

## 2.6 Solving Inequalities

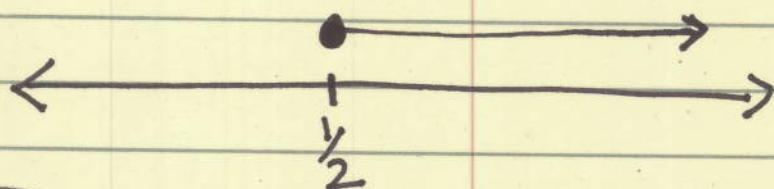
(#20)

$$3x + 11 \geq 2 + x$$

$-x \quad -1 \quad -1 \quad -x$

$$2x \geq 1$$

$$\boxed{x \geq \frac{1}{2}} \quad \text{Solution } \left[\frac{1}{2}, \infty\right)$$



(#26)

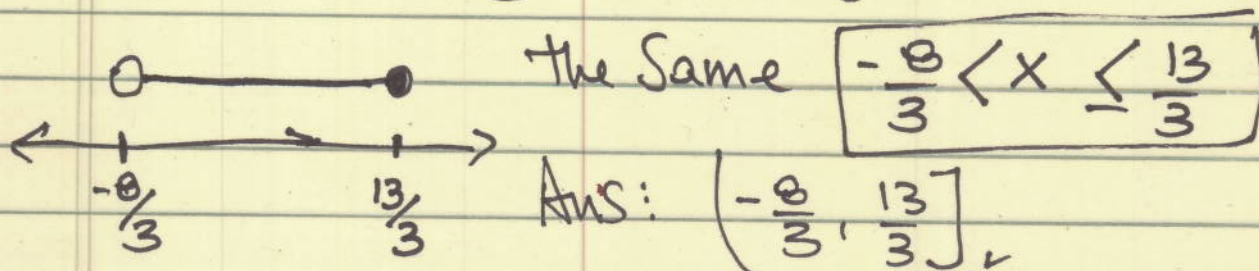
$$-8 \leq -3x + 5 < 13$$

$$-8 \leq -3x + 5 \quad \text{and} \quad -3x + 5 < 13$$

$$\begin{array}{ccc} -8 & \leq & -3x + 5 < 13 \\ -5 & & -5 \end{array}$$

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$$\begin{array}{ccc} -13 & \leq & -3x < 8 \\ \frac{-13}{-3} & \downarrow & \frac{-8}{-3} \\ \frac{13}{3} & \geq & x > \frac{8}{3} \end{array}$$



The Same

$$\boxed{-\frac{8}{3} < x \leq \frac{13}{3}}$$

$$\text{Ans: } \left(-\frac{8}{3}, \frac{13}{3}\right]$$

$$|x| = |-x| \checkmark$$

#46

$$3|4 - 5x| \leq 9$$

$$3|5x - 4| \leq 9$$

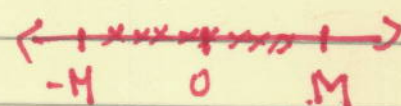
$$|5x - 4| \leq 3$$

$$\begin{array}{ccc} -3 & \leq & 5x - 4 & \leq & 3 \\ +4 & & +4 & & +4 \end{array}$$

$$1 \leq 5x \leq 7$$

$$\frac{1}{5} \leq x \leq \frac{7}{5}$$

$$\left[\frac{1}{5}, \frac{7}{5}\right] \checkmark$$

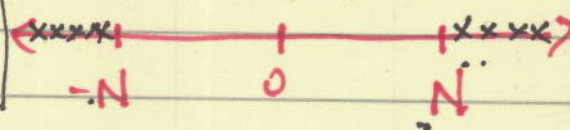


Key  $|x| < M$

$$-M < x < M$$

Key  $|x| > N$

$$x < -N \text{ or } x > N$$



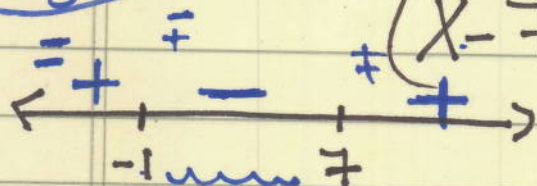
66

$$x^2 - 6x + 9 < 16$$

$$x^2 - 6x - 7 < 0$$

$$(x - 7)(x + 1) < 0$$

Sign



Ans:  $(-1, 7) \checkmark$