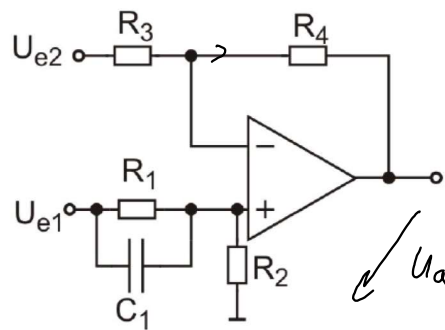


$R_2 = 1k\Omega$
 $R_4 = 10k\Omega$
 $C_1 = 100nF$
 $U_{e1} = 5 + 5 \cdot \sin(\omega t)$
 $U_{e2} = -2 + 2 \cdot \sin(\omega t)$
 OPV ideal



a) Super pos: $U_{e1} = 0$

$$U_a \cdot U_{R4} = -I \cdot R_4 = -\frac{U_{e2}}{R_3} \cdot R_4$$

$U_{e2} = 0$

$$Z_1 = \frac{R_1 \cdot \frac{1}{j\omega C_1}}{R_1 + \frac{1}{j\omega C_1}}$$

$$U_2 = U_3 = U_{e1} \cdot \frac{R_2}{\frac{R_1 \cdot \frac{1}{j\omega C_1}}{R_1 + \frac{1}{j\omega C_1}} + R_2}$$

$$U_3 = U_a \cdot \frac{R_3}{R_3 + R_4} \rightarrow U_a = U_3 \cdot \frac{R_3 + R_4}{R_3}$$

$$U_a = U_{e1} \cdot \frac{R_3 + R_4}{R_3} \cdot \frac{R_2}{\frac{R_1 \cdot \frac{1}{j\omega C_1}}{R_1 + \frac{1}{j\omega C_1}} + R_2} - U_{e2} \cdot \frac{R_4}{R_3}$$

b) $U_a(0) = U_{e1} - 0,5 U_{e2} = U_{e1} \cdot \frac{R_3 + R_4}{R_3} \cdot \frac{R_2}{\underbrace{\frac{R_1 j\omega C_1}{R_1 j\omega C_1 + 1}}_{=0} + R_2} - U_{e2} \cdot \frac{R_4}{R_3}$

$$= U_{e1} \cdot \underbrace{\frac{R_3 + R_4}{R_3} \cdot \frac{R_2}{R_1 + R_2}}_{=1} - U_{e2} \cdot \underbrace{\frac{R_4}{R_3}}_{=0,5}$$

$$R_3 = \frac{R_4}{0,5} = 20k\Omega$$

$$1,5 = \frac{20k + 10k}{20k} \cdot \frac{1k}{1k + R_1}$$

$$\frac{2}{3} 1k + \frac{2}{3} R_1 = 1k \rightarrow R_1 = \left(1k - \frac{2}{3} 1k\right) \cdot \frac{3}{2} = \frac{1}{2} k = 500\Omega$$

c) In Standard form bringen

$$\omega\text{-Abh. Teil: } \frac{R_3 + R_4}{R_3} \cdot \frac{R_2}{\frac{R_1}{R_1 j\omega C_1 + 1} + R_2} = \frac{R_3 + R_4}{R_3} \cdot \frac{R_2}{\frac{R_1 + R_1 R_2 j\omega C_1 + R_2}{R_1 j\omega C_1 + 1}}$$

$$= \frac{R_3 + R_1}{R_3} \cdot \frac{R_2 \cdot R_1 j\omega C_1 + R_2}{R_1 + R_1 R_2 j\omega C_1 + R_2} = \frac{R_3 + R_1}{R_3} \cdot \frac{R_2}{R_1 + R_2} \cdot \frac{1 + j\omega C_1 R_1}{1 + j\omega C_1 \frac{R_1 R_2}{R_1 + R_2}}$$

$$\omega_{g1} = \frac{1}{C_1 R_1}$$

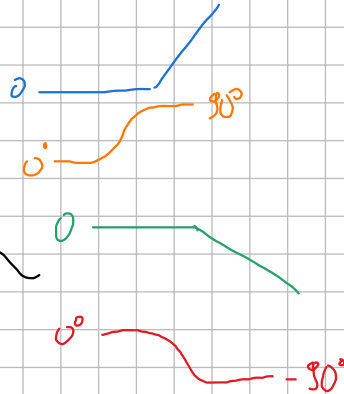
$$\omega_{g2} = \frac{R_1 + R_2}{C_1 R_1 R_2}$$

$$f_{g1} = \frac{1}{2\pi C_1 R_1}$$

$$f_{g2} = \frac{R_1 + R_2}{2\pi C_1 R_1 R_2}$$

d) ?

e) $V_n = \frac{U_{an}}{U_{en}} = \frac{1 + j\omega C_1 R_1}{1 + j\omega C_1 \frac{R_1 R_2}{R_1 + R_2}}$



$$f_{g1} = 3,18 \text{ kHz} < f_{g2} = 4,77 \text{ kHz}$$

