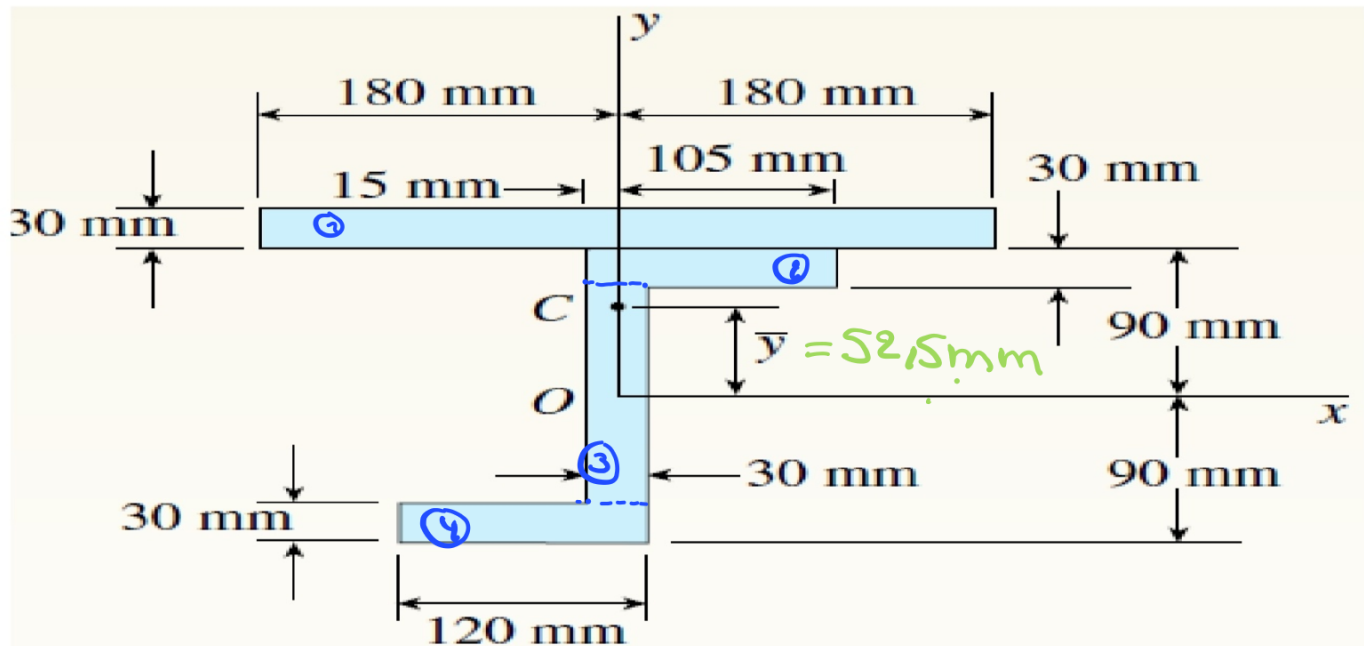


No reply Homework 2:

Calculate the moment of inertia I_{xc} with respect to an axis through the centroid C and parallel to the x axis for the composite area (you must find $I_{xc} = 106.10^6 \text{ mm}^4$).

Calculate the product of inertia I_{xy} for the composite area (you find $I_{xy} = 24,3.10^6 \text{ mm}^4$).



$$I_{xc} = ?$$

$$\begin{aligned} \text{we have } I_{xc} &= I_x - A d^2 \\ &= I_x - A \bar{y}^2 \end{aligned}$$

$$I_x = \sum_{i=1}^4 I_{x_i}$$

$$* \bar{y} = ?$$

i	A_i	\bar{y}_i	$A_i \cdot \bar{y}_i$
1	10 800	105	1134000
2	3600	75	270000
3	3600	0	0
4	3600	-75	-270000
$\sum_{i=1}^4$	21 600	//	1134 000

$$\bar{y} = \frac{\sum A_i \bar{y}_i}{\sum A_i} = 52,5 \text{ mm}$$

$$* I_x = \sum_{i=1}^4 I_{x_i} = ?$$

$$I_{x_1} = I_{x_{c1}} + A_1 d^2$$

$$I_{x_c} (\text{rectangle}) = \frac{b R^3}{12}$$

$$I_{x_1} = \frac{b R^3}{12} + A_1 \cdot \bar{y}_1^2$$

$$= \frac{360 \times (30)^3}{12} + 10800 \cdot (105)^2$$

$$I_{x_1} = 119880000 \text{ mm}^4$$

$$I_{x_2} = I_{x_{c_2}} + A_2 d^2$$

$$= \frac{b R^3}{12} + A_2 \cdot \bar{y}_2^2$$

$$= \frac{120 \times (30)^3}{12} + 3600 + (75)^2$$

$$I_{x_2} = 20520000 \text{ mm}^4$$

$$I_{x_3} = I_{x_{c_3}} + A_3 \cdot d^2$$

$$= I_{x_{c_3}} + A_3 \bar{y}_3^2$$

$$= I_{x_{c_3}} = \frac{b R^3}{12} = \frac{30 \cdot 120^3}{12}$$

$$I_{x3} = 4320000 \text{ mm}^4$$

$$I_{x4} = I_{xc4} + A_4 d^2$$

$$= \frac{b R^3}{12} + A_4 \cdot \bar{y}_4^2$$

$$= \frac{120 \times (30)^3}{12} + 3500 (75)^2$$

$$I_{x4} = 20520000 \text{ mm}^4$$

$$I_x = \sum_{i=1}^4 I_{xi} = 165240000 \text{ mm}^4$$

$$I_{xc} = I_x - A d^2$$

$$A = \sum_{i=1}^4 A_i \quad / \quad d = \bar{y}$$

$$I_{xc} = 165240000 - 21600 \times 52,5^2$$

$$= 105705000 \simeq 106 \times 10^6 \text{ mm}^4$$