

Q. using BLT, design High-pass filter, monotonic in passband with cutoff frequency of 1000 Hz and down 10 dB at 350 Hz. The sampling freq is 5000 Hz. Implement using basic building blocks. show derivation for this filter. Demonstrate filter output for 5 different freq. ranging from 100 Hz to 10000 Hz

Ans

Given:

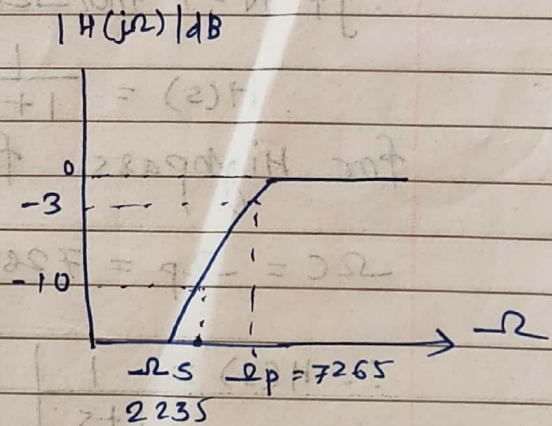
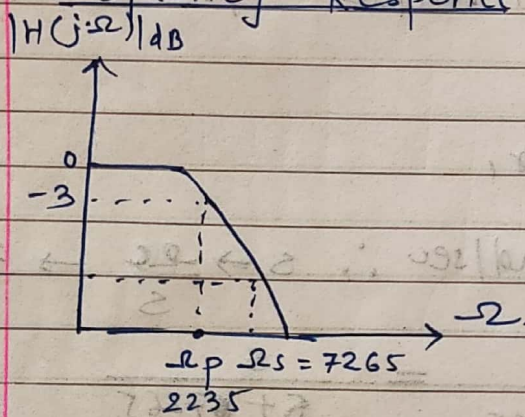
$$\alpha_p = 3 \text{ dB}, \quad \omega_c = \omega_p = 2\pi \times 1000 = 2000\pi \text{ rad/s}$$

$$\alpha_s = 10 \text{ dB}, \quad \omega_s = 2\pi \times 350 = 700\pi \text{ rad/sec}$$

$$f_s = 5000 \text{ Hz.}$$

$$T = \frac{1}{f_s} = \frac{1}{5000} = 2 \times 10^{-4} \text{ sec.}$$

Frequency Response:



As we know,

- Passband freq. (H.P.F) = Stopband freq. (L.P.F)
- * Stopband freq. (H.P.F) = Passband freq. (L.P.F)
- * monotonic filter = Butterworth. filter.

$$\begin{aligned} -\alpha_p &= \frac{2}{T} \tan \frac{\omega_p T}{2} \\ &= \frac{2}{2 \times 10^{-4}} \tan \left(\frac{2000\pi \times 2 \times 10^{-4}}{2} \right) \\ &= 10^4 \tan(0.2\pi) \\ &= 7265 \text{ rad/sec} \end{aligned}$$

$$\begin{aligned}\Omega_s &= \frac{\omega_s}{T} \tan \frac{\omega_s T}{2} \\ &= \frac{2}{2 \times 10^{-4}} \tan \left(\frac{700 \pi \times 2 \times 10^{-4}}{2} \right) \\ &= 10^4 \tan (0.07 \pi) \\ &= 2235 \text{ rad/sec.}\end{aligned}$$

The order of filter,

$$\begin{aligned}N &= \frac{\log \sqrt{\frac{10^{0.1\alpha_s} - 1}{10^{0.1\alpha_p} - 1}}}{\log \frac{\Omega_s}{\Omega_p}} = \frac{\log \sqrt{\frac{10^{0.1(60)} - 1}{10^{0.1(3)} - 1}}}{\log \frac{7265}{2235}} = \frac{\log 3}{\log 3.25} \\ &= 0.932.\end{aligned}$$

\therefore if $N=1$ then $\Omega_c = 1 \text{ rad/sec.}$ for buttworth filter

$$H(s) = \frac{1}{1+s}$$

for Highpass filter,

$$\Omega_c = \Omega_p = 7265 \text{ rad/sec} \therefore s \rightarrow \frac{\Omega_s}{s} \rightarrow \frac{7265}{s}$$

$$\therefore H(s) = \frac{1}{1+s} \bigg|_{s = \frac{7265}{s}} = \frac{s}{s + 7265}$$

using BLT,

$$H(z) = H(s) \bigg|_{s = \frac{2}{T} \left[\frac{1-z^{-1}}{1+z^{-1}} \right]}$$

$$= \frac{s}{s + 7265} \bigg|_{s = \frac{2}{2 \times 10^{-4}} \left[\frac{1-z^{-1}}{1+z^{-1}} \right]} = \frac{1000 (1-z^{-1} / (1+z^{-1}))}{1000 \left[\frac{1-z^{-1}}{1+z^{-1}} \right] + 7265}$$

$$H(z) = \frac{0.5792 (1-z^{-1})}{1 - 0.1584 z^{-1}}$$