

## 2.3 complex numbers.

Imaginary. form  $a + bi$

Where  $i = \sqrt{-1}$  or  $i^2 = -1$

$a + bi$

↑ Real part

$$\sqrt{-4} = \sqrt{-1} \sqrt{4} = i2 = \boxed{2i}$$

Simplify:  $(3+i) + (2-3i)$ .

$$3+i + 2-3i$$

$$\boxed{5-2i}$$

$$\sqrt{-4} + (-4 - \sqrt{-4}).$$

$$\cancel{\sqrt{-4}} + 4 - \cancel{\sqrt{-4}} = \boxed{-4}$$

$$(3+2i) + (4-i) - (7+i) = \boxed{0}$$

$$\sqrt{-4} \sqrt{-16} = 2i 4i = 8i^2 = \boxed{-8}$$

$$(2-i)(4+3i) = 8+6i - 4i - 3i^2 = \boxed{11+2i}$$

$$(3+2i)^2 = 9+12i+(2i)^2 = \boxed{5+12i}$$

$\sqrt{a} \sqrt{b} = \sqrt{ab}$  true only if  $a, b > 0$

Simplify  $\frac{2+3i}{4-2i}$  form  $a+bi$

Hint:  $(a+bi)(a-bi) = a^2 + b^2$   
 $\uparrow$   
 conjugate.

Rationalize.  $\frac{2+3i}{4-2i} \cdot \frac{4+2i}{4+2i} = \frac{\quad}{4^2 + 2^2}$

$$\frac{8+4i+12i-6}{20} = \frac{2+16i}{20}$$

$$= \boxed{\frac{1}{10} + \frac{4}{5}i}$$

Write  $-6i^3 + i^2$  in the form  $a+bi$

$$i^2 [-6i + 1]$$

$$-(-6i + 1) = \boxed{-1 + 6i}$$

$$i^{137} = i^{136} i = (i^2)^{68} i$$

$$\frac{1}{(2i)^3} = \frac{1}{-8i} \cdot \frac{i}{i} = \frac{i}{8}$$

$$= (-1)^{68} i = \boxed{i} \checkmark$$

Quiz upto 2.2  
2.3

Quadratic  
Inequalities