Some Basic divide & Conquere scenario.

-> I hope you know merge sort + quick sort + binary/ termany search by now.

the closest pairs of points: You are traying to find the smallest distance between two points in a given array.

lets say we have total of 10 points, (p) each having (ny) co-ordinate value.

$$d(Pi, Pj) = \sqrt{(2i-2i)^2 + (2i-2j)^2}$$

we need to find the smallest $d(Pi, Pi)$

#approach 1: brute-force: use nested loop for two point and check all the combination \Rightarrow $(O(n^2))$

ideas -> you can sort the array with n-dimentions check the distance of y

-> can use divide & conquer.

assume the points in right hat

ust half

P10

P2 P3

P8 | P2 P3

PE

using divide 8 conquer if we find the closest pairs in the reight half of the plain and similarly closest padre in the left half, it may solve the problem. for an example: from reight half => (PyP3) and left half = (Partz). now the lessen of these two will be the answer of we can just divide it recursively and add all the anscoon to get the minimum. However! If you take a book at the pair (Py, Pso) we are ignoring. So the steps will be: Step 1: L -> left half of P (in the example, 1,2,8,7,10) P -> reight half of p(" " " , 3,4,5,9,6) Step 2: find (LIL2) - closest pair in all points of L find (P1,P2) -> " " " " " " " P L1,L2 step 3: 5 = min of d(1,10), d(P1,P2)} step 4: find (M, M2) -> eloseot split pair who intersected in both side (Pn, Py, S) =) the range for off-set is the 5 we calculated

not be closest anyways.

Step 5: return min & d(L, L), d(P, P), d(M, M2)}

Elaborating step 4, find any terminal point closeratto the boundary. (.

here from left side, biggest in value holder $P_{10}(\overline{X})$ will be selected. not with the value of S in S tep 3 the range of S tep 4's search will be (X-S, X+S), Y = SY

Where y is sorted. [this sort can be bypassed if it's sorted at the beginning]. now find the pair

with the smallest distance (Parks) where P1 belongs

forom the left side, Pr belongs from the Right side.

base case can be if the total number of points are a constant small enough just each it bruteforce. (points number <=3)

optimizing step 4 is the key forc better perstormance and (nlogn) solution. It's easier said than done.

Manimum Sub-array Sum!

Sub-array means one continuous paret of an array which is >= 1 of length. &<= length (array) to visudlize the problem:

consider an array of length 3: $\begin{array}{c|c}
0 & 1 & 2 \\
\hline
-2 & 10 & 1
\end{array}$ Sub arrays are \rightarrow [-2], [10], [1], [-2, 10,1] \\
(\int_{\text{out}} \)

man 2 subartray $= 11 \Rightarrow [10, 1]$

SolN => bruteforce

ans = $-\infty$

for (subsize = 1; subsize <=n, subsize++) { for (ind =0; ind <=n; ind++) }

if (ind + sbsize>n) break

sum = 0

for (i= ind; ix statesize + ind); i++) {

sum + = arr [i]

ans = max (ans, sum)

SOIN" -> stig optimized. you can bypass the inner Loop because you don't mid to calculate from screatch forceach subarriay, example: 1 2 3 4 > Subannay sum = 10

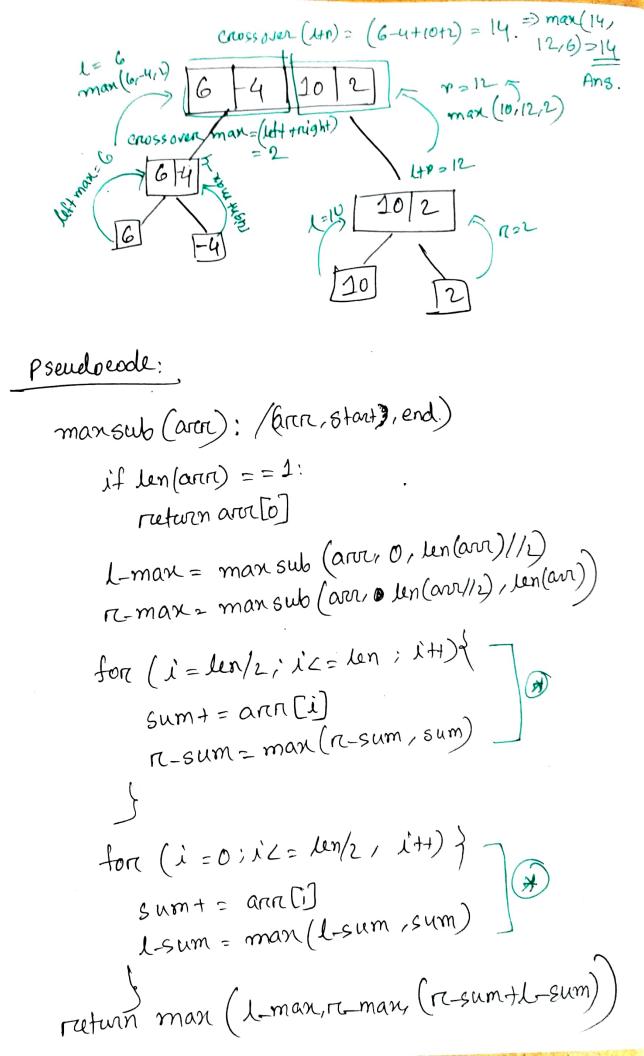
[3 2 3 +4 -> sum of subannay 3+ [4] [1]2) + 3 -> sum of subarray 2+ [3] - 1 u 1 + [2] so, we can go from the bottom to the top and use the smaller subarray sum to ealculate the bigger one. T(n) = O(NL)

Sol^N 3 => divide and conquer

[6 - 4 | 10 | -2]

[man subarray (man from intersect/overflow man subarray)

[from left-half point from right half



D heep in mind, the crossover sum only stores the man Sum it can obtain by going from one half to another It must cross over the mid line ! [you can call it as manimum confinuous sum

Integer multiplication:

rows

let's see the traditional approach.

4567 x 1234 18268 -> (~ 2n operation for each digit 1 3 701 - - of input n; depending how many 9 1 34-- Carry tits are adding) [each row -> 2n~ total > 2n2 (approx.) 5635678

summing all values from top to bottom also takes - 2n2 given forceach digit in additions care performed and manimum n carrry bits can be there; for n digit -> ~2m2.

So, the total time cost/run time forca multiplication 2 ndigit number: O(n) = ~4n2

$$=) T(n) = O(N^2)$$

Divide & Conque Approach: [Karratsuba Multiplication]

@ Observation: y = 12 34

50, $x = 4567 = a \times 100 + b = 745 \times 10 + 67$ $= 2 \times 10^{m/2} + 6$

Similarly, y = C+10 1/2 +d So, $x*y \Rightarrow (a*10^{m/2}+b) \times (c*10^{m/2}+d)$ \Rightarrow $(a*10^{n/2}) \times (e*10^{n/2}) + (ad*10^{n/2}) + (be*10^{n/2}) + bd$ =) [ae] *100/2).2 +[ad+be] *100/2 +[bd] -> Karrat Sulva Equation [now, if we can calculate these 4 multiplications it can be done en divide & conquer since its getting 10 1/2 each time, thus breaking it further will divide itself by another 2, almost like "merge-sorct" fashion. but still, 4 multiplication each level is not the efficient approach. The generalized version of Karatsuba has 3 steps. 1) find lac (1) find bod (11) find (a+b)(c+d) -ac-bd , deraing; astad+bc+bd-ac-bd,) = ad+be; now making it an only 3 multiplication task instead of 4.

if we look at the code,

learnatsuba
$$(n, b)$$
:

if $n < 10$ on $9 < 10$!

| return $n \neq y$

else:

 $n = man - digit(n, y)$
 $h = n//2$
 $a = n//(10^{h})$
 $b = n'/(10^{h})$
 $c = y//(10^{h})$
 $d = y//(10^{h})$

Pseudocede

$$T(n) = 3T(n/2) + O(n)$$

=) $T(n) = O(n \log_{2}^{3}) \Rightarrow O(n^{1.58})$

its a considerable sump-up from the traditional one. In value where n -> x, this will be more efficient.