TTK4130 Modeling and Simulation Assignement 1 lugebrigt Stamnes Reinsborg

1a) 1. and 3. are already State space.

$$2. \ddot{x} + C\dot{x} + g\left(1 - \left(\frac{x}{x}\right)^{\kappa}\right) = 0$$

$$\times_z = \dot{\times} = \dot{\times}_i$$

$$\begin{bmatrix} \dot{X}_1 \\ \dot{X}_2 \end{bmatrix} = \begin{bmatrix} (-\dot{X}_2 - g(1 - \left(\frac{X_4}{X_1}\right)^K)) \frac{1}{C} \\ -CX_2 - g(1 - \left(\frac{X_4}{X_1}\right)^K) \end{bmatrix}$$

$$= \begin{bmatrix} \times_2 \\ -C \times_2 - g(1 - (x_i)^k) \end{bmatrix}$$

$$\mathcal{A}\mathcal{U}_{1} = b\sqrt{x_{1}} = \sum_{io'} \frac{a^{2}\mathcal{U}_{i}^{2}}{b^{2}} > 0$$

$$u_1(u_2-x_2) = -C(u_3-\overline{x_2})$$

$$-X_2U_1+U_1U_2=-CU_3+CX_2$$

$$CU_3 + U_1U_2 = (C + U_1) \times_2 =) \times_{20} = \frac{CU_3 + U_1U_2}{C + U_1}$$

$$= 9 = 9 \left(\frac{x}{x}\right)^{\kappa}$$

$$\left(\frac{X_{10}^{A}}{X}\right)^{K} = 1$$
 $\frac{X_{0} = X_{d}}{X_{20} = 0}$

$$y^2 - \frac{yx}{\ln\sqrt{x^2 + y^2}} + x^2 + \frac{yx}{\ln\sqrt{x^2 + y^2}} = 0$$

$$x^2 + y^2 = 0 \Rightarrow x = 0$$

$$y_0 = 0$$

C) 1.
$$\dot{X}_{1} \approx \frac{\partial f}{\partial x_{1}}\Big|_{X_{10}, X_{20}} (x_{1} - x_{10})$$

$$= -\frac{b}{2} \frac{1}{\sqrt{X_{10}^{11}}} (x_{1} - x_{10})$$

$$= -\frac{b}{2} \frac{b}{a u_1} (x_1 - x_1 o) = -\frac{b^2}{2 a u_1} (x_1 - \frac{a^2 u_1^2}{b^2})$$

$$\dot{X}_{z} \approx \frac{\partial f}{\partial x_{1}} \Big|_{x_{10}, x_{20}} (x_{01} - x_{10}) \\
+ \frac{\partial f}{\partial x_{2}} \Big|_{x_{10}, x_{20}} (x_{2} - x_{10}) \\
= -\frac{\mathcal{A}}{x_{10}^{2}} \Big(\mathcal{U}_{1} \Big(\mathcal{U}_{1} - x_{10} \Big) + \mathcal{C} \Big(\mathcal{U}_{2} - x_{10} \Big) \Big) \Big(x_{1} - x_{10} \Big) \\
+ \frac{\partial \mathcal{U}_{1}}{x_{10}} - \frac{\mathcal{A} \mathcal{C}}{x_{10}} \\
\vdots \\
\dot{x}_{1} = \begin{bmatrix} x_{1} \\ -\mathcal{C} x_{1} - g(1 - (x_{1})^{K}) \end{bmatrix} \\
\dot{x}_{1} \approx \frac{\partial f}{\partial x_{2}} \Big|_{x_{10}, x_{20}} (x_{2} - x_{20}) \\
= x_{2} \\
\dot{x}_{2} \approx \frac{\partial f}{\partial x_{1}} \Big|_{x_{10}, x_{20}} (x_{1} - x_{10}) \\
+ \frac{\partial f}{\partial x_{2}} \Big|_{x_{10}, x_{20}} (x_{2} - x_{20}) \\
= \int_{\mathcal{A}} \int_{x_{10}, x_{20}} (x_{2} - x_{20}) \\
= \int_{x_{10}, x_{20}, x_{20}} (x_{2} - x_{20}) \\
= \int_{x_{10}, x_{20}, x_{20}} (x_{2} - x_{20}) \\
= \int_{x_{10}, x_{20}, x_{20}, x_{20}, x_{20}} (x_{2} - x_{20}) \\
= \int_{x_{10}, x_{20}, x_{20$$

$$\frac{dx}{dx} = \frac{1}{\log(\sqrt{x^2 + y^2})} - \frac{x^2}{(x^2 + y^2)\log^2(\sqrt{x^2 + y^2})}$$

$$d)$$
 3. $[\div]$ $[\circ]$

$$\begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$det(A) = 1$$

$$det(A - \lambda I) = \begin{vmatrix} -\lambda & 1 \\ -1 & -\lambda \end{vmatrix}$$

$$= \lambda^2 + 1 = 0$$

Marginally stable

l og 4 positiv

2. $\dot{x} = \begin{bmatrix} 0 & 1 \\ g & \\ x & -C \end{bmatrix} \begin{bmatrix} x, \\ x \\ \end{bmatrix} + \begin{bmatrix} 0 \\ -g & \\ \end{bmatrix}$

$$A = \begin{bmatrix} -\lambda & 1 \\ A - \lambda I \end{pmatrix} = \begin{bmatrix} -\lambda & 1 \\ \frac{3K}{Xa} & -\lambda - C \end{bmatrix}$$

$$= \lambda^{2} + \lambda C - \frac{gK}{Xa}$$

$$\lambda = -C + \sqrt{C^{2} - 4.1, (-\frac{gK}{Xa})}$$

$$Z$$

Always a root in r.h.p

=) Unstable

(Mod Sim A1 - forts.)

(2a) I observe that $X' = X^2$ Curves further and that upwards as lime goes and that $X' = \sqrt{|X|}$ Platters out.

b) Mathematically, of course, this doesn't make much sense, so there's probably something wrong with how I use ode 45.

 $X'=X^2$ has the general solution $X=\frac{-1}{t+c}$ and the special sol.

 $X = +\frac{1}{t-1}$ given X(0) = 1

which should just shoot up to intinity and beyond as t-> 1, making a really ugly graph.

I got a flat graph after some fiddling with X'= VIXI using ODE 45. Not sure why it looks like that, but I'm assuring it's to teach us that "computers have their

3a) we get something like this:

$$H'' = (b-d)H - baH^2 - iHZ$$
 $\dot{I} = -(a+d)I + iHZ$
 $\dot{Z} = aI + rD - nHZ$
 $\dot{D} = d(H+I) - rD + nHZ$

and given:

 $\dot{H} + \dot{I} + \dot{Z} + \dot{D} = bH - baH^2$

- b) See graphs
- c) I think in the model with the quavantine, those that die within, vespouvers as # Zombies outside the quavantine. This could probably be fixed adding another parameter:

De = dead in quarantine

