

ECE428 HW3

Q1.

- a) `elif message.contents == "Election":`
 `# fill in the rest`
 `self.leader = self.pid # Assign the new leader`
 `for pid in self.group:`
 `if pid < self.pid:`
 `#Send Coord msg to all lower-number processes`
 `unicast (self.pid, "Coordinator")`
- b) P4 will send election msg to all the process with second highest PID P7, and P7 sends Coordinator msg to all of the lower-numbered processes(P1-P6). Hence, totally $1+6=7$ msg
- c) P4 send election to P7 first within T, then P7 send to P1-P6 Coordinator msg simultaneously within T. Hence, totally $T+T=2T$
- d) P4 will still send election msg to P7 since the failure of P7 has not been detected. Within time out P4 does not get response from P7 so it sends election msg to P6. Then P6 send Coordinator msg to P1-P5. Hence totally $2+5 = 7$
- e) P4 send election msg to P7 and does not get response within $T+T = 2T$ (Time out should be $2T$ for a round of msg transmission). Then P4 send election msg to P6 within T. And P6 send Coordinator msg to P1-P5 simultaneously within T. Hence, totally $2T+T+T=4T$
- f) Best case: exactly P7 detect P8's failure and send Coordinator msg to the lower with T.
Worst case: exactly P1 detect P8's failure while P7-P2 failed while P1 initiate the election. Then $2T * 6 = 12T$ is needed.

Q2.

- a) i) No. A counterexample could be that there exist two processes carry the same interger zinput (i.e. $x_k = x_{k+1}$) and in this scenario it will mistakenly take x_k as the max value since it think that x_k is pass through the whole loop while actually it is just passed to the next process.
- ii) The judgement that x_k is pass through a whole loop can not just be the value of it. Instead, there should be something record whether process p_i has been checked. i.e Initialize a sent `p_check` as a blank set, when p_i pass msg (PROPOSAL, X_K , p_i), `p_check.append(p_i)`. Then change the judgement `else #b==X_K` into `elif p_i in p_check`. By doing this the safety could be guaranteed.

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b) PROPOSAL = 0
   DECIDED = 1
   self_PID = # unique for each process pi (i.e PID for pi is i)
   X_K = # my input
   Y_K = NONE

```

```

def start_consensus():
    if X_K == 1:
        send(1, PROPOSAL, self_PID)
    else: # X_K == 0
        send(-1, PROPOSAL, self_PID)

def receive_message(a, b, PID):
    if Y_K is not None:
        continue # Ignore msg after decided state
    if b == DECIDED:
        if a > 0:
            Y_K = 1
        elif a < 0:
            Y_K = 0
        else:
            Y_K = 2
        send(a, b, PID)
    elif b == PROPOSAL:
        if X_K = 1:
            send(a+1, PROPOSAL, PID)
        else:
            send(a-1, PROPOSAL, PID)

```

Q3.

- a) B-multicast. We have assumed that unicast channels are reliable and considered Time out. We do not care on the failure in the multicast of Query msg, so pair-to-pair B-multicast should be used.
- b) $2T$
- c) R-multicast. In the multicast of Decision msg, the phenomenon that the send may fail after it send the Decision msg could exist, which ask the reliability of multicasting Decision msg. And we do not care on the future input so pair-to-pair B-multicast is not needed.
- d) Query msg from P_i to P_j within T

Reply msg with X_i from Each P_j to P_i within T

Decision y_i from p_i to each p_j within T

Totally, $3T$.

- e) The process P_i may fail after multicasting msg to the group. And no failure detection is used to check the failure of P_i . Hence the future part of the algorithm could be meaningless and the safety could not be guaranteed for not reaching a consensus in the group.

Q4.

- a) i. A1, A2, A3

ii. A2, A3

iii. P_1 will send Accept msg after the Promise msg is taken after getting voted by the majority of acceptors (after receiving promise msg from Acceptor A1). Hence $3T+2T = 5T$. P_2 will send Accept msg after the Promise msg is taken by Acceptor A3. Hence $7T+2T = 9T$.

iv. Yes, by iii we know P_1 could send Accept msg to A1 and A2 at Time 5 and it take one time unit. So at Time 6 the P_1 could be accepted by A1 and A2 while at Time 7 the Prepare msg just arrive at A3 ($6 < 7$). Hence, P_1 could be accepted by a majority of acceptors. ($2/3 > 1/2$)

- b) i. A1, A2

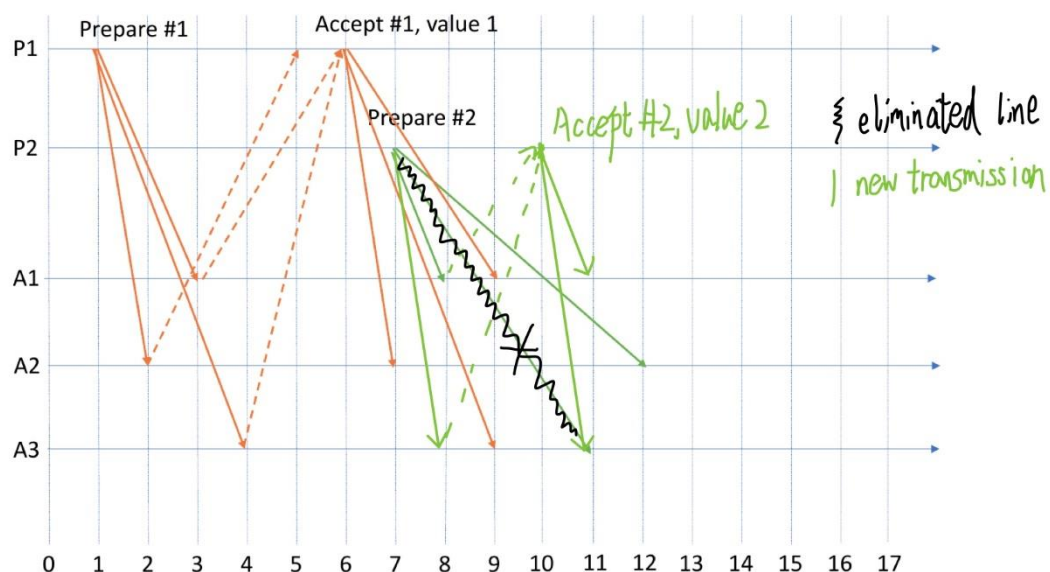
ii. A1, A2, A3

iii. P_2 will send Accept msg after getting the Promise msg by the majority of acceptors (after A3). Hence $11T+2T=13T$

iv. All of the acceptors: A1, A2, A3.

v. value 1. Since P_2 has not start sending Accept msg.

vi. Change the arrived Time of Prepare msg to A3 from $11T$ to $8T$ hence P_1 has not been accepted by all of the acceptors (at $9T$, $8 < 9$).



Q5.

a) P5

b) $75+5=50+30$

At time 80ms P2 and P3 votes for themselves

P3 votes for P3

P2 votes for P2

P4 votes for P3 since P3's election msg arrived faster than from P2

P5 votes for P2 since P2's election msg arrived faster than from P3

c) All votes for P5

Because at $50+15 = 65$, P5 begins send election msg to all the other processes. P5 votes for P5.

P4 received P5 election at $65+15 = 80$ ($80 < 20+75$) so it votes for P5

P3 received P5 election at $65+20 = 85$ ($80 < 5+100$) so it votes for P5

P2 received P5 election at $65+5 = 70$ ($80 < 30+150$) so it votes for P5

d) P2, P3, P5, P1, P4