

# ECAP770

# ADVANCE DATA STRUCTURES

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# Learning Outcomes



After this lecture, you will be able to

- digit folding method / pairing method,
- multiplication Method.

# Hash function

- A hash function is any function that can be used to map a data set of an arbitrary size to a data set of a fixed size, which falls into the hash table.
- The values returned by a hash function are called hash values, hash codes, hash sums, or hashes

# Characteristics of hash function

- **Uniform Distribution** : For distribution throughout the constructed table.
- **Fast** : The generation of hash should be very fast, and should not produce any considerable overhead.
- **Less collisions** : Collisions occur when pairs of elements are mapped to the same hash value. These should be avoided

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# Hash function

- Methods for calculating the hash function
  - Division method
  - Mid square method
  - Digit folding method / pairing method
  - Multiplication Method

# Digit folding method

- The folding method for constructing hash functions begins by dividing the item into equal-size pieces (the last piece may not be of equal size).
- These pieces are then added together to give the resulting hash value.



# Folding method

- Fold shift
- Fold boundary
  - The left and right numbers are folded on fixed boundary between them and the centre.
  - The two outside values are then reversed.

# Digit folding method

- Case 1: if hash table size is 100 (0-99) and sum in 3 digits, then we will ignore last carry, if any.

Or

- Case 2: if hash table size is 100 (0-99) and sum in 3 digits, then we need to perform the extra step of dividing by 100(size of table) and keeping the remainder.

# Folding method: case 1

Key: 122122

Parts: 12 21 22

Sum: 55

Hash value: 55

Index	Actual data
0	
1	
.....	
55	122122
.....	
99	

Hash table

# Folding method: case 2

Key: 234567

Parts: 23 45 67

Sum: 135

Ignore last carry

Hash value: 35

Index	Actual data
0	
1	
.....	
35	234567
.....	
99	

Hash table

# Folding method: case 3

Key: 234567

Parts: 23 45 67

Sum: 135 mod 100 = 35

Sum mod with table size

Hash value: 35

Index	Actual data
0	
1	
.....	
35	234567
.....	
99	

Hash table



# Fold boundary: case 1

Key: 142123

Parts: 14 21 23

41 21 32

Sum: 94

Hash value: 94

Index	Actual data
0	
1	
.....	
94	142123
.....	
99	

Hash table

# Fold boundary: case 2

Key: 354027

Parts: 35 40 27

53 40 72 value reversed

Sum: 165

Ignore last carry

Hash value: 65

Index	Actual data
0	
1	
.....	
65	354027
.....	
99	

Hash table

# Multiplication Method

$$h(\text{key}) = \text{floor}(\text{table size} * (\text{key} * A)) \% \text{size}$$

Or

$$h(k) = \text{floor}(n( kA \bmod 1 ))$$

- $K = \text{key}$
- $A$  is constant value between 0 and 1
- Knuth recommends  $A = 0.6180339887\dots$  (Golden Ratio)

# Multiplication Method

- 1) Choose constant
- 2) Multiply key  $k$  by  $A$
- 3) Extract fractional part of  $kA$  (this gives us a number between 0 and 1)
- 4) Multiply fractional part by  $m$  and take floor of the multiplication (this transforms a number between 0 and 1, to a discrete number between 0 and  $m-1$  that we can map to slot in the hash table)

# Example: Multiplication Method

$k=34$

Size of table = 100

$A=0.618033$

$h(34) = \text{floor}(100(34 * 0.618033)) \% 100$

$= \text{floor}(3461.80) \% 100$

$= 3461 \% 100$

$= 61$

Index	Actual data
0	
1	
....	
61	34
....	
99	

Hash table





That's all for now...