Exercise set 5. Due 10.05.2023.

Name and surname:

Student number:

1. Perform a bifurcation analysis (classify the type of bifurcation that occurs if possible as well), on the following systems of differential equations.

(a)

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \mu x - x^2$$

$$\frac{\mathrm{d}y}{\mathrm{d}t} = x - y$$

(b)

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \mu x - x^3$$

$$\frac{\mathrm{d}y}{\mathrm{d}t} = -y$$

(c)

$$\frac{\mathrm{d}x}{\mathrm{d}t} = y + \mu x$$

$$\frac{\mathrm{d}y}{\mathrm{d}t} = -x + \mu y - x^2 y$$

Note, only consider the origin for this question.

2. Perform a bifurcation analysis on,

$$\frac{\mathrm{d}x}{\mathrm{d}t} = -2x^2 + y$$
$$\frac{\mathrm{d}y}{\mathrm{d}t} = \mu x - x^3 + y,$$

but only investigate the steady state at the origin. For which values of μ do bifurcations occur?

3. Nondimensionalize the following differential equation,

$$\frac{\mathrm{d}N}{\mathrm{d}t} = RN\left(1 - \frac{N}{K}\right) - \frac{BN^2}{A^2 + N^2}$$

by choosing $x = \frac{N}{K}$ and $\tau = tR$.