
++++	