

$$V = \int_a^b A(x) \, dx \quad \dots \text{ volume when you know a cross-section area function}$$

$$V = \int_a^b \pi \cdot (f(x))^2 \, dx \quad \dots \text{ disk method about x-axis}$$

$$V = \int_a^b \pi \cdot (f(x)^2 - g(x)^2) \, dx \quad \dots \text{ washer method about x-axis}$$

$$V = \int_c^d \pi [x_R(y)^2 - x_L(y)^2] \, dy \quad \dots \text{ washer method about y-axis}$$

$$V = \int_a^b 2\pi x \cdot f(x) \, dx \quad \dots \text{ cylindrical shells ; rotation of area below } y = f(x) \text{ rotated about y-axis}$$

$$L = \int_a^b \sqrt{1 + (f'(x))^2} \, dx \quad \dots \text{ arclength of a plane curve } y = f(x)$$

$$SA = \int_a^b 2\pi f(x) \cdot \sqrt{1 + (f'(x))^2} \, dx \quad \dots \text{ lateral surface area when } y = f(x) \text{ is rotated about the x-axis}$$

$$x^* = \frac{\sum_{k=1}^n (m_k \cdot x_k)}{\sum_{k=1}^n m_k} \quad \dots \text{ center of mass for a discrete point-mass system}$$

$$M = \int_a^b \delta(x) \, dx \quad \dots \text{ mass of a thin rod with variable density } \delta(x)$$

$$x^* = \frac{\int_a^b x \cdot \delta(x) \, dx}{\int_a^b \delta(x) \, dx} \quad \dots \text{ center of mass for a thin rod with variable density } \delta(x)$$

$$x^* = \frac{\int_a^b x(f(x) - g(x)) \, dx}{\int_a^b (f(x) - g(x)) \, dx} \quad y^* = \frac{\int_a^b \frac{1}{2} \cdot (f(x)^2 - g(x)^2) \, dx}{\int_a^b (f(x) - g(x)) \, dx} \quad \dots \text{ center of mass } (x^*, y^*) \text{ for a lamina}$$

(these two will be given on the exam)

$$W_k = F_k \cdot D_k = (\text{weight density}) \cdot V_k \cdot D_k \quad \dots \text{ work done in pumping liquids out of tanks.}$$

$$F_k = (\delta \cdot g \cdot h_k) \cdot A_k \quad \dots \text{ force acting on a 2-D plate subject to hydrostatic pressure.}$$