Defining Language TWO

- Extend Language ONE with:
 - Variables
 - An ML-style let expression for defining them

TWO: Syntax

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- A subset of ML expressions
- This grammar is unambiguous
- A sample Language TWO expression:
 let val y = 3 in y*y end
- What does the parse tree for the above expression look like?

TWO: Abstract Syntax

Additional abstract syntax nodes for language TWO:

- (1) var(X) dereferences a variable X
- (2) <u>let(X,E1,E2)</u> binds the variable X to expression E1 in the context of expression E2.

Example: the TWO program

```
let val y = 3 in y*y end
```

will result in the AST

```
let(y, const(3), times(var(y), var(y)))
```

From Parse Tree to Prolog AST

- Consider: 2 * let x = 5 in 1+x end
 - Parse tree?
 - AST?
 - Prolog AST?

TWO: Semantics

In order to provide semantics we need to remember the values assigned to variables -- binding environments, contexts.

In our case, for the Prolog based semantics, we let the terms bind(X,K) represent the binding of variable X to value K. A context is simply a list of these binding terms:

```
[bind(y, 3), bind(q, 20), bind(z, 5)]
```

Given this binding structure, we can write a predicate, lookup/3, that returns a variable binding for a particular Var

```
lookup(Var,[bind(Var,Value)| _ ],Value).
lookup(Var,[ _ |Rest],Value) :- lookup(Var,Rest,Value).
```

Finds the most recent binding of variable Var if there is one.

TWO: Prolog Interpreter

val2 / 3 - interpretation predicate, first argument: AST; second argument: context; third argument: semantic value.

Examples

```
let val y = 3 in y*y end
?- val2(let(y,const(3),times(var(y),var(y))),[ ],X).

X = 9
Yes
```

```
let val y = 3 in
   let val y = 1 in
   let val y = 2 in
   x*x
   end
end
end
```

Exercises

- Use the semantics of TWO to show the following:
 - Assume that the context C = [bind(y,3)] then the semantic value of '2*y' is 6
 - The semantic value of '2 * let x = 3 in x * x end' is 18
 - The semantic value of 'let x = 1 in let y = x + 1 in y end end' is 2

Exercises

• Use thesemantics to compute the meaning of the following expressions in TWO (use the rules given in the notes, the book has many typos):

```
1) let val y = 3 in 2*y end
```

Note: first construct an abstract syntax tree, then give the representation in Prolog notation, and then show the computation in oursemantics.