

# PlaNet

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Learning Latent Dynamics  
for Planning from Pixels

# PlaNet Deep Planning Network

- Scalable Model-based RL
- Efficient planning in **latent space** with large batch size
- Reaches top performance using 200X fewer episodes

# PlaNet Deep Planning Network

## ■ Recurrent State Space Model (RSSM)

Deterministic & Stochastic Components

## ■ Latent Overshooting

Latent Space Result로 Latent Sequence Model을 굴리는게 장기예측에 적합

# **Recurrent State Space Model**

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# Recurrent State Space Model (RSSM)

보이는게 State의 전부가 아닐 수 있다. (Non-Marcov)

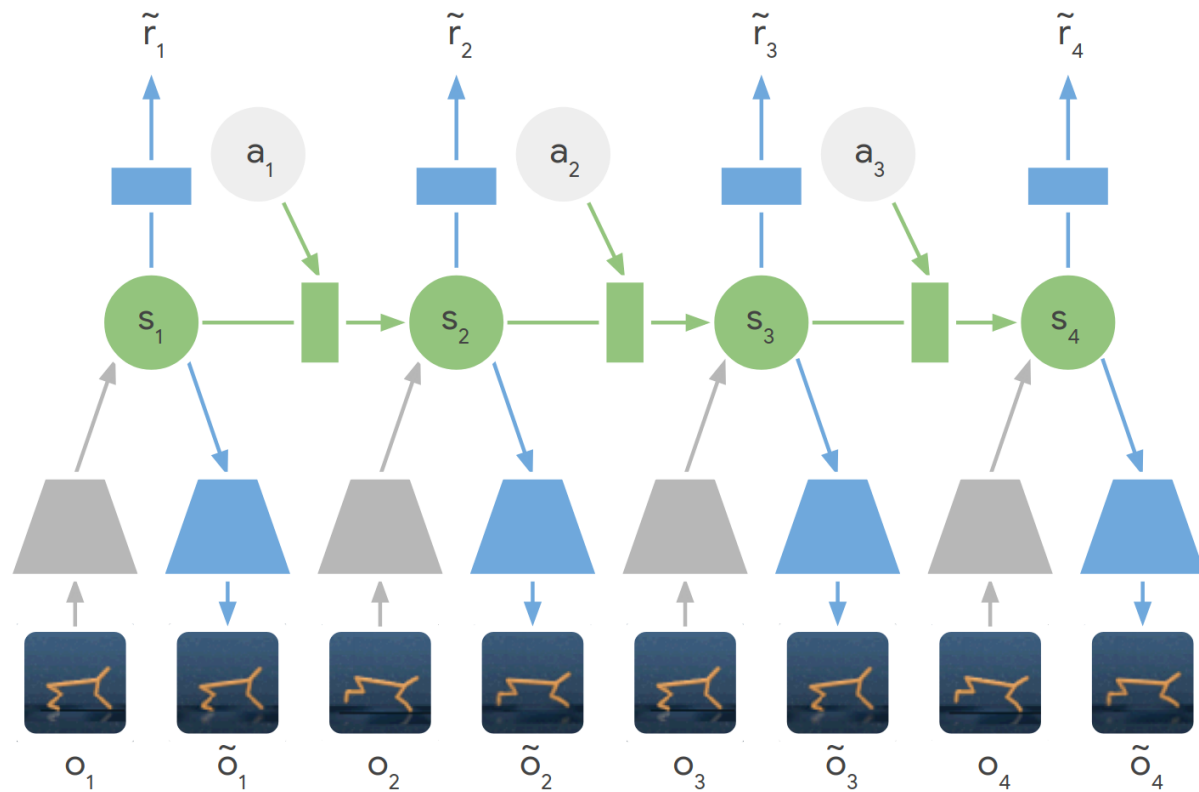
Partially Observable Markov Decision Process를 Markov Decision Process로 바꾸는 기법



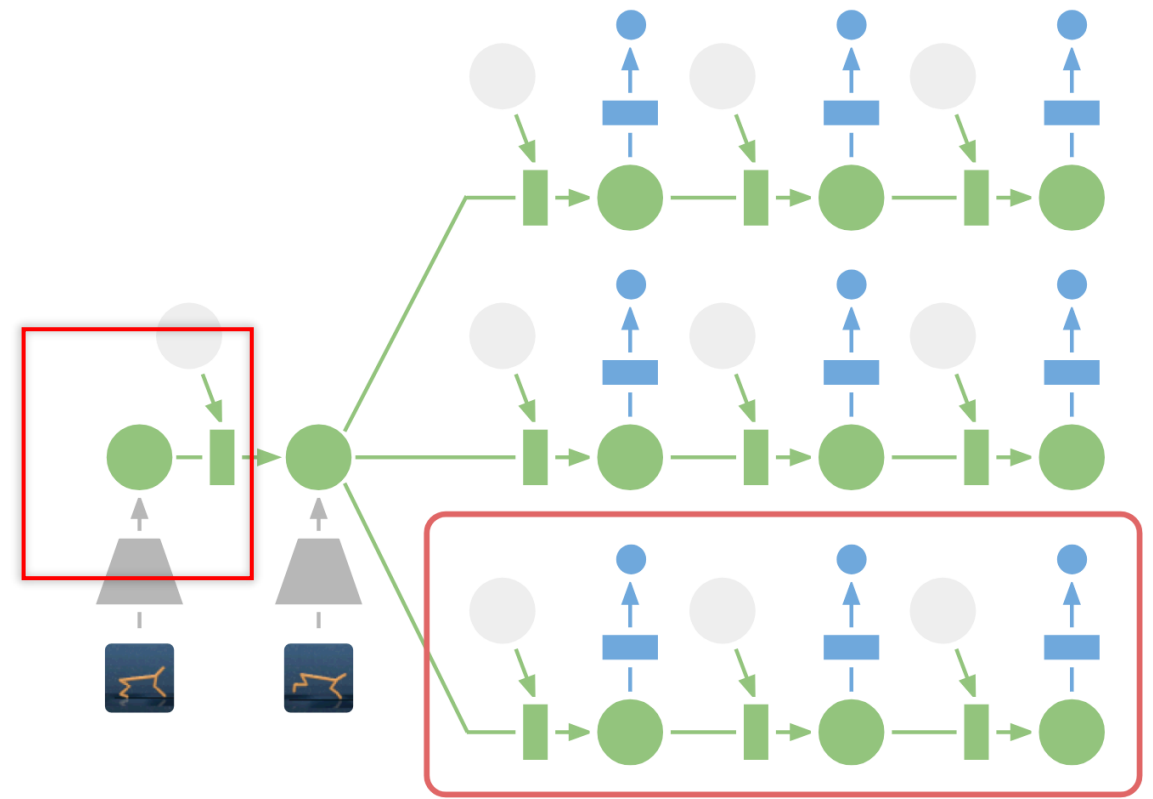
DQN에서는 비슷하게 이미지 네 장을 묶어 하나의 State로 취급하는 것과 유사하게 (Non-Marcov를 Markov하게 바꾸는 기법으로 제시하는 것이다.

# Recurrent State Space Model (RSSM)

Learned Latent Dynamics Model

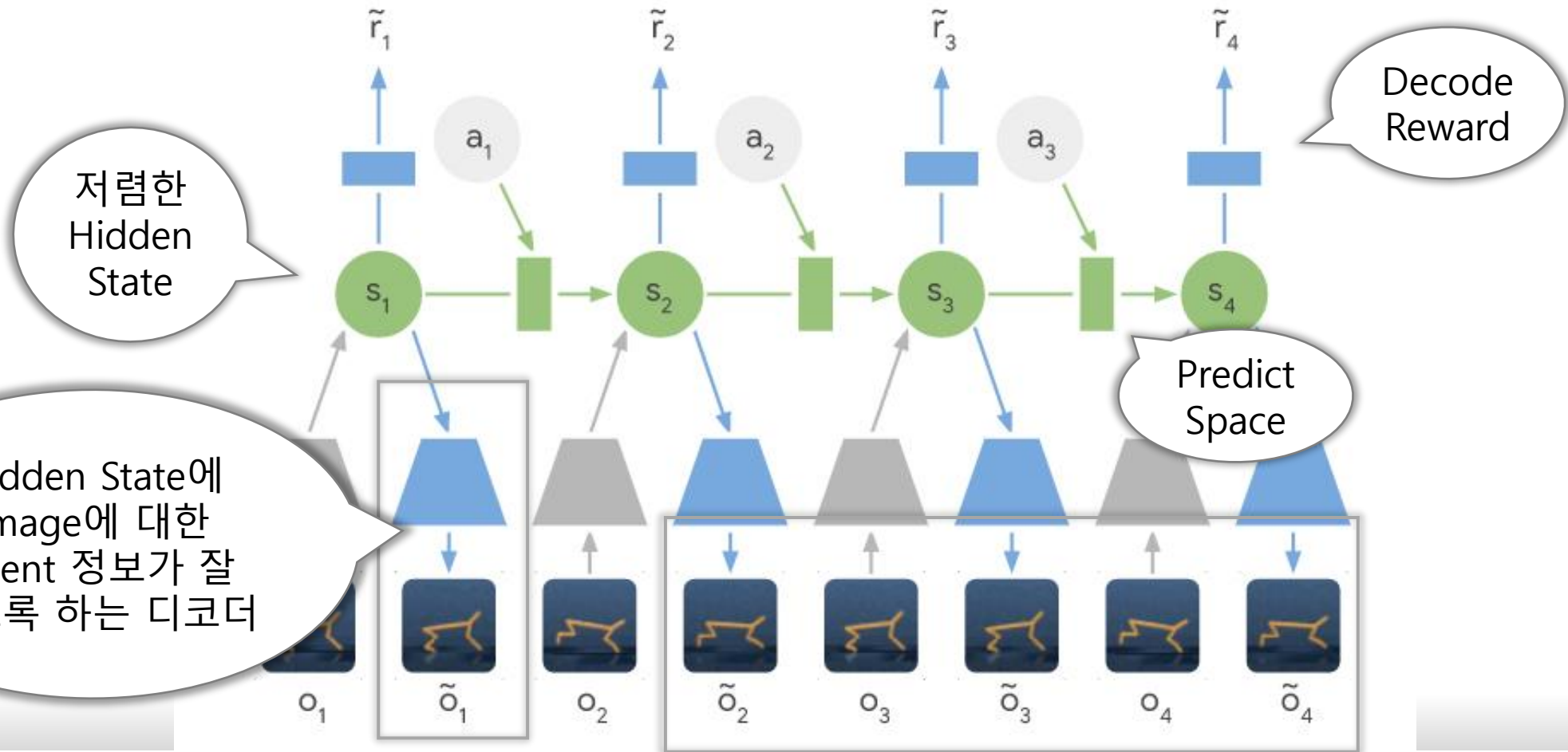


Planning in Latent Space



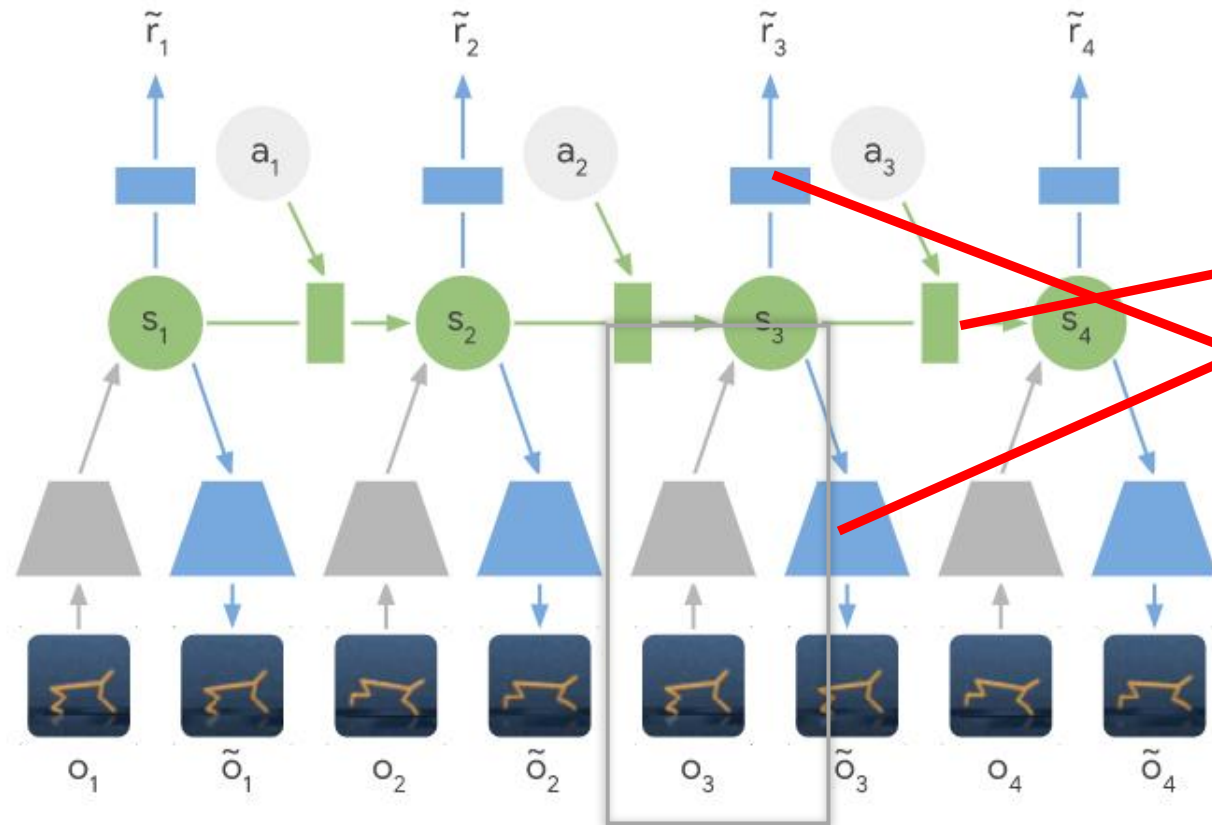
# Recurrent State Space Model (RSSM)

## ■ Learned Latent Dynamics Model



# Recurrent State Space Model (RSSM)

## ■ Learned Latent Dynamics Model



Transition function:

$$s_t \sim p(s_t | s_{t-1}, a_{t-1})$$

Observation function:

$$o_t \sim p(o_t | s_t) \quad (1)$$

Reward function:

$$r_t \sim p(r_t | s_t)$$

Policy:

$$a_t \sim p(a_t | o_{\leq t}, a_{< t}),$$

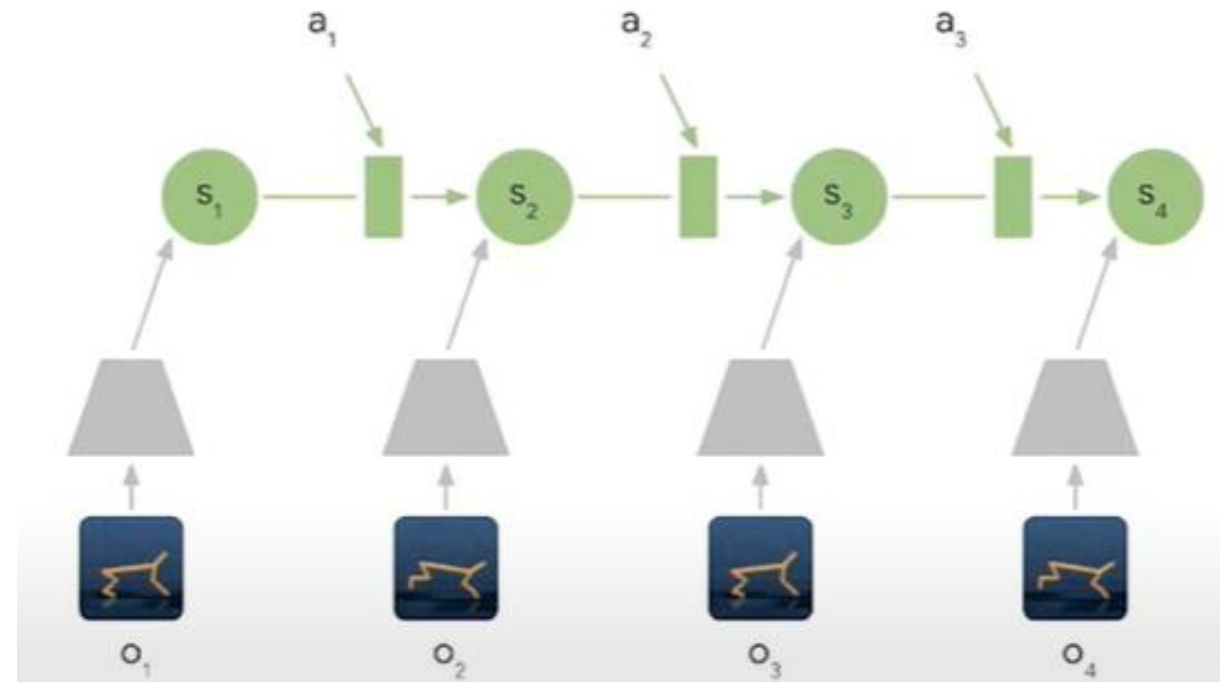
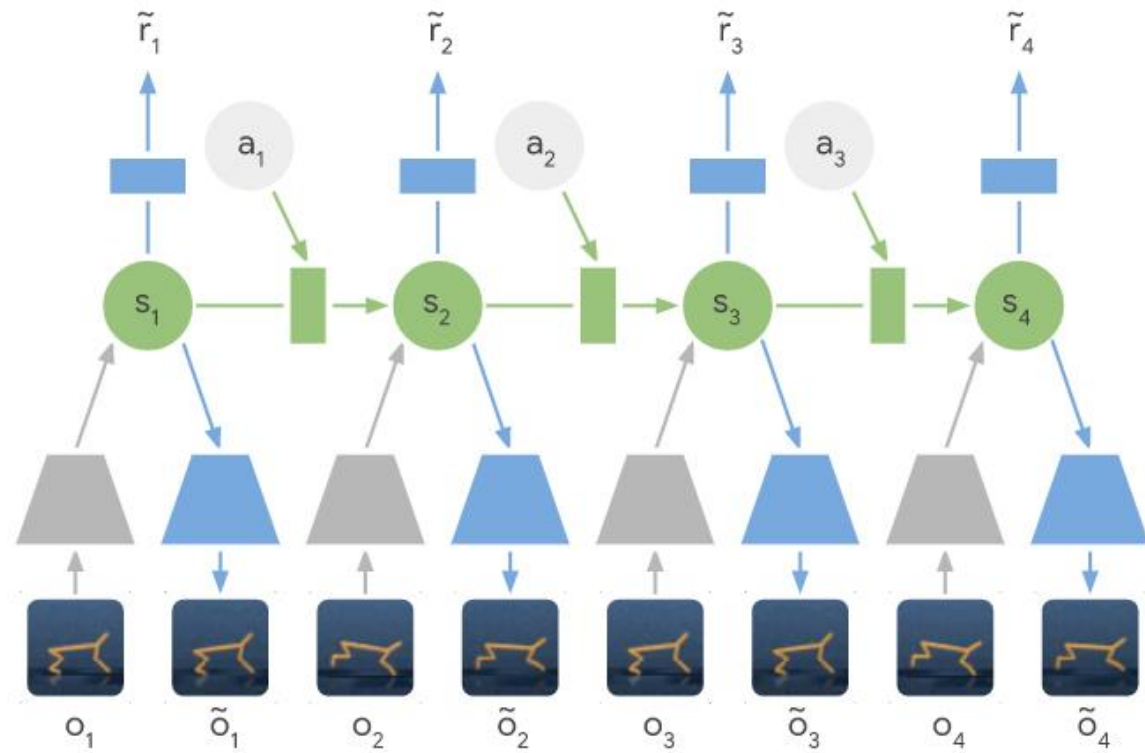
Policy는?

Model-free처럼 Policy Net을 사용하는 게 아니고  
굴려온 RNN이용해서 그때그때 **Planning**한다.

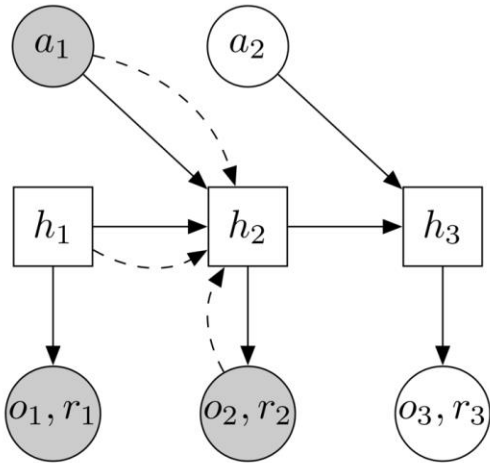


# Recurrent State Space Model (RSSM)

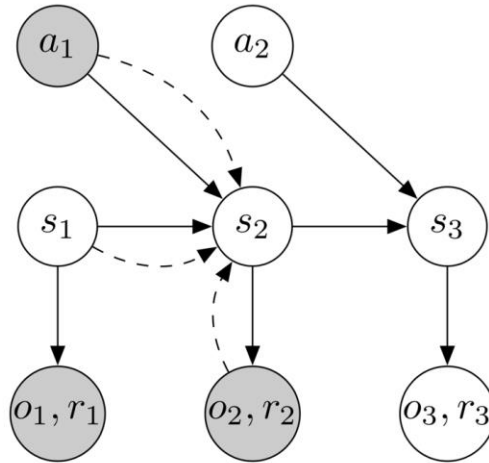
## ■ Learned Latent Dynamics Model



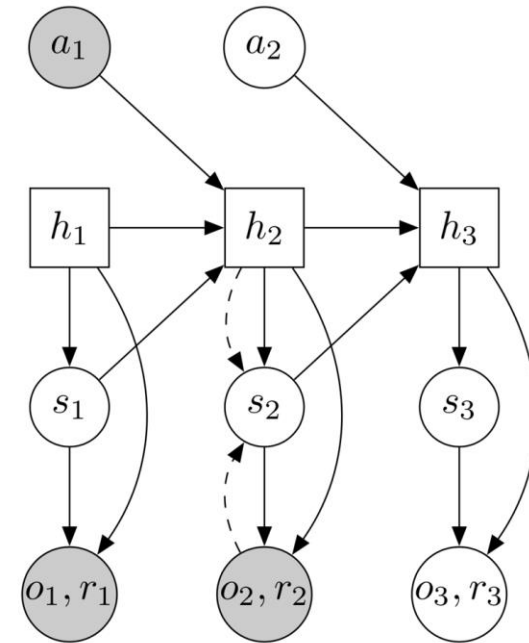
# Recurrent State Space Model (RSSM)



(a) Deterministic model (RNN)



(b) Stochastic model (SSM)



(c) Recurrent state-space model (RSSM)

# Recurrent State Space Model (RSSM)

RSSM에서 State는 Deterministic & Stochastic Components 으로 이루어져 있다.

## Deterministic Components

Discrete Time step  
Hidden states  
Image observations  
Continuous action vectors  
Scalar rewards

$t$   
 $s_t$   
 $o_t$   
 $a_t$   
 $r_t$

## Stochastic Components

Transition function:

$$s_t \sim p(s_t \mid s_{t-1}, a_{t-1})$$

Observation function:

$$o_t \sim p(o_t \mid s_t) \quad (1)$$

Reward function:

$$r_t \sim p(r_t \mid s_t)$$

Policy:

$$a_t \sim p(a_t \mid o_{\leq t}, a_{< t}),$$

# Recurrent State Space Model (RSSM)

## Motivation

### Deterministic

Stochastic transitions make it difficult for the transition model to reliably remember information for multiple time steps.

### Stochastic

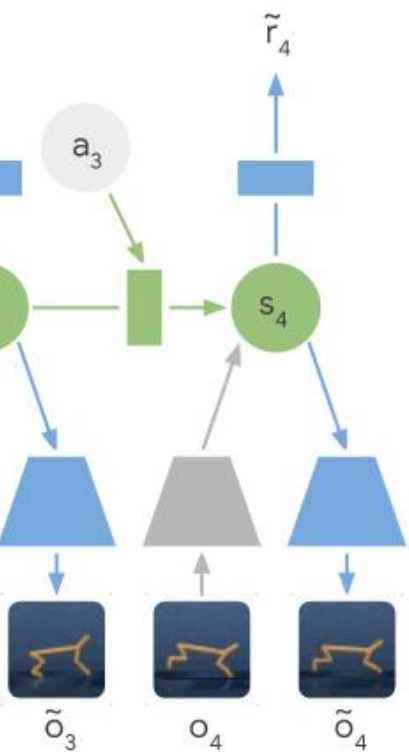
Split the state into stochastic and deterministic parts, allowing the model to robustly learn to predict multiple futures.

## Detail

All information about the observations must pass through the sampling step of the encoder to avoid a deterministic shortcut from inputs to reconstructions.

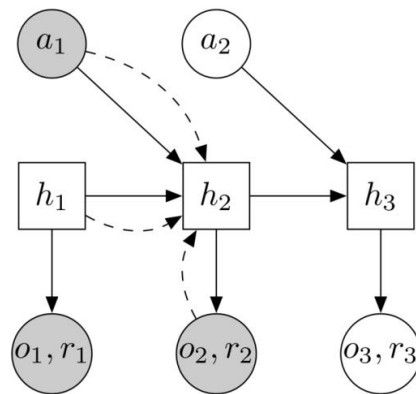
# Latent Dynamics (PlaNet, Deep Planning Network)

## ■ Recurrent State Space Model (RSSM)

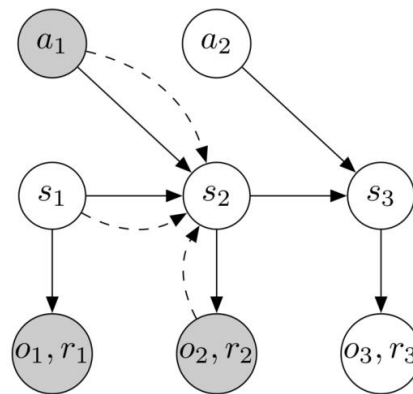


Transition function:  
 Observation function:  
 Reward function:  
 Policy:

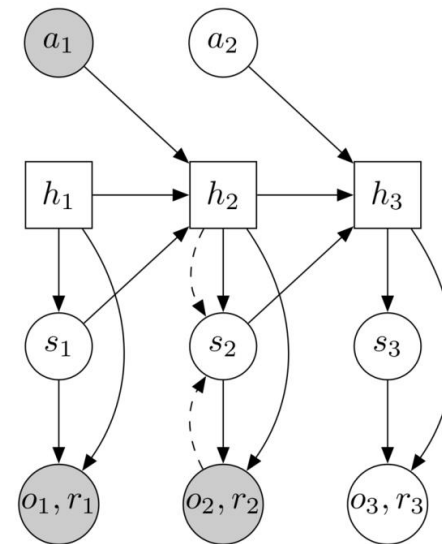
$$\begin{aligned}
 s_t &\sim p(s_t \mid s_{t-1}, a_{t-1}) \\
 o_t &\sim p(o_t \mid s_t) \\
 r_t &\sim p(r_t \mid s_t) \\
 a_t &\sim p(a_t \mid o_{\leq t}, a_{< t}),
 \end{aligned} \tag{1}$$



(a) Deterministic model (RNN)



(b) Stochastic model (SSM)



(c) Recurrent state-space model (RSSM)

Deterministic state model:

Stochastic state model:

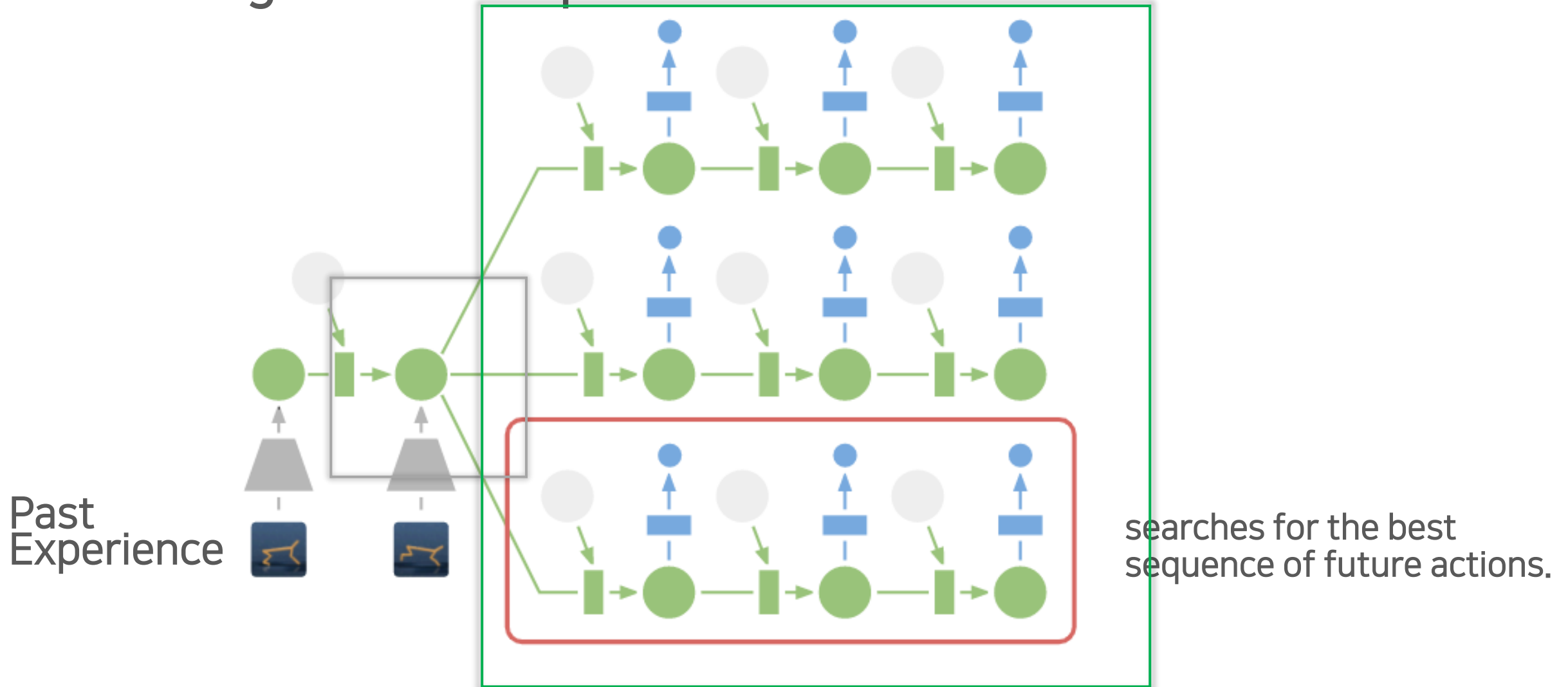
Observation model:

Reward model:

$$\begin{aligned}
 h_t &= f(h_{t-1}, s_{t-1}, a_{t-1}) \\
 s_t &\sim p(s_t \mid h_t) \\
 o_t &\sim p(o_t \mid h_t, s_t) \\
 r_t &\sim p(r_t \mid h_t, s_t),
 \end{aligned} \tag{4}$$

# Latent Dynamics (PlaNet, Deep Planning Network)

## ■ Planning in Latent Space



# Latent Dynamics (PlaNet, Deep Planning Network)

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**Algorithm 1: Deep Planning Network (PlaNet)**

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**Input :**

|          |                  |                                |                   |
|----------|------------------|--------------------------------|-------------------|
| $R$      | Action repeat    | $p(s_t   s_{t-1}, a_{t-1})$    | Transition model  |
| $S$      | Seed episodes    | $p(o_t   s_t)$                 | Observation model |
| $C$      | Collect interval | $p(r_t   s_t)$                 | Reward model      |
| $B$      | Batch size       | $q(s_t   o_{\leq t}, a_{< t})$ | Encoder           |
| $L$      | Chunk length     | $p(\epsilon)$                  | Exploration noise |
| $\alpha$ | Learning rate    |                                |                   |

```
1 Initialize dataset  $\mathcal{D}$  with  $S$  random seed episodes.
2 Initialize model parameters  $\theta$  randomly.
3 while not converged do
    // Model fitting
4   for update step  $s = 1..C$  do
5     Draw sequence chunks  $\{(o_t, a_t, r_t)_{t=k}^{L+k}\}_{i=1}^B \sim \mathcal{D}$ 
      uniformly at random from the dataset.
6     Compute loss  $\mathcal{L}(\theta)$  from Equation 8.
7     Update model parameters  $\theta \leftarrow \theta - \alpha \nabla_{\theta} \mathcal{L}(\theta)$ .

    // Data collection
8    $o_1 \leftarrow \text{env.reset}()$ 
9   for time step  $t = 1..\lceil \frac{T}{R} \rceil$  do
10    Infer belief over current state  $q(s_t | o_{\leq t}, a_{< t})$  from
      the history.
11     $a_t \leftarrow \text{planner}(q(s_t | o_{\leq t}, a_{< t}), p)$ , see
      Algorithm 2 in the appendix for details.
12    Add exploration noise  $\epsilon \sim p(\epsilon)$  to the action.
13    for action repeat  $k = 1..R$  do
14       $r_t^k, o_{t+1}^k \leftarrow \text{env.step}(a_t)$ 
15       $r_t, o_{t+1} \leftarrow \sum_{k=1}^R r_t^k, o_{t+1}^k$ 
16   $\mathcal{D} \leftarrow \mathcal{D} \cup \{(o_t, a_t, r_t)_{t=1}^T\}$ 
```

PlaNet은 Planning을 위해  
**Cross Entropy Method (CEM)** 을 사용했다.

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**Algorithm 2: Latent planning with CEM**

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**Input :**

|     |                                 |                                |                      |
|-----|---------------------------------|--------------------------------|----------------------|
| $H$ | Planning horizon distance       | $q(s_t   o_{\leq t}, a_{< t})$ | Current state belief |
| $I$ | Optimization iterations         | $p(s_t   s_{t-1}, a_{t-1})$    | Transition model     |
| $J$ | Candidates per iteration        | $p(r_t   s_t)$                 | Reward model         |
| $K$ | Number of top candidates to fit |                                |                      |

```
1 Initialize factorized belief over action sequences  $q(a_{t:t+H}) \leftarrow \text{Normal}(0, \mathbb{I})$ .
2 for optimization iteration  $i = 1..I$  do
    // Evaluate  $J$  action sequences from the current belief.
3   for candidate action sequence  $j = 1..J$  do
4      $a_{t:t+H}^{(j)} \sim q(a_{t:t+H})$ 
5      $s_{t:t+H+1}^{(j)} \sim q(s_t | o_{1:t}, a_{1:t-1}) \prod_{\tau=t+1}^{t+H+1} p(s_{\tau} | s_{\tau-1}, a_{\tau-1}^{(j)})$ 
6      $R^{(j)} = \sum_{\tau=t+1}^{t+H+1} \mathbb{E}[p(r_{\tau} | s_{\tau}^{(j)})]$ 

    // Re-fit belief to the  $K$  best action sequences.
7    $\mathcal{K} \leftarrow \text{argsort}(\{R^{(j)}\}_{j=1}^J)_{1:K}$ 
8    $\mu_{t:t+H} = \frac{1}{K} \sum_{k \in \mathcal{K}} a_{t:t+H}^{(k)}, \quad \sigma_{t:t+H} = \frac{1}{K-1} \sum_{k \in \mathcal{K}} |a_{t:t+H}^{(k)} - \mu_{t:t+H}|$ 
9    $q(a_{t:t+H}) \leftarrow \text{Normal}(\mu_{t:t+H}, \sigma_{t:t+H}^2 \mathbb{I})$ 
10 return first action mean  $\mu_t$ .
```

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# Latent Dynamics (PlaNet, Deep Planning Network)

## ■ Objective Function

$$\begin{aligned} \ln p(o_{1:T} \mid a_{1:T}) &\triangleq \ln \int \prod_t p(s_t \mid s_{t-1}, a_{t-1}) p(o_t \mid s_t) ds_{1:T} \\ &\geq \sum_{t=1}^T \left( \underbrace{\mathbb{E}_{q(s_t \mid o_{\leq t}, a_{< t})} [\ln p(o_t \mid s_t)]}_{\text{reconstruction}} \leftarrow \right. \\ &\quad \left. - \underbrace{\mathbb{E}_{q(s_{t-1} \mid o_{\leq t-1}, a_{< t-1})} [\text{KL}[q(s_t \mid o_{\leq t}, a_{< t}) \parallel p(s_t \mid s_{t-1}, a_{t-1})]}]_{\text{complexity}} \right). \end{aligned} \quad (3)$$

**Limitation** Gradient가 한 step만 흐르기 때문에, 1-step prediction만 보장한다



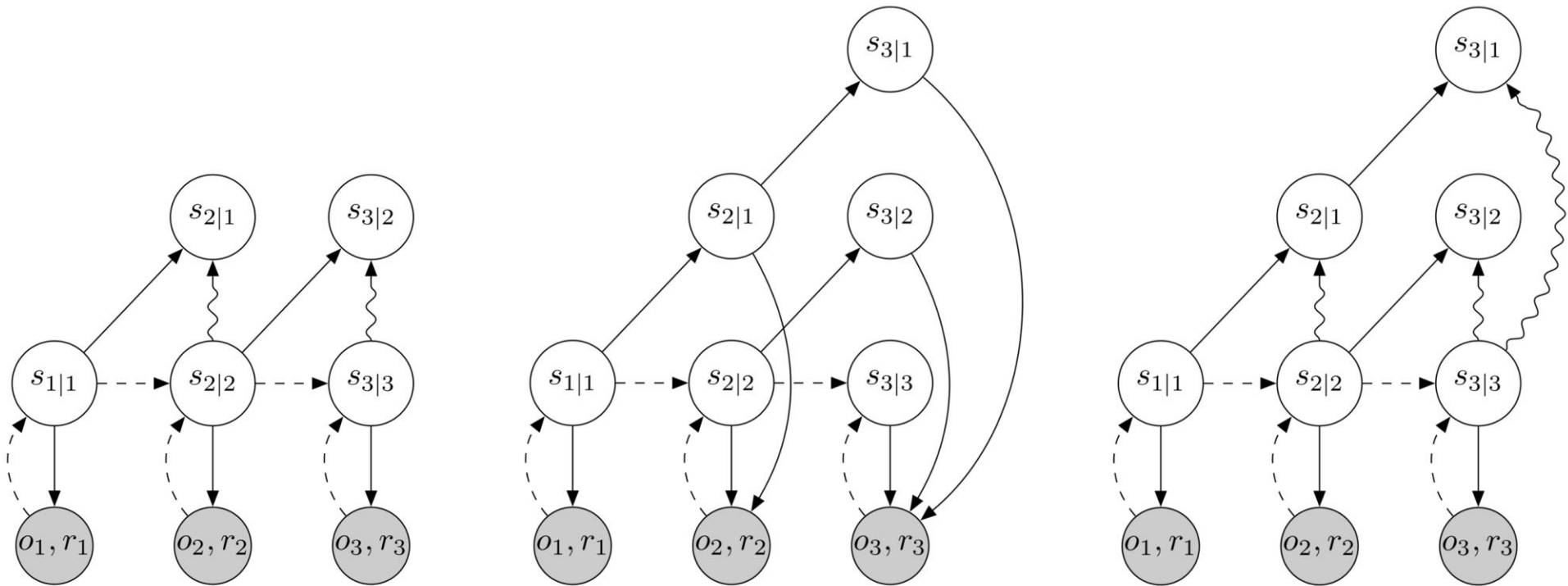
# Latent Overshooting

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# Latent OverShooting

## Motivation

multi-step prediction은 추가 image를 가하지 않았을 때 **latent space에서의 손실**로 개선할 수 있다.



(a) Standard variational bound

(b) Observation overshooting

(c) Latent overshooting

# Latent OverShooting

## ■ Define Multi Step Prediction

$$\begin{aligned} p(s_t \mid s_{t-d}) &\triangleq \int \prod_{\tau=t-d+1}^t p(s_\tau \mid s_{\tau-1}) ds_{t-d+1:t-1} \\ &= \mathbb{E}_{p(s_{t-1} \mid s_{t-d})} [p(s_t \mid s_{t-1})]. \end{aligned} \quad (5)$$

*$d = 1$  or  $\square$  1-step prediction*

## ■ Objective Function (given distance d)

$$\begin{aligned} \ln p_d(o_{1:T}) &\triangleq \ln \int \prod_{t=1}^T p(s_t \mid s_{t-d}) p(o_t \mid s_t) ds_{1:T} \\ &\geq \sum_{t=1}^T \left( \underbrace{\mathbb{E}_{q(s_t \mid o_{\leq t})} [\ln p(o_t \mid s_t)]}_{\text{reconstruction}} \leftarrow \right. \\ &\quad \left. - \underbrace{\mathbb{E}_{\frac{p(s_{t-1} \mid s_{t-d}) q(s_{t-d} \mid o_{\leq t-d})}{p(s_{t-1} \mid s_{t-d}) q(s_{t-d} \mid o_{\leq t-d})}} [\text{KL}[q(s_t \mid o_{\leq t}) \parallel p(s_t \mid s_{t-1})]]}_{\text{multi-step prediction}} \right). \end{aligned} \quad (6)$$

*와 ~ Markov하다 !*

# Latent OverShooting

■ **Objective Function** (all distances up to the planning horizon.)

$$\begin{aligned} \frac{1}{D} \sum_{d=1}^D \ln p_d(o_{1:T}) \geq & \sum_{t=1}^T \left( \underbrace{\mathbb{E}_{q(s_t | o_{\leq t})} [\ln p(o_t | s_t)]}_{\text{reconstruction}} \leftarrow \right. \\ & \left. - \underbrace{\frac{1}{D} \sum_{d=1}^D \beta_d \mathbb{E}_{\substack{p(s_{t-1} | s_{t-d}) q(s_{t-d} | o_{\leq t-d})}} [\text{KL}[q(s_t | o_{\leq t}) \parallel p(s_t | s_{t-1})]]]}_{\text{latent overshooting}} \right). \quad (7) \end{aligned}$$

# Latent OverShooting

■ **Objective Function** (all distances up to the planning horizon.)

$$\begin{aligned} \frac{1}{D} \sum_{d=1}^D \ln p_d(o_{1:T}) \geq & \sum_{t=1}^T \left( \underbrace{\mathbb{E}_{q(s_t | o_{\leq t})} [\ln p(o_t | s_t)]}_{\text{reconstruction}} \leftarrow \right. \\ & \left. - \underbrace{\frac{1}{D} \sum_{d=1}^D \beta_d \mathbb{E}_{\substack{p(s_{t-1} | s_{t-d}) q(s_{t-d} | o_{\leq t-d})}} [\text{KL}[q(s_t | o_{\leq t}) \parallel p(s_t | s_{t-1})]]]}_{\text{latent overshooting}} \right). \quad (7) \end{aligned}$$

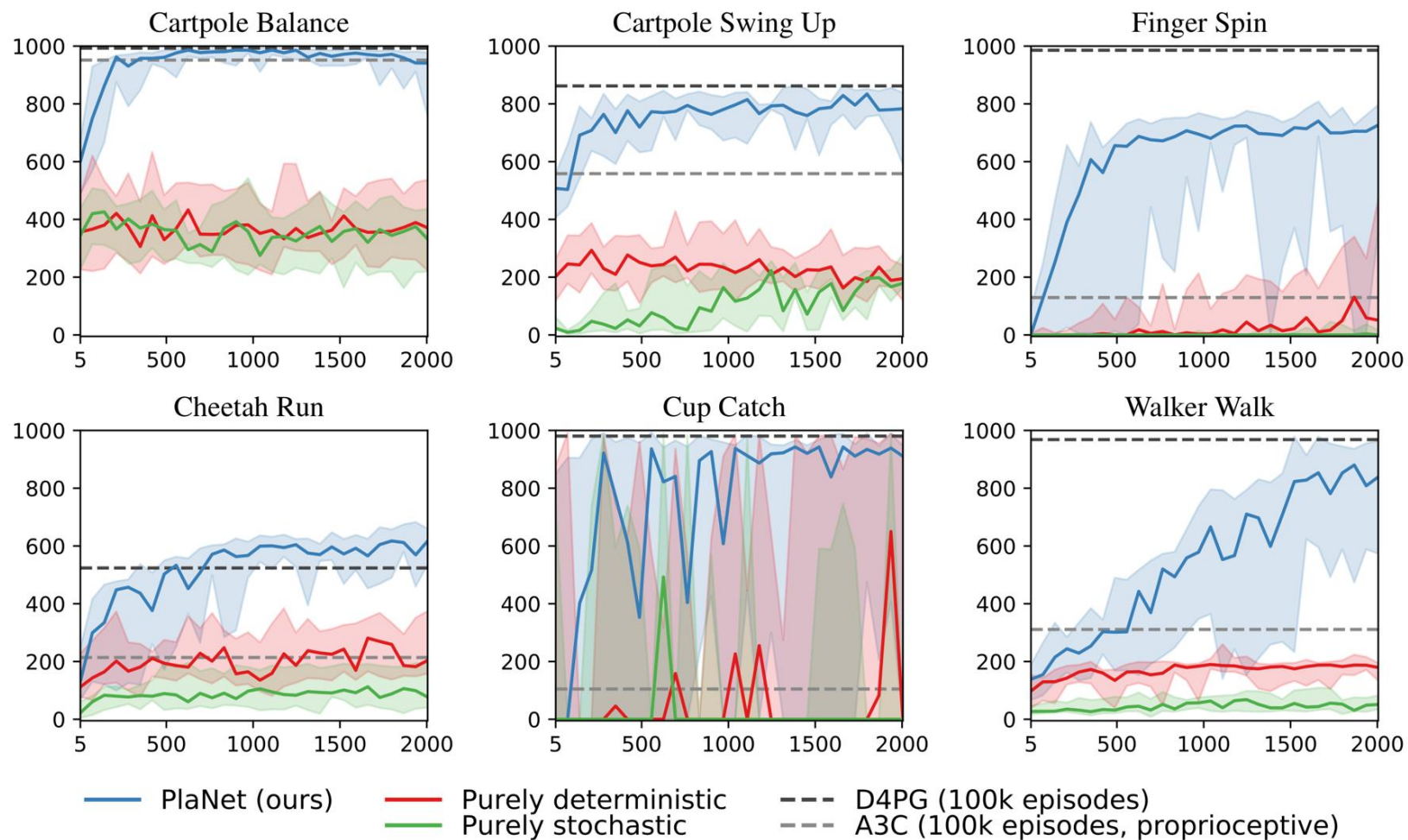
# Experiments

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# Comparison (Model-Free Method)

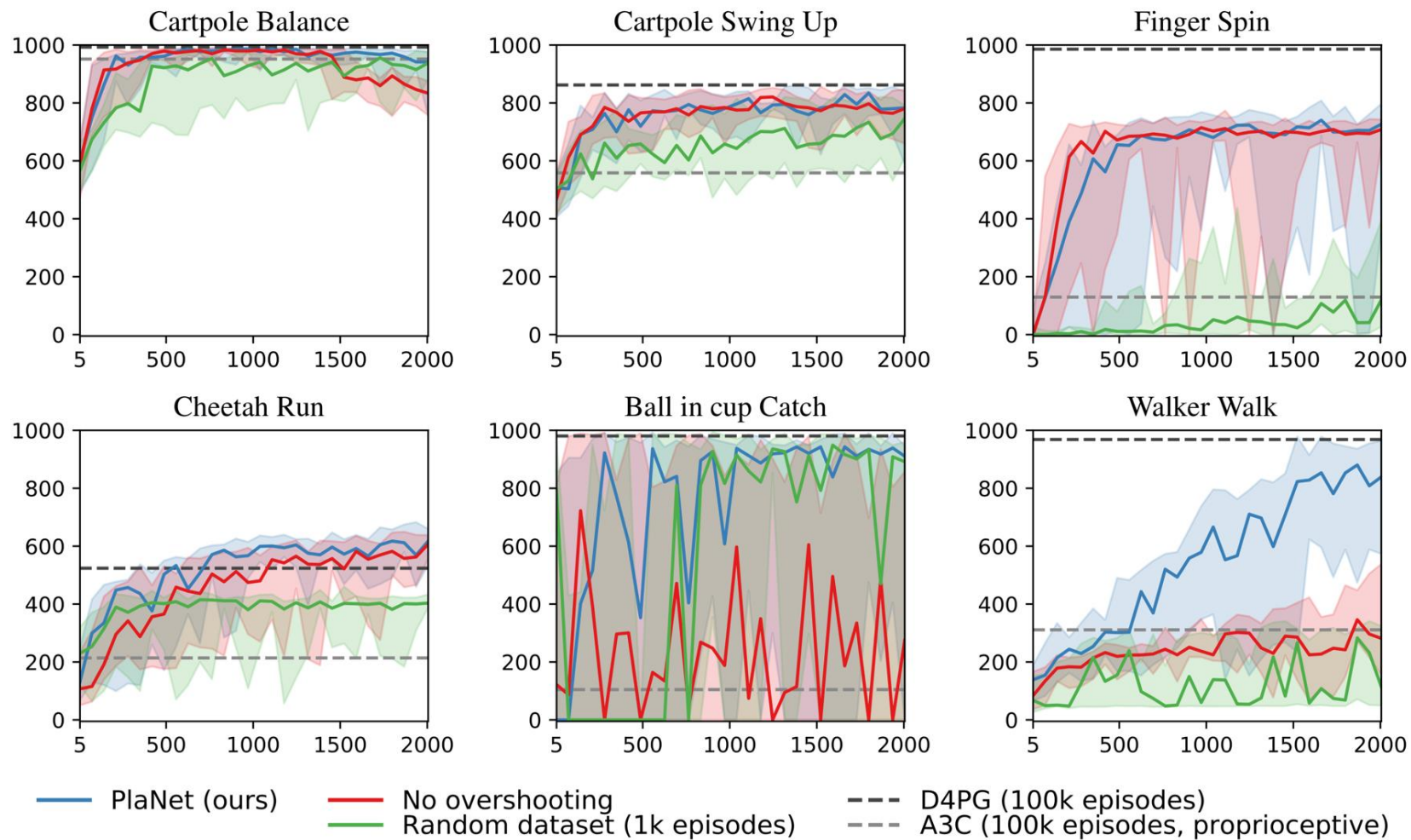
| Method   | Modality        | Episodes | Cartpole<br>Balance | Cartpole<br>Swingup | Finger<br>Spin | Cheetah<br>Run | Ball in cup<br>Catch | Walker<br>Walk |
|--|-----------------|----------|---------------------|---------------------|----------------|----------------|----------------------|----------------|
| A3C  | proprioceptive  | 100,000  | 952                 | 558                 | 129            | 214            | 105                  | 311            |
| D4PG   | pixels          | 100,000  | 993                 | 862                 | 985            | 524            | 980                  | 968            |
| PlaNet (ours)                                  | pixels          | 2,000    | 986                 | 831                 | 744            | 650            | 914                  | 890            |
| CEM + true simulator                           | simulator state | 0        | 998                 | 850                 | 825            | 656            | 993                  | 994            |
| Data efficiency gain PlaNet over D4PG (factor) |                 |          | 100                 | 180                 | 16             | 50+            | 20                   | 11             |

# Model





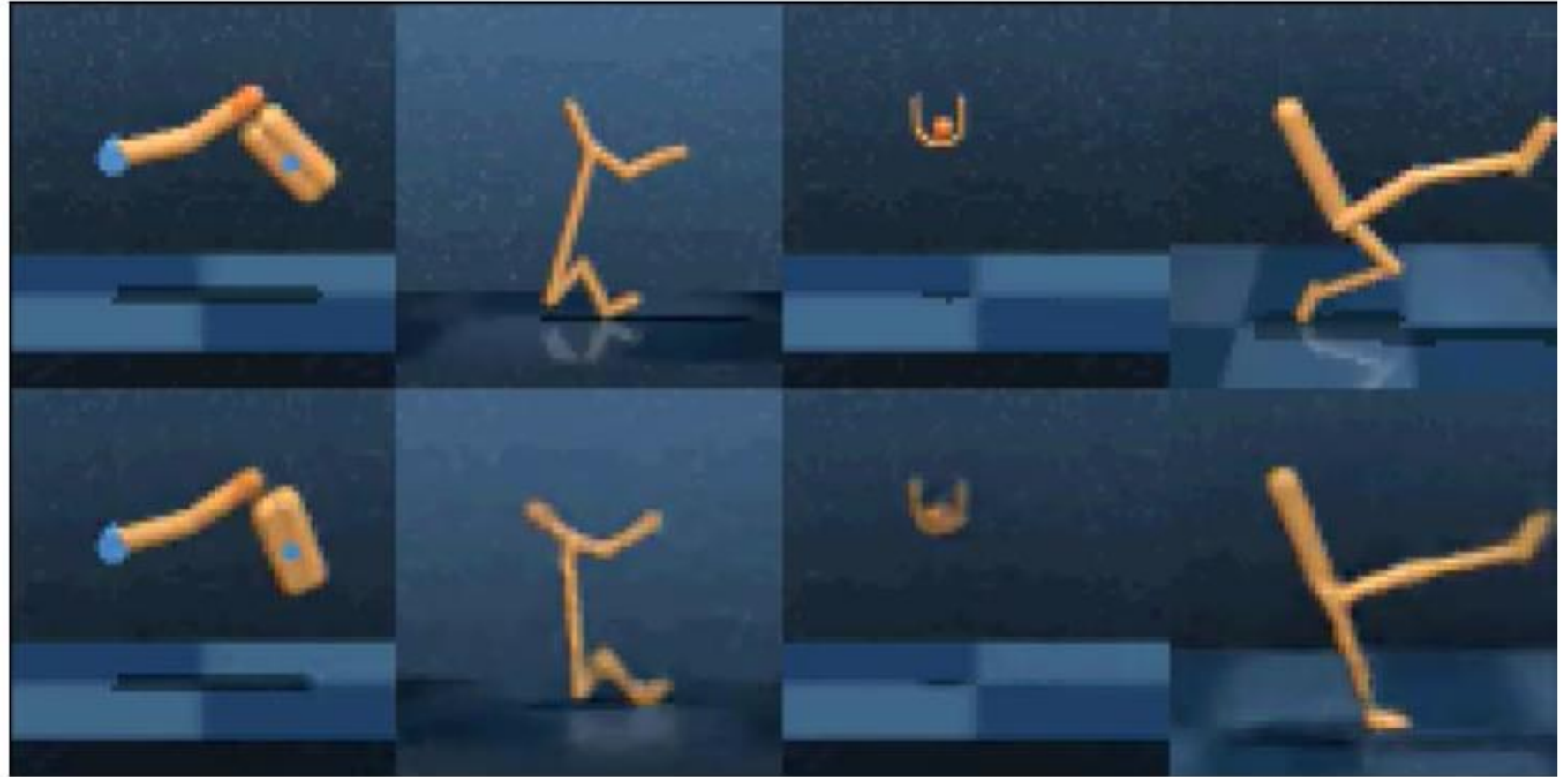
# Agent



# One agent all tasks

Episode

Prediction



# Relative Works

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# Relative Works

- 1. Planning in state space**
- 2. Hybrid agents**
- 3. Multi-step predictions**
- 4. Latent sequence models**
- 5. Video prediction**

**End !**