

Support Vector Machine - Confusion Matrix

Test Data Count 134	Predicted (0) Not Purchased	Predicted (1) Purchased
Actual (0) Not Purchased	82 True - Not Purchased	26 False - Not Purchased
Actual (1) Purchased	3 False - Purchased	23 True - Purchased

Accuracy: What is the correct Classification of this model ?

$$\begin{aligned} &= \frac{\text{True(Purchased)} + \text{True(Not Purchased)}}{\text{True(Purchased)} + \text{True(Not Purchased)} + \text{False(Purchased)} + \text{False(Not purchased)}} \\ &= \frac{23 + 82}{23 + 82 + 3 + 26} \end{aligned}$$

Accuracy = 0.78

Recall for Purchased: Out of all actual purchases, how many did we correctly identify ?

$$\begin{aligned} &= \frac{\text{True(Purchased)}}{\text{True(Purchased)} + \text{False(Not Purchased)}} \\ &= \frac{23}{23 + 26} = \frac{23}{49} = 0.469 \end{aligned}$$

Recall for Purchased = 0.47

Recall for Not Purchased:

$$\begin{aligned} &= \frac{\text{True(Not Purchased)}}{\text{True(Not Purchased)} + \text{False(Purchased)}} \\ &= \frac{82}{82 + 3} = \frac{82}{85} = 0.96 \end{aligned}$$

Recall for Not Purchased = 0.96

Precision for Purchased:

Out of all predicted purchases, how many did we correctly identify ?

$$\begin{aligned} &= \frac{True(Purchased)}{True(Purchased)+False(Purchased)} \\ &= \frac{23}{23+3} \end{aligned}$$

Precision for Purchased = 0.88

Precision for Not Purchased:

$$\begin{aligned} &= \frac{True(Not Purchased)}{True(Not Purchased)+False(Not Purchased)} \\ &= \frac{82}{82+26} = 0.759 \end{aligned}$$

Precision for Not Purchased = 0.76

F1 score: Overall performance of Purchased

$$\begin{aligned} &= 2 * \frac{Recall*Precision}{Recall+Precision} \\ &= 2 * \frac{0.47*0.88}{0.47+0.88} = 2 * \frac{0.413}{1.35} = 2 * 0.305 \end{aligned}$$

F1 score for Purchased = 0.61

F1 score: Overall performance of Not Purchased

$$\begin{aligned} &= 2 * \frac{Recall*Precision}{Recall+Precision} \\ &= 2 * \frac{0.96*0.76}{0.96+0.76} = 2 * \frac{0.729}{1.72} = 2 * 0.423 = 0.847 \end{aligned}$$

F1 score for Not Purchased = 0.85

Macro Average: Average performance of Precision.

$$\begin{aligned}\text{Macro Average} &= \frac{\text{Precision(Purchased)} + \text{Precision(Not Purchased)}}{2} \\ &= \frac{0.88 + 0.76}{2} \\ &= \frac{1.64}{2} = 0.82\end{aligned}$$

Macro Average of Precision = 0.82

Macro Average: Average performance of Recall

$$\begin{aligned}\text{Macro Average} &= \frac{\text{Recall(Purchased)} + \text{Recall(Not Purchased)}}{2} \\ &= \frac{0.47 + 0.95}{2} \\ &= \frac{1.43}{2} = 0.715\end{aligned}$$

Macro Average of Recall = 0.72

Macro Average: Average performance of F1-Score

$$\begin{aligned}\text{Macro Average} &= \frac{\text{F1(Purchased)} + \text{F1(Not Purchased)}}{2} \\ &= \frac{0.61 + 0.85}{2} \\ &= \frac{1.4}{2}\end{aligned}$$

Macro Average of F1-Score = 0.73

Weighted Average: What is the sum of the product of each class ?

$$\begin{aligned}\text{Weighted Average of Precision} &= \text{Precision of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\ &\quad \text{Precision Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}} \\ &= 0.88 * \frac{49}{134} + 0.76 * \frac{85}{134}\end{aligned}$$

$$= 0.88 * 0.36 + 0.76 * 0.63$$

$$= 0.316 + 0.478$$

$$= 0.79$$

Weighted Average of Precision = 0.79

Weighted Average: Recall

$$= \text{Recall of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\ \text{Recall Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}}$$

$$= 0.47 * \frac{48}{134} + 0.96 * \frac{85}{134}$$

$$= 0.47 * 0.35 + 0.96 * 0.63$$

$$= 0.164 + 0.604$$

$$= 0.76$$

Weighted Average of Recall = 0.76

Weighted Average: F1 measure

$$= \text{F1 score of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\ \text{F1 score of Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}}$$

$$= 0.61 * \frac{48}{134} + 0.85 * \frac{85}{134}$$

$$= 0.61 * 0.35 + 0.85 * 0.62$$

$$= 0.213 + 0.527$$

$$s = 0.74$$

Weighted Average of F1 score = 0.74

