



# **Formal Methods for Multi-agent Systems**

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# Introduction and motivation

## **Challenge:**

In complex environments how to ensure that agents will behave as we expect them to, or at least will not behave in unacceptable or undesirable ways?

## **Possible answer:**

High level abstractions that can lead to simpler techniques for design and development.

# Introduction and motivation

## Formal methods help

- In understanding of system design at a level higher than a specific implementation
- To debug specifications and validate system implementations
- In the long run, in helping developing a clearer understanding of problems and solutions

# Theoretical background

# Predicate and Modal Logic

## Predicate logic

- Atomic propositions
- Connectives:  $\wedge$ ,  $\vee$ ,  $\neg$ ,  $\rightarrow$

## Modal logic

- $\Box$  – necessity operator
- $\Diamond$  – possibility operator
- Sets of possible worlds with accessibility relation

# Dynamic and Temporal Logic

## **Dynamic logic (modal logic of action)**

- Adds different kinds of actions
- Necessity and possibility are based upon different types of actions available

## **Temporal logic (Logic of time)**

- Linear vs. Branching
- Discrete vs. Dense
- Moment-based vs. Period-based

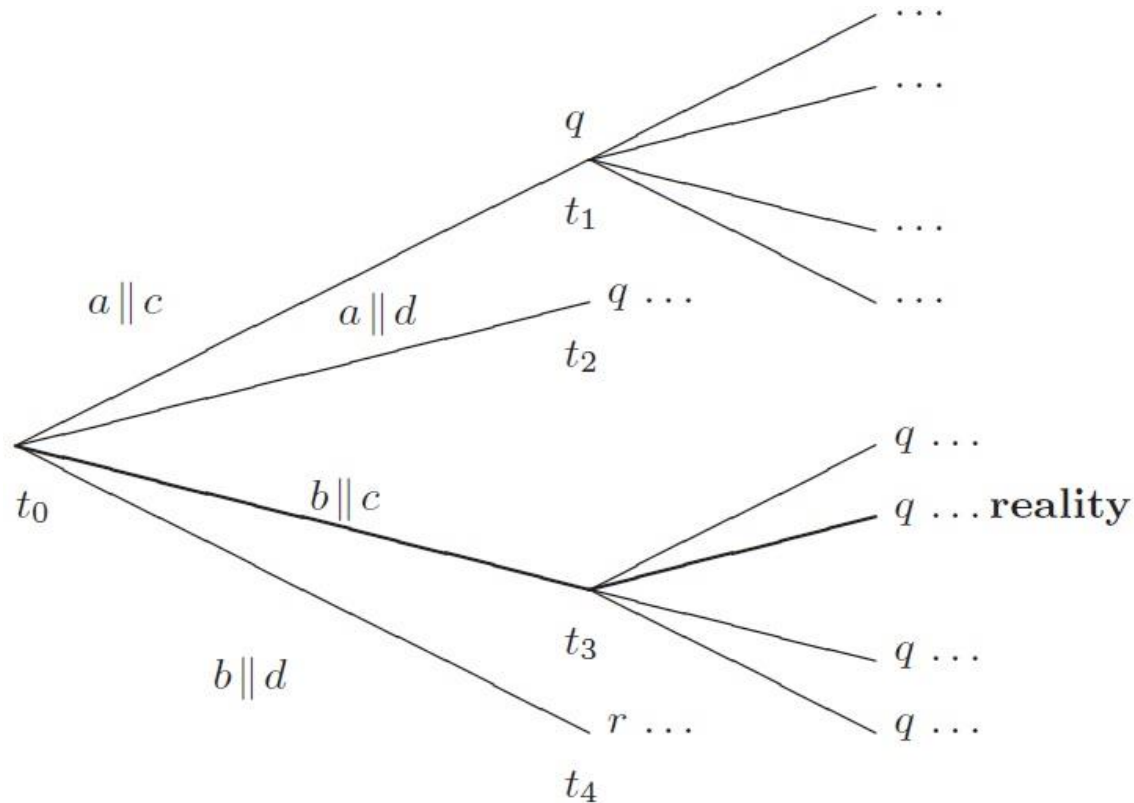
# Linear Temporal Logic

## Linear temporal logic

- $p \cup q$  – true at moment  $t$  iff  $q$  holds at future moment and  $p$  holds on all moments between  $t$  and selected occurrence of  $q$ .
- $Fp$  –  $p$  holds sometimes in the future on a given path
- $Gp$  –  $p$  always holds in the future on a given path
- $Xp$  –  $p$  holds in the next moment
- $Pq$  –  $q$  held in a past moment



# Branching Temporal Logic



# Branching Temporal and Action Logic

Branching-time temporal and action language

- $Ap$  –  $p$  holds in all paths at the present moment
- $Ep$  –  $p$  holds in some path at the present moment
- $Rp$  –  $p$  holds in the real path at the present moment

# Formal methods for a single agent

# The BDI Model

Formalizing agent's cognitive specifications:

- *Bel* – belief
- *Des* – desire (goal if achievable and consistent)
- *K<sub>h</sub>* – know-how
- *Int* – intention

Example:

$DesAFwin \wedge IntEFbuy \wedge \neg BelAFwin$

# Constraints for Intentions

1. Satisfiability

$$xIntp \rightarrow EFp$$

2. Temporal Consistency

$$(xIntp \wedge xIntq) \rightarrow xInt(Fp \wedge Fq)$$

3. Persistence does not entail success

$$EG((xIntp) \wedge \neg p) \text{ is satisfiable}$$

4. Persist while succeeding

# Abstract Architecture

Inputs to the system

- Events are received via an event queue
- Events of two kinds
  - External (environmental)
  - Internal

Outputs from the system

- Atomic actions performed by `execute()` function

# Abstract BDI Interpreter

## **BDI-interpreter**

initialize-state();

**do**

options := option-generator(event-queue,B,G,I);

selected-options := deliberate(options,B,G,I);

update-intentions(selected-options,I);

execute(I);

get-new-external-events();

drop-successful-attitudes(B,G,I);

drop-impossible-attitudes(B,G,I);

**until** quit.

# Plans

(a)

**Type:** drink-soda

**Invocation:**

g-add(quenched-thirst)

**Precondition:** have-glass

**Add List:** {quenched-thirst}

**Body:**

①

have-soda

②

drink

③

(b)

**Type:** drink-water

**Invocation:**

g-add(quenched-thirst)

**Precondition:** have-glass

**Add List:** {quenched-thirst}

**Body:**

①

open-tap

②

drink

③

(c)

**Type:** get-soda

**Invocation:**

g-add(have-soda)

**Precondition:** true

**Add List:** {have-soda}

**Body:**

①

open-fridge

②

get-soda

③



# Generate Options

```
option-generator(trigger-events)
options := {};
for trigger-event  $\in$  trigger-events do
  for plan  $\in$  plan-library do
    if matches(invocation(plan), trigger-event) then
      if provable(precondition(plan), B) then
        options := options  $\cup$  {plan};
return(options).
```

# Deliberate options

```
deliberate(options)
if length(options) ≤ 1 then return(options);
else metalevel-options := option-generator(b-add(option-set(options)));
    selected-options := deliberate(metalevel-options);
    if null(selected-options) then
        return(random-choice(options));
else return(selected-options).
```

# Example trace

Bel	Goal	Int	<i>done</i>	<i>succeeded</i>
glass	—	—	—	—
unchanged	quench	—	—	g-add(quench)
unchanged	unchanged	{ soda; drink}	—	g-add(soda)
$\neg$ remove-soda	unchanged	—	fridge	fridge, g-add(quench)
unchanged	unchanged	{ drink}	tap	tap
quench	—	—	drink	drink

# Formal methods for multiple agents

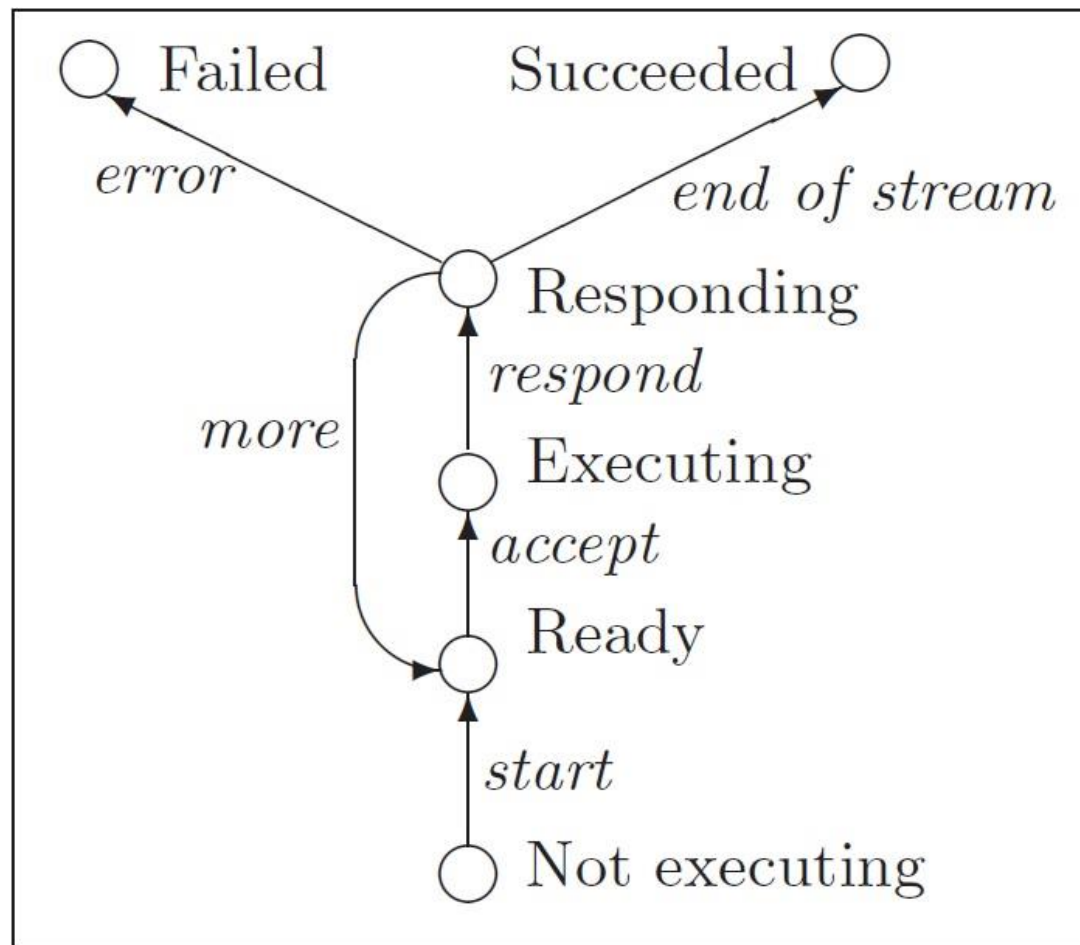
# Coordination Architecture

Agents are represented as small “skeletons”, which include only events significant for coordination

Event classes:

- Flexible – may be delayed or omitted
- Inevitable – may be delayed
- Immediate
- Triggerable – based on external request

# Agent Skeleton – Example



# Specification language

Linear-time language with restrictions

- $\cdot$  – “before” temporal operator
- $\odot$  – concatenation of two traces first of which is finite



# Coordination Relationships

	Name	Description	Formal notation
R1	$e$ is required by $f$	If $f$ occurs, $e$ must occur before or after $f$	$e \vee \bar{f}$
R2	$e$ disables $f$	If $e$ occurs, then $f$ must occur before $e$	$\bar{e} \vee \bar{f} \vee f \cdot e$
R3	$e$ feeds or enables $f$	$f$ requires $e$ to occur before	$e \cdot f \vee \bar{f}$
R4	$e$ conditionally feeds $f$	If $e$ occurs, it feeds $f$	$\bar{e} \vee e \cdot f \vee \bar{f}$
R5	Guaranteeing $e$ enables $f$	$f$ can occur only if $e$ has occurred or will occur	$e \wedge f \vee \bar{e} \wedge \bar{f}$
R6	$e$ initiates $f$	$f$ occurs iff $e$ precedes it	$\bar{e} \wedge \bar{f} \vee e \cdot f$
R7	$e$ and $f$ jointly require $g$	If $e$ and $f$ occur in any order, then $g$ must also occur (in any order)	$\bar{e} \vee \bar{f} \vee g$
R8	$g$ compensates for $e$ failing $f$	if $e$ happens and $f$ does not, then perform $g$	$(\bar{e} \vee f \vee g) \wedge (\bar{g} \vee e) \wedge (\bar{g} \vee \bar{f})$



# Summary

- Formal methods helps in understanding the design and used for validation purposes
- Different types of logics are being used in formal methods
- BDI concept is used to represent agent's logical structure
- In multi-agent systems “agent skeleton” concept is used for coordination

# Questions?