

# Support Vector Machine - Confusion Matrix

Test Data Count 134	Predicted (0) Not Purchased	Predicted (1) Purchased
Actual (0) Not Purchased	82 True - Not Purchased	26 False - Not Purchased
Actual (1) Purchased	3 False - Purchased	23 True - Purchased

**Accuracy:** What is the correct Classification of this model ?

$$\begin{aligned}
 &= \frac{\text{True(Purchased)} + \text{True(Not Purchased)}}{\text{True(Purchased)} + \text{True(Not Purchased)} + \text{False(Purchased)} + \text{False(Not purchased)}} \\
 &= \frac{23+82}{23+82+3+26}
 \end{aligned}$$

Accuracy = 0.78

**Recall for Purchased:** Out of all actual purchases, how many did we correctly identify ?

$$\begin{aligned}
 &= \frac{\text{True(Purchased)}}{\text{True(Purchased)} + \text{False(Not Purchased)}} \\
 &= \frac{23}{23+26} = \frac{23}{49} = 0.469
 \end{aligned}$$

Recall for Purchased = 0.47

**Recall for Not Purchased:**

$$\begin{aligned}
 &= \frac{\text{True(Not Purchased)}}{\text{True(Not Purchased)} + \text{False(Purchased)}} \\
 &= \frac{82}{82+3} = \frac{82}{85} = 0.96
 \end{aligned}$$

Recall for Not Purchased = 0.96

### Precision for Purchased:

Out of all predicted purchases, how many did we correctly identify ?

$$= \frac{\text{True(Purchased)}}{\text{True(Purchased)} + \text{False(Purchased)}}$$
$$= \frac{23}{23+3}$$

Precision for Purchased = 0.88

### Precision for Not Purchased:

$$= \frac{\text{True(Not Purchased)}}{\text{True(Not Purchased)} + \text{False(Not Purchased)}}$$
$$= \frac{82}{82+26} = 0.759$$

Precision for Not Purchased = 0.76

**F1 score:** Overall performance of Purchased

$$= 2 * \frac{\text{Recall} * \text{Precision}}{\text{Recall} + \text{Precision}}$$
$$= 2 * \frac{0.47 * 0.88}{0.47 + 0.88} = 2 * \frac{0.413}{1.35} = 2 * 0.305$$

F1 score for Purchased = 0.61

**F1 score:** Overall performance of Not Purchased

$$= 2 * \frac{\text{Recall} * \text{Precision}}{\text{Recall} + \text{Precision}}$$
$$= 2 * \frac{0.96 * 0.76}{0.96 + 0.76} = 2 * \frac{0.729}{1.72} = 2 * 0.423 = 0.847$$

F1 score for Not Purchased = 0.85

**Macro Average:** Average performance of Precision.

$$\begin{aligned}\text{Macro Average} &= \frac{\text{Precision(Purchased)} + \text{Precision(Not Purchased)}}{2} \\ &= \frac{0.88 + 0.76}{2} \\ &= \frac{1.64}{2} = 0.82\end{aligned}$$

Macro Average of Precision = 0.82

**Macro Average:** Average performance of Recall

$$\begin{aligned}\text{Macro Average} &= \frac{\text{Recall(Purchased)} + \text{Recall(Not Purchased)}}{2} \\ &= \frac{0.47 + 0.95}{2} \\ &= \frac{1.43}{2} = 0.715\end{aligned}$$

Macro Average of Recall = 0.72

**Macro Average:** Average performance of F1-Score

$$\begin{aligned}\text{Macro Average} &= \frac{\text{F1(Purchased)} + \text{F1(Not Purchased)}}{2} \\ &= \frac{0.61 + 0.85}{2} \\ &= \frac{1.4}{2}\end{aligned}$$

Macro Average of F1-Score = 0.73

**Weighted Average:** What is the sum of the product of each class ?

$$\begin{aligned}\text{Weighted Average of Precision} &= \text{Precision of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\ &\quad \text{Precision Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}} \\ &= 0.88 * \frac{49}{134} + 0.76 * \frac{85}{134}\end{aligned}$$

$$\begin{aligned}
&= 0.88 * 0.36 + 0.76 * 0.63 \\
&= 0.316 + 0.478 \\
&= 0.79
\end{aligned}$$

Weighted Average of Precision = 0.79

### Weighted Average: Recall

$$\begin{aligned}
&= \text{Recall of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\
&\quad \text{Recall Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}} \\
&= 0.47 * \frac{48}{134} + 0.96 * \frac{85}{134} \\
&= 0.47 * 0.35 + 0.96 * 0.63 \\
&= 0.164 + 0.604 \\
&= 0.76
\end{aligned}$$

Weighted Average of Recall = 0.76

### Weighted Average: F1 measure

$$\begin{aligned}
&= \text{F1 score of Purchased} * \frac{\text{Total count of Purchased in Test Set}}{\text{Total count of Test set}} + \\
&\quad \text{F1 score of Not Purchased} * \frac{\text{Total count of Not Purchased in Test Set}}{\text{Total count of Test set}} \\
&= 0.61 * \frac{48}{134} + 0.85 * \frac{85}{134} \\
&= 0.61 * 0.35 + 0.85 * 0.62 \\
&= 0.213 + 0.527 \\
&= 0.74
\end{aligned}$$

Weighted Average of F1 score = 0.74

