



# EPEA516

## ANALYTICAL SKILLS II

Dr. Harish Mittu  
Associate Professor

# Learning Outcomes



After this lecture, you will be able to

- solve different problems based on series completion.

# Problem 1

- Insert the missing number in the following series:

5, 8, 12, 17, 23, ....., 38

- $T_2 - T_1 = 8 - 5 = 3$
- $T_3 - T_2 = 12 - 8 = 4$
- $T_4 - T_3 = 17 - 12 = 5$
- $T_5 - T_4 = 23 - 17 = 6$
- $T_6 - T_5 = X - 23 = 7$
- $T_7 - T_6 = 38 - X = 8$

# Problem 1

- Insert the missing number in the following series:

5, 8, 12, 17, 23,....., 38

- $T_2 - T_1 = 8 - 5 = 3$ ;  $T_3 - T_2 = 12 - 8 = 4$ ;  $T_4 - T_3 = 17 - 12 = 5$
- $T_5 - T_4 = 23 - 17 = 6$ ;  $T_6 - T_5 = X - 23 = 7$ ;  $T_7 - T_6 = 38 - X = 8$
- $30 - 23 = 7$  and  $38 - 30 = 8$
- X or missing number = 30
- 5, 8, 12, 17, 23, **30**, 38

## Problem 2

- Insert the missing number in the given series:

4, 9, 20, 43, 90,    ?

- $T_2 = 9 = \underline{2} \times 4 + \underline{1}$
- $T_3 = 20 = \underline{2} \times 9 + \underline{2}$
- $T_4 = 43 = \underline{2} \times 20 + \underline{3}$
- $T_5 = 90 = \underline{2} \times 43 + \underline{4}$
- $T_6 = 2 \times 90 + 5 = 185$
- 4, 9, 20, 43, 90, **185**



# Problem 3

- Insert the missing number in the given series:

1, 1, 4, 8, 9, 27, 16, ?

- First Series – 1, 4, 9, 16, .....

or  $1^2, 2^2, 3^2, 4^2, \dots$

- Second Series – 1, 8, 27, .....

or  $1^3, 2^3, 3^3, \dots$

or  $1^3, 2^3, 3^3, 4^3, \dots$

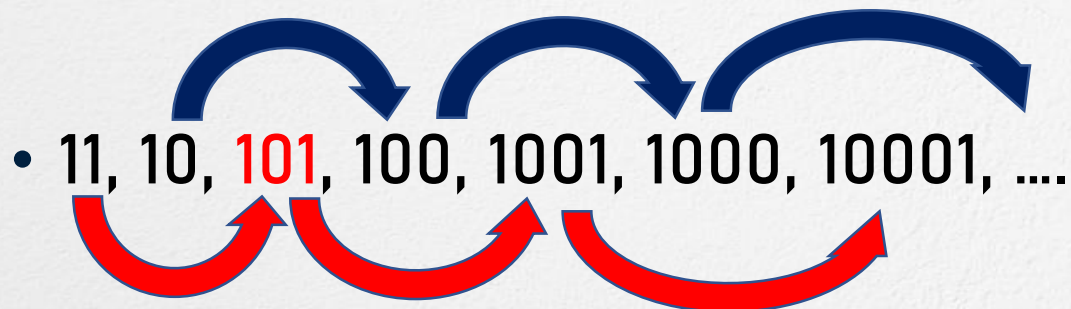
- Missing Number = 64

# Problem 4

- Fill in the missing number in the following series:

11, 10, ?, 100, 1001, 1000, 10001, ....

- $T_2 = 10, T_4 = 100, T_6 = 1000, \dots$
- $T_1 = 11, T_3 = ?, T_5 = 1001, T_7 = 10001, \dots$
- $T_3 = 101$



# Problem 5

- Find the fifth term in the following series:

99, 95, 86, 70,.....?

- $T_2 - T_1 = 95 - 99 = -4 = -2^2$
- $T_3 - T_2 = 86 - 95 = -9 = -3^2$
- $T_4 - T_3 = 70 - 86 = -16 = -4^2$
- $T_5 - T_4 = X - 70 = -25 = -5^2$
- $T_5 = X = 70 - 25 = 45$
- 99, 95, 86, 70, 45



# Problem 5

- Find the number corresponding to question mark in the following series:

0, 3, 12, 30, ?, 105, 168

- $T_2 - T_1 = 3 - 0 = 3$
- $T_3 - T_2 = 12 - 3 = 9$
- $T_4 - T_3 = 30 - 12 = 18$
- $T_5 - T_4 = X - 30 = ?$
- $T_6 - T_5 = 105 - X = ?$
- $T_7 - T_6 = 168 - 105 = 63$

# Problem 5

$$\begin{array}{ccccccc} 0, & 3, & 12, & 30, & X, & 105, & 168 \\ \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \\ 3 & 9 & 18 & X - 30 & 105 - X & 63 \end{array}$$

- $a_2 - a_1 = 9 - 3 = 6$
- $a_3 - a_2 = 18 - 9 = 9$
- $a_4 - a_3 = X - 30 - 18 = X - 48$
- $a_5 - a_4 = 105 - X - (X - 30) = 135 - 2X$
- $a_6 - a_5 = 63 - (105 - X) = X - 42$

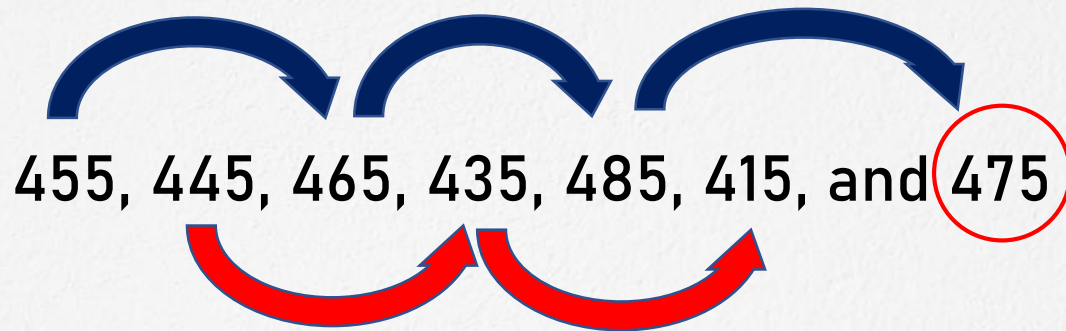
# Problem 5

$$\begin{array}{ccccccc} 0, & 3, & 12, & 30, & X, & 105, & 168 \\ \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \underbrace{\quad} & \\ 3 & 9 & 18 & X - 30 & 105 - X & 63 & \end{array}$$

- $a_2 - a_1 = 9 - 3 = 6; a_3 - a_2 = 18 - 9 = 9$
- $a_4 - a_3 = X - 30 - 18 = X - 48;$
- $a_5 - a_4 = 105 - X - (X - 30) = 135 - 2X$
- $a_6 - a_5 = 63 - (105 - X) = X - 42$
- $X = 60$
- $3, 9, 60 - 48 = 12, 135 - 2 \times 60 = 15, \text{ and } 60 - 42 = 18$

# Problem 6

- Find out the wrong number in the following series:



- 455, 465, 485, and 475
- $465 - 455 = 10$ ;  $485 - 465 = 20$ ; and  $475 - 485 = -10$
- 445, 435, and 415
- $435 - 445 = -10$ ; and  $415 - 435 = -20$
- Correct number =  $485 + 30 = 515$



# Problem 7

- Find out the wrong number in the following series:

1, 5, 11, 19, 29, and 55

- $5 - 1 = 4$
- $11 - 5 = 6$
- $19 - 11 = 8$
- $29 - 19 = 10$
- $55 - 29 = 26$
- Correct number =  $29 + 12 = 41$



# Problem 8

- Find out the wrong number in the following series:

2, 4, 4, 16, 8, 256, and 64

- 2, 4, 8, and 64
- $2^1, 2^2, 2^3$ , and  $2^6$
- 4, 16, and 256
- $2^2, 2^4$ , and  $2^8$
- Correct number =  $2^4 = 16$

# Problem 9

- In the following questions a number series is given. After the series a number is given followed by a, b, c, d and e. Complete the series starting with the number given following the sequence of the given series.

1, 9, 65, 393

2, a, b, c, d, e

- $9 = 1 \times 8 + 1$
- $65 = 9 \times 7 + 2$
- $393 = 65 \times 6 + 3$

# Problem 9

- 1, 9, 65, 393
- 2, a, b, c, d, e
- $9 = 1 \times 8 + 1; 65 = 9 \times 7 + 2; 393 = 65 \times 6 + 3$
- $a = 2 \times 8 + 1 = 17$
- $b = 17 \times 7 + 2 = 121$
- $c = 121 \times 6 + 3 = 729$
- $d = 729 \times 5 + 4 = 3649$
- $e = 3649 \times 4 + 5 = 14601$

# Problem 10

- Find out the wrong number in the following series:

3, 10, 24, 54, 108, 220, and 444

- $10 = 2 \times 3 + 4$

- $24 = 2 \times 10 + 4$

- $54 = 2 \times 24 + 6$

- $108 = 2 \times 54 + 0$

- $220 = 2 \times 108 + 4$

- $444 = 2 \times 220 + 4$

- Correct number  $52 = 2 \times 24 + 4$  and  $108 = 2 \times 52 + 4$

# Conclusion

- Pattern - Series
- Missing Number/Wrong Number
- Complete/Correct Series



# Summary

- Problems - Series Completion

**That's all for now...**