

# MoE-Gyro: Self-Supervised Over-Range Reconstruction and Denoising for MEMS Gyroscopes

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## Abstract

MEMS gyroscopes play a critical role in inertial navigation and motion control applications but typically suffer from a fundamental trade-off between measurement range and noise performance. Existing hardware-based solutions aimed at mitigating this issue introduce additional complexity, cost, and scalability challenges. Deep-learning methods primarily focus on noise reduction and typically require precisely aligned ground-truth signals, making them difficult to deploy in practical scenarios and leaving the fundamental trade-off unresolved. To address these challenges, we introduce **Mixture of Experts for MEMS Gyroscopes (MoE-Gyro)**, a novel self-supervised framework specifically designed for simultaneous over-range signal reconstruction and noise suppression. **MoE-Gyro** employs two experts: an Over-Range Reconstruction Expert (ORE), featuring a Gaussian-Decay Attention mechanism for reconstructing saturated segments; and a Denoise Expert (DE), utilizing dual-branch complementary masking combined with FFT-guided augmentation for robust noise reduction. A lightweight gating module dynamically routes input segments to the appropriate expert. Furthermore, existing evaluation lack a comprehensive standard for assessing multi-dimensional signal enhancement. To bridge this gap, we introduce **IMU Signal Enhancement Benchmark (ISEBench)**, an open-source benchmarking platform comprising the GyroPeak-100 dataset and a unified evaluation of IMU signal enhancement methods. We evaluate **MoE-Gyro** using our proposed **ISEBench**, demonstrating that our framework significantly extends the measurable range from  $\pm 450^\circ/\text{s}$  to  $\pm 1500^\circ/\text{s}$ , reduces Bias Instability by 98.4%, and achieves state-of-the-art performance, effectively addressing the long-standing trade-off in inertial sensing.

## 1 Introduction

MEMS gyroscopes are essential inertial sensors extensively utilized in navigation and control systems such as autonomous vehicles, unmanned aerial vehicles (UAVs), robotics, and precision-guided munitions[1, 2, 3]. In these high-dynamic applications, critical performance metrics of gyroscopes include measurement range (full-scale angular velocity) and noise characteristics, notably Angle Random Walk (ARW) and Bias Instability (BI). However, commercial MEMS gyroscopes typically encounter a fundamental performance trade-off: enhancing the measurement range generally results in elevated ARW and BI, whereas sensors optimized for low noise inherently possess a restricted angular velocity measurement capability[4, 5]. This fundamental contradiction significantly limits their effectiveness in high-angular-rate scenarios requiring precise inertial measurements.

Addressing this critical limitation without incurring additional sensor complexity or manufacturing costs remains a significant and unresolved challenge in inertial sensor research. Traditional solutions

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primarily involve structural and circuit-level strategies, such as resonant frequency tuning (mode-splitting)[6, 7], closed-loop force-feedback control[8, 9], and multi-range readout electronics[10]. Although these methods deliver incremental gains, they require tighter fabrication tolerances and more complex control circuitry, increasing both power draw and manufacturing cost [11]. Thus, traditional strategies have yet to adequately resolve these critical trade-offs[12]. Recent advancements in deep learning have emerged as promising solutions for mitigating noise in gyroscopes and, by extension, in complete inertial-measurement-unit (IMU) signals (e.g., CNN[13], LSTM\_GRU[14], HEROS\_GAN[15]). However, these approaches rely on fully supervised training and thus require precisely time-synchronized noisy/clean rotation pairs data that are expensive to collect. Meanwhile, current self-supervised methods (e.g., LIMU-BERT[16], IMUDB[17]) lack a unified framework that handles both denoising and over-range reconstruction, leaving unresolved the core trade-off that low-noise sensors accept only a limited angular rate range. Moreover, previous work is limited to a few single-signal test environments, lacking a multidimensional benchmark that captures the full spectrum of enhancement performance; a public suite spanning diverse operational scenarios is essential for fair comparison and real progress.

To overcome the limitations above, we introduce **MoE-Gyro**, the first self-supervised unified architecture that tackles both over-range reconstruction and denoising. A lightweight gate dynamically routes each input signal segment to two specialized experts, an Over-Range Reconstruction Expert (ORE) and a Over-Range Reconstruction Expert (DE), thus cutting inference memory because, in practice, only a single expert is active for most segments. Both experts are trained end-to-end on a shared Masked Autoencoder(MAE) [18] backbone with purely self-supervised objectives, eliminating the need for costly, time-synchronised ground-truth labels. We further introduce task-specific more optimisations. For the ORE, a Gaussian-Decay Attention (GD-Attn) module in the decoder automatically focuses on the most relevant context for peak reconstruction, while a physics-informed energy regulariser (PINN) enforces consistency with the gyroscope’s mechanical model, boosting generalisation across sensors. For the DE, we adopt a dual-branch complementary cross-mask that captures weak signal features while smoothing high-frequency noise, and we employ FFT-guided noise injection during training to strengthen the learned denoising mapping. Together, these innovations deliver a unified, fully self-supervised solution that simultaneously broadens range and suppresses noise in commercial MEMS gyroscopes. In addition, we release **ISEBench**, the first open-source benchmark with a unified suite of evaluation metrics, providing a common benchmark for future research on IMU signal enhancement. Our key contributions can be summarized as follows:

- Unified self-supervised MoE framework that simultaneously reconstructs over-range signals and reduces noise, breaking the long-standing range–noise trade-off without extra hardware.
- We propose a Gaussian-Decay Attention (GD-Attn) and a physics-informed neural network (PINN) loss, extending the measurable range of a typical  $\pm 450$  °/s MEMS gyroscope to  $\pm 1500$  °/s.
- We design a dual-branch complementary masking strategy combined with FFT-guided augmentation, significantly reducing Bias Instability on the test set by 98.4% .
- We release **ISEBench**, the first open source benchmark specifically tailored for comprehensive evaluation of IMU signal enhancement, along with a dedicated dataset for over-range reconstruction, facilitating fair comparisons and fostering rapid progress within the community.

## 2 Related Works

### 2.1 IMU over-range signal reconstruction.

Reconstructing saturated signal segments in IMUs remains a critical but significantly under explored problem. Among the few representative studies, HEROS-GAN[15] formulates the problem as a fully supervised generative task, relying heavily on paired saturated and reference data for training. Alternatively, Matlab 2023b[19] release introduced a polynomial-based extrapolation function that estimates saturated peaks from their neighboring points; however, this model-driven approach is inherently sensitive to noise and struggles under highly dynamic conditions. However, existing studies have not explored self-supervised approaches or integrated IMU-specific physical constraints into the reconstruction task.

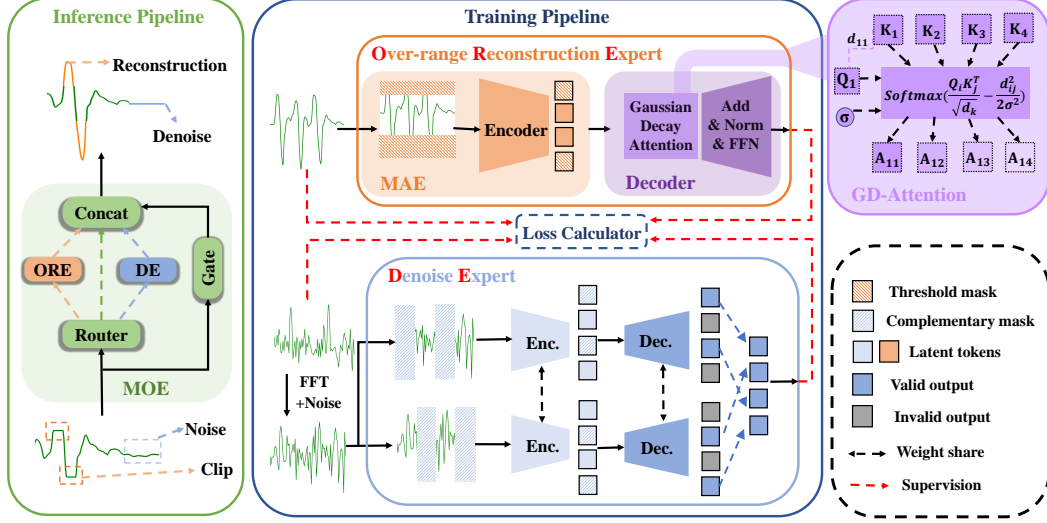


Figure 1: Pipeline of MoE-Gyro framework. During inference, a low-quality signal stream is segmented, routed by a gate to suitable expert, and the enhanced outputs are concatenated to form the final signal. During training, both experts are optimised in a fully self-supervised manner on a shared MAE backbone, each equipped with task-specific masking, attention, and loss mechanisms.

## 2.2 IMU signal denoise.

In contrast to the sparse literature on over-range reconstruction, signal enhancement research for IMUs has largely centred on noise suppression. Classical, model-driven filters such as EMD denoising[20] and Savitzky–Golay smoothing[21] can isolate and attenuate noise, yet they depend on accurate noise priors, which often fail to transfer across sensors or operating conditions. More recent data-driven approaches, including CNN[13], LSTM-GRU hybrids[14], and the IMUDB[17], replace explicit priors with learned representations and have therefore attracted wider adoption.

## 3 Method

**Motivation.** Although recent supervised and self-supervised models have markedly improved IMU denoising, simply grafting multiple task heads onto one backbone to unify denoising and over-range reconstruction proves unreliable. After normalization, clipped-peak errors dwarf background noise by several orders of magnitude, so reconstruction gradients dominate training, and the network largely ignores the denoising head. The resulting scale-imbalance leaves one task under-fitted and the other only partially solved, curbing overall accuracy and generalization[22, 23, 24].

This observation motivates a decoupled, self-supervised Mixture-of-Experts design in which each task is handled by a dedicated specialist while global features are shared only when beneficial. By adopting a shared Masked Autoencoder (MAE) encoder combined with lightweight task-specific decoders, each expert is allowed to specialize independently. Moreover, we introduce dedicated task-oriented masking strategies, a Gaussian-Decay Attention mechanism, and physics-informed constraints to ensure stable and targeted optimization. This modular, decoupled design ultimately enables more effective training and significantly improved enhancement performance.

**Overview.** Figure 1 shows the **MoE-Gyro** architecture for self-supervised inertial signal enhancement. The raw signal is first segmented, and a gate then applies a simple heuristic to route each segment to the Over-Range Reconstruction Expert (ORE), the Denoise Expert (DE), both experts, or directly to the output. The ORE follows a standard MAE backbone but adds a task-specific threshold mask to focus on in-range features, and inserts a Gaussian-Decay Attention block in the decoder to selectively amplify peak region information during reconstruction. The DE adopts a dual-branch MAE design in which two parameter-shared encoders/decoders operate on complementary masks, allowing the network to capture intrinsic signal correlations while aggressively suppressing high-

frequency noise. Finally, the gated outputs of the two experts are concatenated to yield the enhanced signal. The precise routing and concating logic is summarized in Algorithm 1.

### 3.1 Over-range Reconstruction Expert

**Gaussian-Decay Attention.** Windowed or local attention has proved effective in vision and language models because it reduces distraction from distant, less relevant context[25, 26]. Such locality is especially valuable for over-range reconstruction, because the information required to restore a clipped peak is concentrated within a short temporal window around the peak. However, a fixed window ignores sensor-specific dynamics and, being a non-differentiable mask, cannot adapt itself during learning. Inspired by these issues, we introduce **Gaussian-Decay Attention (GD-Attn)**, which replaces the binary window mask with a learnable, continuous Gaussian bias. For a query-key pair  $(i, j)$  separated by  $d_{ij} = |i - j|$  steps, GD-Attn adds a learnable Gaussian bias  $B_{ij} = -\frac{d_{ij}^2}{2\sigma^2}$ , where the single trainable parameter  $\sigma$  is initialised to a nominal window size and clamped for stability. With queries  $Q$ , keys  $K$ , and values  $V$ , the resulting attention is

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#### Algorithm 1: MoE route and concat

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**Input:** segment  $x[1:L]$

**Output:** enhanced  $y[1:L]$

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```

1  $y \leftarrow x$ ;
2  $peak \leftarrow$  3 consecutive clipped?;
3  $noise \leftarrow$  run of  $n$  samples  $< \tau$ ?;
4 if  $peak$  then
5    $\hat{p} \leftarrow$  PeakExpert( $x$ )
6 end
7 if  $noise$  then
8    $\hat{n} \leftarrow$  DenoiseExpert( $x$ )
9 end
10 for  $t \leftarrow 1$  to  $L$  do
11   if  $peak$  and  $x_t$  clipped then
12      $y_t \leftarrow \hat{p}_t$ ;
13   else if  $noise$  and  $|x_{t:t+n-1}| < \tau$  then
14      $y_{t:t+n-1} \leftarrow \hat{n}_{t:t+n-1}$ ;  $t \leftarrow t + n$ ;
15   end
16 end
17 return  $y$ 
```

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$$\text{Output} = \tilde{A}V, \quad \tilde{A} = \text{softmax}(QK^\top / \sqrt{d_k} + B) \quad (1)$$

This Gaussian bias yields a soft, differentiable window whose effective width is learned end-to-end; as  $\sigma \rightarrow \infty$  the bias disappears and GD-Attn reduces to standard global attention, whereas finite  $\sigma$  smoothly down-weights distant tokens and concentrates capacity on the peak region.

**Correlation Loss.** Pure  $L_2$  reconstruction matches amplitudes but overlooks local dynamics, often smoothing peaks. To recover both trend and extrema we define a two-term *correlation loss*  $\mathcal{L}_{\text{corr}}$ :

$$\mathcal{L}_{\text{corr}} = \frac{1}{|\mathcal{M}|} \sum_{t \in \mathcal{M}} (\Delta x_t - \Delta \hat{x}_t)^2 + \lambda_{\text{sign}} \frac{1}{|\mathcal{E}|} \sum_{t \in \mathcal{E}} (x_t - \hat{x}_t)^2 \quad (2)$$

where  $\Delta x_t = x_t - x_{t-1}$  and  $\Delta \hat{x}_t$  are first-order differences of the ground-truth and reconstructed signals;  $\mathcal{M}$  is the set of masked time steps;  $\mathcal{E} = \{t \in \mathcal{M} \mid \text{sign}(\Delta x_t) \neq \text{sign}(\Delta x_{t+1})\}$  marks sign-change (peak/valley) positions within the mask; and  $\lambda_{\text{sign}}$  weights the extremum term ( $\lambda_{\text{sign}} = 1$  by default). The first term aligns local slopes, while the second preserves peak and valley amplitudes, jointly yielding sharper and more faithful reconstructions.

**Physics-informed energy loss (PINN).** To improve generalisation and ensure that the reconstructed waveform remains physically plausible, we add a physics-informed regulariser derived from the displacement-power relationship of an IMU's proof mass. Let  $x_t$  denote the reconstructed angular-rate (or acceleration) sequence inside the masked region  $\mathcal{M}$ . We compute the first and second discrete derivatives  $\Delta x_t = x_t - x_{t-1}$ ,  $\Delta^2 x_t = x_{t+1} - 2x_t + x_{t-1}$ , and define the instantaneous *specific power*  $e_t = (\Delta^2 x_{t-1} + \Delta^2 x_t) \Delta x_t$ . Averaging over the mask gives the normalised energy

$$\bar{E} = \frac{1}{|\mathcal{M}|} \sum_{t \in \mathcal{M}} e_t, \quad E_{\text{norm}} = \sigma(\bar{E}) \quad (3)$$

where  $\sigma(\cdot)$  is the sigmoid. Extremely low or high power violates the mass-spring dynamics implicit in most MEMS sensors, so we penalise both extremes with a barrier term

$$\mathcal{L}_{\text{pinn}} = -\log(E_{\text{norm}}) - \kappa \log(1 - E_{\text{norm}}) \quad (4)$$

where  $\kappa$  balances the two sides ( $\kappa = 1$  in all experiments). This loss drives the reconstructed segment toward a moderate energy level, complementing the  $L_2$  and correlation objectives.

### 3.2 Denoise expert

**Dual-branch complementary masking.** The Denoise Expert employs a **dual-branch MAE** whose two branches share all encoder and decoder weights[27, 28]. For each length- $L$  segment we construct two fixed 50 % masks in a cross pattern so that every even patch index is visible to branch A and masked for branch B, and vice-versa. Formally,  $\mathcal{M}_A \cup \mathcal{M}_B = \{1, \dots, L\}$  and  $\mathcal{M}_A \cap \mathcal{M}_B = \emptyset$ , guaranteeing complementarity. Each branch receives the same noisy input but reconstructs only its own masked positions, which prevents information leakage while ensuring that no salient sample is ever hidden from both branches. After patch embedding the two masked sequences are processed by the shared encoder, padded with mask tokens, and decoded. The partial reconstructions  $y_A$  and  $y_B$  are fused as  $y_{\text{final}} = y_A \cdot \mathcal{M}_A + y_B \cdot \mathcal{M}_B$ , yielding a full-length denoised signal. Weight sharing regularises the model and promotes the extraction of universal features, enabling more effective suppression of high-frequency random noise.

**FFT-guided training augmentation.** Inspired by noise-injection strategies proven effective in speech enhancement[29, 30], we introduce an FFT-guided noise-injection scheme that synthesises spectrally matched corruption to create realistic training pairs. We create realistic pairs on-the-fly by injecting weak but genuine motion snippets, guided by the noise power spectrum: (1) Noise-floor estimation: For each raw noise segment we compute its FFT and obtain the power-spectral density (PSD). The median PSD value serves as the local noise floor  $P_{\text{noise}}$ . (2) Weak-signal injection: We randomly sample a short motion clip  $s(t)$  from a separate repository of real IMU recordings (e.g., walking, hand-held rotations). The clip is amplitude-scaled to  $\alpha s(t)$  with  $\alpha = \beta \sqrt{P_{\text{noise}}} / \max_t |s(t)|$ , where  $\beta$  is a constant. The scaled clip is then added to the raw noise, yielding  $x_{\text{mix}}(t) = x_{\text{noise}}(t) + \alpha s(t)$ . (3) Additional corruption: After analysing the PSD, we synthesise spectrally matched noise (targeting the frequency bands that dominate QN, ARW, and BI) and add it to the mixture, producing a heavier corruption that forces the model to learn a true denoising mapping rather than smoothing  $x_{\text{mix}} \leftarrow x_{\text{mix}} + x'_{\text{noise}}(t)$ . (4) Training target: The mixture  $x_{\text{mix}}$  is fed to the dual-branch MAE, while the reference signal is defined as  $x_{\text{clean}} = x_{\text{noise}}(t) + \alpha s(t)$ , without the extra corruption. This forces the network to suppress the added noise yet retain the weak real motion. This FFT-guided augmentation supplies a realistic, controllable SNR and teaches the model to enhance subtle motion cues rather than over-smooth them.

## 4 Datasets & Benchmark

This section first details the datasets used for training and evaluation, and then describes **IMU Signal Enhancement Benchmark (ISEBench)**, the unified benchmark we release for fair and comprehensive assessment of IMU signal enhancement methods.

### 4.1 Datasets

We conduct all experiments on three publicly available dataset. **GyroPeak-100** (released with this paper) is a 100 Hz collection captured from the iPhone 14 on-board IMU with ground-truth peak annotations and serves as the sole source for training and evaluating the over-range reconstruction network. For the denoising task we adopt the Visual-Inertial dataset [17] and the Autonomous Platform Inertial dataset [31], both down-sampled to 100 Hz for consistency. Together, these datasets cover a broad spectrum of motion dynamics, providing a balanced and comprehensive testbed for the proposed signal-enhancement pipeline. We follow an 80 / 20 split of each dataset for training and testing, respectively, and all experiments are executed on a single NVIDIA RTX-4060 GPU.

### 4.2 ISEBench: IMU Signal Enhancement Benchmark

To systematically and objectively evaluate the performance of the proposed inertial signal enhancement methods, we introduce and design a comprehensive testbench named **IMU Signal Enhancement Benchmark (ISEBench)**. The **ISEBench** is specifically tailored for inertial measurement unit (IMU) signal enhancement, providing a unified evaluation framework that covers multiple practical scenarios.

Table 1: Performance comparison on **ISEBench**. The best result is **boldfaced** and the second best is underlined. For clarity, each P\_MSE entry is written as  $P\_MSE_i/P\_MSE_{RAW}$ , and all Allan-variance metrics are reported as the percentage reduction relative to the raw signal (the omitted values are provided in Appendix C).

Model\Metric	Peak Rec. ( $\tau = 450^\circ/s$ )			Weak Sig. SNR $\uparrow$ dB	Allan Variance			AVG.rank
	PSNR $\uparrow$ dB	P_MSE $\downarrow$ -	Corr $\uparrow$ -		QN $\downarrow$ ( $^\circ/s$ )	ARW $\downarrow$ ( $^\circ/\sqrt{h}$ )	BI $\downarrow$ ( $^\circ/h$ )	
RAW	2.67	1	-	10.18	0	0	0	-
Matlab 2023[19]	6.03	0.515	0.86	10.02	-25.8%	-3.1%	+5.4%	7.0
EMD[20]	5.44	0.655	0.77	13.85	-91.1%	-85.9%	<u>-96.8%</u>	5.3
SG_filter[21]	4.35	0.767	0.79	12.03	-85.0%	-86.3%	-90.0%	6.6
CNN[13]	5.76	0.621	0.85	14.3	-62.5%	-35.9%	-79.4%	6.1
LSTM_GRU[14]	5.95	0.495	0.87	<u>19.23</u>	-80.8%	-85.0%	-93.1%	4.3
KNN[31]	3.72	0.752	0.67	12.54	-85.7%	-34.3%	-47.5%	7.7
HEROS_GAN[15]	<u>7.7</u>	<u>0.354</u>	<u>0.89</u>	16.86	<u>-92.8%</u>	-51.6%	-58.3%	3.6
IMUDB[17]	6.59	0.442	0.82	17.76	-85.8%	<u>-87.8%</u>	-93.7%	<u>3.4</u>
<b>MoE-Gyro</b>	<b>8.19</b>	<b>0.325</b>	<b>0.92</b>	<b>24.19</b>	<b>-98.0%</b>	<b>-94.1%</b>	<b>-98.4%</b>	<b>1</b>

Different from prior works that typically rely on isolated or single evaluation metrics, **ISEBench** incorporates a structured metric set categorized into three distinct aspects to thoroughly quantify enhancement performance.

**Evaluation Metrics: 1. Over-range Reconstruction Metrics:** Over-range reconstruction assesses the model’s ability to recover over-range peaks that are lost when the raw signal is clipped at a dynamic-range threshold  $\tau$  before being fed to the network. During evaluation we supply the model with the clipped input  $x_{\text{clip}} = \text{clip}(x, \pm\tau)$  while using the unclipped signal  $x$  as ground truth, and we compute all metrics only on those samples for which  $|x| > \tau$ . Concretely, we report **Peak Signal-to-Noise Ratio (PSNR)**, which measures the reconstruction quality of the clipped portions;

$$MSE = \frac{1}{N} \sum_{t=1}^N (x_t - \hat{x}_t)^2, \quad \text{PSNR} = 10 \log_{10} \left( \frac{(|\text{Peak}_{\max}| - |\tau|)^2}{MSE} \right). \quad (5)$$

**Correlation (Corr)**, the Pearson linear correlation[32] between the reconstructed and ground-truth waveforms over the same peak regions; and **Peak Mean-Squared Error (PMSE)**, which provides a point-wise accuracy measure at the detected peak locations. Let  $\mathcal{P}$  be the index set of local peaks;

$$\text{PMSE} = \frac{1}{|\mathcal{P}|} \sum_{t \in \mathcal{P}} (y_t - \hat{y}_t)^2. \quad (6)$$

**2. Weak Signal Enhancement Metric:** This metric assesses the capability of the proposed approach in extracting and enhancing low-amplitude signals: **Signal-to-Noise Ratio (SNR)**[33] evaluates weak signal recovery effectiveness. **3. Static Noise Performance Metrics:** To characterize sensor performance in static (non-moving) conditions, we adopt standard inertial measurement unit performance metrics defined by Allan variance[34], including: **Angle Random Walk (ARW)**, **Quantization Noise (QN)** and **Bias Instability (BI)**. These metrics are computed following standard Allan variance analysis methodology described comprehensively in prior studies. The formulas for the above seven metrics are given in the Appendix A.

Together, these metrics constitute **ISEBench**, a unified and transparent yardstick for inertial-signal-enhancement research. In the following experiments we leverage **ISEBench** to benchmark our model against state-of-the-art baselines, highlighting its effectiveness.

## 5 Experiments

### 5.1 Comparison with Previous Results

For the quantitative comparison, we pit **MoE-Gyro** against nine carefully reproduced baselines drawn from three methodological families: classic model-driven signal processors (EMD, Savitzky–Golay filtering, and the Matlab over-range signal reconstruction function); fully supervised deep networks (CNN, kNN, LSTM–GRU and HEROS\_GAN); and the self-supervised model, IMUDB. To ensure fairness, all supervised baselines are retrained on matched data: clipped and full pairs from our Peak

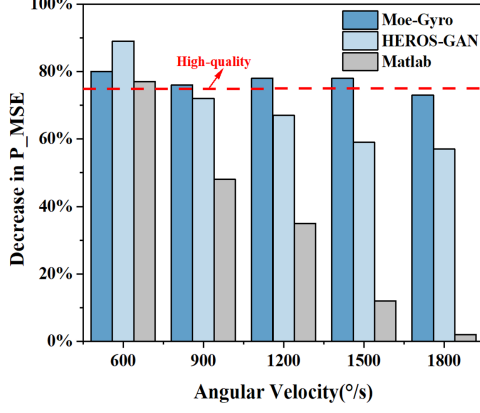


Figure 2: Comparison of reconstruction P\_MSE. We compare **MoE-Gyro** with two representative baselines, a drop of more than 75 % (dashed reference) marks high-quality recovery.

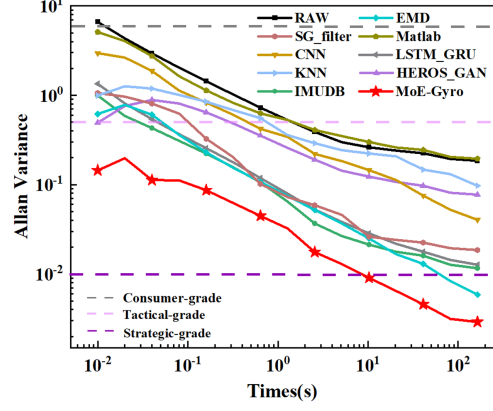


Figure 3: Allan-variance comparison. The red curve corresponds to **MoE-Gyro** and shows the best Allan-variance performance—raising the device from consumer to nearly strategic grade.

database for over-range reconstruction and clean/noisy pairs from the *Autonomous Platform Inertial* dataset for denoising. Each method is executed exactly as specified in its original paper, using the authors’ code when available or a validated re-implementation otherwise. The resulting performance in **ISEBench** is summarized in Table 1. **MoE-Gyro** attains the best average rank across all metrics.

We analyze the performance of different methods separately for over-range reconstruction and denoising tasks. Regarding over-range reconstruction, Table 1 shows that classical model-driven methods indeed raise PSNR and Corr, but their P\_MSE remains large, revealing limited accuracy at the peak locations. Because these methods extrapolate by incrementally fitting the visible portion of the waveform. Meanwhile, we compare **MoE-Gyro** with the best data-driven baseline (HEROS-GAN) and the best model-driven baseline (Matlab2023) by plotting the relative P\_MSE reduction at different angular velocity thresholds (Fig. 2). At 1500°/s our method still achieves high-quality peak reconstruction, whereas HEROS-GAN deteriorates noticeably beyond 900°/s; the model-driven filter ceases to reconstruct peaks effectively once the angular velocity exceeds 600°/s. These results further substantiate the limitations discussed above. **MoE-Gyro** outperforms all baselines thanks to (i) an adaptive MAE mask that keeps peak-relevant patches, (ii) Gaussian-Decay Attention that concentrates decoding on the clipped region, and (iii) a carefully engineered loss that restores local dynamics (see ablations).

In terms of denoising performance, classical filters lower Allan-variance terms but also erase faint motion, so SNR barely improves. Supervised deep-learning baselines, trained as single multitask networks, likewise sacrifice SNR because the much larger reconstruction loss dominates optimisation. By routing segments to a dedicated Denoise Expert and training it with FFT-guided noise augmentation, **MoE-Gyro** delivers the highest SNR while further reducing QN, ARW, and BI; Allan-variance curves in Fig.3 visualise the gain.

## 5.2 Real-world Experiment

To intuitively demonstrate the practical capability of our framework in handling severe over-range conditions, we randomly select a representative segment from the test set for visualization (Fig. 4). The segment includes measurements from a low-range IMU (IM900,  $\pm 450^\circ/\text{s}$ ), the corresponding ground truth, and the enhanced output from our

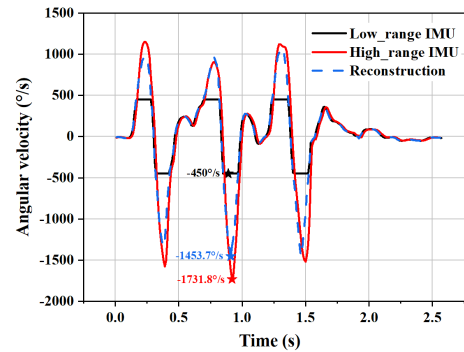


Figure 4: Range-extension visualisation. At an actual angular rate of  $-1731.8^\circ/\text{s}$ , our method reconstructs the signal clipped at the  $450^\circ/\text{s}$  sensor limit to  $-1453.7^\circ/\text{s}$ .

Table 2: MoE ablation results.

Model	PSNR $\uparrow$	SNR $\uparrow$	Mem $\downarrow$
ORE+DE	8.19	24.58	129
SingleNet	7.23	12.9	64.7
<b>MoE-Gyro</b>	<b>8.19</b>	<b>24.19</b>	<b>71.3</b>

Table 3: Impact of GD-Attn Placement

Setting	PSNR $\uparrow$	P_MSE $\downarrow$	Corr $\uparrow$
No GD-Attn	8.08	0.345	0.87
Encoder-only	8.03	0.345	0.88
Enc.+Dec.	8.27	0.335	0.90
<b>Decoder-only</b>	<b>8.29</b>	<b>0.324</b>	<b>0.92</b>

**MoE-Gyro.** At the highlighted peak, the true angular velocity reaches  $-1731.8^\circ/\text{s}$ , significantly exceeding the measurement limit of the IM900 sensor. Despite this substantial clipping, **MoE-Gyro** effectively reconstructs the peak to  $-1453.7^\circ/\text{s}$ , accurately capturing key signal dynamics beyond the nominal range. By contrast, the best competing method we tested lifts the same peak only to  $-1287^\circ/\text{s}$  and exhibits pronounced waveform distortion around the apex, detailed traces are provided in Appendix C. This capability suggests substantial potential for expanding the practical utility of low-cost, limited-range inertial sensors.

### 5.3 Ablation Studies

In this section, we conduct ablation experiments on the components of our method. By systematically enabling or disabling each component, or substituting it with simpler counterparts, we quantify how much performance each element contributes to the final system.

**Ablation on the MoE.** To assess the impact of the MoE architecture itself, we compare alternative expert-invocation schemes with a single multi-task network of equal size. Table 2 shows that the full MoE-Gyro achieves virtually identical enhancement to calling both the ORE and DE, indicating that the router and concatenation do not degrade either task. A single multi-task network of identical size trails behind on both metrics, confirming the advantage of explicit task decoupling. Since most of the time the MoE architecture calls only a single expert to process a segment, **MoE-Gyro** requires roughly half GPU memory consumed when both experts are run unconditionally, while matching their combined quality, demonstrating a clear efficiency gain.

#### Ablation on the Over-range Reconstruction Expert.

We systematically evaluate the individual contributions of GD-Attn, the correlation loss, and the PINN regularizer in our Over-range Reconstruction Expert. First, we investigate the optimal placement of the GD-Attn module (Tab. 3). Results show decoder-only integration of GD-Attn achieves the largest improvement. This demonstrates GD-Attn’s critical role in refining latent representations specifically at the decoding stage, effectively focusing reconstruction capacity on clipped regions.

Second, we compare our proposed physics-informed energy loss (PINN) against a conventional second-order smoothness prior (Tab. 4)[35, 36]. When evaluated on unseen data, our PINN consistently outperforms the smoothness regularizer, improving PSNR by 0.27 dB and reducing P\_MSE by 8%, highlighting the strong generalization ability provided by the physics-based constraint.

Finally, we comprehensively explore all combinations to quantify their cumulative and complementary effects (Tab. 5). Individually,

GD-Attn significantly improves peak restoration, correlation loss notably enhances waveform fidelity, and PINN markedly stabilizes signal reconstruction. Jointly, these components interact positively, resulting in the best overall trade-off in reconstruction quality and stability.

Table 4: PINN vs. Second-Order Smoothness.

Loss	PSNR $\uparrow$	P_MSE $\downarrow$	Corr $\uparrow$
Smoothness	8.02	0.354	0.88
<b>PINN (<math>\kappa = 1</math>)</b>	<b>8.29</b>	<b>0.324</b>	<b>0.92</b>

Table 5: Component ablation results.

Model	PSNR $\uparrow$	P_MSE $\downarrow$	Corr $\uparrow$
No Components	7.68	0.369	0.88
GD-Attn	7.96	0.364	0.90
Corr	7.83	0.354	0.91
PINN	7.95	0.345	0.90
GD+Corr	8.21	0.350	0.91
GD+PINN	8.19	0.339	0.91
Corr+PINN	8.08	0.340	0.91
<b>All</b>	<b>8.29</b>	<b>0.324</b>	<b>0.92</b>



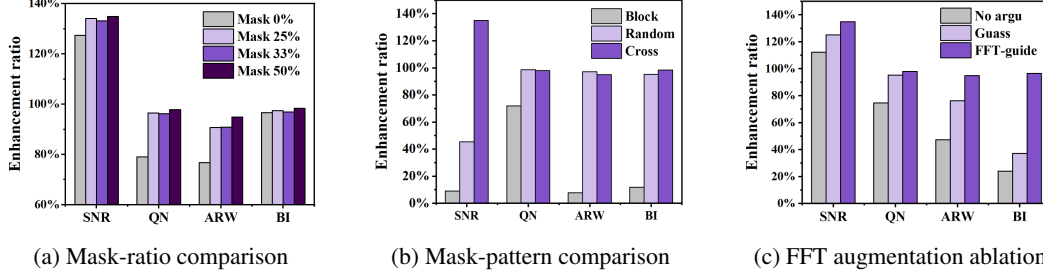


Figure 5: Ablation studies for the Denoise Expert. (a) Mask ratio: a 50 % mask yields the strongest denoising effect; (b) Mask pattern: the cross mask outperforms block and random patterns; (c) FFT augmentation: FFT-guided noise injection gives the largest performance gain.

**Ablation on the Denoise Expert.** We isolate and analyze three key design choices within the denoising expert: mask strategy, weight sharing, and augmentation strategy. First, we optimize the complementary mask ratio from 0% to 50% (Fig. 5a), finding that a dual-branch architecture with a 50% mask ratio consistently yields superior noise suppression performance. Next, holding this ratio fixed, we compare different mask patterns (Fig. 5b). A block mask removes large contiguous regions and thus underperforms significantly, while random masking shows improvements on Allan metrics but still exhibits suboptimal SNR due to residual noise leakage. Our deterministic cross mask achieves the best balance, matching random masking on Allan metrics while outperforming in SNR, attributed to complete temporal coverage and minimal information gaps.

We then examine the effectiveness of parameter sharing between branches (Tab. 6). While independent branches double model capacity, full encoder-decoder weight sharing reduces parameters by 50% and GPU memory usage by 45% with negligible impact on denoising quality. Partial sharing variants either reduce efficiency gains or degrade signal quality. Thus, full weight sharing represents the optimal complexity-performance trade-off and is adopted.

Table 6: Weight-Sharing study

Weight sharing	SNR $\uparrow$	GPU mem $\downarrow$	Params $\downarrow$
No share	24.51	116.8	27.8
E share	24.35	76.2	17.15
D share	24.27	105.0	24.64
<b>E+D share</b>	<b>24.19</b>	<b>64.4</b>	<b>13.9</b>

Finally, we evaluate the impact of our FFT-guided augmentation strategy (Fig. 5c). Compared to a baseline without augmentation, Gaussian noise injection modestly improves SNR but leaves Allan metrics largely unaffected. Our FFT-guided augmentation introducing spectrally matched synthetic noise, achieves comprehensive gains across all metrics. These results validate the superiority of using realistic spectral characteristics to train a more robust denoiser.

## 6 Conclusion

In this work, we introduced **MoE-Gyro**, a novel self-supervised Mixture-of-Experts framework tailored to simultaneously address the long-standing trade-off between measurement range and noise performance in MEMS gyroscopes. **MoE-Gyro** leverages masked autoencoder (MAE) architectures to independently optimize two dedicated experts: an Over-Range Reconstruction Expert (ORE), enhanced by Gaussian-Decay Attention and physics-informed constraints for accurate reconstruction of saturated signals; and a Denoise Expert (DE), utilizing complementary masking and FFT-guided augmentation to significantly reduce noise without requiring labeled data. Additionally, we introduced **ISEBench**, the first open-source evaluation benchmark designed for fair and comprehensive assessment of IMU signal-enhancement methods. Experiments on **ISEBench** demonstrated that **MoE-Gyro** extends the measurable range from  $\pm 450$  °/s to  $\pm 1500$  °/s and reduces Bias Instability by 98.4%, significantly surpassing existing baselines. Despite these advancements, the relatively large size of our proposed architecture may pose challenges for resource-constrained embedded deployments; future work could thus explore model compression techniques to enable more efficient deployment. Our study opens a promising path to deep learning-based performance upgrades for MEMS inertial sensors and establishes a solid baseline for future research in inertial signal enhancement.

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## A Metric Definitions in ISEBENCH

For completeness we list the analytical forms of the seven evaluation metrics used throughout ISEBENCH. Let  $y = \{y_t\}_{t=1}^N$  be the ground-truth sequence,  $\hat{y} = \{\hat{y}_t\}_{t=1}^N$  the reconstructed (or denoised) sequence, and  $\mathcal{P} \subseteq \{1, \dots, N\}$  the set of local peaks or valleys indices.

### A.1 Over-range reconstruction metrics

**Peak-averaged PSNR.** For each test segment  $s$  we first locate its maximum absolute in-range value  $\text{Peak}_{\max}^{(s)} = \max_{t \in s} |y_t|$  and then compute the dataset-level mean peak

$$\overline{\text{Peak}}_{\max} = \frac{1}{S} \sum_{s=1}^S \text{Peak}_{\max}^{(s)}. \quad (7)$$

Let Clip denote the sensor’s full-scale range (e.g.  $\pm 450^\circ/\text{s}$ ). The peak-averaged PSNR is defined as

$$\text{PSNR} = 10 \log_{10} \left( \frac{(\overline{\text{Peak}}_{\max} - \text{Clip})^2}{\frac{1}{N} \sum_{t=1}^N (y_t - \hat{y}_t)^2} \right). \quad (8)$$

Here the numerator reflects the *average recoverable headroom* between the sensor’s clip level and the typical (mean) peak amplitude, yielding a scale that is consistent across all segments.

**Correlation (Corr).** Corr measures the linear similarity between the reconstructed signal  $\hat{y}$  and the ground truth  $y$ , serving as an indicator of reconstruction linearity. It is defined as:

$$\text{Corr} = \frac{\sum_{t=1}^N (y_t - \bar{y})(\hat{y}_t - \bar{\hat{y}})}{\sqrt{\sum_{t=1}^N (y_t - \bar{y})^2} \sqrt{\sum_{t=1}^N (\hat{y}_t - \bar{\hat{y}})^2}} \quad (9)$$

where  $\bar{y} = \frac{1}{N} \sum_{t=1}^N y_t$  and  $\bar{\hat{y}} = \frac{1}{N} \sum_{t=1}^N \hat{y}_t$  are the mean values of the true and reconstructed sequences, respectively, over  $N$  samples.

**Peak Mean Squared Error (P\_MSE).** P\_MSE directly measures the average reconstruction error at the clipped-peak locations, quantifying the fidelity of peak recovery. Let  $\mathcal{P}$  be the set of time indices where the true signal exceeds the sensor’s range (i.e. the clipped samples). Then

$$\text{P\_MSE} = \frac{1}{|\mathcal{P}|} \sum_{t \in \mathcal{P}} (y_t - \hat{y}_t)^2 \quad (10)$$

where  $y_t$  is the ground truth and  $\hat{y}_t$  the reconstructed value at sample  $t$ .

### A.2 Weak Signal Enhancement Metric

**Signal-to-Noise Ratio (SNR).** SNR quantifies the relative power of the desired signal versus background noise. Let  $\{s_t\}_{t=1}^N$  be the segment of interest and  $\{n_t\}_{t=1}^N$  the corresponding noise-only sequence. We define

$$P_{\text{signal}} = \frac{1}{N} \sum_{t=1}^N s_t^2, \quad P_{\text{noise}} = \frac{1}{N} \sum_{t=1}^N n_t^2. \quad (11)$$

Then

$$\text{SNR} = 10 \log_{10} \left( \frac{P_{\text{signal}}}{P_{\text{noise}}} \right). \quad (12)$$

### A.3 Weak Signal Enhancement Metric

**Allan Variance Computation.** Given a sequence of angular-rate measurements  $\{x_k\}$  sampled at interval  $T_0$ , we first form non-overlapping averages over clusters of length  $\tau = m T_0$ :

$$\bar{x}_i(\tau) = \frac{1}{m} \sum_{k=(i-1)m+1}^{im} x_k, \quad i = 1, \dots, M, \quad (13)$$

where  $M = \lfloor N/m \rfloor$ . The Allan variance at cluster time  $\tau$  is then

$$\sigma_y^2(\tau) = \frac{1}{2(M-1)} \sum_{i=1}^{M-1} \left( \bar{x}_{i+1}(\tau) - \bar{x}_i(\tau) \right)^2, \quad (14)$$

and the Allan deviation is  $\sigma_y(\tau) = \sqrt{\sigma_y^2(\tau)}$ .

From  $\sigma_y(\tau)$  we derive three standard performance parameters:

$$\text{QN} = \frac{\sigma_{-1}(1)}{\sqrt{3}} \quad (\text{slope } -1 \text{ at } \tau = 1) \quad (15)$$

$$\text{ARW} = \sigma_{-\frac{1}{2}}(1) \quad (\text{slope } -\frac{1}{2} \text{ at } \tau = 1) \quad (16)$$

$$\text{BI} = \sigma_{y,\min} \sqrt{\frac{2 \ln 2}{\pi}} \quad (17)$$

Here,  $\sigma_{-1}(1)$  denotes the value of  $\sigma_y(\tau)$  at  $\tau = 1$  extrapolated along the slope  $-1$  region, and  $\sigma_{-\frac{1}{2}}(1)$  denotes the analogous intercept for the slope  $-1/2$  region. Within the testbench, QN and ARW are extracted from the log-log slopes of the raw signal's Allan deviation curve and  $\sigma_{y,\min}$  is the minimum deviation used to compute bias instability.

## B Derivation of the Physics-Informed Energy Loss

**Mechanical background.** For a MEMS proof mass of unit mass ( $m=1$ ) moving along one axis, the instantaneous mechanical energy is  $\mathcal{E}(t) = \frac{1}{2}v^2(t) + \frac{1}{2}kx^2(t)$ , where  $x(t)$  and  $v(t) = \dot{x}(t)$  are displacement and velocity, and  $k$  is the effective spring constant. The specific power(time rate of change of energy per unit mass) is

$$\mathcal{P}(t) = \frac{d\mathcal{E}}{dt} = a(t)v(t), \quad a(t) = \ddot{x}(t). \quad (18)$$

**Discrete approximation.** Our network reconstructs a discrete angular-rate (or acceleration) sequence  $\{x_t\}_{t \in \mathbb{Z}}$  with unit sample period ( $\Delta t=1$ ). We approximate the first and second derivatives by

$$\Delta x_t = x_t - x_{t-1}, \quad \Delta^2 x_t = x_{t+1} - 2x_t + x_{t-1}. \quad (19)$$

Substituting (16) into (17) and centring the acceleration term yields a discrete specific power

$$e_t = \underbrace{\left( \frac{1}{2}\Delta^2 x_{t-1} + \frac{1}{2}\Delta^2 x_t \right)}_{\text{acc. at } t} \Delta x_t. \quad (20)$$

**Mask-averaged normalised energy.** Given the set  $\mathcal{M}$  of masked (to-be-reconstructed) indices, we take the mean specific power

$$\bar{E} = \frac{1}{|\mathcal{M}|} \sum_{t \in \mathcal{M}} e_t, \quad (21)$$

and pass it through a sigmoid  $E_{\text{norm}} = \sigma(\bar{E}) \in (0, 1)$  to bound the value and allow symmetrical penalties on both extremes.

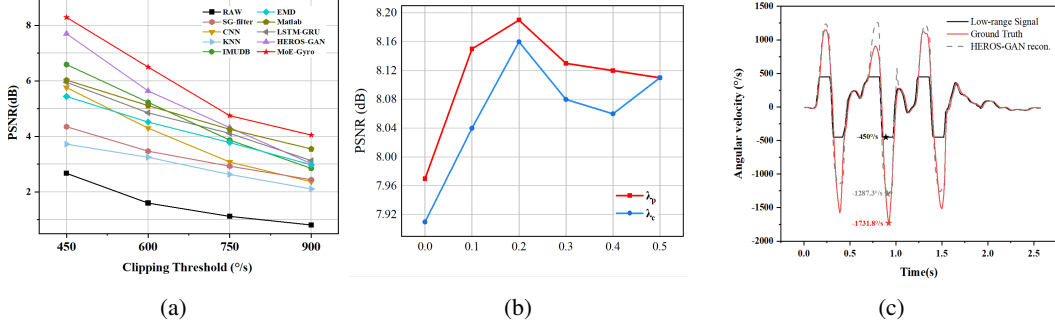


Figure 6: Additional Experiments. (a) Clipping-Threshold Analysis. **MoE-Gyro** maintains the best performance across all tested saturation, model-driven methods improve in relative ranking as the threshold rises. (b) Sensitivity analysis of  $\lambda$  in loss; (c) Reconstruction by HEROS-GAN.

**Barrier formulation.** Very small  $E_{\text{norm}}$  corresponds to an over-damped (excessively smooth) reconstruction, whereas values near one indicate unphysical high-frequency ringing. We therefore introduce the barrier

$$\mathcal{L}_{\text{pinn}} = -\log(E_{\text{norm}}) - \kappa \log(1 - E_{\text{norm}}). \quad (22)$$

where  $\kappa$  balances the penalty on the high-energy side ( $\kappa=1$  in our experiments). Minimising (20) drives  $E_{\text{norm}}$  toward a moderate value, enforcing a physically plausible energy level while remaining fully differentiable.

## C Supplementary Experiments and Data

**Analysis on clipping threshold.** In the main text we report results for a clipping threshold of  $\pm 450^\circ/\text{s}$ . To evaluate robustness under more severe saturation, we additionally clip all test signals at  $\pm 600^\circ/\text{s}$ ,  $\pm 750^\circ/\text{s}$  and  $\pm 900^\circ/\text{s}$  and repeat the reconstruction experiments. For each clipping range, the corrupted signals are processed by our Over-Range Expert and the PSNR is computed.

As depicted in Figure 6a, increasing the clipping threshold naturally reduces the average recoverable headroom  $\text{Peak}_{\text{max}} - \text{Clip}$ , leading to lower absolute PSNR values. Crucially, however, our Over-Range Expert still delivers substantial PSNR gains over the raw clipped signals at every tested threshold, demonstrating its robustness across sensors with varying measurement ranges.

**Loss-weight sensitivity.** The total reconstruction loss is  $\mathcal{L} = L_2 + \lambda_c L_{\text{corr}} + \lambda_p L_{\text{pinn}}$ . We fix  $\lambda_p = 0.5$  and vary  $\lambda_c$  from 0.1 to 0.5, then fix  $\lambda_c = 0.5$  and vary  $\lambda_p$  over the same range. As shown in Figure 5(b), the highest PSNR is achieved at  $(\lambda_c, \lambda_p) = (0.5, 0.2)$ . We also evaluated the symmetric setting ( $\lambda_c = \lambda_p = 0.2$ ), which underperformed the asymmetric combination. Therefore, we adopt  $\lambda_{L_2} = 1$ ,  $\lambda_c = 0.5$ , and  $\lambda_p = 0.2$  for all over-range reconstruction experiments.

**Real-World Over-Range Reconstruction with HEROS-GAN.** To benchmark against the current state of the art, we applied HEROS-GAN[15] to the same real-world test segment (Fig.6c). While HEROS-GAN succeeds at reconstructing the overall waveform shape, it systematically underestimates extreme values—recovering the highlighted peak to only  $-1287.3^\circ/\text{s}$ —and introduces spurious oscillations. This behavior underscores its limited capacity for precise peak recovery under severe clipping.

**Supplementary Data for Table 1.** For completeness, all numerical entries omitted from Table 1 are reported here in Table 7.

## D Future Directions

In this part, we discuss our plans for future work. **Current limitation:** The present **MoE-Gyro** prototype contains a comparatively large number of parameters; although it runs in real time on a desktop GPU, such model size still hinders low-cost embedded deployment.

Table 7: Full benchmark results corresponding to Table 1.

Model\Metric	Peak Rec. ( $\tau = 450^\circ/s$ )	Allan Variance		
	P_MSE $\downarrow$ ( $^\circ/s$ ) <sup>2</sup>	QN $\downarrow$ ( $^\circ/s$ )	ARW $\downarrow$ ( $^\circ/\sqrt{h}$ )	BI $\downarrow$ ( $^\circ/h$ )
RAW	181456	0.0004	0.32	10.03
Matlab 2023	93371	0.0002956	0.31	+5.4%
EMD	118916	0.0000357	0.045	<u>0.32</u>
SG_filter	139175	0.00006	0.044	1.0
CNN	112750	0.00015	0.205	2.07
LSTM_GRU	89847	0.0000767	0.048	0.69
KNN	136533	0.0000573	0.21	5.27
HEROS_GAN	<u>64302</u>	<u>0.0000287</u>	0.155	4.18
IMUDB	<u>80158</u>	<u>0.0000567</u>	<u>0.039</u>	0.63
<b>MoE-Gyro</b>	<b>59017</b>	<b>0.000008</b>	<b>0.019</b>	<b>0.157</b>

**Planned extensions.** (1) Model compression. We will explore how to shrink the network while preserving—or minimally degrading—its reconstruction and denoising accuracy. (2) Hardware co-design. We plan to fabricate an in-house, low-cost MEMS inertial unit and integrate it end-to-end with **MoE-Gyro**. This co-design will allow us to demonstrate a complete, cost-effective pipeline—from sensor to software—that breaks the range-noise trade-off in practical applications.

## E Broader Impacts

This work aims to improve inertial-sensor signal quality through a self-supervised Mixture-of-Experts framework. Enhanced MEMS gyroscopes can benefit a wide spectrum of applications—from consumer electronics and robotics to autonomous navigation—by enabling higher accuracy without added hardware complexity. While better motion sensing may indirectly influence downstream systems (e.g., drones, vehicles, or defense technologies), we do not foresee any immediate, unique societal risks posed by the algorithm itself beyond those already associated with general improvements in sensor signal processing.