MSML610: Advanced Machine Learning

Knowledge Representation

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References:

- Mostly papers and Internet
- AIMA 7: Logical agents
- AIMA 8, First-order logic
- AIMA 9: Inference in first-order logic
- AIMA 10, Knowledge representation

Knowledge Representation

- Knowledge Representation
 - Basics of Knowledge Representation
 - Examples of Logic
 - Logical Agents
 - Ontologies
 - Reasoning in Ontologies
- Propositional logic
- First-order Logic
- Non-classical Logics
- Description Logics

Basics of Knowledge Representation

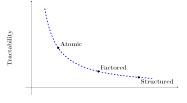
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What is Knowledge Representation?

- Knowledge Representation (KR) is the study of how to formally encode information so that machines can reason with it
 - E.g., rules, logic, ontologies, semantic networks
 - It is at the heart of symbolic AI and complements learning-based approaches
- Defines:
 - structure (how knowledge is organized)
 - semantics (what it means)
- Serves as a bridge between perception (data) and reasoning (logic)
 - Essential for explainability and transparency in intelligent systems
- Enables machines to:
 - Draw conclusions
 - Perform planning
 - Answer queries
 - . . .

Expressiveness vs. Tractability

- Tradeoff in Al / ML
 - Expressiveness: richness of concepts that can be captured
 - Tractability: whether reasoning can be performed efficiently
 - More expressive languages lead to harder computation



Expressiveness

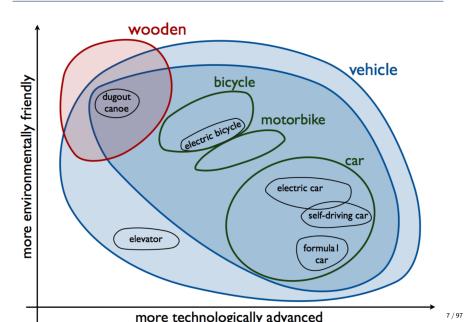
- Choosing the right knowledge representation formalism depends on the application needs
 - Atomic
 - Treats each state as a single, indivisible entity
 - E.g., depth-first search algorithms (e.g., E3 in Chess)
 - Simple and fast but limited in capturing complex relationships
 - Factored
 - E.g., propositional logic
 - E.g., $P_{1,1}$: "Pit in square (1,1)", $B_{1,2} \Leftrightarrow (P_{1,1} \vee P_{2,2} \vee P_{1,3})$
 - Captures relationships between variables but can't express complex structures
 - Structured
 - E.g., first-order logic
 - $\forall x \forall y \ Father(x, y) \Rightarrow Parent(x, y) = "A \ father of a person is their parent"$
 - More expressive but undecidable in general

Symbolic vs. Sub-symbolic Representation

- Symbolic knowledge representation uses discrete, human-readable symbols
 - E.g., logic, knowledge graphs
 - Interpretable and suitable for rule-based reasoning
 - Struggle with ambiguity
- Sub-symbolic knowledge representation uses learned, distributed representations
 - E.g., vector embeddings
 - E.g., deep learning excels at perception and pattern recognition
 - Lack transparency
- Neuro-symbolic approaches blends the two approaches
 - Reason over learned concepts using structured logic



Neuro-symbolic Approach: Conceptual Spaces



Procedural vs Declarative Approaches

Procedural approach

- Focuses on how a task is done
- Encodes desired behavior directly into the program
- E.g., a robot programmed with specific steps to navigate a maze

Declarative approach

- Specifies what the goal is, not how to achieve it
- Describes relationships between actions and goals
- Leaves solution search to the system
- E.g., describing the goal "reach the exit" and letting the system find the path

Comparison

- Procedural: more control, less flexibility
- Declarative: more abstraction, easier to modify or extend

Integration of approaches

- Many successful AI systems use a hybrid
- Declarative knowledge can be compiled into procedural code
- E.g., a planner generates procedures (plans) from declarative goals

Examples of Logic

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Propositional Logic

- Uses atomic statements (propositions) and logical connectives
 - Syntax
 - Atomic formulas: P, Q
 - Connectives: NOT (\neg) , AND (\land) , OR (\lor) , IMPLIES (\Longrightarrow)
 - Semantics
 - Based on truth tables
 - Each proposition has a binary truth value: true or false
 - Inference mechanisms
 - Modus ponens: from P and $P \implies Q$, infer Q
 - Resolution: derive contradictions to infer conclusions
- Applications: best used in closed and well-defined environments
 - Digital circuit design
 - Rule-based systems
 - Simplified AI models
- Limitations
 - · Cannot represent objects, relations, or quantifiers
 - Not suitable for open or dynamic domains

First-Order Logic (FOL)

Extension of propositional logic

- Introduces predicates, variables, and quantifiers
 - Variables x
 - Predicate Human(x)
 - Universal quantifier "for all" ∀
 - Existential quantifier "there exists" ∃
- E.g., $\forall x (Human(x) \implies Mortal(x)) = "All humans are mortal"$
- Represents more complex and structured knowledge than propositional logic
- Can model properties, relationships, and quantification over objects

Inference mechanisms

- Unification: matches predicates with variables
- Resolution: deduces new facts from known statements
- Model checking: verifies truth of statements under specific interpretations

Computational properties

- Inference is semi-decidable: valid conclusions may require infinite time
- More powerful but computationally more complex than propositional logic

Applications

- Knowledge representation
- Automated theorem proving
- Semantic web and ontologies

Rule-Based Systems (1/2)

- A rule-based system uses "if-then" rules to derive conclusions or make decisions
 - It mimics human decision-making by applying logical rules to a set of facts

Key Components

- Knowledge base: stores facts and rules
- Inference engine: applies rules to known facts to infer new facts or take actions
- · Working memory: holds current facts being considered

How It Works

- Match: find rules whose conditions match current facts
- Conflict resolution: decide which rule to apply if multiple rules match
- Act: apply the chosen rule to modify facts or trigger actions
- Repeat: continue until no more rules can be applied
- E.g.,
 - Rule: If a patient has a fever and a rash, then suggest measles
 - Fact: Patient has a fever and a rash
 - Conclusion: Suggest measles

Rule-Based Systems (2/2)

Pros

- Easy to modify and update rules
- Transparent and explainable reasoning
- Good when expert knowledge can be clearly articulated

Cons

- Hard to scale to very large or complex domains
- Cannot handle uncertainty without extensions (e.g., probabilistic reasoning)
- Rule conflicts and maintenance can become challenging

Applications

- Expert systems (e.g., medical diagnosis, technical troubleshooting)
- Business rule engines
- Game AI
- Legal reasoning tools

Reasoning and Inference in Logic

- Logical inference is the process of deriving new facts from known ones using formal rules
 - Used to make decisions and answer questions based on a Knowledge Base
- Knowledge base (KB):
 - A structured set of facts and rules used for logical reasoning
- Inference engine:
 - Mechanism that applies logical rules to a KB to derive conclusions or answer queries
 - Forward chaining:
 - Starts with known facts and applies inference rules to extract more data
 - E.g., given $A \rightarrow B$ and A, infer B
 - Backward chaining:
 - Begins with a goal and works backward to find supporting facts
 - E.g., to prove B, check if $A \rightarrow B$ and then prove A
 - Resolution:
 - A complete inference rule for propositional and first-order logic
 - Useful in automated theorem proving
 - Entailment ($KB \models \alpha$):
 - Sentence α is entailed by KB if it is true in all models where KB is true

Grounding and Symbol Anchoring

Grounding

- Connecting abstract symbols to real-world entities or observations
- E.g., the symbol Apple must be linked to the fruit "apple" in the world
- Essential for making representations meaningful beyond pure syntax
 - Enables agents to act meaningfully in the real world
 - · Avoids purely symbolic manipulation without real-world relevance

Symbol Anchoring

- Specific instance of grounding where sensory data anchors symbols in an agent's memory
- E.g., a robot sees a round red object and anchors it to the symbol Apple

Challenges

- Sensory data is noisy and incomplete
- Mapping from real-world inputs to abstract concepts can be complex and context-dependent

Applications

- Robotics (object recognition, manipulation)
- Natural language understanding
- Autonomous agents and cognitive systems

Logical Agents

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Reflex Agents

- Reflex agents act based on the current percept, ignoring percept history
 - Operate using a condition-action rule: "if condition, then action"
 - Rely on predefined rules
 - Have no internal state or memory
 - E.g., a thermostat turns on the heater if temperature < threshold
- Pros
 - Fast and efficient in well-defined environments
- Cons
 - Struggle with complex or partially observable environments
 - · Cannot plan ahead or learn from experience
- Application
 - Simple or fully observable environments where quick reactions are sufficient

Knowledge-based agents

- Intelligence is achieved by reasoning on an internal representation of knowledge
- Knowledge-based agents:
 - Form representations of a complex world
 - Use inference to derive new representations about the world
 - Use new representations to deduce actions
 - Accept tasks as goal descriptions
 - Achieve competence by learning new knowledge
 - Adapt to environmental changes by updating knowledge
 - Utilize a knowledge base to store information
 - Explain actions based on their knowledge
 - E.g., a medical diagnosis system using patient data to infer diseases and suggest treatments
 - E.g., a chess-playing program using a database of moves to plan strategy
 - Require mechanisms to update their knowledge base with new information
 - · Handle incomplete or uncertain information through probabilistic reasoning

Logic / Knowledge Base (1/2)

- Knowledge base (KB) is a set of:
 - \bullet Sentences α expressing assertions (observed, assumed or derived) about the world
 - E.g., "it rains", "the ground is dry", "the ground is wet"
 - Rules
 - E.g, "If it rains, the ground gets wet"
- Knowledge representation language is a formal way of creating sentences about the world
- Syntax specifies all the sentences α that are well-formed in a logic / knowledge base
 - E.g., in arithmetic the sentence:
 - "x + y = 4" is well-formed
 - "x4y+=" is not well-formed
- Semantics is the meaning of sentences (i.e., their truth) with respect to each possible world
 - E.g., the sentence x + y = 4
 - Is true in the world (model) in which x = 2, y = 2
 - Is false in the world x = 1, y = 1

Logic / Knowledge Base (2/2)

- Axiom is sentence taken as given without being derived from other sentences
- Inference is a process of deriving new sentences from old ones
 - It should be done in a "logical" way, i.e., the answer should "follow" from what is in the knowledge base
- Truth values of a sentence
 - In most logics every sentence is either true or false
 - Fuzzy logic allows sentences to have different degrees of truth
 - Probabilistic logic allows sentences to have different probability of being true

Model and possible worlds

- We want to represent worlds where there is rain and wet ground
 - In each possible world/model, values are assigned to all relevant variables
 - "Possible worlds" can be thought of as real environments
 E.g., a world where Rain is true and WetGround is false
 - Model m is a mathematical abstraction of "possible world"
 - E.g., m is (Rain = F, WetGround = T)
 - Each possible world is a complete assignment of truth values to all relevant propositions
 - World 1: (Rain = T, WetGround = T)
 - World 2: (Rain = T, WetGround = F)
 - World 3: (Rain = F, WetGround = T)
 - World 4: (Rain = F, WetGround = F)
- E.g., we represent worlds with "men and women sitting at a table"
 - The model represents all possible worlds as (x men, y women)
 - The sentence x + y = 4 is true in certain worlds and false in others
 - In worlds with x = 2 men and y = 2 women sitting at the table, x + y = 4 is true

Satisfaction of a sentence in a model

- Any model m fixes all the variables $x_1, ..., x_n$ used in sentences
 - E.g., (Rain = T, WetGround = T)
- If a sentence α is true in model m, we say "the model m satisfies the sentence α "
 - E.g., the model (Rain = T, WetGround = F) satisfies $\alpha : Rain = T$
 - Note: this seems backwards, since in our common way of reasoning, the model is fixed and sentences are evaluated as true or false
- $M(\alpha)$ is the set of all the models in which α is true
 - E.g., $M(Rain = T) = \{(Rain, WetGround), (Rain, \neg WetGround)\}$

Logical entailment

- Logical entailment between sentences is the relation representing the fact that a sentence follows logically from another sentence in a KB, e.g.,
- " α entails β " (written $\alpha \models \beta$) iff (by def) in every model in which α is true, β is also true, e.g.,
 - α : "Rain \implies WetGround" entails β : "(Rain = T, WetGround = F)"
 - Equivalent to $M(\alpha) \subseteq M(\beta)$
- E.g., in the table world
 - α : "x = 0", β : " $x \cdot y = 0$ "
 - α entails β since in any model in which x=0 is true, also $x\cdot y=0$ is true, regardless of the value of y
- Intuition:
 - Entailment is not related to a proof, it just "preserves truth" across all models
 - "If you believe your KB, you must believe the entailed sentences"

Logical Entailment vs Implication

- Entailment and implication are related but distinct
 - Logical entailment is about truth following from known facts
 - Implication is about a relationship between two statements
- Logical entailment ($KB \models \alpha$):
 - ullet Means lpha is always true in any world where KB is true
 - E.g.,
 - KB: "It is raining", "If it rains, the ground is wet"
 - Entailed: "The ground is wet"
- Implication $(A \implies B)$:
 - A statement in logic that says: "If A is true, then B is true"
 - · Doesn't guarantee A or B is true by itself
 - Implication is true unless A is true and B is false
 - E.g.,
 - A: "It is raining", B: "The ground is wet"
 - ullet $A \Longrightarrow B$ is the statement "If it is raining, then the ground is wet"
 - This statement can be true even if it's not raining

Model Checking Procedure

 M(KB) represents all the models / possible worlds that are true given our KB

• Problem:

• We want to verify whether "a sentence α is entailed by KB" (KB $\models \alpha$)

Solution:

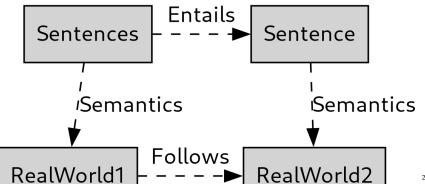
- According to the definition, we need to verify that α is true in all the models in which KB is true
 - I.e., $M(KB) \subseteq M(\alpha)$
- Model checking procedure (brute force)
 - 1. Enumerate all the models / possible worlds
 - 2. Find which models are possible given the KB, i.e., M(KB)
 - 3. Check whether the sentence α is true in all the models that are compatible with the $K\!B$

Sound and Complete Inference Algorithm

- The ideal inference algorithm is both sound and complete
- Sound inference algorithm
 - Derives only sentences entailed from KB
 - "Whatever the inference algorithm finds, it's correct", i.e., no false positives
 - · E.g., model checking is sound
 - · It works only when the space of models is finite
 - When it works, it is truth preserving
- Complete inference algorithm
 - Can derive any sentence entailed from KB
 - "The inference algorithm doesn't miss anything," i.e., no false negatives

Isomorphism between Representation and World

- A sound and complete inference algorithm should yield conclusions guaranteed to be true in any world where the premises are true
- In other words, even if the inference operates on "syntax" (the internal representation):
 - "Sentences in the representation" correspond to "aspects of the real world"
 - "Entailment between sentences in the representation" corresponds to "implication between aspects of the real world"



Grounding

- Grounding is the operation of linking abstract symbols (e.g., words, logical variables, ..) to reality (e.g., objects, entities, or situations in the real world)
 - It is the bridge between representation in a KB and the world
- A philosophical question: how can we know that a KB accurately reflects the real world?
 - We can't be sure
 - Do we live in a simulation? What is reality?
- We assume that is correct
 - Agent's sensors create a sentence in the KB when something happens in the real world

```
IF smell = burning THEN food_is_burning
IF object = {red, round, small} THEN object_is_tomato
```

- We assume that "learning" (generalizing particular cases to general cases) is possible and typically correct
 - IF food_is_burning THEN turn_off_stove
 - Learning is still fallible
 - · E.g., maybe somebody is cooking on a grill

Ontologies

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Ontologies (in computer science)

An ontology:

- Is a formal, explicit representation of a domain
- Describes the types of things that exist and how they relate to each other
- E.g., some components are:
 - Classes: types of things
- Individuals: specific objectsProperties: how things are related

• Examples:

- A medical ontology defines relationships between diseases, symptoms, and treatments
- A geographical ontology describes cities, states, and countries
- Semantic web (an extension of the current web to give meaning to information)

Purpose

- Provide a common vocabulary for a domain of knowledge
- Enable machines and humans to understand and share information consistently
- Enable reasoning about entities and their relationships

Related Concepts

- Schema: database-oriented structure, often more rigid than ontologies
- Taxonomy: simpler hierarchical classification (like a tree)

Ontologies: Main Components

- Classes / Concepts:
 - Represent general concepts in a domain
 - E.g., Person, City, Car
- Individuals / Instances:
 - Specific, concrete examples of classes
 - E.g., GP (an instance of Person), Rome, Ferrari 458
- Properties / Relations:
 - Describe interactions or associations between classes or instances
 - E.g., isMortal, locatedIn, hasAge
- Attributes / Data values
 - Specify data associated with instances
 - E.g., (GP, hasAge, <your_guess>)
- Constraints
 - Rules that restrict the kinds of values a property can take
 - E.g., (Ferrari 458, mustBe, red)
- Axioms:
 - · Logical statements that define rules and constraints
 - Used to infer new knowledge
 - E.g., all humans are mortal: $\forall x (Person(x) \implies Mortal(x))$
- Hierarchies:
 - Organize classes and properties into parent-child relationships

Ontology: Example University

- Classes: general types of things
 - Student
 - Professor
 - Course
 - Department



- Properties: relationships between Classes
 - $\bullet \ \ \mathsf{takesCourse} \ (\mathtt{Student} \to \mathtt{Course})$
 - ullet teachesCourse (Professor o Course)
 - $\bullet \ \, \mathtt{belongsToDepartment} \ (\mathsf{Student}, \ \mathsf{Professor} \to \mathtt{Department})$
 - ullet offersCourse (Department o Course)
- Individuals / Instances: examples of Classes
 - Student: Alice, Bob
 - Professor: GP, DrNo
 - Course: DATA605, MSML610
 - Department: ComputerScience, Mathematics
- Axioms: logical rules that must be true
 - Every Course must be taught by exactly one Professor
 - Every Student must belong to exactly one Department
 - A Department offers at least one Course

Reasoning in Ontologies

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Example of Reasoning Tasks (1/4)

Subsumption

- "Is class A a subclass of B?"
- Check whether one concept is more general than another
- E.g., if Person subsumes Student, every Student is necessarily a Person
- Important for building taxonomies and ontologies

Satisfiability:

- "Can an instance of a concept exist?"
- Test if a concept is logically consistent (i.e., without contradiction)
- E.g., if the concept FlyingPenguin requires flying but is also defined as a penguin (which cannot fly), it might be not satisfiable

Classification

- Organize concepts into a hierarchy
- Automatically organize concepts into a hierarchy by checking subsumption relationships
- E.g., given definitions of Animal, Bird, and Penguin, classification places
 Penguin under Bird, and Bird under Animal

Example of reasoning tasks in KR (2/4)

Instance Checking

- "Is a specific individual an instance of a concept?"
- E.g., is GP an instance of Student?

Consistency Checking

- "Is the entire knowledge base free of contradictions?"
- E.g., no Person is both Alive and Dead at the same time

Realization

- "What is the most specific class an instance belongs to?"
- E.g., discovering that GP is a Professor rather than just a Human

Retrieval

- Find all individuals that satisfy a certain condition
- E.g., retrieve all instances classified as TeachingAssistant

Example of reasoning tasks in KR (3/4)

Query Answering

- Answer complex queries about the knowledge base
- E.g., "Find all Person that study at the university and are not Student"

Abduction

- Given an observation, infer the best explanation
- E.g., seeing a Person carrying a backpack and wearing flip-flops in the snow and infer that is likely a Student

Deduction

- Infer consequences that logically follow from facts and rules
- E.g., if John is a Student in ComputerScience then he can attend MSML610

E.g., of reasoning tasks in KR (4/4)

Belief Revision

- Update the knowledge base when new, possibly conflicting, information arrives
- E.g., learning that not every student in ComputerScience can take MSML610 and revise a previous rule

Temporal Reasoning

- Reason about events over time
- E.g., If EventA happens before EventB, then EventB cannot Cause EventA

Causal Reasoning

- Infer causes and effects among entities or events
- E.g., inferring that (Storm, Cause, Flooding) based on temporal and physical knowledge

Ontologies tools: Protege Example

- Protégé is a free, open-source platform for building ontologies
 - Developed at Stanford
- Provides tools to construct and visualize ontologies
 - Users can define classes, properties, individuals, and relationships
- Enable reasoning over ontologies using plugins
 - E.g., checking consistency, inferring new knowledge
- Supports:
 - Major ontology languages
 - OWL (Web Ontology Language)
 - RDF (Resource Description Framework)
 - Multiple serialization formats
 - RDF/XML, Turtle, OWL Functional Syntax
- Use cases:
 - Domain-specific knowledge modeling (e.g., biomedicine, law)
 - Semantic Web applications
 - Al systems that require structured knowledge

Propositional logic

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Propositional Logic

- Propositional logic is a formal system for reasoning about statements that can be true or false
 - Syntax defines the allowable sentences
 - · Consists of proposition symbol and logical connectives
 - E.g., *P* ∧ *Q*
 - Semantics is the way in which the truth of sentences is determined
 - Truth tables or deduction rules evaluate the truth value of complex sentences
 - E.g., if P is true and Q is false then $P \wedge Q$ is false
- Atomic representation
 - No internal structure within atomic propositions
- Uses:
 - SAT solvers
 - Tools for determining if a propositional logic formula can be satisfied
 - E.g., used in hardware verification and scheduling problems
 - Expert systems
 - Systems that use logic rules to mimic human decision-making
 - E.g., medical diagnosis systems
 - Rule-based agents
 - · Agents that operate based on a set of predefined rules
 - E.g., automated customer service chatbots

Proposition symbol

- Proposition symbol
 - Is an atomic sentence consisting of a single symbol
 - E.g., P, Q, North
 - Doesn't have truth value, it is just a symbol for a real-world statement
 - Stands for a proposition that can be true or false
 - E.g., $K_{E.5}$ = "the Knight is in E5"
 - $K_{E,5}$ is not composed of any other symbol, it is an atomic symbol
 - True and False are proposition symbols with inherent truth values

Sentences

- Atomic sentence:
 - Is a sentence composed of a single proposition symbol
- Complex sentence:
 - Is constructed from simpler (sentences) using parentheses and logical connectives
 - Note: it is a recursive definition that allow to build more complex sentences
- Each sentence (atomic or complex) can be only true or false
- Common logical connectives
 - Not: ¬
 - And: ∧ (looks like an "A" for "and")
 - Or: ∨ (comes from Latin "vel" which means "or")
 - Implies: ⇒
 - If and only if: \iff

Proposition Logic: Weather Example

- Proposition symbols are
 - Rain = "it's raining"
 - Cold = "it's cold"
 - *Sunny* = "it's sunny"
 - *Snow* = "it's snowing"
 - Cloudy = "it's cloudy"
- Atomic sentence can be positive (e.g., Rain) or negated (e.g., $\neg Rain =$ "it's not raining")
- Negation
 - E.g., $\neg(Rain \lor Cloudy) = "it's not the case that it's raining or cloudy"$
- Conjunction
 - E.g., $Rain \wedge Cold = "it's raining and it's cold"$
- Disjunction
 - E.g., Rain \lor Snow = "it's either raining or snowing"
- Implication is a sentence containing a premise (aka antecedent), the connective ⇒, and a conclusion (aka consequent)

Grammar in BNF form

- Use BNF to formally represent the grammar of propositional logic
- Ambiguous, i.e., the same sentence can be parsed in multiple ways
 - E.g., $\neg A \lor B = (\neg A) \lor B \text{ or } \neg (A \lor B)$?
- To eliminate ambiguity define the precedence for each operator
 - E.g., ¬ has higher precedence than ∧, ∨ so: ¬A ∨ B means (¬A) ∨ B

```
Sentence \rightarrow AtomicSentence \mid ComplexSentence
AtomicSentence \rightarrow True \mid False \mid P \mid Q \mid R \mid \dots
ComplexSentence \rightarrow (Sentence)
\mid \neg Sentence
\mid Sentence \wedge Sentence
\mid Sentence \wedge Sentence
\mid Sentence \Rightarrow Sentence
```

Semantics of propositional logic

- ullet Semantics are rules for determining the truth of a sentence lpha with respect to a model m
 - We want to determine if a sentence is true or false, given a possible world
- In propositional logic, a model m fixes the truth value (true or false) for every proposition symbol/atomic sentence, e.g.,
- The models are abstractions of the real world and have no a-priori connection to a specific world, e.g.,
 - $P_{1,2}$ is just a symbol and can mean:
 - "There is a pit in [1, 2]" or
 - "I'm in Paris today and tomorrow"

Computing the truth value of a sentence

- The truth value of a sentence can be derived from the truth of the proposition symbols (recursively from the model m), e.g.,
- If the KB is based on proposition symbols $P_{1,2}, P_{2,2}, P_{3,1}$:

$$m = \{P_{1,2} = F, P_{2,2} = F, P_{3,1} = T\}$$

- All sentences α are constructed from atomic sentences (assigned by the model m) and the five connectives:
 - $\neg P$ is T iff P is F in m
 - $P \wedge Q$ is T iff P and Q are both true in m
 - $P \lor Q$ is T iff P or Q are true in m
 - $P \implies Q$ is true unless P is true and Q is false in m
 - $P \iff Q$ is true iff P and Q are both true or both false in m
- Truth table contains the truth value of a sentence (no matter how complex) for each possible assignment of truth values to its components

• E.g.,
$$X = A \wedge B \vee C$$

Interpretation of Implication

- In a logical implication $P \implies Q$ there is no causation between P and Q
 - E.g., "5 is odd implies that Tokyo is the capital of Japan" is a true sentence in propositional logic (although very odd)
- Pathological cases for implication
 - An implication is true whenever the antecedent is false
 - E.g., "5 is even implies pigs fly" is true
 - E.g., "5 is even implies Sam is smart" is true, even if Sam is not smart
 - The reason is that $P \Longrightarrow Q$ is saying "If P is true, I claim that Q is true. Otherwise I am making no claim"

Model Checking is Sound and Complete

- Model checking algorithm:
 - Enumerate all models (truth tables)
 - Check if α is true for every model where KB is true
- The model checking algorithm is:
 - Sound
 - "Any inference made by the algorithm is correct"
 - Implements the definition of entailment
 - Complete
 - "Any true sentence is inferred correctly by the algorithm"
 - ullet Works for any $K\!B$ and lpha
 - Always terminates (finite number of models)
- Complexity of model checking with n variables
 - Time complexity is $O(2^n)$ (NP-complete)
 - Worst case is exponential
 - Average case is better than exponential
 - Space complexity is O(n) since enumeration is depth-first

Propositional Theorem Proving

- ullet To prove a desired sentence lpha under a knowledge base KB
 - \bullet Apply rules of inference to construct a proof of α
 - Any sentence can have only one of the following truth values:
 - 1. True
 - 2. False
 - 3. Undecidable under the KB
- Theorem proving vs. model checking:
 - Model checking involves enumerating all models to show the sentence is true/false in all models where KB is true
 - If the proof is short, theorem proving can be more efficient than model checking

Logical equivalence of sentences

- Two sentences α and β are logically equivalent $\alpha \equiv \beta$
 - Iff they are true in the same set of models:

$$M(\alpha) = M(\beta)$$

• Iff they entail each other:

$$\alpha \models \beta \land \beta \models \alpha$$

• E.g., $P \lor Q \equiv Q \lor P$

Logical equivalences (1/2)

ullet Commutativity of \wedge and \vee

$$(\alpha \wedge \beta) \equiv (\beta \wedge \alpha)$$
$$(\alpha \vee \beta) \equiv (\beta \vee \alpha)$$

Associativity of ∧ and ∨

$$(\alpha \wedge \beta) \wedge \gamma \equiv \alpha \wedge (\beta \wedge \gamma) \equiv \alpha \wedge \beta \wedge \gamma$$
$$(\alpha \vee \beta) \vee \gamma \equiv \alpha \vee (\beta \vee \gamma) \equiv \alpha \vee \beta \vee \gamma$$

Distributivity of ∧ over ∨

$$\alpha \wedge (\beta \vee \gamma) \equiv (\alpha \wedge \beta) \vee (\alpha \wedge \gamma)$$

Distributivity of ∨ over ∧

$$\alpha \vee (\beta \wedge \gamma) \equiv (\alpha \vee \beta) \wedge (\alpha \vee \gamma)$$

Double negation elimination:

$$\neg(\neg\alpha)\equiv\alpha$$

Logical equivalences (2/2)

• Contraposition:

$$(\alpha \implies \beta) \equiv (\neg \beta \implies \neg \alpha)$$

• Implication elimination:

$$(\alpha \implies \beta) \equiv (\neg \alpha \lor \beta)$$

Biconditional elimination:

$$(\alpha \iff \beta) \equiv (\alpha \implies \beta) \land (\beta \implies \alpha)$$

• De Morgan:

$$\neg(\alpha \land \beta) \equiv (\neg\alpha \lor \neg\beta)$$
$$\neg(\alpha \lor \beta) \equiv (\neg\alpha \land \neg\beta)$$

Valid sentence

- A valid sentence α is true for all the models
 - E.g., *P* ∨ ¬*P*
 - Aka "tautology"
 - Every tautology is equivalent to the sentence *True*
- ullet Contradiction is a sentence lpha that is false for all the models
 - E.g., *P* ∧ ¬*P*
 - Every contraction is equivalent to the sentence False

Deduction theorem

• The sentence α entails β (written $\alpha \models \beta$) iff the sentence $\alpha \implies \beta$ is a tautology, i.e., is equivalent to True

Satisfiability

- A sentence α is satisfiable iff α is true for some model
- SAT problem is about determining satisfiability of sentence in propositional logic
 - \bullet One can enumerate all the possible models until one is found to satisfy the sentence α
 - It is NP-complete
- A sentence α is un-satisfiable iff α is never true (i.e., a contradiction)
- · Validity and satisfiability
 - α is valid (i.e., a tautology) iff $\neg \alpha$ is un-satisfiable
 - By contrapositive α is satisfiable iff $\neg \alpha$ is not valid ($\neg \alpha$ is not a tautology)

Proof by contraction

- The sentence $\alpha \models \beta$ is true iff the sentence $(\alpha \lor \neg \beta)$ is un-satisfiable (i.e., a contradiction)
- In other words in a proof by contradiction:
 - Assume α
 - Assume that the sentence β is false and
 - Prove that this leads to a contradiction
 - Thus β must be true

First-order Logic

- Knowledge Representation
- Propositional logic
- First-order Logic
- Non-classical Logics
- Description Logics

Natural languages

- Natural languages (e.g., English, Italian) are:
 - Expressive
 - Medium for communication rather than representation
 - Ambiguous
 - E.g., "spring" is both a "season" and "something that goes boing"
 - Context-dependent
 - · Meaning depends on the sentence and context
 - E.g., "Look!"
- Sapir-Whorf hypothesis
 - Understanding of the world is influenced by language
 - Language influences thought (even through arbitrary grammatical features, e.g., gender of nouns)
 - Some languages lack words for certain concepts (e.g., direction)

Programming languages

- A programming language (e.g., C++, Python) is a formal language
 - Data structures represent facts
 - Code updates data structures in a domain-specific way
- Cons:
 - Programming is procedural (vs declarative)
 - Programming languages lack:
 - 1. A general mechanism for deriving facts from other facts
 - Code updates data structures based on programmer's domain knowledge
 - 2. Expressiveness to handle partial information
 - A variable represents a single value or unknown
 - Can't easily handle partial information or quantify uncertainty
 - E.g., "A white knight is in b1 or in f6"
- Declarative language (e.g., propositional logic, first order logic)
 - Knowledge and inference are separate:
 - 1. Knowledge represents the domain-specific problem
 - 2. Inference is domain independent
 - Compositional semantics
 - The meaning of a sentence is a function of the meaning of its parts

Propositional logic

- E.g., *P* ∧ *Q*
- Pros
 - Declarative
 - Semantics is based on relation between sentences and possible worlds
 - Can deal with partial information
 - E.g., "A white knight is in b1 or in f6" is represented with $WK1_{b1} \lor WK2_{f6}$
 - Compositional semantics
 - The meaning of a sentence is a function of the meaning of its parts
 - Context independent
 - Unambiguous
- Cons
 - Can't concisely describe environment with many objects, e.g.,
 - In English "The pawn is in a cell around b6" requires all the possible states to be enumerated

First-Order Logic (FOL): Intro

- First-order logic (FOL) extends propositional logic by:
 - Introducing quantifiers (\forall, \exists)
 - Using predicates to represent properties and relations
- Combines pros of propositional logic with pros of natural language
 - Built around objects and relations
 - Allows to express facts about some or all objects, e.g.,
 - "Some humans have blue eyes"
 - "Squares neighboring the Wumpus are smelly"
- FOL provides expressive power to represent structured, relational knowledge

First-Order Logic: Syntax

- **Constants**: represent specific objects (e.g., Socrates)
- Predicates: describe properties or relations (e.g., Human(x))
- Functions: map tuples of objects to objects (e.g., Mother(x))
- Variables: placeholders (e.g., x, y)
- **Quantifiers**: $\forall x$ (for all x), $\exists x$ (there exists an x)

Sentence -> AtomicSentence | ComplexSentence AtomicSentence \rightarrow Predicate | Predicate(Term,...) | Term = Term ComplexSentence → (Sentence) ¬ Sentence Sentence A Sentence Sentence ∨ Sentence Sentence ⇒ Sentence Sentence +> Sentence Quantifier Variable, ... Sentence Term → Function(Term...) Constant Variable Quantifier $\rightarrow \forall \mid \exists$ $Constant \rightarrow A \mid X_1 \mid John \mid \cdots$ $Variable \rightarrow a \mid x \mid s \mid \cdots$ Predicate → True | False | After | Loves | Raining | · · · Function → Mother | LeftLeg | · · · OPERATOR PRECEDENCE : ¬,=, ∧, ∨, ⇒, ↔

- •
- Term is a logical expression that refers to an object in a FOL model
- Atomic sentence = predicate symbol (i.e., which corresponds to relations) followed by a list of terms in parenthesis (i.e., constant or function symbol) Predicate(Term1, Term2,...)
 - E.g., Brother(Richard, John), under the model / interpretation, Richard is the brother of John
 - E.g., Married(Father(Richard), Mother(John))
- Complex sentences = sentences using logical connectives complex, with 62/97

Quantifiers and Scope

- Quantifiers express properties of entire collections of objects, instead of enumerating objects by name (like in propositional logic)
- Universal quantifier: $\forall x P(x)$
 - Universal quantifier makes a statement about every object
 - Statement is true if P(x) is true for all x
- Existential quantifier: $\exists x P(x)$
 - Existential quantifier makes a statement about some object (without naming it)
 - True if P(x) is true for at least one x
- Scope determines the portion of a formula a quantifier applies to
- Variables are bound by quantifiers or free (unbound)
- Sentences with no free variables are called closed formulas
- Example:
 - $\forall x (Cat(x) \rightarrow Mammal(x))$

Nested quantifiers

- express more complex sentences using multiple quantifiers
- The order of quantifiers is important, so one can use parentheses to clarify
- Example:
 - "Brothers are siblings": $\forall x, y Brother(x, y) \implies Sibling(x, y)$
 - $\forall x, y Sibling(x, y) \iff Sibling(y, x)$ (symmetric relationship)
 - "Everybody loves somebody": $\forall x \exists y Loves(x, y)$
 - "There is someone loved by everyone": $\exists y \forall x Loves(x, y)$

Connection between \forall and \exists

• The two quantifiers are connected through negation and De Morgan rules

$$(\forall x \neg P) \iff (\neg \exists x)$$
$$\neg(\forall x P) \iff (\exists x \neg P)$$
$$(\forall x P) \iff (\neg \exists x \neg P)$$
$$(\exists x P) \iff (\neg \forall x \neg P)$$

First-order logic: Semantics

- Semantics define how sentences are interpreted in a domain
- Symbols represent entities, relationships, and functions in the domain
 - Constant symbols represent specific objects
 - E.g., Alice, GP, CS101
 - Predicate symbols represent relationships among objects
 - E.g., EnrolledIn(Student, Class), Teaches(Professor, Class), IsStudent(x), IsProfessor(x)
 - Function symbols represent mappings between objects
 - E.g., AdvisorOf(Student), DepartmentOf(Professor)
- An interpretation maps the world to its mathematical description, and vice versa
 - There are many possible interpretations
 - The intended interpretation is the one that is the most natural
 - ullet E.g., map the symbol $\emph{GP}
 ightarrow$ me
- Example:
 - Sentence: $\forall x (Human(x) \rightarrow Mortal(x))$
 - True if for every x in the domain, Human(x) implies Mortal(x)

Inference in First-Order Logic

- Goal: derive new sentences from existing ones using sound rules
- Universal Instantiation:
 - From $\forall x P(x)$ infer P(c) for any constant c
- Existential Instantiation:
 - From $\exists x P(x)$ infer P(c) with a new constant c
- Modus Ponens and other propositional rules apply
- FOL inference is semi-decidable:
 - If a sentence is entailed, a proof can be found
 - If not entailed, proof search may not terminate

Representing Knowledge in FOL

- FOL enables representation of:
 - General rules: $\forall x (Bird(x) \rightarrow CanFly(x))$
 - Specific facts: *Bird(Tweety)*
- Complex relations captured through predicates:
 - Loves(Romeo, Juliet), GreaterThan(3,2)
- Functions express object construction:
 - FatherOf (John)
- Knowledge base built from axioms and facts
- Enables reasoning about objects, properties, and their relationships

Non-classical Logics

- Knowledge Representation
- Propositional logic
- First-order Logic
- Non-classical Logics
- Description Logics

Ontological commitment

- Ontological commitments are assumptions about reality made by a language
- Different formal models make different assumptions on how the truth of sentences is defined:
 - Propositional logic:
 - The world consists of facts that are either true or false
 - First-order logic:
 - The world consists of objects with relations among them that hold or do not hold
 - Temporal logic:
 - Facts about objects and relations hold at particular times or intervals
 - Higher-order logic:
 - Relations of first-order logic are objects themselves
 - E.g., can make assertions about relations (e.g., "all relations are transitive")

Epistemological commitment

- Epistemological commitment is a possible states of knowledge by an agent with respect to each fact
 - Ontological commitment = what exists in the world
 - Epistemological commitment = what an agent believes about facts
- E.g,
 - Propositional logic, first-order logic
 - 3 possible states of belief regarding any sentence: true, false, or unknown
 - Probability theory
 - There is a degree of belief in [0, 1] about each sentence

Non-monotonic Logic

- Non-monotonic logic is a type of logic where adding new information can invalidate previous conclusions
- Contrast with Classical (Monotonic) Logic
 - In classical logic, once something is proven, it stays proven even if more information is added
 - In non-monotonic logic, conclusions can change as new facts are learned

• E.g.,

- Initial knowledge: "Birds typically fly"
- Conclusion: "Tweety is a bird, so Tweety can fly"
- New information: "Tweety is a penguin"
- Revised conclusion: "Tweety cannot fly"

Why it Matters

- Real-world situations often involve incomplete or evolving knowledge
- Non-monotonic logic allows systems to reason flexibly and adapt to new circumstances

Default reasoning

- Default reasoning is reasoning where assumptions are made by default in the absence of contrary evidence
 - It allows conclusions based on typical situations unless exceptions are found
- Key Idea
 - Assume the most likely case unless specified otherwise
 - If new information contradicts the assumption, revise the conclusion
- E.g.,
 - Default rule: "Typically, birds can fly"
 - Fact: "Tweety is a bird"
 - Conclusion: "Tweety can fly"
 - New fact: "Tweety is a penguin"
 - Revised conclusion: "Tweety cannot fly"
- Why It Is Useful
 - In real life, information is often incomplete or uncertain
 - Default reasoning allows systems to function reasonably without knowing everything

Non-Monotonic Logic: University Example

Initial Facts

- Alice is a Student
- Alice belongs to the ComputerScience department
- CS101 is a Course offered by the ComputerScience department
- Default rule: Students in the ComputerScience department take classes in their department

Initial Reasoning

- Since Alice is a Student in ComputerScience, by default Students take CS101
- Conclusion: Alice takesCourse CS101

New Information

 Alice is an exchange student who does not meet the prerequisites for CS101

Revised Reasoning

New conclusion: Alice does not takeCourse CS101

Common Sense Reasoning

- Common sense reasoning is the ability to make assumptions, draw conclusions based on everyday knowledge about the world
 - Involves typical, unstated knowledge that humans take for granted, e.g.,
 - "If you drop a glass, it will likely break"
 - Knowing that "people eat food when they are hungry" without being explicitly told

Characteristics

- Deals with incomplete, uncertain, or ambiguous information
- Relies on defaults, heuristics, and typical patterns rather than strict logical proofs
- Often flexible and tolerant of exceptions

Challenges

- Common sense knowledge is vast, informal, and often not precisely defined
- Difficult to encode all of it explicitly in a machine-readable form
- Handling exceptions and contradictions is complex

Techniques

- Knowledge graphs
- Non-monotonic logic
- Probabilistic reasoning
- Machine learning models trained on large, diverse data

Common Sense Reasoning: University Example

Initial facts

- Alice is a Student
- Bob is a Student
- CS101 is a Course offered by the ComputerScience department

Common sense knowledge

- Students typically enroll in courses offered by their department
- Students usually attend classes they are enrolled in
- Professors usually teach the courses they are assigned

Reasoning steps

- Alice belongs to the ComputerScience department
- CS101 is offered by the ComputerScience department
- Common sense suggests Alice is likely enrolled in CS101, even if enrollment is not explicitly stated
- Therefore, it is reasonable to assume: Alice takesCourse CS101

New information

- Alice is pursuing research only and not taking courses
- The assumption that *Alice takesCourse CS*101 must be revised

Open World vs Closed World Assumptions

Closed World Assumption (CWA)

- Missing information is false, e.g.,
 - Fact: "Alice takes CS101" is known
 - Nothing is said about Bob
 - Under CWA: Conclude Bob does not take CS101
- Common in databases and logic programming

Open World Assumption (OWA)

- Missing information is unknown, not false, e.g.,
 - Fact: "Alice takes CS101" is known
 - Nothing is said about Bob
 - Under OWA: Cannot conclude if Bob takes CS101: it is unknown
- Common in Semantic Web, RDF, ontologies

Applications

- OWA
 - Semantic Web (RDF, OWL)
 - Knowledge representation with incomplete or growing data
- CWA
 - Traditional relational databases (SQL)
 - Business rules and systems requiring complete data

Inductive Logic Programming

Inductive Logic Programming

- Learns logical rules from examples and common sense knowledge
- Given positive and negative examples, and background facts, infer logical rules that explain the examples

Example

- Background: "Birds have wings"
- Positive example: "Tweety can fly"
- Negative example: "Penguin cannot fly"
- Learned rule: "Birds can fly unless they are penguins"

Features

- Produces human-readable logical rules
- Integrates learning with symbolic reasoning
- Supports background knowledge integration

Challenges

- Computational complexity with large datasets
- · Handling noisy, incomplete, or ambiguous data

Description Logics

- Knowledge Representation
- Propositional logic
- First-order Logic
- Non-classical Logics
- Description Logics
 - Semantic Web

Description Logic

- Description Logic
 - Represents structured knowledge about a domain
 - Balances expressivity and computational efficiency
 - More expressive than propositional logic, less than first-order logic
- Core building blocks:
 - Concepts / classes: abstract groups
 - E.g., Person, Animal
 - Roles / properties: binary relations between individuals
 - E.g., hasChild, ownsPet
 - Individuals / instances: specific objects
 - E.g., GP, Nuvolo
- Supports reasoning tasks such as:
 - Concept subsumption: "is A a subset of B?"
 - Instance checking: "does a belong to A?"
- Syntax often combines:
 - Atomic concepts and roles
 - Logical constructors $(\sqcap, \sqcup, \neg, \forall, \exists)$
 - E.g.,
- Widely used in ontologies, e.g., OWL (Web Ontology Language)

ALC

- Attributive Concept Language with Complements (ALC) is a basic but expressive description logic
 - Concepts can be combined using logical operators, e.g.,
 - □ means "and"
 - □ means "or"
 - ¬ means "not"
 - Allows for existential and universal quantification, e.g., $\exists R.C, \forall R.C$
- Interpretation is set-theoretic
 - Concepts as sets, roles as binary relations
- Example:
 - "All students take some course": Student

 ∃takes.Course
- ALC:
 - Is decidable
 - balances expressiveness and computational complexity
 - Is basis for more complex logics used in OWL
 - Practical for moderate-sized ontologies

SHOIN

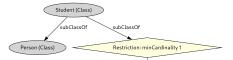
- SHOIN is a description logic more expressive than ALC
- Components:
 - S: Allows transitive properties
 - E.g., ancestorOf is transitive
 - \mathcal{H} : Supports role hierarchies
 - E.g., hasSon \sqsubseteq hasChild
 - O: Introduces specific individuals
 - E.g., John is a nominal class
 - ullet \mathcal{I} : Enables roles to be navigated backward
 - E.g., isChildOf is inverse of hasChild
 - \mathcal{N} : Sets cardinality constraints
 - E.g., "has exactly 1 passport"
- E.g.,:
 - "Exactly two children" Person \sqsubseteq (= 2 hasChild. \top)
- Characteristics
 - More powerful but reasoning is harder (exponential complexity)
 - Model richer real-world scenarios
 - Foundation for OWL DL reasoning capabilities

OWL

- OWL = Web Ontology Language
 - Semantic web language designed to represent complex knowledge about things and their relationships
 - Enables rich knowledge representation on the web (based on SHOIN)
 - "OWL" easier to pronounce than "WOL"
 - Supports formal semantics for machine reasoning
 - Key constructs:
 - Classes, properties, individuals, axioms
- Example:
 - ullet "Every cat is a mammal" Cat \sqsubseteq Mammal
- OWL variants:
 - OWL Lite: simpler, for classification hierarchies
 - OWL DL: full expressiveness with decidable reasoning
 - OWL Full: maximum expressiveness, but undecidable
- Applications
 - Semantic search
 - Biomedical data

Example of OWL in RDF

```
1.
   <rdf:RDF xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#"
 3.
             xmlns:owl="http://www.w3.org/2002/07/owl#"
             xmlns:rdfs="http://www.w3.org/2000/01/rdf-schema#"
 4.
             xmlns:ex="http://example.org/">
 5.
      <owl:Class rdf:about="http://example.org/Person"/>
 6.
 7.
      <owl:Class rdf:about="http://example.org/Student">
 8.
        <rdfs:subClassOf rdf:resource="http://example.org/Person"/>
        <rdfs:subClassOf>
 9.
10.
          <owl:Restriction>
11.
            <owl:onProperty rdf:resource="http://example.org/hasAdvisor"/>
12.
            <owl:minCardinality rdf:datatype="http://www.w3.org/2001/XMLSchema#nonNegat</pre>
13.
            </owl:minCardinality>
14.
15.
          </owl:Restriction>
        </rdfs:subClassOf>
16.
17.
      </owl:Class>
18.
      <owl:ObjectProperty rdf:about="http://example.org/hasAdvisor"/>
19. </rdf:RDF>
20. ``
```



RDF (Resource Description Framework)

- RDF is a standard model for data interchange on the web
 - · Represent structured information in a machine-readable way
- Basic building block is a triple (Subject, Predicate, Object)
 - Subject: the entity being described, e.g., Nuvolo
 - Predicate: the property or relationship, e.g., isA
 - Object: the value or another entity, e.g., Dog
- Key Features:
 - Statements are directed graphs of nodes and edges
 - Components of the triple are URIs (Uniform Resource Identifiers) to ensure global uniqueness or literals (e.g., strings, numbers), e.g., http://example.org/Nuvolo
- Use Cases:
 - Building knowledge graphs
 - Enabling semantic search
 - Supporting ontologies (e.g., OWL)

Subject	Predicate	Object
Book123	hasTitle	"The Great Gatsby"
Book123	hasAuthor	Author456
Author456	hasName	"F. Scott Fitzgerald"
Book123	publishedYear	"1925"
Book123	belongsToGenre	"Fiction"

SPARQL

- SPARQL is the query language for RDF data
 - Allows users to retrieve and manipulate data stored in RDF format
- Key Concepts:
 - Triple Patterns: Query fragments that match triples in an RDF graph
 - Basic Graph Pattern: A set of triple patterns combined
 - Variables: Stand in for unknown parts of the triples (e.g., ?person, ?animal)
- Main Query Types:
 - SELECT: Retrieve specific variables from the data
 - CONSTRUCT: Create new RDF triples based on query results
 - ASK: Return a boolean indicating whether a pattern exists
 - DESCRIBE: Return an RDF graph describing resources
- Example:
 - "Find all resources that are of type Bird"
 SELECT ?animal WHERE { ?animal rdf:type ex:Bird }

Semantic Web

- Knowledge Representation
- Propositional logic
- First-order Logic
- Non-classical Logics
- Description Logics
 - Semantic Web

Semantic Web

- The Semantic Web extends the current Web by enabling machines to understand and interpret data
 - HTML is human-readable but lacks semantic structure for computers
 - The Semantic Web adds meaning / semantics to data
 - Allow better data integration, automation, and discovery across sites

Key Technologies

- RDF (Resource Description Framework): base data model
- SPARQL: query language for RDF data
- OWL (Web Ontology Language): define rich ontologies

Current Status

- Some core ideas (e.g., structured data and ontologies) are widely adopted
- Full vision remains only partially realized

Challenges

- Complexity of widespread adoption
- · Issues around privacy, data ownership, and feasibility
- Need for standardization and tools

Criticism

- Skepticism about practicality and scalability
- Concerns about centralization and censorship

WikiData

- WikiData is a free, open, collaborative knowledge base
 - Stores structured data for Wikipedia
 - Accessible via APIs using SPARQL queries

Graph-based data model

- Item: represents an entity or concept, e.g.,
 - Q42 → Douglas Adams
- Property: describes a relationship or attribute, e.g.,
 - P31 (instance of), P27 (country of citizenship)
- Value: specific data linked to an item via a property, e.g.,
 - Q42 (Douglas Adams) ightarrow P31 (instance of) ightarrow Q5 (human)
 - Q42 \rightarrow P106 (occupation) \rightarrow Q36180 (science fiction writer)
- Reference: supports a claim by citing a source, e.g.,
 - Stating Douglas Adams's citizenship with a reference to a biography
- Qualifier: adds context or additional information to a statement
 Q90 (Paris) → P1082 (population) → "2,165,423"
 - With qualifier: P585 (point in time) → "2021"

• Meaning: "The population of Paris was 2,165,423 in the year 2021"

Applications:

- Knowledge graph
- Semantic search
- Al reasoning
- Data enrichment

DBPedia

- DBpedia extracts structured content from Wikipedia
 - Creates a large-scale, multilingual knowledge graph for querying
 - Data is extracted as RDF triples (subject-predicate-object), e.g.,
 - "Berlin" entity linked with properties like dbo:country Germany, dbo:populationTotal 3.7M
 - Enables semantic queries over Wikipedia data via SPARQL endpoints
- Applications
 - Semantic Web research
 - Enhancing AI models with real-world knowledge

Semantic Networks

- Semantic Networks represent knowledge as graphs of concepts and relations
 - Nodes represent concepts
 - Edges represent relations (e.g., "is-a", "part-of")
 - E.g., if a Dog is an Animal, it inherits Animal traits
 - Examples: WordNet, ConceptNet
- Pros
 - Easy to visualize and traverse
 - Support reasoning
 - Common in early AI systems and current KG applications

WordNet

- WordNet is a large lexical database of English words
 - Designed to model the semantic relationships between words
 - Groups words into sets of synonyms
 - Manually curated, ensuring high-quality semantic relations
 - Can be incomplete for domain-specific language
- Key Components:
 - Synsets: Sets of synonyms expressing a distinct concepts
 - E.g., {car, automobile} share the same synset
 - Relations between synsets:
 - Is-a relationships (e.g., Dog is a type of Animal)
 - Part-whole relationships (e.g., Wheel is a part of Car)
 - Opposite meanings
- Structure:
 - Semantic network where nodes are synsets and edges are relations
 - Organized hierarchically, especially for nouns and verbs
- Applications:
 - Word sense disambiguation: choose the correct meaning of a word in context
 - Semantic similarity measures: how close two concepts are
 - Information retrieval and question answering systems

ConceptNet

- ConceptNet is a large knowledge graph
 - Connects words and phrases with labeled semantic relationships
 - Represents commonsense knowledge about the world
- Key Characteristics:
 - Designed to capture knowledge that people generally assume but often leave unstated
 - · Focuses on making AI systems more human-like in their understanding
- Structure:
 - Nodes: concepts (words or phrases)
 - Edges: semantic relationships between concepts, e.g.,
 - IsA: (dog, animal)
 - PartOf: (wheel, car)
 - UsedFor: (knife, cutting)
 - CapableOf: (bird, fly)
 - Causes: (fire, smoke)
- Example Triple:
 - (bicycle, UsedFor, transportation)
- Applications:
 - Natural language understanding
 - Question answering and chatbots
 - Commonsense reasoning in AI
 - Semantic search and recommendation systems

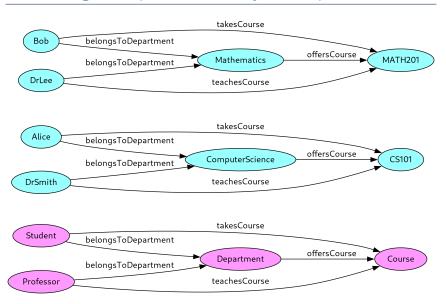
Frame-Based Representations

- Frame-based systems represent structured knowledge about objects, events, or situations
- Key Concepts:
 - Frame: A data structure for a concept or entity
 - E.g., a frame for Dog might include properties like hasLegs, hasFur, barks
 - Slots: attributes or relationships associated with the frame
 - E.g., slot hasLegs with value 4
 - Slot fillers: values or links to other frames that fill the slots
 - . E.g., slot eats might link to another frame Meat
- Example:
 - Frame: Dog
 - Slots:
 - isA: Animal
 - hasLegs: 4
 - sound: Bark
 - canDo: [Run, Fetch]
- Features:
 - Inheritance: frames can inherit slots and slot values from more general frames. e.g..

Knowledge Graphs (KGs)

- KGs represent entities and their relationships as a graph structure
 - Nodes = entities
 - Edges = relations
 - E.g., "Paris \rightarrow isCapitalOf \rightarrow France"
- Query languages like SPARQL allow expressive information retrieval
- KGs support reasoning via path traversal and schema inference
- Applications:
 - Question answering
 - Recommendation
 - Semantic search
- Widely used by Google, Facebook, and academic search engines

Knowledge Graph: University Example



Technologies

TransE (Translation Embedding)

- Embedding model for knowledge graph completion
- Represents relationships as translations in vector space: $h + r \approx t$
- Good for 1-to-1 relations, less effective with complex patterns

RotatE

- Embeds entities in complex space
- Models relations as rotations: $t = h \circ r$ where \circ is complex multiplication
- Captures symmetry, antisymmetry, inversion, and composition

DeepProbLog

- Combines ProbLog (probabilistic logic) with deep learning
- Supports neural predicates in logic programs
- · Learns probabilistic facts and neural components jointly

PyMLN

- Python-based Markov Logic Network (MLN) system
- MLNs combine first-order logic with probabilistic graphical models
- Allows reasoning with weighted logical rules

ProbLog

- Probabilistic logic programming language
- Extends Prolog by attaching probabilities to facts
- Computes success probabilities of queries

• Tuffy 97/97