

ECAP770

ADVANCE DATA STRUCTURES

Ashwani Kumar
Assistant Professor

Learning Outcomes



After this lecture, you will be able to

- digit folding method / pairing method,
- multiplication Method.

Hash function

- A hash function is any function that can be used to map a data set of an arbitrary size to a data set of a fixed size, which falls into the hash table.
- The values returned by a hash function are called hash values, hash codes, hash sums, or hashes

Characteristics of hash function

- Uniform Distribution : For distribution throughout the constructed table.
- Fast : The generation of hash should be very fast, and should not produce any considerable overhead.
- Less collisions : Collisions occur when pairs of elements are mapped to the same hash value. These should be avoided

Characteristics of hash function

- Uniform Distribution : For distribution throughout the constructed table.
- Fast : The generation of hash should be very fast, and should not produce any considerable overhead.
- Less collisions : Collisions occur when pairs of elements are mapped to the same hash value. These should be avoided

Characteristics of hash function

- Uniform Distribution : For distribution throughout the constructed table.
- Fast : The generation of hash should be very fast, and should not produce any considerable overhead.
- Less collisions : Collisions occur when pairs of elements are mapped to the same hash value.
These should be avoided

Hash function

- Methods for calculating the hash function
 - Division method
 - Mid square method
 - Digit folding method / pairing method
 - Multiplication Method

Digit folding method

- The folding method for constructing hash functions begins by dividing the item into equal-size pieces (the last piece may not be of equal size).
- These pieces are then added together to give the resulting hash value.

Folding method

- Fold shift
- Fold boundary
 - The left and right numbers are folded on fixed boundary between them and the centre.
 - The two outside values are then reversed.

Digit folding method

- Case 1: if hash table size is 100 (0-99) and sum in 3 digits, then we will ignore last carry, if any.

Or

- Case 2: if hash table size is 100 (0-99) and sum in 3 digits, then we need to perform the extra step of dividing by 100(size of table) and keeping the remainder.

Folding method: case 1

Key: 122122

Parts: 12 21 22

Sum: 55

Hash value: 55

Index	Actual data
0	
1	
....	
55	122122
....	
99	

Hash table

Folding method: case 2

Key: 234567

Parts: 23 45 67

Sum: 135

Ignore last carry

Hash value: 35

Index	Actual data
0	
1	
...	
35	234567
...	
99	

Hash table

Folding method: case 3

Key: 234567

Parts: 23 45 67

Sum: 135 mod 100 = 35

Sum mod with table size

Hash value: 35

Index	Actual data
0	
1	
...	
35	234567
...	
99	

Hash table

Fold boundary: case 1

Key: 142123

Parts: 14 21 23

41 21 32

Sum: 94

Hash value: 94

Index	Actual data
0	
1	
....	
94	142123
....	
99	

Hash table

Fold boundary: case 2

Key: 354027

Parts: 35 40 27

53 40 72 value reversed

Sum: 165

Ignore last carry

Hash value: 65

Index	Actual data
0	
1	
...	
65	354027
...	
99	

Hash table

Multiplication Method

$$h(\text{key}) = \text{floor}(\text{table size} * (\text{key} * A)) \% \text{size}$$

Or

$$h(k) = \text{floor}(n(kA \bmod 1))$$

- K= key
- A is constant value between 0 and 1
- Knuth recommends A = 0.6180339887... (Golden Ratio)

Multiplication Method

- 1) Choose constant
- 2) Multiply key k by A
- 3) Extract fractional part of $k A$ (this gives us a number between 0 and 1)
- 4) Multiply fractional part by m and take floor of the multiplication (this transforms a number between 0 and 1, to a discrete number between 0 and $m-1$ that we can map to slot in the hash table)

Example: Multiplication Method

$k=34$

Size of table = 100

$A=0.618033$

$$h(34) = \text{floor} (100(34 * 0.618033)) \% 100$$

$$=\text{floor} (3461.80) \% 100$$

$$=3461 \% 100$$

$$=61$$

Index	Actual data
0	
1	
.....	
61	
34	
.....	
99	

Hash table

That's all for now...