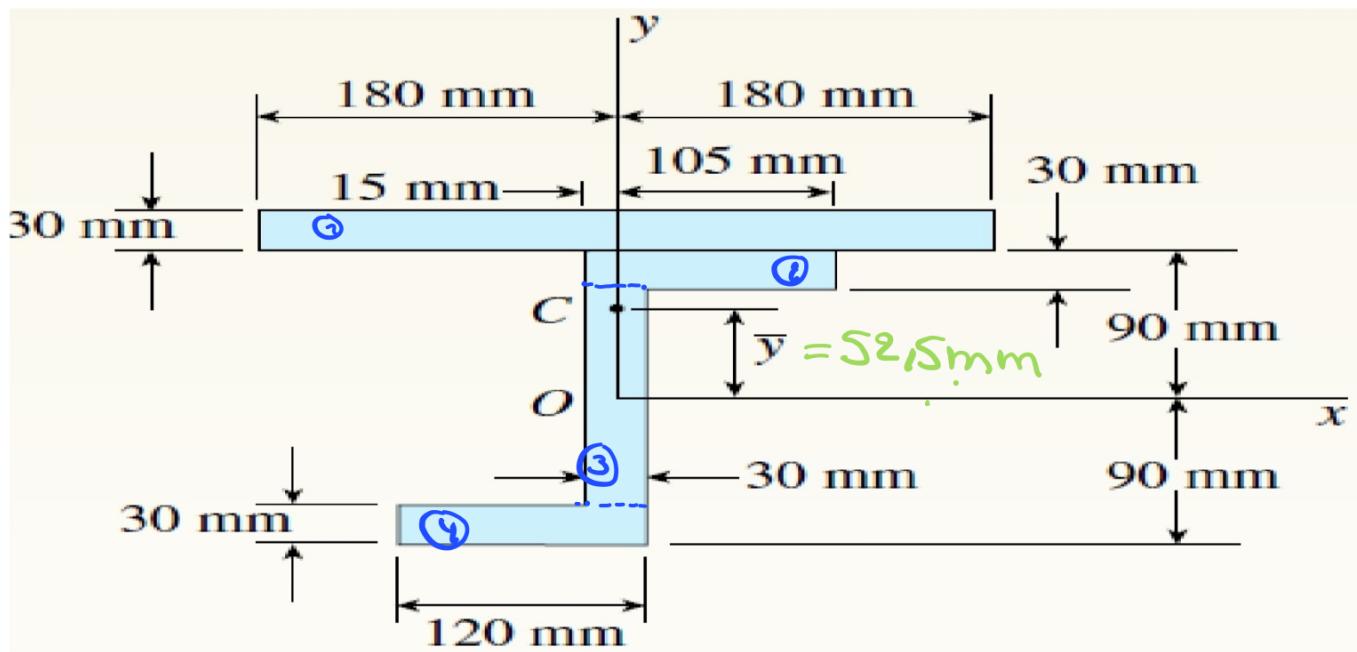


**No reply Homework 2:**

Calculate the moment of inertia  $I_{xc}$  with respect to an axis through the centroid C and parallel to the x axis for the composite area (you must find  $I_{xc} = 106 \cdot 10^6 \text{ mm}^4$ ).

Calculate the product of inertia  $I_{xy}$  for the composite area (you find  $I_{xy} = 24,3 \cdot 10^6 \text{ mm}^4$ ).



$$I_{xc} = ?$$

$$\begin{aligned} \text{we have } I_{xc} &= I_x - A d^2 \\ &= I_x - A \bar{y}^2 \end{aligned}$$

$$I_x = \sum_{i=1}^4 I_{xi}$$

$$*\bar{y}=?$$

i	$A_i$	$\bar{y}_i$	$A_i \cdot \bar{y}_i$
1	10800	105	1134000
2	3600	75	270000
3	3600	0	0
4	3600	-75	-270000
$\sum_{i=1}^4$	21600	$\equiv$	1134000

$$\bar{y} = \frac{\sum A_i \bar{y}_i}{\sum A_i} = 52,5 \text{ mm}$$

$$* I_x = \sum_{i=1}^4 I_{x,i} = ?$$

$$I_{x_1} = I_{xc_1} + A_1 d^2$$

$I_{xc_1} (\text{rectangle}) = \frac{b R^3}{12}$

$$I_{x_1} = \frac{bR^3}{12} + A_1 \cdot \bar{y}_1^2$$

$$= \frac{360 \times (30)^3}{12} + 10800 \cdot (105)^2$$

$$I_{x_1} = 119880000 \text{ mm}^4$$

$$I_{x_2} = I_{x_{c_2}} + A_2 \cdot d^2$$

$$= \frac{bR^3}{12} + A_2 \cdot \bar{y}_2^2$$

$$= \frac{120 \times (30)^3}{12} + 3600 \cdot (75)^2$$

$$I_{x_2} = 20520000 \text{ mm}^4$$

$$I_{x_3} = I_{x_{c_3}} + A_3 \cdot d^2$$

$$= I_{x_{c_3}} + \cancel{A_3 \bar{y}_3^2}$$

$$= I_{x_{c_3}} = \frac{bR^3}{12} = \frac{30 \cdot (120)^3}{12}$$

$$I_{x_3} = 4320000 \text{ mm}^4$$

$$I_{x_4} = I_{x_{c_4}} + A_4 d^2$$

$$= \frac{b f^3}{12} + A_4 \cdot \bar{y}_4^2$$

$$= \frac{120 \times (30)^3}{12} + 3500 (75)^2$$

$$I_{x_4} = 20520000 \text{ mm}^4$$

$$\bar{I}_x = \sum_{i=1}^4 I_{x_i} = 165240000 \text{ mm}^4$$

$$I_{x_c} = I_x - A d^2$$

$$A = \sum_{i=1}^4 A_i / d = \bar{y}$$

$$I_{x_c} = 165240000 - 24600 \times 52,5^2$$

$$= 105705000 \approx 106 \times 10^6 \text{ mm}^4$$